

## FORCE AND MOTION

## EXERCISES

## Section 4.2 Newton's First and Second Laws

12. **INTERPRET** This problem involves the application of Newton's second law. The object under consideration is the train and the physical quantity of interest is the net force acting on the train.

**DEVELOP** The net force can be found by using Equation 4.3,  $\vec{F}_{\text{net}} = m\vec{a}$ .

**EVALUATE** Using Equation 4.3, the magnitude of the force acting on the train is found to be

$$F_{\text{net}} = ma = (1.5 \times 10^6 \text{ kg})(2.5 \text{ m/s}^2) = 3.8 \times 10^6 \text{ N}$$

**ASSESS** The result is reasonable, since by definition, one newton is the force required to accelerate a 1-kg mass at the rate of  $1 \text{ m/s}^2$ .

13. **INTERPRET** This problem involves Newton's 2<sup>nd</sup> law for a locomotive with different loads.

**DEVELOP** By Equation 4.3, the locomotive accelerates due to the force:  $a = F/m$ .

**EVALUATE** (a) The mass in this case is just the locomotive itself

$$a = \frac{(1.2 \times 10^5 \text{ N})}{61 \times 10^3 \text{ kg}} = 2.0 \text{ m/s}^2$$

(b) If the locomotive is pulling a train then the mass is the sum

$$a = \frac{(1.2 \times 10^5 \text{ N})}{(61 \times 10^3 \text{ kg}) + (1.4 \times 10^6 \text{ kg})} = 0.082 \text{ m/s}^2$$

**ASSESS** These seem like reasonable accelerations. The locomotive by itself could reach 60 mi/h in 13 s, but pulling the train it would take over 5 and a half minutes to reach this speed.

14. **INTERPRET** We interpret this as a problem involving the application of Newton's second law. The object under consideration is the airplane and the physical quantity of interest is the plane's mass.

**DEVELOP** We shall assume that the runway is horizontal (so that the vertical force of gravity and the normal force of the surface cancel) and neglect aerodynamic forces (which are small just after the plane begins to move). Then the net force equals the engine's thrust and is parallel to the acceleration. The plane's mass can be found by using Equation 4.3,  $\vec{F}_{\text{net}} = m\vec{a}$ .

**EVALUATE** Using Equation 4.3, the mass of the plane is found to be

$$m = \frac{F_{\text{net}}}{a} = \frac{1.1 \times 10^4 \text{ N}}{7.2 \text{ m/s}^2} = 1.53 \times 10^3 \text{ kg}$$

**ASSESS** First, the units are consistent since  $1 \text{ N} = 1 \text{ kg} \cdot \text{m/s}^2$ . The result is reasonable, since by definition, one newton is the force required to accelerate a 1-kg mass at the rate of  $1 \text{ m/s}^2$ .

15. **INTERPRET** This problem involves Newton's second law. The object of interest is the passenger, and we are to calculate the force required to stop the passenger in the given time.

**DEVELOP** Assume that the seatbelt holds the passenger firmly to the seat, so that the passenger also stops in 0.14 s without incurring any secondary impact. The passenger's average acceleration is  $a_{av} = (0 - v_0)/t$  and his mass is 60 kg. Insert these quantities into Newton's second law to find the force.

**EVALUATE** The average force exerted by the seatbelt on the passenger is

$$F_{av} = ma_{av} = -mv_0/t = -\frac{(60 \text{ kg})}{0.14 \text{ s}}(110 \text{ km/h})\left(\frac{1000 \text{ m}}{\text{km}}\right)\left(\frac{1 \text{ h}}{3600 \text{ s}}\right) = -13 \text{ kN}$$

**ASSESS** The negative sign indicates that the force is opposite to the direction of the initial velocity.

16. **INTERPRET** This problem involves Newton's second law and kinematics, with which we need to find the relationship between force and stopping distance.

**DEVELOP** From Equation 4.3, we see that the net force on a car of given mass is proportional to the acceleration,  $F_{net} \propto a$ . We can then relate the three quantities, displacement, velocity, and acceleration, by Equation 2.11,  $v^2 = v_0^2 + 2a(x - x_0)$ .

**EVALUATE** To stop a car in a distance  $x - x_0$ , the acceleration is

$$a = \frac{v^2 - v_0^2}{2(x - x_0)} = \frac{-v_0^2}{2(x - x_0)}$$

Therefore, we see that  $F_{net} \propto v_0^2$ , so doubling  $v_0$  quadruples the magnitude of  $F_{net}$ .

**ASSESS** The conclusion that  $F_{net} \propto v_0^2$  is an important fact to remember when driving at high speeds.

17. **INTERPRET** This problem involves Newton's 2<sup>nd</sup> law for constant mass.

**DEVELOP** By Equation 4.3, the kinesin force imparts an acceleration on the molecular complex of  $a = F/m$ .

**EVALUATE** Recall from Appendix B that the SI prefix pico (p) corresponds to  $10^{-12}$ , so

$$a = \frac{F}{m} = \frac{6.0 \times 10^{-12} \text{ N}}{3.0 \times 10^{-18} \text{ kg}} = 2.0 \times 10^6 \text{ m/s}^2$$

**ASSESS** This is an extraordinarily large acceleration, but it would only be applied for a fraction of a second, so the final velocity would be reasonable.

18. **INTERPRET** This problem involves Newton's second law and kinematics. We want to find the force required to accelerate a car to cover a certain distance within a given time interval.

**DEVELOP** The displacement of the car as a function of time is given by Equation 2.10,

$x = x_0 + v_0 t + \frac{1}{2} a t^2$ . The equation can be used to solve for the acceleration  $a$ . Also, from Newton's second law, we see that the net force on a car of given mass is proportional to the acceleration,  $F_{net} \propto a$ .

**EVALUATE** Using Equation 2.10 with  $v_0 = 0$ , the acceleration of the car is

$$a = \frac{2(x - x_0)}{t^2} = \frac{2(400 \text{ m})}{(4.95 \text{ s})^2} = 32.6 \text{ m/s}^2$$

Newton's second law gives the average net force on the car as

$$F_{net} = ma = (940 \text{ kg})(32.6 \text{ m/s}^2) = 3 \times 10^4 \text{ N}$$

to a single significant figure. The force acts in the direction of the motion.

**ASSESS** Our answer for the acceleration  $a$  can be checked by using other kinematic equations. The speed of the car after 4.95 s is  $v = at = (32.6 \text{ m/s}^2)(4.95 \text{ s}) = 161 \text{ m/s}$ . Using Equation 2.11,  $v^2 = v_0^2 + 2a(x - x_0)$  we find the distance traveled to be

$$x - x_0 = \frac{v^2 - v_0^2}{2a} = \frac{(161 \text{ m/s})^2 - 0}{2(32.6 \text{ m/s}^2)} = 400 \text{ m}$$

in agreement with the value given in the problem statement.

19. **INTERPRET** This problem involves Newton's second law and kinematics. The object of interest is the egg, and we are to calculate the minimum stopping distance so that the egg does not experience a force greater than 1.5 N.

**DEVELOP** For the average net force on the egg to not exceed the stated limit, the magnitude of the deceleration should satisfy  $a_{\text{av}} \leq F_{\text{max}}/m = 1.5 \text{ N}/0.085 \text{ kg} = 17.6 \text{ m/s}^2$ . Insert this acceleration into kinematic Equation 2.11  $v^2 = v_0^2 + 2a(x - x_0)$  to find the minimum stopping distance.

**EVALUATE** The minimum stopping distance is

$$x - x_0 \geq \frac{(1.2 \text{ m/s})^2}{35.3 \text{ m/s}^2} = 0.041 \text{ m} = 4.1 \text{ cm}$$

**ASSESS** Notice that the units work out to units of distance, as expected.

20. **INTERPRET** We interpret this as a problem involving the application of Newton's second law. The object under consideration is the car and the physical quantity of interest is the bumper deformation to withstand the impact force and avoid damage.

**DEVELOP** For the force on the bumper not to exceed the stated limit, the magnitude of the deceleration should satisfy  $a_{\text{av}} \leq F_{\text{max}}/m$ . The deformation of the bumper can then be calculated from Equation 2.11,  $v^2 = v_0^2 + 2a(x - x_0)$ .

**EVALUATE** From the reasoning above, the magnitude of the maximum acceleration is

$$a_{\text{av}} = \frac{F_{\text{max}}}{m} = \frac{65,000 \text{ N}}{1300 \text{ kg}} = 50 \text{ m/s}^2$$

With an initial speed of  $v_0 = 10 \text{ km/h} = 2.78 \text{ m/s}$ , the minimum bumper deformation is

$$x - x_0 = \frac{|v^2 - v_0^2|}{2a} = \frac{|0 - (2.78 \text{ m/s})^2|}{2(50 \text{ m/s}^2)} = 0.0772 \text{ m} = 7.7 \text{ cm}$$

**ASSESS** A bumper is typically allowed to deform up to a maximum of 12.5 cm before stopping the car.

#### Section 4.4 The Force of Gravity

21. **INTERPRET** This problem involves using Newton's second law to convert the usual units of acceleration ( $\text{m/s}^2$ ) to  $\text{N/kg}$ . We are also asked to explain why it makes sense to express acceleration in  $\text{N/kg}$  when speaking of mass and weight.

**DEVELOP** Newton's second law relates the units of mass (kg), distance (m), time (s), and force (N). Use this to solve the problem.

**EVALUATE** From Newton's second law (for constant mass),  $\vec{F}_{\text{net}} = m\vec{a}$ , we see that force (N) is the same as mass (kg)  $\times$  acceleration ( $\text{m/s}^2$ ), which can be expressed mathematically as  $\text{N} = \text{kg} \cdot \text{m/s}^2$ . This can be rearranged to find  $\text{m/s}^2 = \text{N/kg}$ . It makes sense to use the units  $\text{N/kg}$  when speaking of mass and weight because kg is a unit of mass and N is a unit of force (i.e., a weight).

**ASSESS** An acceleration is thus a mass per unit force.

22. **INTERPRET** This problem involves the acceleration due to gravity. We are to use it to identify the planet on which the spaceship has crashed based on the gravitational force experienced.

**DEVELOP** If the mass and weight are known, then the gravitational acceleration of the planet can be obtained by using Equation 4.5,  $\vec{w} = m\vec{g}$ .

**EVALUATE** The surface gravity of the planet is thus

$$g = \frac{w}{m} = \frac{532 \text{ N}}{60 \text{ kg}} = 8.87 \text{ m/s}^2$$

which is precisely the value for Venus in Appendix E.

**ASSESS** The gravitational acceleration of Venus is lower than that of the Earth. Therefore, the person's weight is less on Venus. The mass, however, remains unchanged.

