



$$12 \times 10^{-3} \frac{2 \times 10^{-3}}{\frac{1}{60} = 5}$$

$$\frac{3 \times 10^8 \text{ m}}{2 \times 10^{11} \times 10^8} = 2 \times 10^{-3}$$

$$1.5 \times 10^8 \text{ km} = 1.5 \times 10^{11} \text{ m} = \text{AU}$$

$$\text{AU} = 1.5 \times 10^{11} \text{ m}$$

1. An astronomical unit (AU) is the average distance between Earth and the Sun, equals  $1.50 \times 10^8$  km. The speed of light is  $3.0 \times 10^8$  m/s. The speed of light in AU per minute is:

- (A) 0.12 AU/min  
 (B) 8.3 AU/min  
 (C) 7.2 AU/min  
 (D) 0.02 AU/min  
 (E) none of these

$$3 \times 10^4$$

2. As a historical fact, Palestine exported (صدرت) in the year 1939, 15 million boxes of oranges, (a box is 16 kg). According to the prices (وفق أسعار) of this year 2010, the value of the exported oranges (قيمة البيرتقال المصدر) is equivalent to:

$$15 \times 10^6 \times 16 \text{ kg} = 15 \times 10^6$$

- A) \$  $3.0 \times 10^{10}$   
 B) \$  $2.0 \times 10^9$   
 C) \$  $4.0 \times 10^6$   
 D) \$  $1.1 \times 10^7$   
 (E) \$  $1.2 \times 10^8$

$$480 \times 10^5$$

$$48 \times 10^7$$

$$240 \times 10^5$$

$$42 \times 10^7$$

$$24 \times 10^7 \quad 2.4 \times 10^8$$

3. A stone is released from a balloon that is ascending (يُصعد) at a constant speed of 20 m/s. Neglecting air resistance, after 25 s the speed of the stone is:

- A) 320 m/s  
 B) 180 m/s  
 C) 300 m/s  
 D) 280 m/s  
 (E) 230 m/s

$$v - u = at$$

$$0 = 20 - 10t$$

$$20 = 10t$$

$$t = 2$$

$$v = 2 \times 10$$

$$20 \text{ m/s}$$

4. The area under a velocity-time graph represents:

- A) acceleration  
 B) change in acceleration  
 (C) displacement  
 D) change in velocity  
 E) speed

$$v \times t =$$

5. A stone is tied to the end of a string and is moving with constant speed around a horizontal circle with a radius of 2.0 m. If it makes two complete revolutions each second, its acceleration is :

$$F = 2\pi r k \quad a = \frac{v^2}{r} \Rightarrow v = 2\pi Fr$$

$$2 \times 3.14 \times 2 \times 2$$

$$+ 2.56$$

$$25$$

- (A) 316 m/s<sup>2</sup>  
 (B) 158 m/s<sup>2</sup>  
 (C) 220 m/s<sup>2</sup>  
 (D) 247 m/s<sup>2</sup>  
 (E) None of these

6. The inertia of a body tends to cause the body to:

- A) speed up  
 B) slow down  
 C) decelerate due to friction  
 D) fall toward the earth  
 (E) resist any change in its motion

7. A projectile's initial speed is four times <sup>أربعة</sup> ~~(ثلاثة أضعاف)~~ its speed at maximum height. Its launch angle (زاوية الإطلاق):

- A) 78.5°  
 B) 70.5°  
 C) 60.0°  
 (D) 75.5°  
 E) 45.0°

$$v_0 = 4 v_0 \cos \phi$$

$$\frac{1}{4} = \cos^2 \phi$$

~~$$v_0 = 4 v_0 \cos \phi$$~~

$$\frac{v_0}{v_0} = 4 \frac{v_0}{2} \cos \phi$$

$$1 = 4 \cos \phi$$

$$\cos \phi = \frac{1}{4}$$

$$\phi = \cos^{-1}\left(\frac{1}{4}\right)$$

8. The coordinate of a particle in meters is given by  $x(t) = 48t - t^3$ , where the time  $t$  is in seconds. The particle is momentarily stops (تتوقف لحظياً) at  $t =$

- A) 2.0 s  
 B) 3.0 s  
 (C) 4.0 s  
 D) 1.0 s  
 E) None of these

$$v_0 \quad v = 48 - 3t^2$$

$$3t^2 = 48$$

$$t^2 = 16$$

$$t = 4$$

$$\begin{aligned}
 &= 2i - 5j + 4k \\
 &= 4i - 2j + 2k \\
 &8 + 10 + 8 = 26
 \end{aligned}$$

$$A \cdot B = AB \cos \theta$$

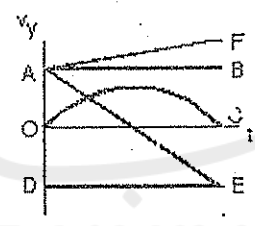
9) The angle between the vectors:  
 $A = 2i - 5j + 4k$  And  $B = 4i - 2j + 2k$

is  $A = 6.7$   $B = 4.89$

- A)  $34^\circ$   
 B)  $80^\circ$   
 C)  $55^\circ$   
 D)  $44^\circ$   
 E) None of these

$$26 = (6.7)(4.89) \cos \theta$$

10. Which of the curves on the graph below best represents  $v_y$  vs.  $t$  for a projectile fired at an angle of  $45^\circ$  above the horizontal?



- A) AE  
 B) DE  
 C) OC  
 D) AB  
 E) AD

11. A 1000-kg airplane moves in straight flight at constant speed. The force of air friction is 1800 N. The magnitude of the net force on the plane is:

- A) 1800 N  
 B) 11800 N  
 C) 2800 N  
 D) zero N  
 E) none of these

$$F_{net} = ma$$

$a = 0$   
 $v_{zer}$

$$V=0$$

$$\int -0.5x^2$$

$$\frac{-0.5x^3}{3}$$

$$V = -\frac{0.5x^3}{3} + 16$$

$$V(x) = -0.25x^3 + 16$$

جامعة بيرزيت  
BIRZEIT UNIVERSITY

2017



2016

مجلس الطلبة

12. Snow is falling vertically at a constant speed of 12 m/s. The angle from the vertical the snow appears to be falling as viewed by the driver of a car traveling on a horizontal road with a speed of 108 km/h is:

- A) 37°
- B) 68°
- C) 59°
- D) 64°
- E) None of these

$V_D$

$$V_{sg} = V_{sp} + V_{pg}$$

$$-12\hat{j} = V_{sp} + 30\hat{j}$$

$$V_{sp} = -30 - 12\hat{j}$$

$12 \downarrow$   
 $\xrightarrow{108} = 30 \text{ m/s}$

13. A 1000-kg elevator is ascending (يصعد) and its speed is increasing at  $3.5 \text{ m/s}^2$ . The tension in the elevator cable (حبل المصعد) is:

- A) 6500 N
- B) 11000 N
- C) 10000 N
- D) 13500 N
- E) None of these

$$T - mg = ma$$
~~$$T - 1000 \times 9.8 = 1000 \times 3.5$$~~
~~$$T - 9.8 \times 10^3 = 3.5 \times 10^3$$~~

$$T = 10 \times 10^3 + 3.5 \times 10^3$$

$$T = 13.5 \times 10^3$$

$$13500$$

14. At a traffic light (إشارة ضوئية), a truck traveling at 40 m/s passes a car at rest. The truck travels at constant velocity and the car accelerates at  $5 \text{ m/s}^2$ . How many seconds will it take for the car to catch up (تلتحق) to the truck?

- A) 9
- B) 16
- C) 15
- D) 11
- E) none of these

$40 \text{ m/s } (v)$

$a = 5 \text{ m/s}^2$

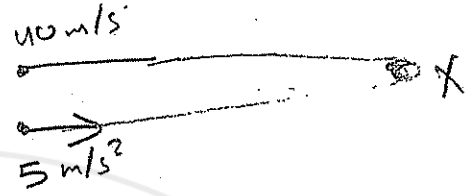
$$x = 40t$$
~~$$x = v_0t + \frac{1}{2}at^2$$~~
~~$$40t = \frac{1}{2} \times 5 \times t^2$$~~

$$40t = \frac{5}{2}t^2$$
~~$$80 = 5t$$~~

$$5 + 2 \cdot 40t$$

$$5 + (t - 8) = 0$$

$$t = 8$$



$$x = 40t$$

$$x = v_0 t + \frac{1}{2} a t^2$$

$$40t = 4.9x + 2$$

$$0 = 4.9t + 2 - 40t$$

$$0 = 5t^2 - 40t$$

$$0 = (5t - 8)$$

$$t = 0, 8$$

2017

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مجلس الطلبة





1. For the following three vectors:

$A = 2i + 3j - 4k$   
 $B = 3i - 5k$   
 $C = 4i - 2j$   
 C.  $(A \times B) =$

$A \times B =$   
 $10j - 9k - 15i + 12j$   
 $= (-15i - 2j - 9k)$   
 ~~$(-15i - 2j - 9k)$~~   
 $-60 + 4$

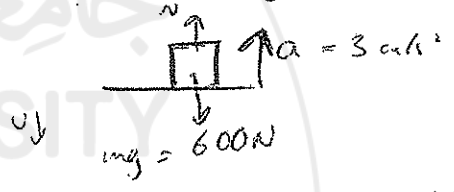
$A \times B = +10j + +9k - 15i + 12j$   
 $= -15i - 2j - 9k$   
 $C(A \times B) = -60i + 4j$   
 $= -60i + 4j$   
 $(4i - 2j)(-60i + 4j)$   
 $-240i^2 - 8j^2$   
 $-240 - 8 = -248$

- A) 36
- B) -56
- C) 64
- D) 56k
- E) zero

2. A girl of mass 60 kg stands on a scale in an elevator. If the elevator is moving down with acceleration of  $3 \text{ m/s}^2$ , the reading of the scale is:

- A) 780 N
- B) 600 N
- C) 820 N
- D) 240 N
- E) 420 N

$-120 = N - 600$   
 $N = 420 \text{ N}$   
 $-ma = N - mg$   
 $-120 = N - 600$   
 $N = 480$

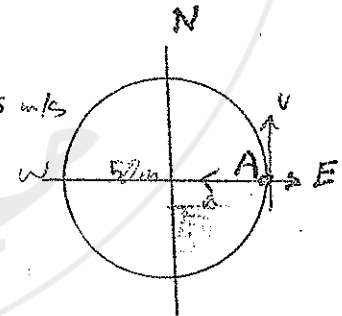


$ma = N - mg \Rightarrow 180 = N - 600$   
 $N = ma + mg = 60(3) + 600 = 780 \text{ N}$

3. A car travels counterclockwise around a flat circle of radius 50 m at a constant speed of 90 km/h. When the car is at point A as shown in the figure, what is the car's acceleration?

