

Chapter-21 Lecture Problems

(21-3) $q_1 = -q_2 = 300 \text{ nC}$

$q_3 = -q_4 = 200 \text{ nC}$

$a = 5 \text{ cm}$

$\vec{F}_3 ?$

All vectors (Forces) must Begin from q_3

$$F_{31} = \frac{9 \times 10^9 \times 200 \times 10^{-9} \times 300 \times 10^{-9}}{(5 \times 10^{-2})^2}$$

$$\vec{F}_{31} = 0.216 \text{ N in } (-y) \text{ or } -\hat{j}$$

$$F_{32} = \frac{9 \times 10^9 \times 200 \times 10^{-9} \times 300 \times 10^{-9}}{(5\sqrt{2} \times 10^{-2})^2}$$

$$\vec{F}_{32} = 0.108 \text{ N at } 45^\circ \text{ with } +x$$

$$F_{34} = \frac{9 \times 10^9 \times 200 \times 10^{-9} \times 200 \times 10^{-9}}{(5 \times 10^{-2})^2}$$

$$\vec{F}_{34} = 0.144 \text{ N in } +x$$

$$\vec{F}_3 = \vec{F}_{31} + \vec{F}_{32} + \vec{F}_{34}$$

$$(F_3)_x = 0.144 + F_{32} \cos 45 = 0.144 + 0.108(0.707) = 0.22 \text{ N}$$

$$(F_3)_y = -F_{31} + F_{32} \sin 45 = -0.216 + 0.108 \sin 45 = -0.14 \text{ N}$$

$$F_3 = \sqrt{F_{3x}^2 + F_{3y}^2} = \sqrt{(0.22)^2 + (-0.14)^2} = 0.26 \text{ N}$$

$$\theta = \tan^{-1}\left(\frac{F_{3y}}{F_{3x}}\right) = \tan^{-1}\left(\frac{-0.14}{0.22}\right)$$

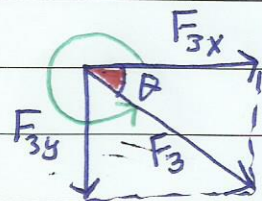
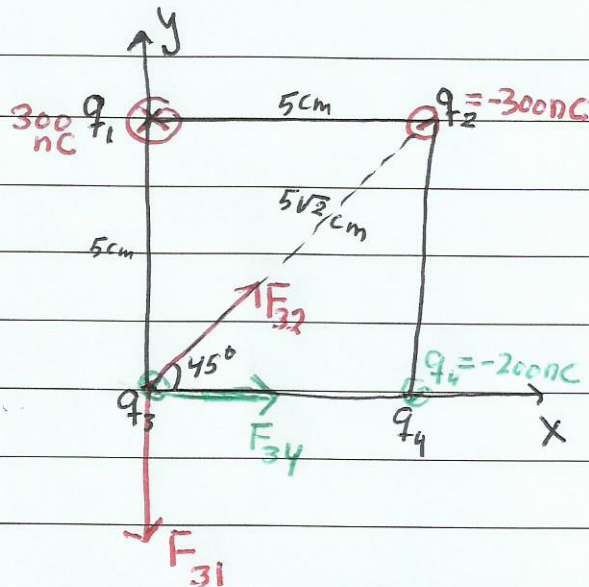
$\theta = -32.5^\circ$

$\vec{F}_3 = 0.22\hat{i} - 0.14\hat{j} \text{ N}$

3 methods to describe \vec{F}_3

① $\vec{F}_3 = 0.26 \text{ N at } 32.5^\circ \text{ with } +x \text{ clockwise}$

② $\vec{F}_3 = 0.26 \text{ N at } 327.5^\circ \text{ with } +x \text{ Counterclockwise}$



(21-6)

q_1 at $x_1 = -a$

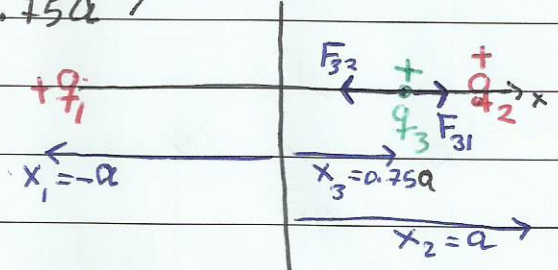
q_2 at $x_2 = +a$

$\vec{F}_3 = 0$ on $q_3 = +Q$

a) Find $\frac{q_1}{q_2}$? when $q_3 = +Q$ at $x_3 = +0.75a$ For $\vec{F}_3 = 0$

both q_1 & q_2 must be positive
OR

both q_1 & q_2 must be negative



$\Rightarrow \frac{q_1}{q_2} = +?$

$$\vec{F}_3 = \vec{F}_{31} + \vec{F}_{32} \quad , \quad \vec{F}_3 = 0 \Rightarrow \vec{F}_{31} = -\vec{F}_{32} \text{ opposite and equal}$$