23. **INTERPRET** This problem asks us to find the mass of an object whose weight on the Moon corresponds to the weight of 35-kg object on the Earth.

**DEVELOP** Use Equation 4.5 to find the weight of the block on the Earth. Use the gravitational acceleration  $g_{\text{M}}$  from Appendix E to calculate the mass that corresponds to an object of this weight on the Moon.

**EVALUATE** To lift a 35-kg block on Earth requires a force at least equivalent to its weight, which is  $w = mg = (35 \text{ kg})(9.8 \text{ m/s}^2) = 343 \text{ N}$ . The same force on the moon could lift a mass  $m = w/g_M = (343 \text{ N})/(1.62 \text{ m/s}^2) = 212 \text{ kg} \approx 210 \text{ kg}$  to two significant figures.

**ASSESS** The weight of a 212-kg object on Earth is  $w = mg = (212 \text{ kg})(9.8 \text{ m/s}^2) = 2078 \text{ N}$ , which is a factor  $g/g_M = (9.8 \text{ m/s}^2)/(1.62 \text{ m/s}^2) = 6$  times more than the weight on the Moon. Thus, you can lift 6 times the mass on the Moon than you can on the Earth.

- 24. INTERPRET** In this problem we are asked about the actual weight, given the mass, of a cereal box in SI units and in ounces.

**DEVELOP** In many contexts, the phrase “net weight” actually refers to the mass, rather than the actual weight (as in this case). Use Equation 4.5 to find the weight of the cereal, and then convert this to ounces using the conversion factor  $1 \text{ oz} = \text{weight of } 0.02835 \text{ kg} = (9.81 \text{ m/s}^2)(0.02835 \text{ kg}) = 0.2778 \text{ N}$  (Appendix C). Recall that  $340 \text{ g} = 0.340 \text{ kg}$ .

**EVALUATE** (a) The actual weight (equal to the gravitational force on the object at the surface of the Earth) is

$$w = mg = (0.340 \text{ kg})(9.81 \text{ m/s}^2) = 3.33 \text{ N}$$

(b) Using the conversion factor from Appendix C we find the weight in ounces is

$$w = (3.33 \text{ N}) \left( \frac{1 \text{ oz}}{0.2778 \text{ N}} \right) = 12.0 \text{ oz}$$

**ASSESS** The word “net” in net weight means just the weight of the contents; gross weight includes the weight of the container, etc. This may be compared with the use of the word in net force, which means the sum of all the forces or the resultant force. A net weight, profit, or other amount is the resultant after all corrections have been taken into account.

- 25. INTERPRET** This is an exercise in converting between mass and weight.

**DEVELOP** The weight on the US side is 10 tons. From Appendix C, we see that 1 ton is equivalent to the weight of 908 kg. Use this conversion to translate the given weight into a mass in kg.

**EVALUATE** If 1 ton = weight of 908 k, 10 = weight of 9080 kg. Thus, you should specify 9000 kg (to a single significant figure) on the Canadian side of the border.

**ASSESS** The conversion between mass and weight on Earth is  $m = w/g$ . Because the English unit of mass (the slug) is rarely used, the direct equivalence between mass in SI units and weight (force) in English units is usually given, as in Appendix C. Thus, 10 tons =  $2 \times 10^4 \text{ lbs}$  is equivalent to the weight of  $(2 \times 10^4 \text{ lb})(0.4536 \text{ kg/lb}) = 9 \times 10^3 \text{ kg}$ .

- 26. INTERPRET** The problem is to find the weight of an object, given its mass and the magnitude of gravitational acceleration.

**DEVELOP** If the mass and the gravitational acceleration are known, the weight can be obtained by using Equation 4.5,  $\vec{w} = m\vec{g}$ . The gravitational acceleration is smaller the farther one is from the Earth's surface.

**EVALUATE** The magnitude of the astronaut's weight on the space station is

$$w = (68 \text{ kg})(0.89 \cdot 9.8 \text{ m/s}^2) = 590 \text{ N}$$

**ASSESS** This would be the weight if the astronaut were somehow standing still at the altitude of the space station. But in fact, the astronaut is in free fall with the space station, so his/her “weight” is zero. That's because an operational definition of weight is the force read on a scale at rest relative to the object being weighed, and the astronaut would float above any scale placed on the space station.

### Section 4.5 Using Newton's Second Law

- 27. INTERPRET** This problem involves kinematics with constant velocity and Newton's second law. We are asked to find the force on the parachute due to air drag. The other force involved is the gravitational force.

**DEVELOP** From kinematics (see, for example, Equation 3.6) we know that a body moving with constant velocity experiences an acceleration of  $a = 0$ . Inserting this into Newton's second law (for constant mass),  $F_{\text{net}} = ma$ , tells us

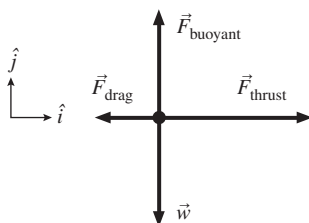
that the net force is  $F_{\text{net}} = 0$ . From the free-body diagram of the situation (see figure below), we see that a zero net force implies that  $F_{\text{drag}} = w$ , from which we can find the drag force exerted by the air.



**EVALUATE** Thus, the drag force is  $F_{\text{drag}} = w = mg = (50 \text{ kg})(9.8 \text{ m/s}^2) = 490 \text{ N}$ .

**ASSESS** Because the acceleration gives the change in velocity over time, a body moving with constant velocity experiences zero instantaneous and zero average acceleration (cf. Equations 3.6 and 2.7).

28. **INTERPRET** This problem involves Newton's second law. There are four forces acting on the boat: two in the horizontal direction and two in the vertical direction. The vertical force pair are the gravitational force and the buoyant force of the water (which hopefully cancel out so that the boat floats on the water). The horizontal forces are the motor's thrust and the drag of the water, which act in opposite directions (see free-body diagram below).



**DEVELOP** Apply Newton's second law to the boat. This gives

$$\vec{F}_{\text{net}} = (F_{\text{thrust}} - F_{\text{drag}})\hat{i} + (F_{\text{buoyant}} - w)\hat{j} = m\vec{a} = m(a_x\hat{i} + a_y\hat{j})$$

Because the boat does not accelerate in the  $\hat{j}$  direction ( $a_y = 0$ ), so  $F_{\text{buoyant}} = w$ . The drag force can be found from the  $\hat{i}$  component of this vector equation, knowing that the mass  $m = 930 \text{ kg}$ ,  $a_x = 2.3 \text{ m/s}^2$ , and  $F_{\text{thrust}} = 3.9 \text{ N}$ .

**EVALUATE** The horizontal component of Newton's second law gives

$$F_{\text{thrust}} - F_{\text{drag}} = ma_x$$

$$F_{\text{drag}} = F_{\text{thrust}} - ma_x = 3900 \text{ N} - (930 \text{ kg})(2.3 \text{ m/s}^2) = 1761 \text{ N} = 1800 \text{ N}$$

to two significant figures. This is the magnitude of the drag force; its direction is  $-\hat{i}$ , so the complete drag force is  $\vec{F}_{\text{drag}} = (-1800 \text{ N})\hat{i}$ .

**ASSESS** As expected, the horizontal component of the drag force is negative, i.e., opposite to the direction of the acceleration.

29. **INTERPRET** This problem involves Newton's second law. The forces acting on the elevator passenger are the gravitational force and the normal force  $F_{\text{elev}}$  that the elevator floor applies on her feet (see free-body diagram below). We are asked to find the latter force.



**DEVELOP** Because this problem involves forces in only one direction, we can dispense with the vector notation.

Apply Newton's second law (for constant mass)  $F_{\text{net}} = ma$  to find the force applied by the floor of the elevator. The

net force is the sum of the forces acting on our passenger, so  $F_{\text{net}} = F_{\text{elev}} - w$  (where  $w = mg$ ), the mass of the passenger is  $m = 52 \text{ kg}$ , and her acceleration is  $a = -2.4 \text{ m/s}^2$ .

**EVALUATE** Newton's second law gives

$$\begin{aligned} F_{\text{net}} &= ma \\ F_{\text{elev}} - w &= ma \\ F_{\text{elev}} &= mg + ma = (52 \text{ kg})(9.8 \text{ m/s}^2 - 2.4 \text{ m/s}^2) = 380 \text{ N} \end{aligned}$$

**ASSESS** Because the elevator accelerates downward, it does not need to support the entire weight of the person, so the force it applies is slightly less than that necessary to counter the gravitational force on the person. What would happen if the elevator accelerated downward at the  $9.8 \text{ m/s}^2$ ? At  $a > 9.8 \text{ m/s}^2$ ?

**30. INTERPRET** We need to use Newton's 2<sup>nd</sup> law to find the lifting force on the plane.

**DEVELOP** There are two forces on the plane: the upward lift provided by the wings and the downward weight from gravity:  $F_{\text{net}} = F_{\text{up}} - mg = ma_{\text{net}}$ , or solving for the lift:  $F_{\text{up}} = m(g + a_{\text{net}})$ . In part (a) the plane holds a constant altitude, so the net acceleration and force must be zero. In part (b), the plane is climbing so the acceleration is positive.

**EVALUATE** (a) When there's no acceleration, the upward force balances the weight:

$$F_{\text{up}} = mg = (560 \text{ t}) \left( \frac{1000 \text{ kg}}{1 \text{ t}} \right) (9.8 \text{ m/s}^2) = 5.5 \times 10^6 \text{ N}$$

(b) When the plane climbs at  $a_{\text{net}} = 1.1 \text{ m/s}^2$ ,

$$F_{\text{up}} = (560 \text{ t}) \left( \frac{1000 \text{ kg}}{1 \text{ t}} \right) (9.8 \text{ m/s}^2 + 1.1 \text{ m/s}^2) = 6.1 \times 10^6 \text{ N}$$

**ASSESS** It obviously takes a lot of force to keep a plane that big in the air. The lift of an airplane is proportional to its wing area. The Airbus A-380 has a wing area of  $845 \text{ m}^2$ , compared to  $541 \text{ m}^2$  for a Boeing 747, which has a smaller mass of 397 metric tons.

**31. INTERPRET** We assume the rocket's acceleration is constant, so we'll need the equations from Chapter 2, Section 4. Once we know the acceleration, we can find the force from the rocket engines using Newton's 2<sup>nd</sup> law.

**DEVELOP** The rocket has to go from rest to  $v = 7200 \text{ km/h}$  in 2 min. We can use Equation 2.7 ( $v = v_0 + at$ ) to find the acceleration. From this we use Equation 4.3 ( $F = ma$ ) to find the force of the rocket and the force on the astronaut.