- A)  $12.5 \text{ m/s}^2$ , North
- B)  $1.6 \text{ m/s}^2$ , West
- C)  $1.6 \text{ m/s}^2$ , East
- D)  $12.5 \text{ m/s}^2$ , West
- E)  $12.5 \text{ m/s}^2$ , East

$r = 50 \text{ m} =$   
 Constant  $v = 90 \text{ km/h} = 25 \text{ m/s}$   
 $a = 0$   
 $a = \frac{v^2}{r} = \frac{90 \times 90}{50}$



$v = 2\pi r \omega$   
 $a = \frac{v^2}{r} = \frac{25^2}{50} = 12.5 \text{ m/s}^2$

$$R = \text{Height} \times v_0 \cos \theta$$

$$45 = \text{Height} \times 15 \times \cos 53^\circ$$

$$T = 5 \text{ sec}$$

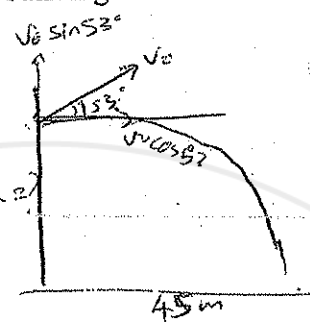
4. A ball is thrown from the edge of the top of a building with an initial velocity of  $15 \text{ m/s}$  at an angle of  $53^\circ$  above the horizontal. The ball strikes the ground a horizontal distance of  $45 \text{ m}$  from the base of the building. Assume that the ground is level. How tall is the building

- A) 75 m
- B) 40 m
- C) 37 m
- D) 65 m
- E) 25 m

$$-h = v_0 \sin \theta t - \frac{gt^2}{2}$$

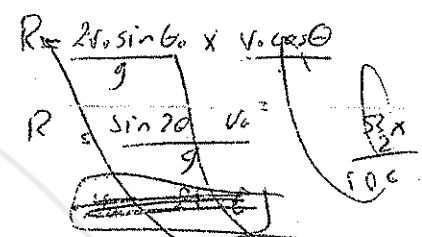
$$-h = 15 \sin 53^\circ \times 5 - \frac{9.8 \times 25}{2}$$

$$-h = -62.6$$



$$v_0 = 15 \text{ m/s}$$

$$\theta = 53^\circ$$



5. If the tension,  $T$ , is  $33 \text{ N}$ ,  $M = 8 \text{ kg}$  and the magnitude of the acceleration,  $a$ , is  $4 \text{ m/s}^2$ , what is the mass,  $m$ , of the suspended object? Assume that all surfaces and the pulley are frictionless?

- A) 5.5 kg
- B) 11 kg
- C) 3.3 kg
- D) 6.6 kg
- E) 2.4 kg

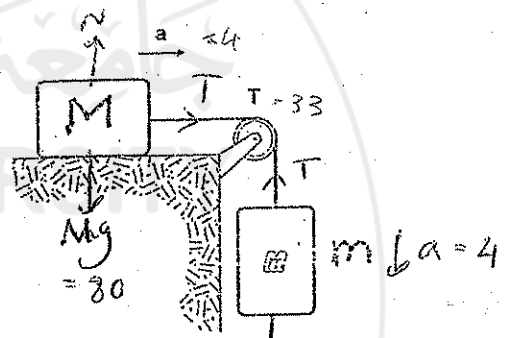
$$-ma = T - mg$$

$$-m \times 4 = 33 - m \times 10$$

$$-4m = 33 - 10m$$

$$+10m$$

$$6m = 33$$



$$x(t) = 2t + t^3$$

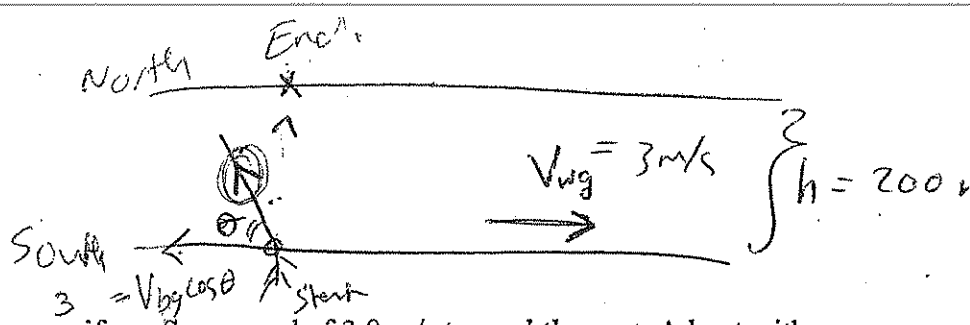
6. The velocity of an object moving in a straight line is given by  $v(t) = 2 + 3t^2$ , where  $t$  is in seconds and  $v$  is in  $\text{m/s}$ . the displacement of the object during the first 2 seconds of motion is:

- A) 20 m
- B) 28 m
- C) 4 m
- D) 12 m
- E) 0 m

$$\text{displacement} = \Delta x = x(2) - x(0)$$

$$= (4 + 8) - (0)$$

$$= 12 \text{ m}$$



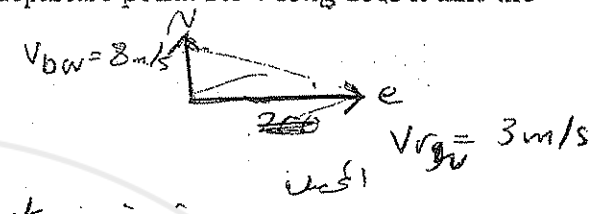
7. A 200-m wide river has a uniform flow speed of 3.0 m/s toward the east. A boat with a speed of 8.0 m/s relative to the water leaves the south bank and heads in such a way that it crosses to a point directly north of its departure point. How long does it take the boat to cross the river?

- A) 17 s
- B) 25 s
- C) 22 s
- ~~D) 27 s~~
- E) 30 s

$v_{br} = ?$   
 $v_{br} = +3\hat{i} + 8\hat{j}$

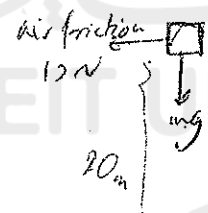
$|v_{br}| = \sqrt{9 + 64} = 8.5 \text{ m/s}$

$v = \frac{x}{t} \Rightarrow 8.5 = \frac{200}{t}$



- A) 5 N
- B) 12 N
- C) 17 N
- D) 7 N
- E) zero

8. A 0.5 kg bird is flying with constant velocity at a height of 20 m. The force of air friction on the bird is 12 N. The net force on the bird is:

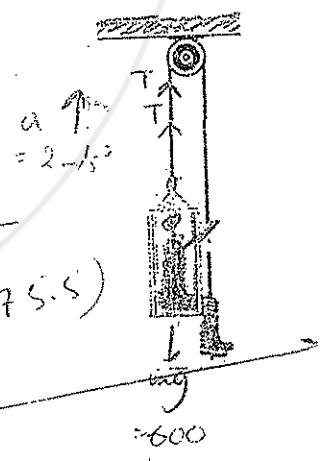


$a = 0$   
 $F_{net} = ma = 0$   
 $-12 + mg = 0$   
 $-12 + 10 = 0$

9. A boy sitting in a chair that hangs from a massless rope, which runs over a massless, frictionless pulley and back down to the boy's hand. The mass of the boy and the chair is 60 kg. With what force he must pull on the rope if he is to rise with an upward acceleration of 2 m/s<sup>2</sup>.

