

# Magnetic fields

• Magnetic force:  $\vec{F}_B = q \vec{v} \times \vec{B}$   
 $= q (vB) \sin\theta$   
 $\theta$  between  $v$  &  $B$

→ Direction of  $F$ : You <sup>right</sup> four fingers is toward  $v$   
Then swap your hand towards  $\vec{B}$   
The direction of your thumb is the direction of  $F_B$  (right hand rule)

→ If  $q$  is negative, the direction of  $F_B$  would be the opposite

## Crossed fields:-

- When two fields: Magnetic and Electric fields are perpendicular
- a charge passing through them has both Magnetic and Electric force
- At equilibrium  $v = \frac{E}{B}$

Haa Haini

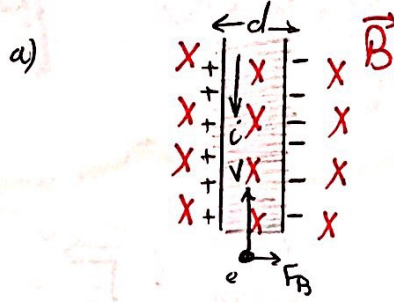
# Applications on Magnetic fields

The Hall effect :-

number of carriers per unit volume  $n = \frac{Bi}{eV_d d}$

$V_H$  ← Hall Potential  
 $i$  ← electric current  
 $d$  ← Thickness  
 $B$  ← Magnetic field

A metal strip

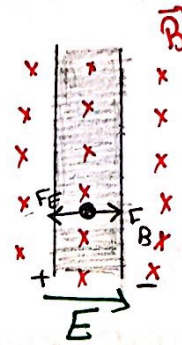


• here a magnetic force  $F_B$  affects the drifting electrons and will push them to the

At equilibrium :-

drift speed  $V_d = \frac{V_H}{Bd}$

Potential difference



• electric force is exerted  
 • equilibrium  
 • a potential difference is created and is called Hall potential difference ( $V_H$ )

• Note that:  $\vec{F}_B$  only changes direction of  $v$  but doesn't affect its magnitude

• A circulating charged particle ( $B \perp v$  always)

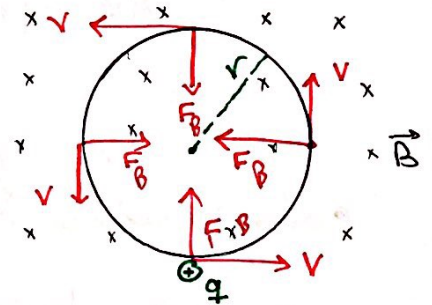
• In General  $F = ma$

• In circular motion  $F = m \frac{v^2}{r}$

• If  $F = F_B \rightarrow qvB = m \frac{v^2}{r}$

$r = \frac{mv}{qB}$

mass  
speed  
charge



(Period)  $T = \frac{2\pi m}{qB}$

(frequency)  $f = \frac{qB}{2\pi m}$

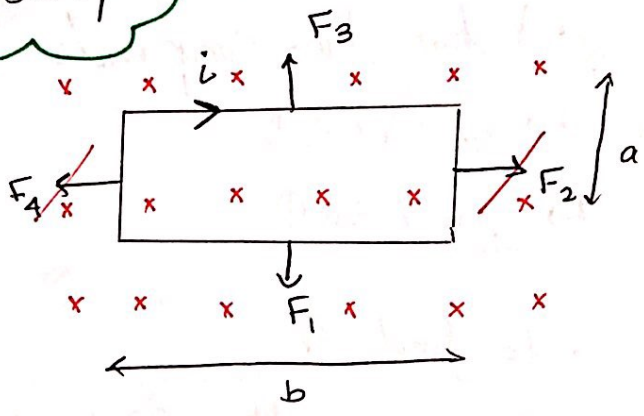
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# Torque on a Current loop

Number of turns of current

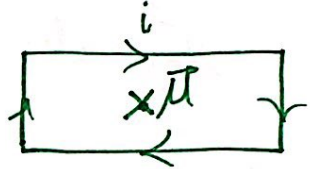
$$\vec{\tau} = N i \vec{A} \times \vec{B}$$

$\vec{A}$  (Area)       $\vec{B}$  (Magnetic field)



• Magnetic Dipole Moment :- ( $\vec{\mu}$ )

•  $\vec{\mu} = N i A$  (Generally) Direction by right hand rule



• when  $\vec{B}$  acts on  $\vec{\mu}$  :

The Torque =  $\vec{\tau} = \vec{\mu} \times \vec{B}$

energy =  $U = -\vec{\mu} \cdot \vec{B}$

$W = \Delta U$   
of an external Magnetic field

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# Helical path

velocity  $\vec{V}$  has two components  
 $\rightarrow V_{||} = V \cos \phi$

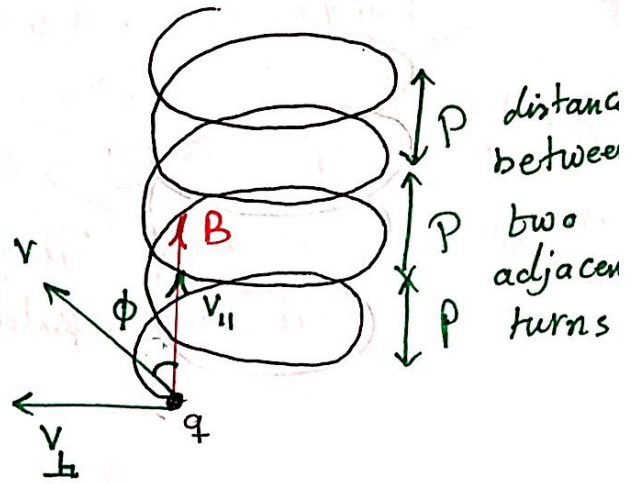
$\rightarrow V_{\perp} = V \sin \phi$

to find  $\phi$

You use the Dot product

$\vec{V} \cdot \vec{B} = V B \cos \theta$

velocity  $\cos \phi = \frac{\vec{V} \cdot \vec{B}}{VB}$  ← vector notation  
 ↑  
 Magnitudes



to find pitch

$P = V_{||} T$  ↑ period

to find r:

$r = \frac{m V_{\perp}}{qB}$

period  $T = \frac{2\pi m}{qB}$

Remember that at equi

$F_B = F_E$

$qE = qvB$

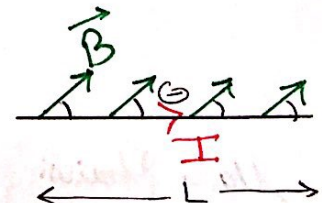
$\frac{v}{E} = vB$

$v = vBd$

# Magnetic force on a Current Carrying Wire

$\vec{F}_B = i \vec{L} \times \vec{B}$

↑  
 direction of the flow  
 of current



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