**EVALUATE** The rocket accelerates at

$$a = \frac{v - v_0}{t} = \frac{7200 \text{ km/h}}{2.0 \text{ min}} = 66.7 \text{ m/s}^2$$

To accelerate a load of 630 Mg, the rocket will need a thrust of

$$F = ma = (630 \times 10^3 \text{ kg})(66.7 \text{ m/s}^2) = 4.2 \times 10^7 \text{ N}$$

During launch, a 75-kg astronaut experiences a force of

$$F = ma = (75 \text{ kg})(66.7 \text{ m/s}^2) = 5.0 \times 10^3 \text{ N}$$

**ASSESS** This is nearly 7 g of acceleration, but astronauts and modern pilots are often trained to handle up to around 9 g without losing consciousness.

**32. INTERPRET** This problem involves kinematics (to find the acceleration of the person), Newton's second law (to find forces acting on the person), and Newton's third law. The forces involved are the gravitational force and the normal force exerted by the floor of the elevator on the person's feet (see free-body diagram from Problem 4.29).

**DEVELOP** Because this is a one-dimensional problem, we can dispense with the vector notation, provided we assign positive values to upward vectors and negative values to downward vectors. The average acceleration is (see Equation 3.5)  $\bar{a} = \Delta v / \Delta t = (-9.3 \text{ m/s}^2) / (2.1 \text{ s}) = -4.38 \text{ m/s}^2$ . The apparent weight  $w_{\text{ap}}$  is simply the force you exert

on the floor of the elevator, which is equal and opposite to the upward force  $F_{\text{elev}}$  ( $w_{\text{ap}} = -F_{\text{elev}}$ ) that the floor exerts on you (Newton's third law).  $F_{\text{elev}}$  and the gravitational force  $w = mg$ , are the two forces that determine your vertical acceleration  $a_y$ . Apply Newton's second law to find your apparent weight and compare it to your actual weight  $w = mg$ .

**EVALUATE** Newton's second law gives

$$F_{\text{net}} = ma$$

$$F_{\text{elev}} + mg = ma$$

$$-w_{\text{ap}} = m(a - g) = m[-4.38 \text{ m/s}^2 - (-9.8 \text{ m/s}^2)] = m(5.43 \text{ m/s}^2)$$

$$w_{\text{ap}} = m(-5.43 \text{ m/s}^2)$$

Comparing the apparent weight to the actual weight gives

$$\frac{w_{\text{ap}}}{w} = \frac{m(-5.43 \text{ m/s}^2)}{m(-9.8 \text{ m/s}^2)} = 55\%$$

Thus,  $w_{\text{ap}}$  is only 55% of the actual weight.

**ASSESS** To see that the expression for  $w_{\text{ap}}$  makes sense, consider the case of free fall. In this limit,  $a = g$  and we have the expected weightless situation,  $w_{\text{ap}} = 0$ .

### Section 4.6 Newton's Third Law

**33. INTERPRET** This problem involves Newton's third law. We are asked to find the third-law force that pairs with the gravitational force from the Earth pulling the elephant toward the Earth.

**DEVELOP** As shown in Figure 4.17, the third-law force that pairs with the Earth's gravitational pull is the gravitational force exerted by the elephant on the Earth, pulling the Earth upward. Apply Newton's third law to calculate this force.

**EVALUATE** Newton's third law gives  $F_{eE} = F_{Ee} = mg = (5600 \text{ kg})(9.8 \text{ m/s}^2) = 55 \text{ kN}$ .

**ASSESS** Note that the magnitudes of the forces in a third-law force pair are equal, but they are oriented in opposite directions.

**34. INTERPRET** This problem involves Newton's third law, Newton's second law, and kinematics. The third-law force pair are the gravitational force the Earth exerts on your friend and the gravitation force your friend exerts on the Earth. Newton's second law allows us to find the acceleration of the objects given the force that acts on them (and their mass). Finally, we will use kinematics to find the displacement of the objects given their acceleration.

**DEVELOP** By Newton's third law, the force the Earth exerts on your friend ( $F_{\text{Ef}}$ ) has the same magnitude as the force your friend exerts on the Earth ( $F_{\text{fE}}$ ) (but is in the opposite direction), so  $F_{\text{Ef}} = F_{\text{fE}}$ . The force exerted by the Earth on your friend is simply her weight, so  $F_{\text{Ef}} = w = mg$ . Use this force in Newton's second law ( $F = ma$ ) to find the accelerations of your friend and of the Earth, then use Equation 2.1,  $x = x_0 + v_0t + at^2/2$ , to find the displacement of each object.

**EVALUATE** From Newton's second law, the magnitude of your friend's acceleration is

$a_f = F_{\text{Ef}}/m_f = m_f g/m_f = g$ . The magnitude of the acceleration of the Earth is  $a_E = F_{\text{fE}}/M_E = F_{\text{Ef}}/M_E = m_f g/M_E$ . By Newton's third law,  $\vec{a}_f$  and  $\vec{a}_E$  point in the opposite directions. If your friend and the Earth both start from rest, the displacement of each is

$$d_f = \frac{1}{2}a_f t^2 = \frac{1}{2}gt^2 \quad (\text{down})$$

$$d_E = \frac{1}{2}a_E t^2 = \frac{1}{2} \frac{m_f g}{M_E} t^2 = \left( \frac{m_f}{M_E} \right) d_f \quad (\text{up})$$

with  $d_f + d_E = 1.2 \text{ m}$ . Solving for  $d_E$  gives

$$d_E = \frac{1.2 \text{ m}}{1 + M_E/m_f} = \frac{1.2 \text{ m}}{1 + (5.97 \times 10^{24} \text{ kg})/(65 \text{ kg})} = 1.3 \times 10^{-23} \text{ m}$$

**ASSESS** The displacement of the Earth is too small to be noticeable; it is about  $10^5$  times smaller than the smallest physically meaningful distances studied to date!

- 35. INTERPRET** This is a one-dimensional problem that involves calculating a force using Hooke's law, and applying Newton's third law to find the force necessary to stretch the spring.

**DEVELOP** Choose a coordinate system in which the extension of the spring is in the positive  $x$  direction. Hooke's law (Equation 4.9) states that a spring will resist compression or extension with a force proportional to the change in the spring's length, or  $F_{sp} = -kx$ , where  $k$  is the spring constant and  $x$  is the extension ( $x > 0$ ) or compression ( $x < 0$ ) of the spring. We are given  $k = 270$  N/m and  $x = 48$  cm = 0.48 m, so we can use Hooke's law to solve the problem.

**EVALUATE** Inserting the given quantities into Hooke's law gives  $F_{sp} = -(270 \text{ N/m})(0.48 \text{ m}) = -130 \text{ N}$ . This means the spring exerts a force in the negative- $x$  direction of 130 N, so by Newton's third law, we must apply a force  $F_{app} = -F_{sp} = 130 \text{ N}$  (i.e., in the positive- $x$  direction).

**ASSESS** If we stretch the spring too far, it will permanently deform and Hooke's law will no longer apply.

- 36. INTERPRET** This is a one-dimensional problem that involves Hooke's law and Newton's third law. We are asked to find the distance a spring with a given spring constant is stretched if we apply a given force to it.

**DEVELOP** Choose a coordinate system in which the applied force is in the positive- $x$  direction. Given the spring force  $F_{sp}$  and the spring constant  $k$ , the length stretched can be calculated by using Hooke's law (Equations 4.9),  $F_{sp} = -kx$ . From Newton's third law, the force applied has the same magnitude as  $F_{sp}$ , but is oriented in the opposite direction, so  $F_{app} = -F_{sp}$ . The problem states that  $F_{app} = 35$  N and  $k = 220$  N/m.

**EVALUATE** Inserting the given quantities into Hooke's law gives

$$x = -\frac{F_{sp}}{k} = \frac{F_{app}}{k} = \frac{35 \text{ N}}{220 \text{ N/m}} = 0.16 \text{ m} = 16 \text{ cm}$$

**ASSESS** Notice that the spring is extended in the positive- $x$  direction, as expected if we apply a force in that direction.

- 37. INTERPRET** This is a one-dimensional problem that involves Hooke's law and Newton's third law. We are asked to find the distance a spring with a given spring constant is stretched if we apply a given force to it.

**DEVELOP** We apply the same reasoning as per Problem 4.36, except that we choose a coordinate system in which the applied force is in the negative- $x$  direction. The problem states that  $k = 340$  N/m and the applied force is the gravitational force (Equation 4.5) on the fish:  $F_{app} = w = mg = -(6.7 \text{ kg})(9.8 \text{ m/s}^2)$ .

**EVALUATE** Inserting the given quantities into Hooke's law gives

$$x = -\frac{F_{sp}}{k} = \frac{F_{app}}{k} = \frac{-(6.7 \text{ N})(9.8 \text{ m/s}^2)}{340 \text{ N/m}} = -0.19 \text{ m} = -19 \text{ cm}$$

Thus the spring stretches 19 cm downward.

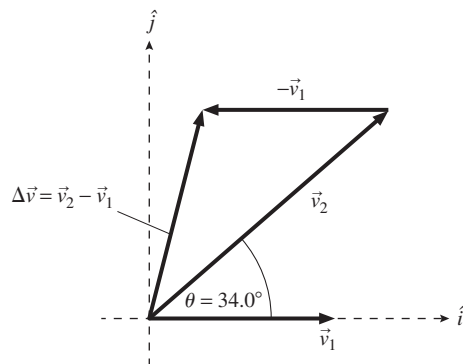
**ASSESS** Notice that the spring is extended in the negative- $x$  direction, as expected if we apply a force in that direction.

## PROBLEMS

- 38. INTERPRET** This problem involves Newton's second law and kinematics. We are asked to find the force required to accelerate an object a given amount, where the acceleration must be calculated from the given mass, initial velocity, and final velocity.

**DEVELOP** Draw a diagram of the situation to define a coordinate system (see figure below). Equation 4.2, which is Newton's second law for constant mass ( $\vec{F}_{net} = m\vec{a}$ ), states that the average force acting on an object is equal to the average acceleration,  $\vec{F}_{net} = m\vec{a}$ . From Equation 3.5  $\vec{a} = \Delta\vec{v}/\Delta t = (\vec{v}_2 - \vec{v}_1)/\Delta t$ , we can calculate the average acceleration, which we can insert into Newton's second law to find the force. We are given the initial velocity,  $\vec{v}_1 = (17.4 \text{ m/s})\hat{i}$  the final velocity,  $\vec{v}_2 = (26.8 \text{ m/s})[\cos(34^\circ)\hat{i} + \sin(34^\circ)\hat{j}] = (22.2 \text{ m/s})\hat{i} + (15 \text{ m/s})\hat{j}$ , the time interval  $\Delta t = 3.41$  s, and the mass  $m = 1.25$  kg.