- A) 720 N
- B) 240 N
- C) 300 N
- D) 360 N
- E) 600 N

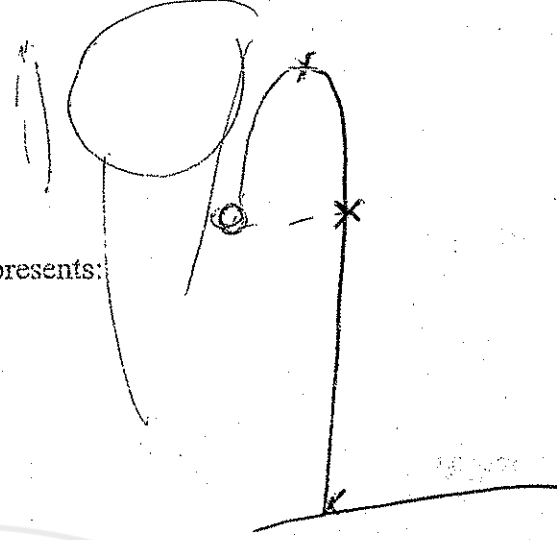
$ma = 2T - mg$   
 $60 \times 2 = 2T - 600$   
 $120 = 2T - 600$



$t = \frac{h}{v_{bg} \sin \theta} = \frac{200}{8 \sin(75.5^\circ)}$

$t = 26.9 \text{ sec}$

$3 = 8 \cos \theta$   
 $\cos \theta = \frac{3}{8}$   
 $\theta = 75.5^\circ$



10. The area under an acceleration-time graph represents:

- A) speed
- B) acceleration
- C) change in acceleration
- D) displacement
- E) change in velocity**

11. The angle between the vectors:

$A = 2i + 4j - 5k$  and  $B = 4i - 5j + 2k$  is:  $A \cdot B = |A||B| \cos \theta$

- A)  $45^\circ$
- B)  $119^\circ$**
- C)  $37^\circ$
- D)  $29^\circ$
- E)  $61^\circ$

$$8 - 20 - 10 = -22 = \sqrt{41+16+25} \sqrt{45} \cos \theta$$

$$8 - 30 = -22 = 45 \cos \theta$$

$$\sqrt{41+16+25} = \sqrt{45}$$

$$\sqrt{16+25+4} = \sqrt{45}$$

12. A balloon is ascending at a constant rate of 15 m/s and is 200 m above the ground when a stone is dropped from it. How long does the stone take to reach the ground?

- A) 16 s
- B) 5 s**
- C) 6.2 s
- D) 3 s
- E) 8 s

$v_0 = 15 \text{ m/s}$

$200 \text{ m}$

$$-200 = -15t - \frac{gt^2}{2}$$

$$-40 = -3t - t^2$$

$$t^2 + 3t - 40 = 0$$

$$(t-5)(t+8) = 0$$

$$t = 5 \text{ sec}$$

$$-200 = 15t - 5t^2$$

$$17 - 3t - 40 = 0$$

$$-3 \pm \sqrt{9 - (4 \times 1 \times -40)}$$

$$\frac{-3 \pm \sqrt{169}}{2} = \frac{13}{2} = 5$$

13. A particle starts from the origin at  $t = 0$  with a velocity of  $(16i - 12j)$  m/s and moves in the xy plane with a constant acceleration of  $a = (3.0i - 6.0j)$  m/s<sup>2</sup>. What is the speed of the particle at  $t = 2.0$  s?

- A) 52 m/s
- B) 39 m/s
- C) 46 m/s
- D) 43 m/s
- E) 33 m/s**

$t = 0 \text{ sec}$

$x = 0$

$v_x = 16 \text{ m/s}$

$a_x = 3 \text{ m/s}^2$

$t = 0$

$x = 0$

$v_y = -12 \text{ m/s}$

$a_y = -6 \text{ m/s}^2$

$v = ?$

at  $t = 2 \text{ s}$

$$v = v_0 + at$$

$$= 16 + 3 \times 2$$

$$= 16 + 6$$

$$= 22 \text{ m/s}$$

$$v = v_0 + at$$

$$= -12 + (-6 \times 2)$$

$$= -12 - 12$$

$$= -24 \text{ m/s}$$

$$V = \sqrt{(22)^2 + (-24)^2}$$

14. A book rests on a table. The reaction force to its weight is:



- A) the force of the Earth on the table
- B) the force of the book on the Earth
- C) the force of the table on the book
- D) the inertia of the book
- E) the force of the Earth on the book

15. Newton's law of universal gravitation is  $F_{\text{grav}} = \frac{Gm_1m_2}{r^2}$

$$F = \frac{GMm}{r^2}$$

Where F is the gravitational force between the masses M and m, r is the distance between them. The SI units of G are:

- A) N.m.kg
- B) N
- C) N.m<sup>-2</sup> kg
- D) N.m<sup>2</sup>.kg<sup>-2</sup>
- E) N.kg<sup>2</sup>

$$N = \frac{G(kg)^2}{m^2}$$

$$\frac{N \cdot m^2}{kg^2} = G$$

16. The position of a particle in meters is given by  $x(t) = 32t - t^4$ , where the time t is in seconds and x in meters. The particle momentarily stops at x =

- A) 31 m
- B) 24 m
- C) 0 m
- D) 48 m
- E) 69 m

$$v = 32 - 4t^3$$

$$0 = 32 - 4t^3$$

$$t^3 = 8$$

$$t = 2 \text{ sec}$$

$$x(2) = 64 - 16$$

$$= 48 \text{ m}$$

17. The U.S.A. national debt in this year 2013 is about \$17 trillion (one trillion =  $10^{12}$ ). If president Obama decides to pay the debt at the rate of \$1000 per second, the time he needs to pay off the debt is:

- A) 540 years
- B) 2 years
- C) 6 months
- D) 1540 years
- E) 54 years

$$\text{debt} = 17 \times 10^{12} \$$$

$$\text{rate} = 1000 \$/\text{sec}$$

$$v = \frac{x}{t} \Rightarrow 1000 \$/\text{sec} = \frac{17 \times 10^{12} \$}{t(\text{sec})}$$

$$t = 1.7 \times 10^{10} \text{ s}$$

$$1 \text{ year} = 1 \times 365.25 \times 24 \times 3600$$

$$1 \text{ year} = 31557600 \text{ sec}$$

$$\text{Page 5} \quad 1.7 \times 10^{10} \text{ sec}$$

$$\underline{540 \text{ year.}}$$



**USEFUL FORMULA and Constants**

$g = 10 \text{ m/s}^2$

**Kinematics equations in linear motion**

1.  $v = v_0 + at$
2.  $x = x_0 + v_0t + \frac{1}{2}at^2$
3.  $v^2 = v_0^2 + 2a\Delta x$
4.  $\bar{v} = \frac{1}{2}(v_1 + v_2)$

**Relative motion**

5.  $\vec{v}_{AB} = \vec{v}_{AC} + \vec{v}_{CB}$

**Projectile motion**

6.  $R = v^2 \sin(2\theta) / g$
7.  $H = v^2 \sin^2(\theta) / 2g$
8.  $y = x \tan(\theta) - gx^2 / 2v_0^2 \cos^2(\theta)$

**Circular motion**

9.  $F = m \frac{v^2}{r}$

**Friction and Drag forces**

10.  $f_k = \mu_k N$
11.  $f_{s,max} = \mu_s N$
12.  $f_D = \frac{1}{2} C_D \rho A v^2$

$\Delta x = \int v dt$   
 $v = -20 \Delta x$   
 $v = -10 t$   
 $100 t^2 = -20 \Delta x$

$100 t^2 = -1$   
 $-20$

$s_{00} = 100 \cdot t + \frac{1}{2} (-10) \cdot t^2$

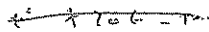
$s_{00} = 100t - 5t^2$

$5t^2 - 100t + 500 = 0 \Rightarrow t^2 - 20t + 100 = 0$

$\Delta x = (100)^2 + 2(-10)(\Delta x)$   
 $(t-20)(t-20)$   
 $t = 20s$

$2 \Delta x = 10000$

$\Delta x = 500$



$v = 100 - 10t$

$t = 10$

$v = 100$       170

$v = v_0 + 10t$       170

170

$110 = \frac{v^2 \sin(20)}{10}$

$1100 = v^2 \sin(20)$

$77,3 = \frac{v^2 \sin^2(20)}{20}$

$1446 = v^2 \sin^2(20)$

$1446 = \sin^2(20) \cdot 1100$

$\frac{1446}{1100} = \sin^2(20)$   
 $1.3145 = \sin^2(20)$

1. Approximately how many times does an average human heart beat (يدق) in a lifetime (مدى الحياة)?

- (a)  $10^5$
- (b)  $10^7$
- (c)  $10^9$
- (d)  $10^{11}$
- (e)  $10^{13}$

2. Express the speed of 4.50 km/h in units of ft/min. (1.00 m = 3.28 ft)

8.6 - 2 m

- (a) 246 ft/min
- (b) 0.246 ft/min
- (c) 165 ft/min
- (d) 82.3 ft/min
- (e) 886 ft/min

5 18 18 km/h → 5 m/s

9.5 → x

$$= \frac{5 \times 9.5}{18} = 1.25 \frac{m}{s} \cdot \frac{3.28 ft}{1 m} \cdot \frac{60}{min}$$

3. A bullet (رصاصة) is fired (أطلقت) straight up with an initial speed of 100.0 m/s. how long will the bullet be in the air?

- (a) 20 s
- (b) 25 s
- (c) 30 s
- (d) 40 s
- (e) 80 s

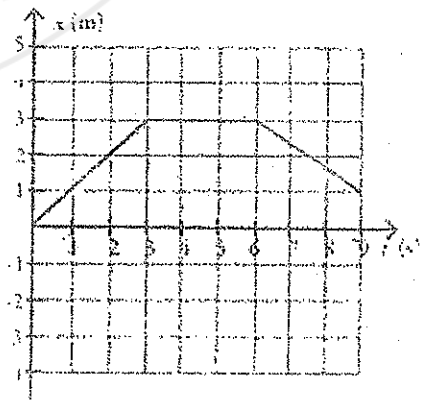
BIRZEIT UNIVERSITY

4. Two objects are thrown from the top of a tall building and experience no appreciable (ملحوظ) air resistance. One is thrown up, and the other is thrown down, both with the same initial speed. Which statement is correct?