$$0 = \frac{k q_1 Q}{(a + 0.75a)^2} + \frac{k q_2 Q}{(0.25a)^2} \Rightarrow \frac{k q_1 Q}{(1.75a)^2} - \frac{k q_2 Q}{(0.25a)^2}$$

$$\frac{q_1}{(1.75)^2} = \frac{q_2}{(0.25)^2} \Rightarrow \frac{q_1}{q_2} = \left(\frac{1.75}{0.25}\right)^2 = (7)^2$$

$$\frac{q_1}{q_2} = +49$$

b) Find $\frac{q_1}{q_2} = ?$ when $q_3 = +Q$ at $x_3 = 1.5a$ For $\vec{F}_3 = 0$

$$\vec{F}_3 = \vec{F}_{31} + \vec{F}_{32}$$

For $\vec{F}_3 = 0$

$$\vec{F}_{31} + \vec{F}_{32} = 0 \Rightarrow$$

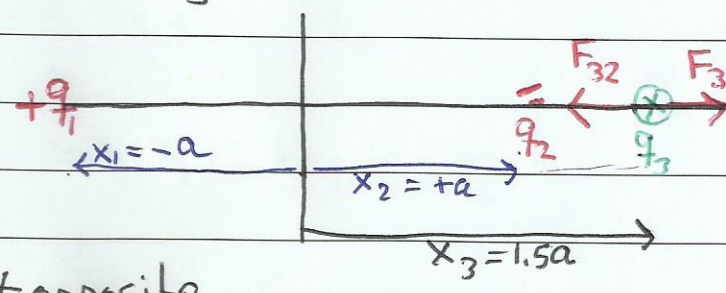
$\vec{F}_{31} = -\vec{F}_{32}$ must be equal & opposite

let q be positive, then q_2 must be negative $\Rightarrow \frac{q_1}{q_2} = -?$

$$\frac{k q_1 Q}{(2.5a)^2} = \frac{k q_2 Q}{(0.5a)^2} \Rightarrow \frac{q_1}{(2.5)^2} = \frac{q_2}{(0.5)^2}$$

$$\frac{q_1}{q_2} = \left(\frac{2.5}{0.5}\right)^2 = (5)^2 = 25 \Rightarrow$$

$$\frac{q_1}{q_2} = -25$$



(21-31)

$$q_1 = q_2 = +4e$$

$$q_3 = +8e$$

$$d = 17.0 \text{ cm}$$

$$x (0 \rightarrow 5 \text{ m})$$

Find x ? for \vec{F}_3 is max

Find x ? For F_3 is min.

Find $(F_3)_{\text{max}}$? $(F_3)_{\text{min}}$?

$$r_{13} = r_{23} = \sqrt{d^2 + x^2}$$

$$F_{31} = F_{32} = \frac{k q_1 q_3}{(r_{13})^2} = \frac{k (4e)(8e)}{[\sqrt{d^2 + x^2}]^2} = \frac{32k e^2}{d^2 + x^2}, \text{ the direction for each Force on the figure.}$$

$$\vec{F}_3 = \vec{F}_{31} + \vec{F}_{32}$$

$$(F_3)_x = \frac{32k e^2}{d^2 + x^2} \cos\theta + \frac{32k e^2}{d^2 + x^2} \cos\theta = 2 \left(\frac{32k e^2}{d^2 + x^2} \right) \left(\frac{x}{\sqrt{d^2 + x^2}} \right)$$

$$(F_3)_x = 64k e^2 \left(\frac{x}{(d^2 + x^2)^{3/2}} \right)$$

$$(F_3)_{\text{min}} = 0 \text{ at } x=0$$

$$(F_3)_y = -F_{31} \sin\theta + F_{32} \sin\theta = 0$$

$$F_3 = 64k e^2 \frac{x}{(d^2 + x^2)^{3/2}}$$

to find F_{max} + F_{min} do $\frac{dF_3}{dx}$ must equal zero

$$\frac{dF_3}{dx} = 64k e^2 \frac{d}{dx} [x(d^2 + x^2)^{-3/2}] dx$$

$$0 = 64k e^2 \left[(1)(d^2 + x^2)^{-3/2} + x \left(-\frac{3}{2} \right) (2x) (d^2 + x^2)^{-5/2} \right]$$

$$\frac{3x^2}{(d^2 + x^2)^{5/2}} = \frac{1}{(d^2 + x^2)^{3/2}} \iff \frac{3x^2}{(d^2 + x^2)^{5/2}} = \frac{(d^2 + x^2)^{5/2}}{(d^2 + x^2)^{3/2}}$$