**EVALUATE** The average acceleration is

$$\bar{\mathbf{a}} = \frac{\mathbf{v}_2 - \mathbf{v}_1}{\Delta t} = \frac{(22.2 \text{ m/s} - 17.4 \text{ m/s})\hat{i} + (15 \text{ m/s})\hat{j}}{3.41 \text{ s}} = (1.408 \text{ m/s}^2)\hat{i} + (4.399 \text{ m/s}^2)\hat{j}$$

Inserting this result into Newton's second law gives

$$\bar{\mathbf{F}}_{\text{net}} = m\bar{\mathbf{a}} = (1.25 \text{ kg})[(1.408 \text{ m/s}^2)\hat{i} + (4.399 \text{ m/s}^2)\hat{j}] = (1.76 \text{ N})\hat{i} + (5.50 \text{ N})\hat{j}$$

The magnitude of this force is  $\bar{F}_{\text{net}} = \sqrt{(1.76 \text{ N})^2 + (5.50 \text{ N})^2} = 5.77 \text{ N}$  and the direction is

$\theta = \text{atan}(F_{\text{net},y}/F_{\text{net},x}) = \text{atan}(5.50 \text{ N}/1.76 \text{ N}) = 72.3^\circ$ , measured CCW from the  $x$  axis.

**ASSESS** Note that the force  $\bar{\mathbf{F}}_{\text{net}}$  is in the same direction as  $\Delta\bar{\mathbf{v}}$ , not the final velocity  $\mathbf{v}_2$ . The latter holds only when the object is initially at rest so that  $\Delta\bar{\mathbf{v}} = \bar{\mathbf{v}}_2$ .

- 39. INTERPRET** This is a one-dimensional problem that involves Newton's second law. We are asked to find an acceleration given the forces acting on a body.

**DEVELOP** We use a coordinate system where the upward direction corresponds to the positive- $x$  direction. For constant mass, Newton's second law is  $\bar{\mathbf{F}}_{\text{net}} = m\bar{\mathbf{a}}$ . The forces acting on your body are the gravitational force,  $\bar{\mathbf{F}}_g = (-mg)\hat{i}$ , and the normal force  $\bar{\mathbf{n}}$  of your seat pushing upward, which is what you feel as your weight ( $n = w = mg$ , see Equation 4.5). We are told that your weight is 70% of its usual value, so we set  $\bar{\mathbf{n}} = 0.7\bar{\mathbf{w}} = (0.7mg)\hat{i}$ . Insert these quantities into Newton's second law to find the plane's acceleration.

**EVALUATE** From Newton's second law, the plane's acceleration is

$$\begin{aligned}\bar{\mathbf{F}}_{\text{net}} &= (-mg)\hat{i} + (0.7mg)\hat{i} = m\bar{\mathbf{a}} \\ \bar{\mathbf{a}} &= (-0.3g)\hat{i} = (-0.3)(9.81 \text{ m/s}^2)\hat{i} = (-2.94 \text{ m/s}^2)\hat{i}\end{aligned}$$

**ASSESS** The airplane accelerates downward, as expected.

- 40. INTERPRET** This is a one-dimensional problem that involves Newton's second law. Two forces are acting on the tree surgeon: the downward gravitational force  $\bar{\mathbf{F}}_g$  and the upward normal force  $\bar{\mathbf{n}}$  from the bucket. We are asked to calculate  $\bar{\mathbf{n}}$  under various conditions.

**DEVELOP** We shall assume that the only vertical forces acting on the tree surgeon are those given; namely, the force of gravity,  $\bar{\mathbf{F}}_g = m\bar{\mathbf{g}}$  acting downward, and the normal force  $\bar{\mathbf{n}}$  of the bucket acting upward. Taking the upward direction to be positive, the net force is  $F_{\text{net}} = -mg + n = ma$ , which gives  $n = m(g + a)$ .

**EVALUATE** For parts (a), (b), and (c), the tree surgeon is not accelerating, so the normal force has the same magnitude as the weight:

$$n = mg = (74 \text{ kg})(9.8 \text{ m/s}^2) = 730 \text{ N}$$

$$\text{(d) If } a = +1.7 \text{ m/s}^2, \quad n = (74 \text{ kg})(9.8 \text{ m/s}^2 + 1.7 \text{ m/s}^2) = 850 \text{ N.}$$

$$\text{(e) For } a = -1.7 \text{ m/s}^2, \quad \text{we have } n = (74 \text{ kg})(9.8 \text{ m/s}^2 - 1.7 \text{ m/s}^2) = 600 \text{ N.}$$

**ASSESS** The upward normal force exerted by the bucket is greatest when the lift is moving upward with a non-zero acceleration. The tree surgeon's feet will feel "heavy."

41. **INTERPRET** This is a one-dimensional problem that involves Newton's second law. We are asked to find the acceleration of the dancer given the forces acting on him.

**DEVELOP** We choose a coordinate system in which the positive  $-y$  direction is upward. For constant mass, Newton's second law is  $\vec{F}_{\text{net}} = m\vec{a}$ , where  $\vec{F}_{\text{net}}$  is the sum of all the forces acting on the dancer. These forces are the gravitational force, which is his weight  $\vec{w} = (-mg)\hat{j}$  (see Equation 4.5) pulling him down, and the normal force of the floor, which we are told is  $\vec{n} = (1.5mg)\hat{j}$ . Sum these to find the net force and his acceleration.

**EVALUATE** Inserting the known quantities into Newton's second law gives

$$\begin{aligned}\vec{F}_{\text{net}} &= m\vec{a} \\ (-mg + 1.5mg)\hat{j} &= m\vec{a} \\ \vec{a} &= (0.50g)\hat{j} = (0.5)(9.8 \text{ m/s}^2)\hat{j} = (4.9 \text{ m/s}^2)\hat{j}\end{aligned}$$

where we have given the answer to two significant figures to match the precision of the input.

**ASSESS** Notice that the acceleration is upward, as expected.

42. **INTERPRET** We're asked for the force needed to bring an object from rest to a certain speed. We will assume that the acceleration is constant.

**DEVELOP** If the speed is attained in a time of  $\Delta t$ , then the acceleration is  $a = v/\Delta t$  (Equation 2.7). If the speed is attained over a distance of  $\Delta x$ , then the acceleration is  $a = v^2/2\Delta x$  (Equation 2.11).

**EVALUATE** (a) The force needed to accelerate the object in  $\Delta t$  is

$$F = ma = \frac{mv}{\Delta t}$$

(b) The force needed to accelerate the object over  $\Delta x$  is

$$F = ma = \frac{mv^2}{2\Delta x}$$

**ASSESS** If we equate these forces, we get  $\Delta x = \frac{1}{2}(v_0 + v)\Delta t$ , which is Equation 2.9.

43. **INTERPRET** This is a one-dimensional problem that involves Newton's second law and kinematics. We are asked to compute the minimum stopping time for the elevator that allows the passengers to remain on the floor.

**DEVELOP** We shall take the positive- $y$  axis as upward. To use Newton's second law,  $\vec{F}_{\text{net}} = m\vec{a}$ , we need to know all the forces acting on the passenger. There are two vertical forces on a passenger, the gravitational force  $\vec{F}_g = \vec{w} = -mg\hat{j}$  downward (see Equation 4.5), and the upward normal force  $\vec{n} = n\hat{j}$  of the floor. The latter is a contact force and always acts in a direction perpendicular to and away from the surface of contact. If the magnitude of this force drops below zero, our passenger will have lost contact with the floor.

**EVALUATE** Inserting the forces into Newton's second law and demanding that  $n > 0$  gives us a condition whereby the passenger stays in contact with the floor:

$$\begin{aligned}\vec{F}_{\text{net}} &= m\vec{a} \\ n - mg &= ma \\ n &= ma + mg > 0 \\ a &> -g\end{aligned}$$

Note that  $m$  is positive. Using Equation 3.8, the time required for the elevator to stop ( $v = 0$ ) from an initial upward velocity ( $v_0 = 5.2 \text{ m/s}$ ) is  $t = (v - v_0)/a = -v_0/a$ . Inserting the limiting condition of  $a = -g$  gives  $t > v_0/g = (5.2 \text{ m/s})/(9.8 \text{ m/s}^2) = 0.53 \text{ s}$ .

**ASSESS** Half a second is a reasonable value. The condition  $n = 0$  is the limit for the person and the floor to remain in contact. As long as the passenger is in contact with the floor, his or her vertical acceleration is the same as that of the floor and the elevator.

44. **INTERPRET** This problem involves the application of Newton's 2<sup>nd</sup> law in two dimensions.

**DEVELOP** The motion is in the  $x$ - $y$  plane, but the object's acceleration  $\vec{a} = (\vec{F}_1 + \vec{F}_2)/m$  is only in the  $y$  direction:  $a_x = 0$ ,  $a_y = (F_{1y} + F_{2y})/m$ . We assume the forces are constant, so the acceleration is constant as well. We can find

the magnitude of this acceleration from the fact that the object goes from  $y_0 = 0$  to  $y = 10.8$  m in 3.00 s. Since it originally only had velocity in the  $x$  direction ( $v_{y0} = 0$ ), Equation 2.10 tells us:

$$a_y = \frac{2(y - y_0)}{t^2}$$

**Evaluate** Solving for the unknown force's magnitude

$$F_{2y} = ma_y - F_{1y} = (2.50 \text{ kg}) \frac{2(10.8 \text{ m})}{(3.00 \text{ s})^2} - 15.0 \text{ N} = -9.0 \text{ N}$$

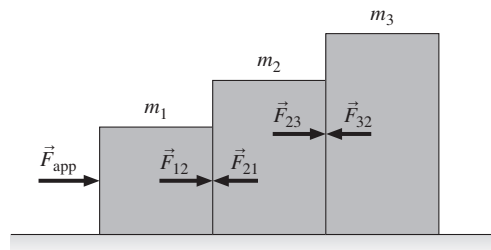
In vector format, our answer is

$$\vec{F}_2 = -9.0 \hat{j} \text{ N}$$

**ASSESS** Because there is no acceleration in the  $x$  direction, the velocity in the  $x$  direction should be constant  $v_x = 1.60$  m/s. Therefore, over  $t = 3.00$  s, the object should move from the origin to  $x = v_x t = 4.80$  m, which agrees with what is reported in the text.

**45. INTERPRET** This problem deals with interaction between different pairs of objects. The key concepts involved here are Newton's second and third laws.