- (a) The one thrown up has negative acceleration while the other has positive acceleration.
- (b) The one thrown up has more displacement
- (c) The one thrown down is traveling faster when hitting ground.
- (d) They have the same time of flight.
- (e) They are traveling at the same speed when hitting ground

5. The figure shows the position of an object as a function of time. During the time interval from time  $t=0.0$  s to time  $t=9.0$  s, The length of the path the object followed is

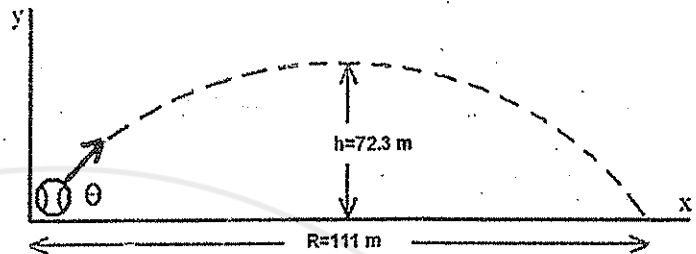
- (a) 1 m
- (b) 3 m
- (c) 5 m
- (d) 6 m
- (e) 9 m





6. A projectile reaches a height of 72.3 m and lands 111 m from the launch point with no air resistance. The angle of launch ( $\theta$ ) is?

- (a)  $20^\circ$   
 (b)  $32^\circ$   
 (c)  $45^\circ$   
 (d)  $69^\circ$   
 (e)  $85^\circ$



7. A 60.0 kg person rides in an elevator while standing on a scale (ميزان). The elevator is traveling downward but slowing at a rate of  $2.00 \text{ m/s}^2$ . The reading on the scale is

- (a) 540 N  
 (b) 480 N  
 (c) 120 N  
 (d) 600 N  
 (e) 720 N

$$\frac{5.20}{5.20}$$

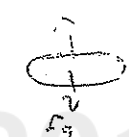


$$mg - N = m \cdot a$$

$$600 = 420$$

8. An object of mass 4.00 kg falls from rest subject to a frictional drag force given by  $F_D = -bv^2$ , where  $v$  is the speed of the object and  $b = 2.5 \text{ N}\cdot\text{s}^2/\text{m}^2$ . What terminal speed will this object reach?

- (a) 1.5 m/s  
 (b) 3.5 m/s  
 (c) 1.0 m/s  
 (d) 4.0 m/s  
 (e) 2.5 m/s



$$mg - F = 4 \cdot a$$

$$40 + 2.5v^2 = 4 \cdot a$$

9. The position vector of a bee (نحلة) is given by  $\vec{r} = -3t^2\hat{i} - (4t + 3)\hat{j} + k$ , where  $r$  is in meters and  $t$  is in seconds. The magnitude of the bee's acceleration is

- (a)  $2 \text{ m/s}^2$   
 (b)  $6 \text{ m/s}^2$   
 (c)  $8 \text{ m/s}^2$   
 (d)  $3 \text{ m/s}^2$   
 (e)  $4 \text{ m/s}^2$

$$\vec{v} = (-6t)\hat{i} - (4)\hat{j} + 0\hat{k}$$

$$\vec{a} = (-6)\hat{i} - 0\hat{j}$$

10. A boat travels at 5.0 km/h in still water (المياه الساكنة) aims at an angle such that it sails straight for the opposite bank of a 300.0 m wide river. If it reaches the opposite side in 0.1 h, what is the speed of the water in the river?

- (a) 3.2 km/h  
 (b) 5.0 km/h  
 (c) 4.0 km/h  
 (d) 2.3 km/h  
 (e) 4.5 km/h

$$\frac{300}{0.1}$$

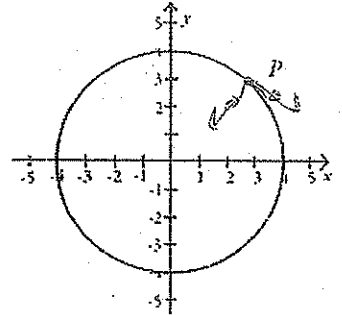
$$\frac{0.3 \text{ km}}{0.1 \text{ h}}$$

$$v = \sqrt{9 + v^2}$$

$$25 = 9 + v^2$$

$$16 = v^2$$

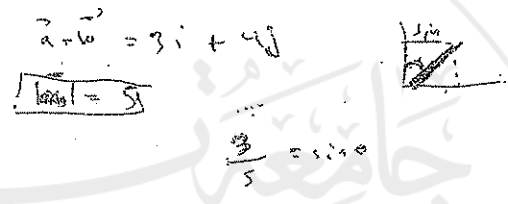
11. Point P in the figure indicates the position of an object traveling at constant speed clockwise around the circle. Which arrow set best represent the directions of the velocity and acceleration of the object at point P respectively (بالترتيب)?



- (a)  $\downarrow, \leftarrow$
- (b)  $\downarrow, \swarrow$
- (c)  $\swarrow, \rightarrow$
- (d)  $\nearrow, \downarrow$
- (e)  $\nearrow, \swarrow$

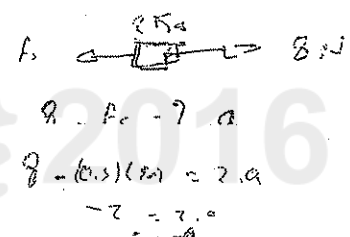
12. Given the two vectors  $\vec{a} = 2\hat{i} + 3\hat{j} + 2\hat{k}$ , and  $\vec{b} = \hat{i} + \hat{j} - 2\hat{k}$ , The angle (in degrees) between  $\vec{a} + \vec{b}$  and the y axis is

- (a) 15
- (b) 37
- (c) 53
- (d) 127
- (e) 143



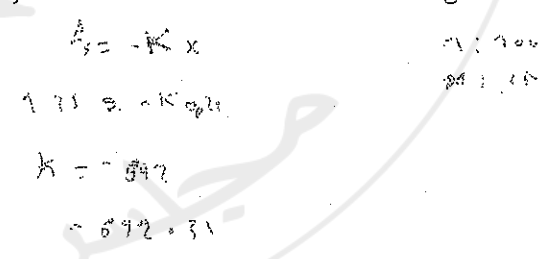
13. A 2 kg wooden block resting on a table is acted upon by a horizontal force of 8 N. If the coefficients of friction  $\mu_s$  and  $\mu_k$  between the block and the table are 0.5 and 0.3 respectively, then the force of friction between the block and the table is?

- (a) 6 N
- (b) 10 N
- (c) 12 N
- (d) 8 N
- (e) 4 N



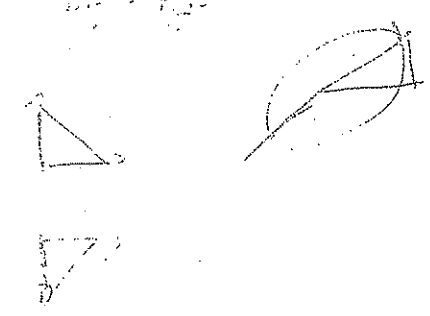
14. A spring stretches by 21.0 cm when a 135 N object is attached. What is the weight of a fish that would stretch the spring by 31.0 cm

- (a) 199 N
- (b) 91.0 N
- (c) 279 N
- (d) 469 N
- (e) 145 N



15. Given the two non-zero vectors  $\vec{A}$  and  $\vec{B}$ . If  $|\vec{A} - \vec{B}| = |\vec{A} + \vec{B}|$ , then the angle between the two vectors  $\vec{A}$  and  $\vec{B}$  is

- (a)  $0^\circ$
- (b)  $30^\circ$
- (c)  $45^\circ$
- (d)  $90^\circ$
- (e)  $180^\circ$

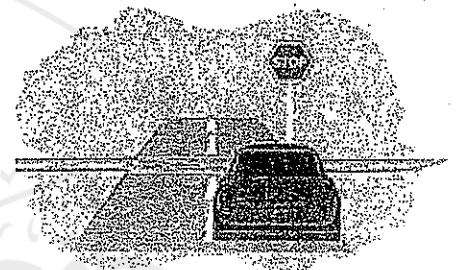


**Essay Problem:**

A car is 55 m from a stop sign and is traveling towards the stop sign at 20.0 m/s. The driver suddenly realizes that she must stop the car. If it takes 0.25 s for the driver to apply the brakes,

- a) what must be the magnitude of the constant deceleration of the car after the brakes are applied so that the car will come to rest at the stop sign?

$$\begin{cases} v = v_0 + at \\ 0 = 20 + a \cdot t \\ a = \frac{-20}{t} \end{cases} \quad \begin{cases} \Delta x = v_0 t + \frac{1}{2} a t^2 \\ 55 = 20t + \frac{1}{2} a t^2 \\ 55 = 20t + \frac{1}{2} \cdot \frac{-20}{t} \cdot t^2 \end{cases}$$