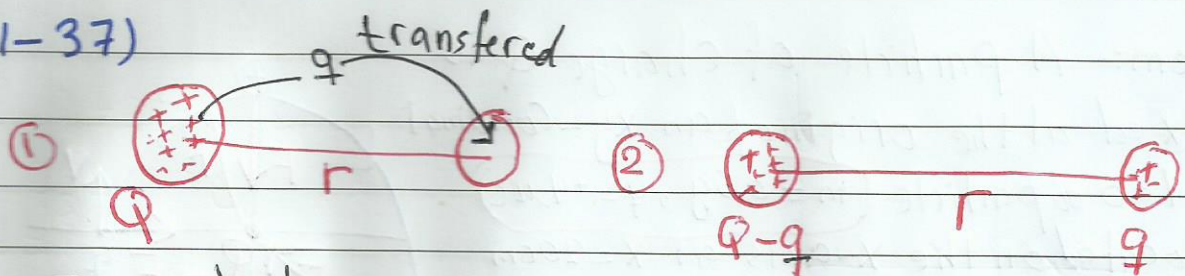
$$3x^2 = d^2 + x^2 \implies 2x^2 = d^2 \implies x = \frac{d}{\sqrt{2}} \text{ for } (F_3)_{\text{max}}$$

$$(F_3)_{\text{max}} = 64k e^2 \left(\frac{d/\sqrt{2}}{[d^2 + d^2/2]^{3/2}} \right)$$

$$= 64k e^2 \left[\frac{d^2}{\sqrt{2} [1.5d^2]^{3/2}} \right]$$

$$k = 9 \times 10^9 \\ d = 17 \times 10^{-2} \text{ m} \\ e = 1.6 \times 10^{-19} \text{ C}$$

(21-37)



a) For what value of q will maximize the force between the 2 spheres

$$F = k \frac{q_1 q_2}{r^2} = k \frac{q(Q-q)}{r^2}$$

$\frac{dF}{dq}$ must be zero for F to be maximum

$$\frac{dF}{dq} = \frac{k}{r^2} \frac{d}{dq} (Qq - q^2) = \frac{k}{r^2} (Q - 2q)$$

$$0 = \frac{k}{r^2} (Q - 2q) \Rightarrow Q - 2q = 0 \Rightarrow q = \frac{1}{2} Q$$

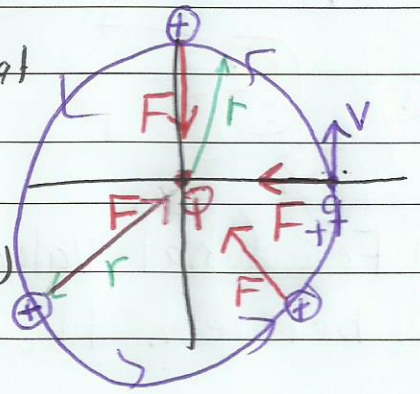
$$\frac{q}{Q} = \frac{1}{2} \text{ for } F_{\max}$$

$$F_{\max} = k \left(\frac{q_1 q_2}{r^2} \right) = \frac{k}{r^2} \left[\left(\frac{1}{2} Q \right) \left(\frac{1}{2} Q \right) \right] = \frac{k Q^2}{4r^2}$$

b) do this part.

Problem:- A particle of charge Q is fixed at the origin of an xy -Coordinate. At $t=0$ a particle ($m=0.5g, q=+4\mu C$) is located on the x -axis at $x=20cm$ moving with speed of $50m/s$ in the $(+y)$

For what value of Q will the moving particle execute circular motion



[Neglect gravitational force on the particle]

For the particle to move circular motion force on the particle must be toward the center $\Rightarrow Q$ must be negative

$$F_q = k \frac{qQ}{r^2}, \quad r=20cm, \quad q=+4 \times 10^{-6}$$

$$\frac{mv^2}{r} = \frac{kqQ}{r^2} \Rightarrow m = 0.5 \times 10^{-3} kg$$

$$Q = \frac{mv^2 r}{kq}$$

$$Q = \frac{(0.5 \times 10^{-3})(50)^2(0.2)}{(9 \times 10^9)(4 \times 10^{-6})} = 6.94 \times 10^{-6} C = 6.94 \mu C$$

$$Q = -6.94 \mu C$$