**DEVELOP** Let the three masses be denoted, from left to right, as  $m_1$ ,  $m_2$ , and  $m_3$ , as shown in the figure below.



We take the right direction to be  $+x$ . We are told that the table is frictionless, so the only horizontal forces are the applied force and the contact forces between the blocks. For example,  $\vec{F}_{12}$  denotes the force exerted by block 1 on block 2. Since the blocks are in contact, they all have the same acceleration  $a$ , to the right. Newton's second law can be applied to each block separately:

$$\begin{aligned} \vec{F}_{\text{app}} + \vec{F}_{21} &= m_1 \vec{a} \\ \vec{F}_{12} + \vec{F}_{32} &= m_2 \vec{a} \\ \vec{F}_{23} &= m_3 \vec{a} \end{aligned}$$

**EVALUATE** Adding all three equations and using Newton's third law ( $\vec{F}_{12} + \vec{F}_{21} = 0$ , etc.), one finds

$$\vec{a} = \frac{\vec{F}_{\text{app}}}{m_1 + m_2 + m_3} = \frac{12 \text{ N}}{1.0 \text{ kg} + 2.0 \text{ kg} + 3.0 \text{ kg}} = 2.0 \text{ m/s}^2 \quad (\text{to the right})$$

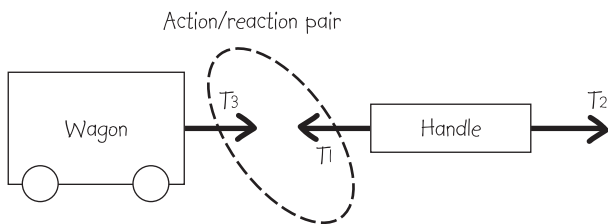
Thus, the force block 2 exerts on block 3 is

$$F_{23} = m_3 a = (3.0 \text{ kg})(2.0 \text{ m/s}^2) = 6.0 \text{ N} \quad (\text{to the right})$$

**ASSESS** You might be tempted to assume that the force on block 3 is just the applied force,  $\vec{F}_{\text{app}}$ , but from that you would wrongly conclude that block 3 is accelerating at  $4 \text{ m/s}^2$ , which would no longer be the same as for the other 2 blocks.

**46. INTERPRET** This problem asks us to consider the tension in the handle when the handle and the wagon are accelerated. The key concepts involved here are Newton's second and third laws.

**DEVELOP** There are two forces on the handle: the tension from the wagon resisting the motion (we'll call this  $\vec{T}_1$ ) and the tension from the child's pulling (we'll call this  $\vec{T}_2$ ). See the figure below.



We'll assume that the only force on the wagon is from the tension in the handle, which we have denoted as  $\vec{T}_3$ . Using the second law, the net horizontal force on the handle and wagon are, respectively,

$$F_{\text{net,h}} = T_2 - T_1 = m_h a$$

$$F_{\text{net,w}} = T_3 = m_w a$$

Where we have assumed that the positive direction is to the right. Since by the third law,  $\vec{T}_1$  and  $\vec{T}_3$  are an action/reaction pair,  $T_1 = m_w a$ . Plugging this in above, we have  $T_2 = (m_w + m_h) a$ .

**EVALUATE** Solving for the tension on both sides of the handle

$$T_1 = (11 \text{ kg})(2.3 \text{ m/s}^2) = 25 \text{ N}$$

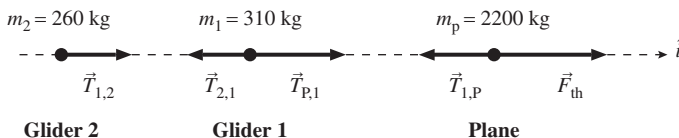
$$T_2 = (11 \text{ kg} + 1.8 \text{ kg})(2.3 \text{ m/s}^2) = 29 \text{ N}$$

These tensions are not equal because if they were, the net force on the handle would be zero and it wouldn't accelerate (contrary to what we are told). One can also argue that the  $T_3 - T_1$  pair is less than  $T_2$  because the former has only has to accelerate the wagon, whereas latter has to accelerate both the wagon and the handle.

**ASSESS** Often times physics problems involving a string (or some other force-transferring object) will assume for simplicity that the string is massless. Under such an approximation, the tensions on the two ends of the string will be equal, since the net force on a massless object is always zero.

47. **INTERPRET** This is a one-dimensional problem that involves Newton's second and third laws. We are asked to find the force applied by the plane, the tension in the ropes, and the net force on the first glider.

**DEVELOP** Make a free-body diagram of the situation (see figure below), on which we have noted all the horizontal forces, the masses of each object, and the coordinate system where the positive- $x$  direction is to the right. Note that we are neglecting the mass of the ropes and any friction forces. From Newton's third law, we know that the third-law force pairs have equal magnitude, but act in opposing directions. Therefore,  $\vec{T}_{1,p} = -\vec{T}_{p,1}$  and  $\vec{T}_{2,1} = -\vec{T}_{1,2}$ . To find the thrust of the propeller, note that the propeller has to accelerate at  $\vec{a} = (1.9 \text{ m/s}^2)\hat{i}$  a total mass  $m_T$  of  $m_T = m_p + m_2 + m_1$ , which we can insert into Newton's second law to find the thrust. Applying Newton's second law to the airplane, glider 1, and glider 2 will also allow us to find the tension in the two ropes, which will then allow us to find the net force on the first glider.



**EVALUATE (a)** The net force on the three-body object is  $\vec{F}_{\text{net}} = \vec{F}_{\text{th}} + \vec{T}_{1,p} + \vec{T}_{p,1} + \vec{T}_{2,1} + \vec{T}_{1,2} = \vec{F}_{\text{th}}$ , where the last equality follows from Newton's third law. Inserting this into Newton's second law gives

$$\vec{F}_{\text{net}} = m_T \vec{a}$$

$$\vec{F}_{\text{th}} = (m_1 + m_2 + m_p) \vec{a} = (2200 \text{ kg} + 310 \text{ kg} + 260 \text{ kg})(1.9 \text{ m/s}^2)\hat{i} = (5.26 \times 10^3 \text{ N})\hat{i}$$

**(b)** Applying Newton's second law to the airplane gives the tension  $\vec{T}_{1,p}$  in the first rope as

$$\vec{F}_{\text{net}} = m_p \vec{a}$$

$$\vec{F}_{\text{th}} + \vec{T}_{1,p} = m_p \vec{a}$$

$$\vec{T}_{1,p} = m_p \vec{a} - \vec{F}_{\text{th}} = (m_2 + m_1) \vec{a} = -(310 \text{ kg} + 260 \text{ kg})(1.9 \text{ m/s}^2)\hat{i} = (-1.08 \times 10^3 \text{ N})\hat{i}$$

where we have used  $\vec{F}_{\text{th}} = (m_1 + m_2 + m_p)\vec{a}$  from part (a). Because the tension force in the rope acts in both directions ( $\pm \hat{i}$ ), we give only the magnitude of the tension force;  $T_1 = 1.1 \times 10^3 \text{ N}$  (to two significant figures).

(c) Applying Newton's second law to the first glider gives the tension  $\vec{T}_{2,1}$  in the second rope as

$$\begin{aligned}\vec{F}_{\text{net}} &= m_1\vec{a} \\ \vec{T}_{p,1} + \vec{T}_{2,1} &= m_1\vec{a} \\ \vec{T}_{2,1} &= m_2\vec{a} - \vec{T}_{p,1} = m_1\vec{a} - (m_2 + m_1)\vec{a} = (-260 \text{ kg})(1.9 \text{ m/s}^2) = (-494 \text{ N})\hat{i}\end{aligned}$$

The tension force in the rope is therefore  $T_2 = 490 \text{ N}$  (to two significant figures).

(d) The net force on the first glider is  $\vec{F}_{\text{net}} = \vec{T}_{2,1} + \vec{T}_{p,1} = (-494 \text{ N} + 1080 \text{ N})\hat{i} = (590 \text{ N})\hat{i}$  (to two significant figures), where we have used  $\vec{T}_{1,p}$  from part (b) and Newton's third law, which gives  $\vec{T}_{p,1} = -\vec{T}_{1,p}$ .

**ASSESS** The tension in the first rope provides the force to accelerate  $m_2$  and  $m_3$ , whereas the tension in the second force accelerates only  $m_3$ .

- 48. INTERPRET** This problem involves applying Newton's second law to find the mass of the rat, given the mass of the cage, the acceleration of the cage + rat system, and the force applied to the cage + rat system.

**DEVELOP** Because this is a one-dimensional, unidirectional problem, we can dispense with vector notation. In this scenario, for constant mass, Newton's second law (Equation 4.3) reads  $F_{\text{net}} = ma$ , where the  $m = m_r + m_c$  is the mass of the rat  $m_r$  plus the mass of the cage  $m_c = 0.320 \text{ kg}$ , and  $F_{\text{net}} = 0.46 \text{ N}$ . Use this formula to find the mass of the cage and the rat, then take the difference to find the mass of the rat.

**EVALUATE** Inserting the given quantities into Newton's second law gives

$$\begin{aligned}F_{\text{net}} &= ma = (m_r + m_c)a \\ m_r &= \frac{F_{\text{net}}}{a} - m_c = \frac{0.46 \text{ N}}{0.40 \text{ m/s}^2} - 0.32 \text{ kg} = 0.83 \text{ kg} = 830 \text{ g}\end{aligned}$$

**ASSESS** A mass of 830 g corresponds to 1.8 lbs on the surface of the Earth. This is a fairly large rat!

- 49. INTERPRET** This is a one-dimensional, unidirectional problem that involves Newton's second law, Hooke's law, and kinematics. We are asked to find the distance traveled by the car in 1 min, given the information necessary to find the acceleration of the car.

**DEVELOP** We must assume that the rope is taught when the truck and car begin to move. Furthermore, because this is unidirectional problem, we will dispense with vector notation. From Hooke's law (Equation 4.9), we know that the elastic towrope exerts a force on the car of magnitude  $F_{\text{sp}} = |-kx|$ , where  $k = 1300 \text{ N/m}$  and  $x = 55 \text{ cm} = 0.55 \text{ m}$ . Insert this force into Newton's second law to find the acceleration of the car (with mass = 1900 kg). Next, use the kinematic Equation 2.10 for constant acceleration,  $x = x_0 + v_0t + at^2/2$ , with  $v_0 = 0$  and  $t = 1 \text{ min} = 60 \text{ s}$  to find the distance  $x - x_0$  traveled by the car.