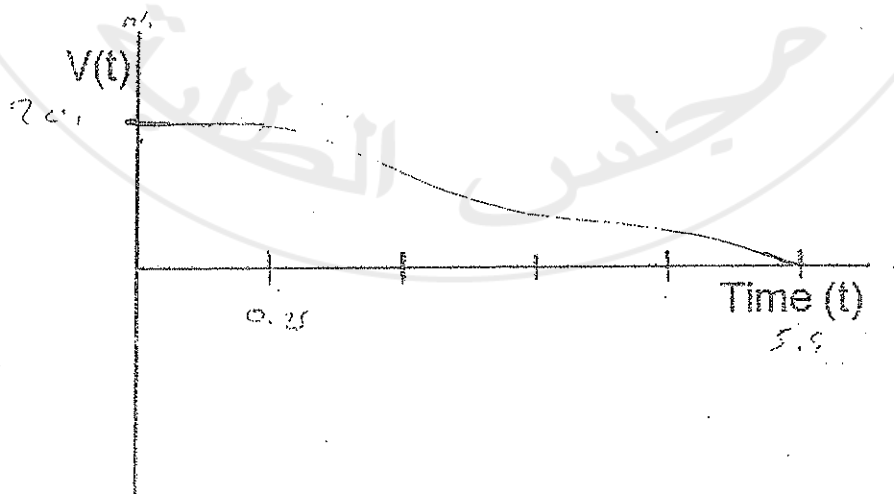
$$\begin{cases} 0 = 20 + a \cdot 0.25 \\ 55 = 20 \cdot 0.25 + \frac{1}{2} a (0.25)^2 \\ 55 = 906 \end{cases}$$

$$\frac{-20}{0.25} = a \quad t = 5.5$$

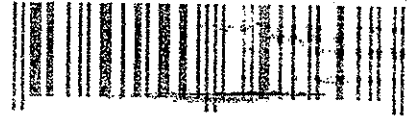
$$a = \frac{-20}{0.25} \text{ m/s}^2$$

$$a = 0.45 \text{ m/s}^2$$

- b) On the adjacent graph paper, plot the velocity of the car as a function of time, indicate (أشر إلى) the starting point, the end point and  $t = 0.25$  seconds on the graph



20



Student Name: Kamal Khlaf

Student No.: 1151626

Please read these instructions and remarks before starting the exam:

- Write your name and student number in the above box.
- Check the class you are in by putting a (✓) mark in the appropriate cell.
- The exam consists of 20 multiple choice problems, answer all of them.
- Mark the correct answers of the multiple choice problems on the answer sheet.
- Turn in the whole exam sheets.

✓	Sec	Instructor Name	Classes Time	✓	Sec	Instructor Name	Classes Time
<input type="radio"/>	1	Sa'Eda Talahmeh	M, W 11:00 - 11:50	<input type="radio"/>	11	Hebah Fatafta	S, W 14:00 - 14:50
<input type="radio"/>	2	Areej A. Rahman	M, W 12:00 - 12:50	<input checked="" type="radio"/>	12	Hebah Fatafta	M, W 08:00 - 08:50
<input type="radio"/>	3	Hazem Abu Sara	S, W 09:00 - 09:50	<input type="radio"/>	13	Hazem Abu Sara	S, W 08:00 - 08:50
<input type="radio"/>	4	Isma'El Badran	S, W 12:00 - 12:50	<input type="radio"/>	14	Areej A. Rahman	M, W 09:00 - 09:50
<input type="radio"/>	5	Ghassan Abbas	M, W 14:00 - 14:50	<input type="radio"/>	15	Ghassan Abbas	M, W 13:00 - 13:50
<input type="radio"/>	6	Ghassan Andoni	M, W 14:00 - 14:50	<input type="radio"/>	16	Areej A. Rahman	M, W 14:00 - 14:50
<input type="radio"/>	7	Sa'Eda Talahmeh	M, W 13:00 - 13:50	<input type="radio"/>	17	Areej A. Rahman	M, W 08:00 - 08:50
<input type="radio"/>	8	Aziz Shawabkeh	M, W 13:00 - 13:50	<input type="radio"/>	18	Isma'El Badran	S, W 09:00 - 09:50
<input type="radio"/>	9	Sharif Ghithan	S, M 13:00 - 13:50	<input type="radio"/>	19	Areej A. Rahman	M, W 15:00 - 15:50
<input type="radio"/>	10	Hebah Fatafta	M, W 12:00 - 12:50	<input type="radio"/>	20	Sharif Ghithan	S, W 12:00 - 12:50

Answer Sheet

(تنقل الإجابات على هذه الصفحة في الربع ساعة الأخيرة قبل تسليم ورقة الامتحان)

	a	b	c	d	e
1	<input type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
	a	b	c	d	e
2	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>
	a	b	c	d	e
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	a	b	c	d	e
4	<input type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
	a	b	c	d	e
5	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>
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	a	b	c	d	e
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	a	b	c	d	e
14	<input type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>

	a	b	c	d	e
15	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
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16	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
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	a	b	c	d	e
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	a	b	c	d	e
19	<input type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
	a	b	c	d	e
20	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>

USEFUL FORMULA and Constants

$g = 10 \text{ m/s}^2$

Kinematics equations in linear motion

1.  $v = v_0 + at$
2.  $x = x_0 + v_0t + \frac{1}{2}at^2$
3.  $v^2 = v_0^2 + 2a\Delta x$
4.  $\bar{v} = \frac{1}{2}(v_1 + v_2)$

Relative motion

5.  $\vec{v}_{AB} = \vec{v}_{AC} + \vec{v}_{CB}$

Projectile motion

6.  $R = v^2 \sin(2\theta) / g$
7.  $H = v^2 \sin^2(\theta) / 2g$
8.  $y = x \tan(\theta) - gx^2 / 2v_0^2 \cos^2(\theta)$

Circular motion

9.  $F = m \frac{v^2}{r}$

$$v_1^2 = v_0^2 + 2g\Delta y$$

$$= 2(10)(125-h)$$

$$= 20(125-h)$$

$$\therefore v_1 = \sqrt{20} \sqrt{125-h}$$

$$v_1 = 2\sqrt{5} \sqrt{125-h}$$

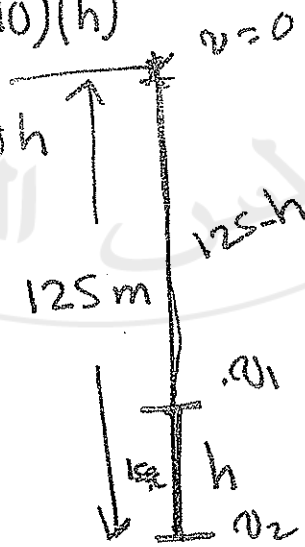
$2 \times (40) = 20(125-h)$   
 $h = 45$

$$v_2^2 = v_1^2 + 2g\Delta y$$

$$\Rightarrow v_2^2 = 20(125-h) + 2(10)(h)$$

$$= 2500 - 20h + 20h$$

$$\Rightarrow v_2 = \sqrt{2500} = 50$$



Bot  $v_2 = v_1 + gt$

$$a = \frac{v_2 - v_1}{t}$$

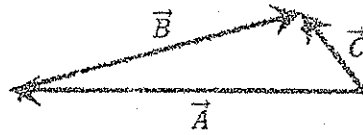
$$\Rightarrow v_2 = v_1 + g = v_1 + 10 \Rightarrow \sqrt{20} \sqrt{125-h} = 40$$

$$\Rightarrow 20(125-h) = 40 \times 40$$

$$125-h = 80$$

1. For the vectors shown in the figure, in terms of vectors  $\vec{A}$  and  $\vec{C}$ , vector  $\vec{B}$  is equal to

- (a)  $\vec{B} = \vec{A} + \vec{C}$
- (b)  $\vec{B} = \vec{A} - \vec{C}$
- (c)  $\vec{B} = \vec{C} - \vec{A}$
- (d)  $\vec{B} = 2\vec{A} - \vec{C}$
- (e)  $\vec{B} = \vec{A} - 2\vec{C}$



$$\vec{A} + \vec{B} = \vec{C}$$

$$\vec{B} = \vec{C} - \vec{A}$$

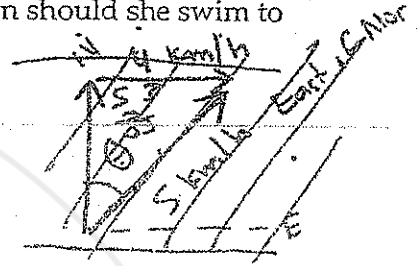
2. A swimmer is able to swim through still water at 5.0 km/h. She wishes to cross the river directly north. The current flows from west to east at 4.0 km/h. In what direction should she swim to make the swimming along a straight line to the north?

- (a) 45° west of north
- (b) 37° west of north
- (c) 45° east of north
- (d) 53° west of north
- (e) 37° east of north

$$\sin \theta = \frac{4}{5}$$

$$\theta = \sin^{-1}(0.8)$$

$$= 53^\circ$$



3. An object is moving to the right, and is experiencing a net force that is directed to the right. The magnitude of the force is decreasing with time. The speed of the object is

- (a) increasing
- (b) decreasing
- (c) remaining constant
- (d) remaining zero all the time
- (e) none of the above

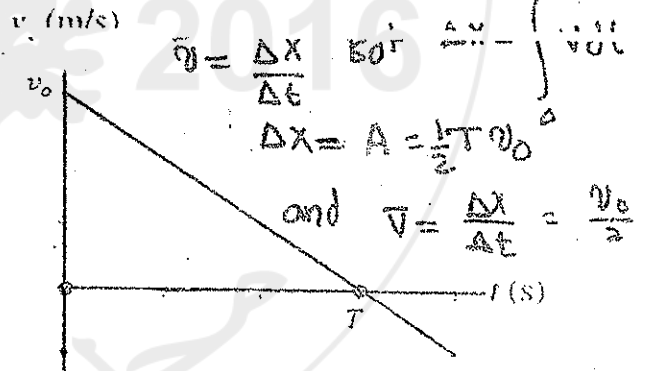


$F = ma$  (a is decreasing)  
But  $v$  is still increasing.