**EVALUATE** From Newton's second law, the acceleration of the car is

$$\begin{aligned}F_{\text{net}} &= F_{\text{sp}} = |-kx| = ma \\ a &= \frac{|-kx|}{m} = \frac{(1300 \text{ N/m})(0.55 \text{ m})}{1900 \text{ kg}} = 0.376 \text{ m/s}^2\end{aligned}$$

The distance traveled is therefore

$$x - x_0 = \overset{=0}{v_0}t + \frac{1}{2}at^2 = \frac{(0.376 \text{ m/s}^2)(60 \text{ s})^2}{2} = 680 \text{ m}$$

**ASSESS** If the towrope is not taught at  $t = 0 \text{ s}$ , then the car will undergo a non-constant acceleration until the rope becomes taught (because the towrope will be supplying a time-varying force as it stretches). Because we do not have information regarding this period of non-constant acceleration, we are obliged to disregard it and assume that the rope is taught at  $t = 0 \text{ s}$ .

- 50. INTERPRET** This problem involves applying Newton's second law and Hooke's law to a spring that connects two blocks, with a given force applied to one of the blocks. We are asked to find distortion of the spring.

**DEVELOP** Given the spring force  $F_{\text{sp}}$  and the spring constant  $k$ , the length stretched can be calculated by using Hooke's law in Equation 4.9:  $F_{\text{sp}} = -kx$  (the negative sign means that the spring force opposes the distortion). The spring stretches until the acceleration of both masses is the same.

**EVALUATE** The magnitude of the spring tension is given by Hooke's law,  $F_{\text{sp}} = k|x|$ , where  $|x|$  is the stretch of the spring. The horizontal component of Newton's second law applied to each mass gives

$$F_{\text{net}}^{(1)} = F_{\text{app}} - F_{\text{sp}} = m_3 a$$

$$F_{\text{net}}^{(2)} = F_{\text{sp}} = m_2 a$$

as indicated in the sketch below. Adding these two equations, the acceleration of the entire system is

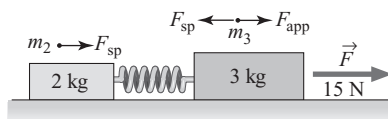
$$a = \frac{F_{\text{app}}}{m_2 + m_3} = \frac{15 \text{ N}}{2.0 \text{ kg} + 3.0 \text{ kg}} = 3.0 \text{ m/s}^2$$

The spring force is therefore

$$F_{\text{sp}} = m_2 a = (2.0 \text{ kg})(3.0 \text{ m/s}^2) = 6.0 \text{ N}$$

Applying Hooke's law, the spring stretches a distance

$$|x| = \frac{F_{\text{sp}}}{k} = \frac{6.0 \text{ N}}{140 \text{ N/m}} = 0.0429 \text{ m} = 4.3 \text{ cm}$$



**ASSESS** The spring force may be rewritten as

$$F_{\text{sp}} = m_2 a = \left( \frac{m_2}{m_2 + m_3} \right) F_{\text{app}}$$

In the limit that  $m_2 \gg m_3$ ,  $F_{\text{sp}} \approx F_{\text{app}}$ . Conversely, if the mass  $m_2$  is negligible, then  $F_{\text{sp}} \approx 0$ , as expected.

51. **INTERPRET** The problem asks us to determine the crumple zone of a car, in order to keep the stopping force on a passenger below a given value.

**DEVELOP** We can think of the crumple zone as the distance,  $\Delta x$ , the car and its passengers continue to travel as they go from the initial speed to zero. We can use Equation 2.11 to relate this distance to the deceleration of the car,

$$v^2 = 0 = v_0^2 - 2a\Delta x$$

Note that we have included a negative sign, so that  $a$  is a positive quantity. Using Equation 4.3, we can derive a limit on the crumple zone from the requirement that the force on the passenger must be less than 20 times his/her weight:

$$F \leq 20F_g \rightarrow a \leq 20g$$

**EVALUATE** The crumple zone is the distance during the crash over which the car comes to rest, so  $\Delta x = v_0^2 / 2a$ . Using the limit on the acceleration, the crumple zone must be at least

$$\Delta x = \frac{v_0^2}{2a} \geq \frac{v_0^2}{2(20g)} = \frac{(70 \text{ km/h})^2}{40(9.8 \text{ m/s}^2)} = 0.96 \text{ m}$$

**ASSESS** This says the car would have to crumple by almost a meter. That's quite a bit, but the pictures of cars in high-speed collisions seem to imply that modern cars can compress by this much.

52. **INTERPRET** This is an application of Newton's 2<sup>nd</sup> law.

**DEVELOP** We're given the acceleration of the frog tongue and its mass, so the force needed is just  $F = ma$ .

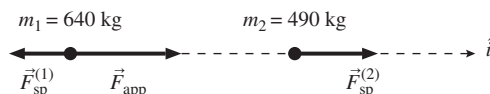
**EVALUATE** Plugging in the given values

$$F = ma = (500 \times 10^{-6} \text{ kg})(250 \text{ m/s}^2) = 0.13 \text{ N}$$

**ASSESS** This is a reasonable amount of force to expect from a frog. The acceleration is so large because the frog's tongue has such a small mass.

- 53. INTERPRET** This problem involves applying Hooke's law to a spring and applying Newton's second law to the two-block system that is connected by the spring. We are asked to find the horizontal force applied to the system given the compression of the spring.

**DEVELOP** Make a free-body diagram of the situation (see figure below). Because the problem is one-dimensional, we will forego the vector notation until the end. From Hooke's law (Equation 4.9) we know that the magnitude of the force exerted on each block by the spring is  $F_{sp} = k|x|$ , where  $k = 8.1 \text{ kN} = 8100 \text{ N}$  and  $|x| = 5.1 \text{ cm} = 0.051 \text{ m}$ . Apply Newton's second law to both blocks and solve for the applied force.



**EVALUATE** Applying Newton's second law to both blocks gives

$$F_{\text{net}}^{(1)} = F_{\text{app}} - F_{\text{sp}} = m_1 a$$

$$F_{\text{net}}^{(2)} = F_{\text{sp}} = m_2 a$$

Solving this, with the help of Hooke's law, for the applied force gives

$$F_{\text{app}} = F_{\text{sp}} + m_1 \left( \frac{F_{\text{sp}}}{m_2} \right) = k|x| \left( \frac{m_1 + m_2}{m_2} \right) = (8100 \text{ N/m})(0.051 \text{ m}) \left( \frac{640 \text{ m} + 490 \text{ m}}{490 \text{ m}} \right) = 950 \text{ N}$$

This force is applied in the direction indicated in the free-body diagram, so  $\vec{F}_{\text{app}} = (950 \text{ N})\hat{i}$ .

**ASSESS** Does the result make sense in the limiting situations? Letting  $m_2 = m_1$  gives  $F_{\text{app}} = 2F_{\text{sp}}$ , which makes sense because the applied force has to accelerate both blocks, whereas the spring only accelerates a single block. If  $m_2 \rightarrow 0$ , then from equations above resulting from Newton's second law, we see that  $F_{\text{app}} = m_1 a$ , as expected.

Finally, if  $m_2 \gg m_1$ , then  $F_{\text{app}} = F_{\text{sp}} = m_2 a$ , which is reasonable if  $m_1$  is very small.

- 54. INTERPRET** The problem involves finding the force exerted on the air by the blade of a helicopter under various conditions. The key concept involved here is Newton's third law.

**DEVELOP** We're asked for the force that the helicopter exerts on the air,  $F_{\text{h} \rightarrow \text{a}}$ . But by Newton's third law, this is equal and opposite to the force that the air exerts on the helicopter,  $F_{\text{a} \rightarrow \text{h}}$ , which is an upward force called the engine's thrust. If we neglect air resistance, the thrust and gravity are the only vertical forces acting on the helicopter, so Newton's second law for the helicopter (positive component up) is:  $F_{\text{a} \rightarrow \text{h}} - mg = ma$ . Therefore, the helicopter exerts a downward force on the air of

$$F_{\text{h} \rightarrow \text{a}} = -F_{\text{a} \rightarrow \text{h}} = -m(g + a)$$

We'll guard the negative sign to remind us that this force is downward.

**EVALUATE** (a) Hovering means zero acceleration,  $a = 0$  (also  $v = 0$ , but the velocity doesn't enter the equation of motion if air resistance is neglected). Therefore, the downward force on the air is

$$F_{\text{h} \rightarrow \text{a}} = -mg = -(4300 \text{ kg})(9.8 \text{ m/s}^2) = -42 \text{ kN}$$

(b) If  $v$  is decreasing downward, then the acceleration must be  $a = 3.2 \text{ m/s}^2$  upward, and

$$F_{\text{h} \rightarrow \text{a}} = -m(g + a) = -(4300 \text{ kg})(9.8 \text{ m/s}^2 + 3.2 \text{ m/s}^2) = -56 \text{ kN}$$

(c) In this case, the acceleration  $a$  is the same as in part (b),  $a = 3.2 \text{ m/s}^2$  upward, so  $F_{\text{h} \rightarrow \text{a}} = -56 \text{ kN}$  as before.

(d) If the speed  $v$  is constant, then  $a = 0$  as the hovering case in part (a), so  $F_{\text{h} \rightarrow \text{a}} = -42 \text{ kN}$  as before.

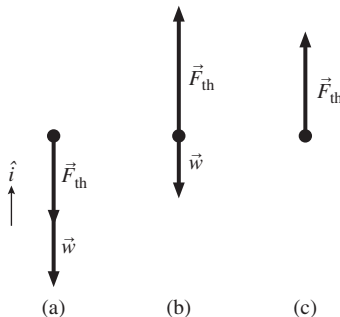
(e) If  $v$  is decreasing upward, then the acceleration points downward:  $a = -3.2 \text{ m/s}^2$ , and

$$F_{h \rightarrow a} = -m(g + a) = -(4300 \text{ kg})(9.8 \text{ m/s}^2 - 3.2 \text{ m/s}^2) = -28 \text{ kN}$$

**ASSESS** The thrust force from the engine is greatest when the helicopter is either moving upward and accelerating, or moving downward and decelerating. In this case, the magnitude of the force exerted on the air is also the greatest, by Newton's third law.

55. **INTERPRET** This problem involves applying Newton's second law to the spacecraft to find the thrust force required to achieve the various accelerations.

**DEVELOP** Draw free-body diagrams of the different situations (see figure below), and apply Newton's second law in each situation to find the requisite thrust. Note that the positive- $x$  direction is upward away from the surface of the Earth. For parts (a) and (b), the weight of the rocket is  $w = mg$  (see Equation 4.5). For part (c), the weight of the rocket is  $w = 0$  because the rocket is in a zero-gravity environment.