4. The velocity of a particle moving along x-axis is plotted against time. The average velocity of the particle during T seconds is:

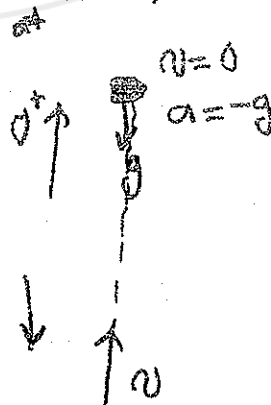
- (a)  $v_0$
- (b)  $v_0/T$
- (c)  $v_0/2$
- (d)  $-v_0/T$
- (e)  $-v_0/2$

$$\Delta x = \frac{1}{2} T v_0$$



5. A ball is shot vertically upward into the air. Which of the following correctly describes the direction of velocity and acceleration of the ball at its maximum elevation?

- (a) Velocity up, acceleration up
- (b) Velocity zero, acceleration zero
- (c) Velocity down, acceleration down
- (d) Velocity zero, acceleration down
- (e) Velocity zero, acceleration up



6. An object has a position vector given by  $\vec{r} = [2.0 + 3.0t]\hat{i} + [3.0 - 2.0t^2]\hat{j}$ , where all quantities are in SI units. What is the magnitude of the velocity of the object at time  $t = 1.0$  s?

- (a) 4.00 m/s  
 (b) 1.00 m/s  
 (c) 2.00 m/s  
 (d) 5.00 m/s  
 (e) 3.50 m/s

$$\vec{v} = \frac{d\vec{r}}{dt} = \frac{d}{dt} [2 + 3t]\hat{i} + (3 - 2t^2)\hat{j}$$

$$= 3\hat{i} - 4t\hat{j}$$

when  $t = 1 \Rightarrow \vec{v} = 3\hat{i} - 4\hat{j} \Rightarrow |\vec{v}| = \sqrt{9+16} = 5$

7. A boy throws a stone from level ground with an initial velocity of 24.0 m/s at 30.0° above the horizontal. How long does it take the stone to land on ground?

- (a) 0.6 s  
 (b) 0.8 s  
 (c) 1.2 s  
 (d) 2.0 s  
 (e) 2.4 s

$v_0 = 24.0$   
 $30^\circ$

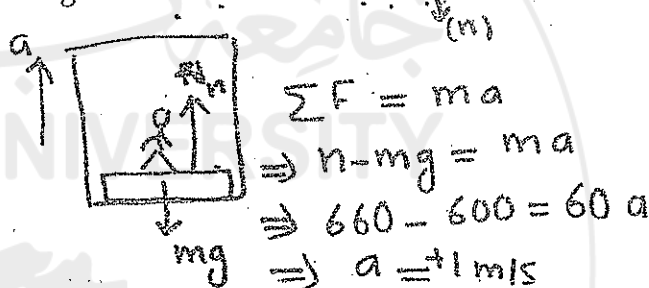
$$v_y = v_0 \sin \theta - gt$$

$$t_m = \frac{v_0 \sin \theta}{g}$$

$$t_f = 2 \left( \frac{v_0 \sin \theta}{g} \right) = \frac{2(24)\left(\frac{1}{2}\right)}{10} = 2.4 \text{ sec}$$

8. A 60 kg girl stands on a scale inside a moving elevator. The scale reads 660 N. The acceleration of the elevator is

- (a) 1.0 m/s<sup>2</sup> downward  
 (b) 1.0 m/s<sup>2</sup> upward  
 (c) 2.0 m/s<sup>2</sup> downward  
 (d) 2.0 m/s<sup>2</sup> upward  
 (e) 0.0 m/s<sup>2</sup>



9. Given the two vector  $\vec{A} = 2\hat{i} + 8\hat{j}$  and  $\vec{B} = 3\hat{i} - \hat{j}$ , the magnitude of vector  $\vec{C} = \vec{A} + 2\vec{B}$  is

- (a) 14.0 units  
 (b) 12.0 units  
 (c) 4.0 units  
 (d) 6.0 units  
 (e) 10.0 units

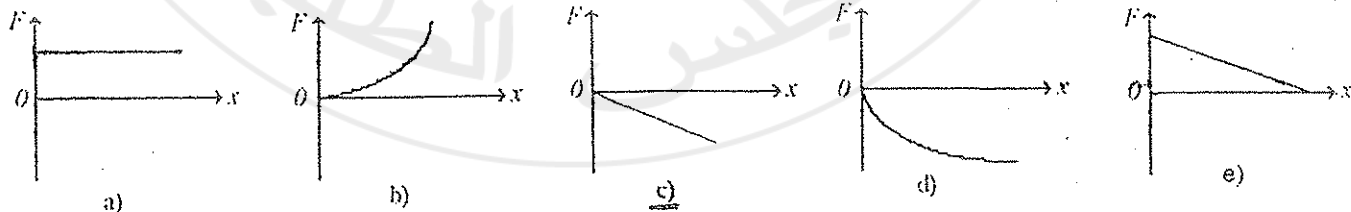
$$\vec{C} = \vec{A} + 2\vec{B}$$

$$= 2\hat{i} + 8\hat{j} + 2(3\hat{i} - \hat{j})$$

$$= 2\hat{i} + 8\hat{j} + 6\hat{i} - 2\hat{j} = 8\hat{i} + 6\hat{j}$$

$$|\vec{C}| = \sqrt{36 + 64} = \sqrt{100} = 10$$

10. Which of the graphs in the figure best illustrates Hooke's Law ( $F$  vs  $x$ )?  $F = -kx$



- (a) Graph a)  
 (b) Graph b)  
 (c) Graph c)  
 (d) Graph d)  
 (e) Graph e)

11. A package is dropped from a balloon moving upward at 15 m/s. If it takes 16.0 s before the package strikes the ground, how high above the ground was the package when it was released if air resistance is negligible?

- (a) 1200 m
- (b) 810 m
- (c) 1520 m
- (d) 1040 m
- (e) 1280 m

~~Ballon~~

$\Delta y = v_0 t + \frac{1}{2} g t^2$

$= -15t + 5t^2$

$\Delta y = -15(16) + 5(16)^2 = 1040 \text{ m}$

$= 0.1 \text{ m}$

12. A fan of radius 10 cm completes one revolution in 3.14 seconds. The acceleration (in  $\text{m/s}^2$ ) of a point on the rim (حافة) of the fan is

- (a) 0.4
- (b) 1.0
- (c)  $0.4\pi$
- (d)  $1.4\pi$
- (e) 9.9

$r = 10 \text{ cm} = 0.1 \text{ m}$

$T = 3.14 \text{ sec/s}$

But  $T = \frac{2\pi r}{v} \Rightarrow T^2 = \frac{4\pi^2 r}{v^2}$

$\Rightarrow T^2 = \frac{4\pi^2 r}{a} \Rightarrow a = \frac{4\pi^2 (0.1)}{T^2} = 0.4\pi$

13. A moving car, when applied the brakes, stopped in a distance of 200 m. If the car applied a constant deceleration of  $1 \text{ m/s}^2$  during the stopping process, then the initial speed of the car was

- (a) 10 km/h
- (b) 20 km/h
- (c) 57 km/h
- (d) 72 km/h
- (e) on km/h

$v^2 = v_0^2 - 2a \Delta x$

$v_0 = 0 \Rightarrow v_0^2 = 2a \Delta x$

$= 2(1)(200) = 400$

$v_0 = 20 \text{ m/s}$

$\frac{20 \text{ m (2000)} (1 \text{ km})}{3.6 \text{ (h)}} \left( \frac{1000 \text{ m}}{1 \text{ km}} \right) = 72 \text{ km/h}$

14. The equation of motion of an object is given by  $x(t) = at - bt^2$ , where  $x$  is in meter,  $t$  in sec, and  $a$  and  $b$  are constants. The units of  $a$  and  $b$  must be respectively

- (a)  $\text{m/s}^2, \text{m/s}^3$
- (b)  $\text{m.s}, \text{m/s}^3$
- (c)  $\text{m/s}, \text{m/s}^2$
- (d)  $\text{m/s}^2, \text{m/s}$
- (e)  $\text{m.s}^2, \text{m.s}^3$

$x = at - bt^2$

$(\text{m}) = \left( \frac{\text{m}}{\text{sec}} \right) (\text{sec}) - \left( \frac{\text{m}}{\text{sec}^2} \right) \text{sec}^2$

15. In going from Birzeit to Ramallah, the number of rotations that a wheel of the car will make during the trip is approximately

- (a)  $5 \times 10^2$  rotation
- (b)  $5 \times 10^3$  rotation
- (c)  $5 \times 10^4$  rotation
- (d)  $5 \times 10^5$  rotation
- (e)  $5 \times 10^6$  rotation