**EVALUATE** (a) For the rocket accelerating toward the Earth, Newton's second law gives

$$\begin{aligned}\vec{F}_{\text{net}} &= \vec{w} + \vec{F}_{\text{th}} = m\vec{a} \\ \vec{F}_{\text{th}} &= m\vec{a} - \vec{w} = m\vec{a} - (-mg)\hat{i} = m(\vec{a} + g\hat{i})\end{aligned}$$

for this part,  $\vec{a} = (-1.40g)\hat{i}$ , so

$$\vec{F}_{\text{th}} = m(-1.40g + g)\hat{i} = (-0.40mg)\hat{i}$$

(b) For this part,  $\vec{a} = (1.40g)\hat{i}$ , so

$$\vec{F}_{\text{th}} = m(1.40g + g)\hat{i} = (2.40mg)\hat{i}$$

(c) For this part,  $w = 0$  and  $\vec{a} = 1.40g\hat{i}$ , so

$$\vec{F}_{\text{th}} = m\vec{a} = (1.40mg)\hat{i}$$

**ASSESS** Notice that for part (c), the direction of the acceleration is in the direction of the force, because there are no other forces (i.e., gravity) to modify the direction of the acceleration. Therefore, the choice of  $\hat{i}$  as the direction of the force is arbitrary. To be completely general, we could have written

$$F_{\text{th}} = (1.40mg) \frac{\vec{F}_{\text{th}}}{F_{\text{th}}}$$

where the last factor is simply the unit vector in the direction of the thrust force.

56. **INTERPRET** You are asked to find out how many passengers an elevator can accommodate within the guideline of safety standards. The forces involved here are the downward gravitational force  $\vec{F}_g$  and the upward cable tension  $\vec{T}$ .

**DEVELOP** Assume that the only forces involved are  $\vec{F}_g$  and  $\vec{T}$  in the vertical direction. Newton's second law gives  $\vec{F}_{\text{net}} = \vec{T} + \vec{F}_g = M\vec{a}$ , where  $M$  is the total mass of the elevator and its passengers. Taking  $+y$  to point upward, the equation in component form is  $T - Mg = Ma_y$ , which implies the total mass is

$$T = M(g + a_y)$$

The tension is greatest when the elevator is accelerating upward ( $a_y > 0$ ).

**EVALUATE** For safety's sake, we require that



$$T \leq \frac{2}{3}T_{\max} = \frac{2}{3}(19.5 \text{ kN}) = 13.0 \text{ kN}$$

Assuming the elevator is accelerating upward at its maximum rate ( $a_y = 2.24 \text{ m/s}^2$ ), the total mass is limited to

$$M = \frac{T}{g + a_y} \leq \frac{13.0 \text{ kN}}{9.8 \text{ m/s}^2 + 2.24 \text{ m/s}^2} = 1080 \text{ kg}$$

Subtracting the mass of the elevator (490 kg), the maximum load in terms of kg and 70-kg passengers is:

$$\begin{aligned} \text{Max load} &= 1080 \text{ kg} - 490 \text{ kg} = 590 \text{ kg} \\ &= 590 \text{ kg} \left( \frac{\text{person}}{70 \text{ kg}} \right) = 8 \text{ persons} \end{aligned}$$

**ASSESS** An elevator that accommodates 8 passengers, with a total mass of 590 kg sounds reasonable. Many passenger elevators, depending on their size, can accommodate up to about 2500 kg.

**57. INTERPRET** We're asked if the thrust from these planes' engines could overcome the weight of the planes. We assume the planes are pointed straight up and then calculate the net force.

**DEVELOP** If the planes were trying to fly upwards (like rockets) their wings would not giving them any lift, so the net force would be:

$$F_{\text{net}} = F_{\text{thrust}} - F_g = ma$$

**EVALUATE** Starting with the F-16:

$$F_{\text{net}} = 132 \text{ kN} - (12 \times 10^3 \text{ kg})(9.8 \text{ m/s}^2) = 14.4 \text{ kN}$$

As this is positive, the F-16 can climb vertically at an acceleration of

$$a = \frac{F_{\text{net}}}{m} = \frac{14.4 \text{ kN}}{12 \times 10^3 \text{ kg}} = 1.2 \text{ m/s}^2$$

Now for the A-380:

$$F_{\text{net}} = 1.5 \text{ MN} - (560 \times 10^3 \text{ kg})(9.8 \text{ m/s}^2) = -3.99 \text{ MN}$$

The negative sign here means that A-380 would fall if it didn't have the lift from its wings.

**ASSESS** You might have guessed that a fighter can climb straight up, whereas a commercial jet liner cannot.

**58. INTERPRET** This problem involves using Hooke's law to compute the total force exerted by two springs (of spring constants  $k_1$  and  $k_2$ ) that are connected side-by-side or end-to-end.

**DEVELOP** For two springs connected side-by-side (in "parallel"),  $F_{\text{Tot}} = F_1 + F_2$  and  $x = x_1 = x_2$  where  $F_{\text{Tot}}$  and  $x$  are the (magnitude of the) force and the stretch of the spring combination, and subscripts 1 and 2 refer to the individual springs. When the springs are connected end-to-end (in "series"), the tension is the same in both springs, so  $F_{\text{Tot}} = F_1 = F_2$  (true for "massless" springs), whereas the total stretch of the two springs is the sum of the stretch of each individual spring;  $x = x_1 + x_2$ .

**EVALUATE (a)** For the "parallel" combination, Hooke's law gives  $F_1 = k_1x_1$  and  $F_2 = k_2x_2$ . Therefore, the total force is  $F_{\text{Tot}} = k_1x_1 + k_2x_2 = (k_1 + k_2)x$ .

**(b)** For the "series" combination, Hooke's law gives

$$\begin{aligned} x &= x_1 + x_2 = \frac{F_1}{k_1} + \frac{F_2}{k_2} = F_{\text{Tot}} \left( \frac{1}{k_1} + \frac{1}{k_2} \right) = F_{\text{Tot}} \left( \frac{k_1 + k_2}{k_1 k_2} \right) \\ F_{\text{Tot}} &= \left( \frac{k_1 k_2}{k_1 + k_2} \right) x \end{aligned}$$

**ASSESS** For a system with many springs, we may define an effective spring constant as  $k_{\text{eff}} = F_{\text{Tot}}/x$ . In the parallel case, we have  $k_p = k_1 + k_2$ , whereas in the series case,  $k_s = k_1 k_2 / (k_1 + k_2)$ . Common experience tells us that the parallel combination is stiffer than the series combination, and thus requires a greater amount of force to

stretch by the same amount. One can readily see this by considering the simple case where  $k_1 = k_2 = k$ . The above formulae give  $k_p = 2k$  and  $k_s = k/2$ .

**59. INTERPRET** This problem is an exercise in calculus to derive a more general form of Newton’s second law for one-dimensional situations.

**DEVELOP** From Appendix A, we see that the derivative of a product,  $d(ab)/dt = a(db/dt) + b(da/dt)$ . Apply this rule to Newton’s second law, with  $a = m$  and  $b = v$ .

**EVALUATE** Using the product rule, Newton’s second law for one-dimensional situations is

$$F_{\text{net}} = \frac{d}{dt}(mv) = m \frac{dv}{dt} + v \frac{dm}{dt} = ma + v \frac{dm}{dt}$$

where we have used Equation 2.5,  $a = dv/dt$ , which defines the instantaneous acceleration.

**ASSESS** The result shows clearly that if the mass is constant in time,  $F = ma$ , which is the usual form of Newton’s second law.

**60. INTERPRET** This problem involves Newton’s second law, in its most general form, to find the force necessary to keep a constant velocity while mass changes. We must find the force applied by the engine on the railroad car as the mass of the railroad car changes.

**DEVELOP** We use the result of Problem 59:  $F = ma + v \frac{dm}{dt}$ . The velocity  $v$  is a constant 2.0 m/s, so the acceleration is  $a = 0$ . The car gains mass at a rate of  $\frac{dm}{dt} = 450 \text{ kg/s}$ .

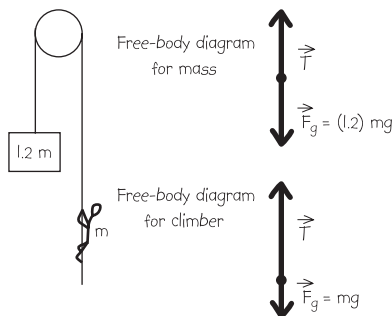
**EVALUATE** Inserting the given quantities into the general form of Newton’s second law gives

$$F = \overset{=0}{ma} + v \frac{dm}{dt} = (2.0 \text{ m/s})(250 \text{ kg/s}) = 500 \text{ N}$$

**ASSESS** Note that no force is required to keep the railroad car itself moving: The  $ma$  term is zero. This 500-N force is the force needed to accelerate the grain so that it is moving at the same speed as the car.

**61. INTERPRET** This problem involves Newton’s second law. We are asked to find the upward acceleration you must have to keep a mass on the other side of the pulley from accelerating. Because the pulley is massless and frictionless, the tension on either side of the pulley is the same.

**DEVELOP** First draw free-body diagrams for the hanging mass and for the climber (see figure below). The mass is not accelerating, so the net force on it must be zero. The climber is accelerating, so the upwards tension force on the climber must be greater than the climber’s weight. We set the tension on the climber’s side equal to the tension on the mass side, and find the resulting acceleration of the climber from Newton’s second law (for constant mass and for one dimension),  $F = ma$ .



**EVALUATE** The net force on the mass is zero, so  $\vec{T} = -\vec{F}_g \Rightarrow T = 1.2mg$ . The net force on the climber is  $\vec{T} + \vec{F}_g = m\vec{a} \Rightarrow T - mg = ma \Rightarrow T = m(g + a)$ . Setting the two tensions equal to each other gives

$$\begin{aligned} 1.2mg &= m(g + a) \\ 1.2g &= g + a \\ a &= 0.2g = (0.2)(9.8 \text{ m/s}^2) = 1.96 \text{ m/s}^2 \end{aligned}$$

**ASSESS** This acceleration is 20% of  $g$ . The mass is 20% more than the mass of the climber. Makes sense, no?

- 62. INTERPRET** This problem is similar to Example 4.5 in the text, except that here the mass is hanging from the spring rather than sitting on top of the spring.

**DEVELOP** We are asked to find the acceleration of the helicopter, but since the mass/spring device moves with the helicopter, the mass's acceleration will be the same as that of the helicopter. The net force on the mass is

$$F_{\text{net}} = F_{\text{spring}} - F_g = -k\Delta y - mg = ma$$

Note that  $\Delta y$  is the distance that the spring is stretched away from its equilibrium. In general this will be negative, as the spring is stretched downward.

**EVALUATE** The acceleration of the helicopter is

$$a = -\frac{k\Delta y}{m} - g$$

**ASSESS** Let's define  $\Delta y_{\text{rest}}$  as the displacement of the spring when the helicopter is at rest ( $a = 0$ ):

$\Delta y_{\text{rest}} = -mg/k$ . Then we can rewrite the equation for the acceleration as

$$a = \frac{g\Delta y}{\Delta y_{\text{rest}}} - g = g \left( \frac{\Delta y}{\Delta y_{\text{rest}}} - 1 \right)$$

If the spring is stretching more (i.e. further downward), then  $|\Delta y| > |\Delta y_{\text{rest}}|$  and  $a > 0$ . In this case, the helicopter is accelerating upwards. The opposite argument can be made for downward acceleration.

- 63. INTERPRET** We are asked to find the acceleration of your reference frame (the airplane) if objects falling with gravitational acceleration appear in your frame of reference to accelerate upward.

**DEVELOP** We choose a coordinate system where the positive- $y$  direction is upward. Because the pretzels are no longer supported by the tray, or anything else, we must conclude that they are accelerating downward at  $g$ . In your frame of reference (i.e., the airplane), they are accelerating upward at  $2 \text{ m/s}^2$ , so the airplane must be accelerating downward even faster than  $g$ . Consider the one-dimensional form of Equation 3.7,  $v = v' + V$ , where  $v$  is the velocity of the pretzel relative to the Earth,  $v'$  is the velocity of the pretzel relative to the airplane, and  $V$  is the velocity of the airplane relative to the Earth. Differentiating this equation with respect to time gives  $a = a' + A$ , where  $a = -g$  is the acceleration of the pretzel relative to the Earth,  $a' = 2.0 \text{ m/s}^2$  is the acceleration of the pretzel relative to the airplane, and  $A$  is the acceleration of the airplane relative to the Earth.

**EVALUATE** From the equation of relative accelerations, we find that  $-g = 2.0 \text{ m/s}^2 + A$ , so  $A = -g - 2.0 \text{ m/s}^2 = -11.8 \text{ m/s}^2$ , or a downward acceleration of  $11.8 \text{ m/s}^2$ .

**ASSESS** This is a downward acceleration that has a larger magnitude than  $g$ . That's what we expected.

- 64. INTERPRET** We are asked to determine whether the stopping force of EMAS is enough to bring a jetliner to rest. This will require the second law and the equations of motion from Chapter 2.

**DEVELOP** The cement blocks provide a force that decelerates the jetliner by  $a = F/m$ . We know the initial velocity of the plane, so the minimum distance of the EMAS to bring the plane to rest ( $v = 0$ ) is

$$\Delta x_{\text{min}} = v_0^2 / 2a$$

where we have used Equation 2.11. If the EMAS is longer than this, it will be able to stop the plane before it plows through all the blocks.

**EVALUATE** Solving for the minimum distance gives

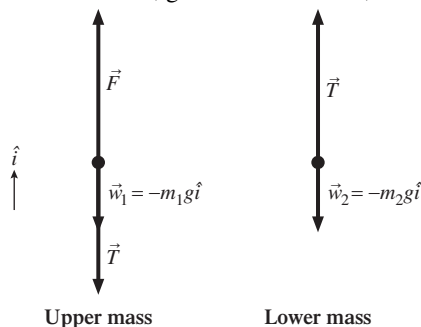
$$\Delta x_{\text{min}} = \frac{mv_0^2}{2F} = \frac{(55 \times 10^3 \text{ kg})(36 \text{ m/s})^2}{2(300 \times 10^3 \text{ N})} = 120 \text{ m}$$

Since the EMAS is 132 m long, the plane will stop with 12 m to spare.

**ASSESS** The plane's initial speed about 80 mi/h, so it seems reasonable that it would take 120 m of concrete blocks to stop the plane.

- 65. INTERPRET** We are asked to find the masses, given accelerations and forces. There are two masses, so we'll solve a system of equations. Newton's second law applies.

**DEVELOP** Begin with a free-body diagram for each mass, as shown in the figure below. Because this is a one-dimensional problem, we will not use vector notation, but instead use negative values for downward vectors and positive values for upward vectors. Apply Newton's second law to both masses to obtain two equations. From these two equations, solve for the two masses, given that  $T = 18 \text{ N}$ ,  $F = 30 \text{ N}$ , and  $a = 3.2 \text{ m/s}^2$ .



**EVALUATE** For mass 1,  $F_{\text{net}} = ma \Rightarrow F - T - w_1 = m_1 a$ , so  $F - T = m_1(g + a)$  Solving for  $m_1$  gives

$$m_1 = \frac{F - T}{g + a} = \frac{30 \text{ N} - 18 \text{ N}}{9.8 \text{ m/s}^2 + 3.2 \text{ m/s}^2} = 0.92 \text{ kg}$$

Similarly for mass 2,  $F_{\text{net}} = ma \Rightarrow T - w_2 = m_2 a \Rightarrow T = m_2(g + a)$

$$m_2 = \frac{T}{g + a} = \frac{18 \text{ N}}{9.8 \text{ m/s}^2 + 3.2 \text{ m/s}^2} = 1.4 \text{ kg}$$

**ASSESS** One way to check our result is to see what the acceleration of the total mass would be with an upward force of 30 N. Using Newton's second law, we find

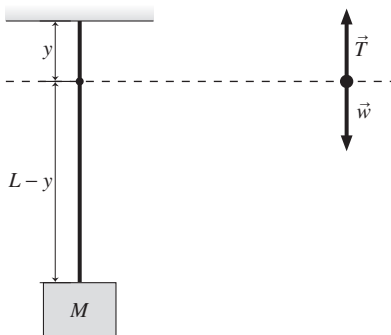
$$F - (m_1 + m_2)g = (m_1 + m_2)a$$

$$a = \frac{F}{m_1 + m_2} - g = \frac{30 \text{ N}}{0.92 \text{ kg} + 1.4 \text{ kg}} - 9.8 \text{ m/s}^2 = 3.2 \text{ m/s}^2$$

as expected.

- 66. INTERPRET** This is a one-dimensional problem involving Newton's second law. We are asked to find an equation describing the tension in a rope where the rope has a uniform mass per unit length. There is also a mass at the end of the rope. We need an equation in terms of  $y$ , where  $y$  is the distance measured downward from the support point and the rope has length  $L$ .

**DEVELOP** Because this is a one-dimensional problem, we will not use vector notation, but use negative values for downward vectors and positive values for upward vectors. Draw a schematic of the situation and a corresponding free-body diagram for an arbitrary point on the rope (see figure below). The mass of the rope below the arbitrary point is  $m_{\text{below}} = m(L \cdot y)/L$ , and the total mass below the arbitrary point is  $M + m_{\text{below}}$ . The weight hanging from the arbitrary point is therefore  $w = (M + m_{\text{below}})g$ . Apply Newton's second law to this arbitrary point and solve for the tension  $T$  of the rope, given that the acceleration of the point is  $a = 0$  because it is stationary.



**EVALUATE** Applying Newton's second law to the arbitrary point gives

$$F_{\text{net}} = ma$$

$$T - w = 0$$

$$T = w = (M + m_{\text{below}})g = Mg + mg\left(\frac{L-y}{L}\right)$$

**ASSESS** To check our answer, we consider some limiting cases. If  $M = 0$  and  $y = 0$ , then the tension should be just the weight of the rope. Inserting these values into the equation above gives

$$T = \overbrace{Mg}^{=0} + mg\left(\overbrace{\frac{L-y}{L}}^{=1}\right) = mg$$

as expected. If the rope is massless, then  $T = Mg$ , which is also what we expect. Finally, if  $y = L$ , then  $T = Mg$ , which is also what we expect.

**67. INTERPRET** We're asked to calculate the amount of jerk on an amusement ride, where jerk is the rate of change in acceleration.

**DEVELOP** The word "rate" implies per time. The jerk is the time derivative of the acceleration. We're given an equation for the force, so the acceleration is just this divided by the mass,  $M$ , of the car and passengers.

**EVALUATE** The acceleration on the amusement ride is

$$a = \frac{F}{M} = \frac{F_0}{M} \sin \omega t$$

The jerk is the time derivative of this:

$$\frac{da}{dt} = \frac{F_0}{M} \omega \cos \omega t$$

The maximum value of the cosine is 1, so the maximum jerk is equal to  $\omega F_0 / M$ .

**ASSESS** If the maximum jerk is too high, some of the passengers may suffer a whiplash.

**68. INTERPRET** You're asked to analyze data from an accelerometer in your laptop.

**DEVELOP** The two forces acting on the laptop are gravity (downwards) and the normal force (upwards) from your lap. The apparent weight is just this normal force, which from Newton's 2<sup>nd</sup> law is equal to:  $n = m(g + a)$ , assuming the positive direction is upwards.

**EVALUATE** The first sign of turbulence is at interval B. The apparent weight is greater than the true weight, so the acceleration is in the upward (positive) direction.

The answer is (a).

**ASSESS** If the plane suddenly goes upwards, everyone on the plane would feel glued to their seats. You and your laptop will feel increases in your apparent weights.

**69. INTERPRET** You're asked to analyze data from an accelerometer in your laptop.

**DEVELOP** The vertical acceleration is registered in how much the apparent weight diverges from the true weight.

**EVALUATE** The apparent weight differs the most from the true weight during interval B.

The answer is (a).

**ASSESS** The change in the weigh during interval D appears to be about half that during interval B.

**70. INTERPRET** You're asked to analyze data from an accelerometer in your laptop.

**DEVELOP** The apparent weight during interval C is just the true weight.

**EVALUATE** If  $n = mg$ , then the vertical acceleration must be zero, or to say it another way, the plane must be moving with constant vertical velocity.

The answer is (d).

**ASSESS** We might be tempted to think the plane has no vertical velocity (at rest with respect to level ground), but the plane can have zero vertical acceleration while still rising or falling steadily.

71. **INTERPRET** You're asked to analyze data from an accelerometer in your laptop.

**DEVELOP** The acceleration in terms of the apparent ( $n$ ) and true ( $mg$ ) weight is:

$$a = g \left( \frac{n}{mg} - 1 \right)$$

**EVALUATE** During interval B, the apparent weight appears to be 5.5 lbs, so the acceleration is  $0.1g \approx 1 \text{ m/s}^2$ . The answer is (b).

**ASSESS** An acceleration of roughly 10% gravity seems reasonable. Compare this to the acceleration experienced by the astronaut in Problem 4.31.