Assume that distance from

Ramallah  $\rightarrow$  Birz. = 20 km

and  $r$  of the wheel = 40 cm =  $0.4 \times 10^{-3} \text{ km}$

\* For the wheel:  $2\pi r = 2\pi (0.4 \times 10^{-3})$

$= 2 \times 3 \times 0.4 \times 10^{-3}$

$= 2.5 \times 10^{-3} \text{ km}$

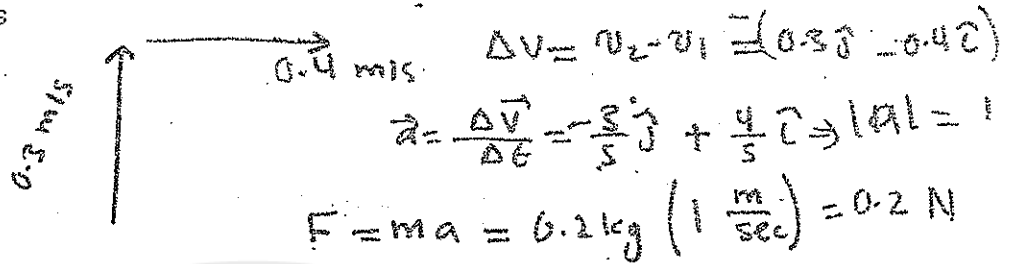
# rotations =  $\frac{20 \text{ km}}{2.5 \times 10^{-3}} = 8 \times 10^3$

$= 5 \times 10^3$



16. A 0.2 kg toy car drives North at a speed of 0.3 m/s, suddenly, after 0.5 seconds, it is found moving East at a speed of 0.4 m/s. The magnitude of the average net force acting on the car during this interval is

- (a) 0.2 N
- (b) 0.5 N
- (c) 1.0 N
- (d) 2.0 N
- (e) 3.0 N



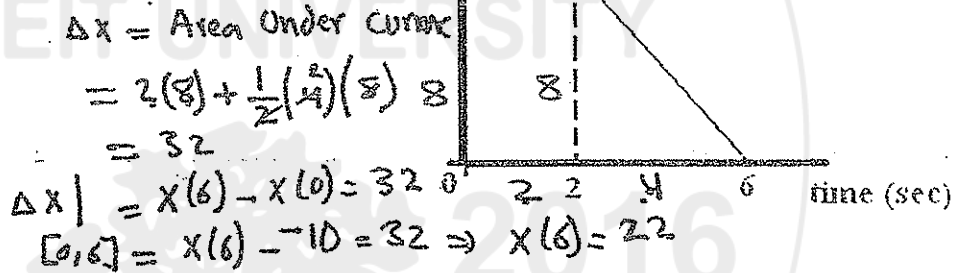
17. The acceleration of an object as a function of time is given by  $a(t) = (3.0 \text{ m/s}^3)t$ , where  $t$  is in seconds. If the object is at rest at time  $t = 0.0$  s, what is the velocity of the object at  $t = 4.0$  s?

- (a) 35.0 m/s
- (b) 0.00 m/s
- (c) 12.0 m/s
- (d) 24.0 m/s
- (e) 48.0 m/s

$a(t) = 3t$  But  $v(0) = 0$   
 $\Delta v = \int_0^4 3t dt = \frac{3}{2}t^2$  Then  
 $v(t) = \frac{3}{2}t^2$   
 $v(4) = \frac{3}{2}(16) = 24$

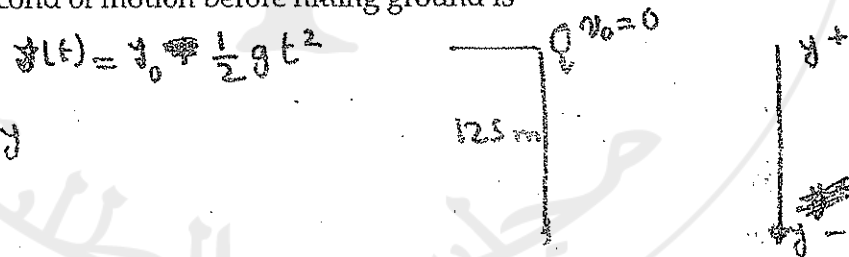
18. The figure shows velocity vs time for a particle that started at  $x = -10 \text{ m}$ . Its position at  $t = 6 \text{ sec}$  is:

- (a) 38 m
- (b) 32 m
- (c) 42 m
- (d) 22 m
- (e) 18 m



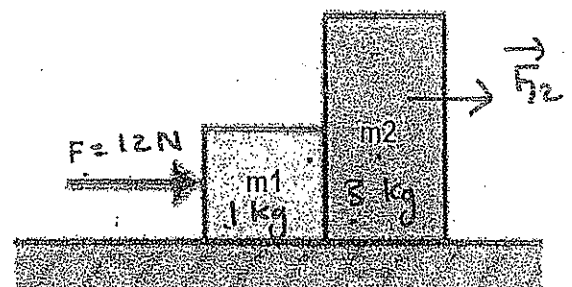
19. A ball is dropped from the top of a building 125 m high. The distance travelled by the ball during the last second of motion before hitting ground is

- (a) 20 m
- (b) 25 m
- (c) 45 m
- (d) 65 m
- (e) 80 m



20. In the adjacent figure, if  $F = 12 \text{ N}$ ,  $m_1 = 1 \text{ kg}$ ,  $m_2 = 3 \text{ kg}$ , then the force acting on  $m_2$  due to  $m_1$  is:

- (a) 0 N
- (b) 12 N
- (c) 3 N
- (d) 5 N
- (e) 9 N



$F = (m_1 + m_2)a$   
 $12 = (1 + 3)a \Rightarrow a = \frac{12}{4} = 3 \text{ m/s}^2$   
 $F_{12} = m_2 a = 3(3) = 9 \text{ N}$

12  
20

+2

Student Name: Waseem Awashra

Student No.: 115.2168

Please read these instructions and remarks before starting the exam:

- Write your name and student number in the above box.
- Check the class you are in by putting a (✓) mark in the appropriate cell.
- The exam consists of 20 multiple choice problems, answer all of them.
- Mark the correct answers of the multiple choice problems on the answer sheet.
- Turn in the whole exam sheets.

✓	#	Instructor	Time	✓	#	Instructor	Time
<input type="checkbox"/>	1	Sa'Eda Talahmeh	MW 12:00 - 12:50	<input type="checkbox"/>	6	Ghassan Andoni	MW 13:00 - 13:50
<input checked="" type="checkbox"/>	2	Sa'Eda Talahmeh	MW 10:00 - 10:50	<input type="checkbox"/>	7	Hebah Fatafta	MW 14:00 - 14:50
<input type="checkbox"/>	3	Ra'Ed Hasan	SW 11:00 - 11:50	<input type="checkbox"/>	8	Aziz Shawabkeh	MW 08:00 - 08:50
<input checked="" type="checkbox"/>	4	Sa'Eda Talahmeh	MW 09:00 - 09:50	<input type="checkbox"/>	9	Hebah Fatafta	MW 15:00 - 15:50
<input type="checkbox"/>	5	Hazem Abu Sara	SW 13:00 - 13:50	<input type="checkbox"/>	10	Ra'Ed Hasan	MW 08:00 - 08:50

Answer Sheet

1 a b c d e

2 a b c d e

3 a b c d e

4 a b c d e

5 a b c d e

6 a b c d e

7 a b c d e

8 a b c d e

9 a b c d e

10 a b c d e

11 a b c d e

12 a b c d e

13 a b c d e

14 a b c d e

15 a b c d e

16 a b c d e

17 a b c d e

18 a b c d e

19 a b c d e

20 a b c d e

## USEFUL FORMULA and Constants

$$g = 10 \text{ m/s}^2$$

### Kinematics equations in linear motion

$$1. v = v_0 + at$$

$$2. x = x_0 + v_0 t + \frac{1}{2} at^2$$

$$3. v^2 = v_0^2 + 2a\Delta x$$

$$4. \bar{v} = \frac{1}{2}(v_1 + v_2)$$

### Relative motion

$$5. \vec{v}_{AB} = \vec{v}_{AC} + \vec{v}_{CB}$$

$$0 = v_0^2 - 5 \times 2 \times 2.5$$

### Projectile motion

$$6. R = v^2 \sin(2\theta) / g$$

$$7. H = v^2 \sin^2(\theta) / 2g$$

$$8. y = x \tan(\theta) - gx^2 / 2v_0^2 \cos^2(\theta)$$

### Circular motion

$$9. F = m \frac{v^2}{r}$$

### Friction and Drag forces

$$10. f_k = \mu_k N$$

$$11. f_{s,max} = \mu_s N$$

$$12. D = \frac{1}{2} C_p A v^2$$

$$D = \frac{1}{2} C_p A v^2$$

$$2d = C_p v^2 A$$

$$v^2 = \frac{2d}{C_p A}$$

$$v = 20 \text{ m/s}$$

$$\Delta x = 50$$

F

$$NMF =$$

$$v^2 = \sqrt{\frac{2d}{C_p A}}$$

$$v_2 = \sqrt{\frac{2d}{C_p A}}$$

$$= \sqrt{\frac{d}{C_p A}}$$

$$v_2^2 = \frac{d}{C_p A} \quad / 2$$

$$2v_2 = v_1$$

$$v_2 = \frac{1}{2} v_1$$

$$v_1^2 = \frac{2d}{C_p A}$$

$$v_1 = \frac{2v_2}{2}$$

1. An object is moving, uniformly, in a circular path of radius 10 cm completes one revolution in  $\pi$  seconds. The acceleration of the object is

- (a)  $0.4 \pi \text{ m/s}^2$
- (b)  $1.0 \text{ m/s}^2$
- (c)  $0.4 \text{ m/s}^2$  ✓
- (d)  $1.4 \pi \text{ m/s}^2$
- (e)  $9.9 \text{ m/s}^2$

$r = 0.1 \text{ m}$   
 $t = \pi$   
 $a = \frac{v^2}{r}$   
 $v = \frac{2\pi r}{t}$   
 $= \frac{2 \times 0.1 \times \pi}{\pi}$   
 $v = 0.2$   
 $a = \frac{(0.2)^2}{0.1}$

2. A vector of magnitude 3 units is added to another vector of magnitude 4 units. The resultant vector can't have a magnitude

- (a) = 1 unit
- (b) = 2 units
- (c) < 3 units
- (d) = 5 units ✓
- (e) > 7 units ✓

$A = 3, B = 4$   
 $A + B = 10$

3. A banked circular road of radius 49 meters is tilted at an angle of 22 degrees. Assuming no friction between the road and the tires of the car, the maximum speed that the car can have without skidding out of the road is about

- (a) 20 km/h
- (b) 25 km/h
- (c) 30 km/h
- (d) 50 km/h ✓
- (e) 70 km/h

$r = 49 \text{ m}, \theta = 22^\circ$   
 $= 14 \times 3.6$   
 $50 \text{ km/h}$   
 $v_{\text{max}} = \sqrt{\tan 22^\circ \times r \times g}$   
 $= \sqrt{49 \times 10 \times \tan 22^\circ}$   
 $= 14 \text{ m/s}$

4. If the effective area of a sky diver is doubled (becomes 2 times as the original area), then compared with the original terminal speed, her new terminal speed will be

- (a) doubled ✗
- (b) Half as much ✓
- (c) 1.73 times as much
- (d) 0.71 times as much
- (e) The same

$a_2 = 2a_1$   
 $V_2 = \frac{1}{2} V_1$

5. A small bird starts from rest flies in a horizontal circle of radius  $\frac{10}{2}$  meters. If it increases its speed at the rate of  $3.0 \text{ m/s}^2$ , its acceleration when it completes one turn is approximately

- (a)  $6.0 \text{ m/s}^2$
- (b)  $1.0 \text{ m/s}^2$
- (c)  $3.0 \text{ m/s}^2$  ✓
- (d)  $4.0 \text{ m/s}^2$
- (e)  $7.0 \text{ m/s}^2$
- (f)  $N > N$

$x_0 = 0$   
 $v_f = v_0 + at$   
 $a = \sqrt{a_c^2 + a_t^2}$   
 $a_t = 3 \text{ m/s}^2$   
 $a_c = \frac{v^2}{r}$   
 $r = \frac{10}{2}$   
 $v = \frac{10}{2}$   
 $v^2 = 2 \times 2 \times \frac{10}{2} = 10$   
 $a_c = \frac{10}{\frac{10}{2}} = 2$   
 $a = \sqrt{2^2 + 3^2} = \sqrt{13} \approx 3.6$

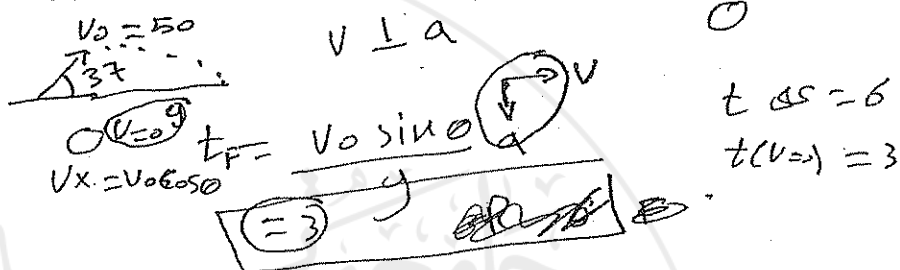
6. The equation of motion of an object is given by  $x(t) = bt + ct^3$ , where  $x$  is in m,  $t$  in sec,  $b$  and  $c$  are constants. The units of  $b$  and  $c$  must be respectively

- (a) m/s, m/s<sup>3</sup>
- (b) m.s, m/s<sup>3</sup>
- (c) m/s, m/s<sup>2</sup>
- (d) m/s<sup>2</sup>, m/s
- (e) m.s<sup>2</sup>, m.s<sup>3</sup>

$$\begin{aligned} x &= bt \\ m &= b s \\ b &= \frac{m}{s} \end{aligned} \quad \left| \quad \begin{aligned} ct^3 &= m \\ c s^3 &= m \\ c &= \frac{m}{s^3} \end{aligned}$$

7. A ball is thrown with initial velocity of 50 m/s at an angle  $\theta = 37^\circ$  with the horizontal. The time needed by the ball to have its velocity perpendicular to its acceleration is:

- (a) 1.5 seconds  $\times$
- (b) 4.5 seconds  $\times$
- (c) 3.0 seconds  $\checkmark$
- (d) 6.0 seconds
- (e) 9.0 seconds  $\times$



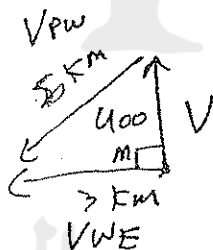
8. The acceleration of an object as a function of time is given by  $a(t) = 2.0 t \text{ m/s}^2$ , where  $t$  is in seconds. If the object is at rest at time  $t = 0.0 \text{ s}$ , then the velocity of the object at time  $t = 5.0 \text{ s}$  is?

- (a) 45.0 m/s
- (b) 0.00 m/s
- (c) 25.0 m/s  $\checkmark$
- (d) 10.0 m/s
- (e) 125.0 m/s

$$\begin{aligned} t_0 = 0 \quad \int a &= v \\ t^2 \Big|_0^t & \\ v &= t^2 \end{aligned}$$

9. A swimmer is able to swim through still water at 5.0 km/h. She wishes to cross directly to the north a 400 m wide river. The current flows from west to east at 3.0 km/h. how long does it take her to cross the river?

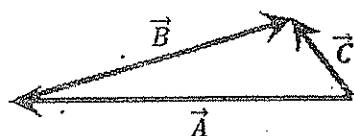
- (a) 0.1 hour  $\checkmark$
- (b) 0.3 hour
- (c) 0.4 hour
- (d) 0.5 hour
- (e) 0.2 hour



$$\begin{aligned} 25 &= v^2 + 9 \\ v^2 &= 25 - 9 \\ v &= 4 \end{aligned} \quad \left| \quad \begin{aligned} v &= \frac{400}{t} \\ a &= \frac{400}{t} \\ \frac{9}{1} &= \frac{0.4}{t} \\ 4t &= \frac{4}{10} \\ t &= \frac{1}{10} \end{aligned}$$

10. For the vectors shown in the figure, which statement is true

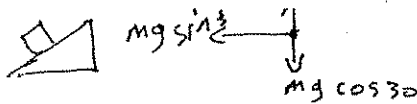
- (a)  $\vec{c} = \vec{A} - 2\vec{B}$
- (b)  $\vec{c} = \vec{A} + \vec{B}$   $\checkmark$
- (c)  $\vec{A} = 2\vec{c} - \vec{B}$
- (d)  $\vec{c} = \vec{B} - \vec{A}$
- (e)  $\vec{c} = \vec{A} - \vec{B}$



$$\begin{aligned} B + A &= C \\ C &= \end{aligned}$$

$$mg \sin 30 = ma$$

$$a = 10$$



$$N = mg$$

11. A wooden block starts from rest on a smooth inclined plane which makes an angle of 30 degrees with the horizontal. The speed of the block after it goes 2.5 m down the incline is

- (a) 5 m/s
- (b) 2 m/s
- (c) 10 m/s
- (d) 12 m/s
- (e) 15 m/s

$$V = V_x \cos 30 + V_y \sin 30$$

$$= V_x \frac{4}{5} + \frac{3}{5} V_y$$

$$2.5 = (0 + V)t$$

$$2.5 = Vt \quad V = \frac{2.5}{t}$$

12. A 4.0-kg mass attached to the end of a string swings in a vertical circle of radius 2.0 m. When the mass is at its highest point, the speed of the mass is 5.0 m/s. At this instant what is the magnitude of the tension in the string?

- (a) 10 N
- (b) 50 N
- (c) 90 N
- (d) 120 N
- (e) 150 N

$$m = 4, r = 2, v = 5$$

$$a = \frac{v^2}{r} = \frac{25}{2} = 12.5$$

$$a = \frac{v^2}{r}$$

$$T - mg = m \times \frac{v^2}{r}$$

$$T - 4 \times 10 = \frac{4}{2} \times 25$$

$$T - 40 = 50$$

$$T = 90 \text{ N}$$

13. A boy runs North at a speed of 7.0 m/s, then East at 7.0 m/s. If it took the boy 1.0 second to change his direction, what is the magnitude and direction of the average acceleration of the boy?

- (a) 10 m/s<sup>2</sup>, South-East
- (b) 10 m/s<sup>2</sup>, North-East
- (c) 7 m/s<sup>2</sup>, South-East
- (d) 7 m/s<sup>2</sup>, South-West
- (e) 14 m/s<sup>2</sup>, South-West

$$v = 7\hat{i} + 7\hat{j}$$

$$a = \frac{\Delta v}{\Delta t}$$

$$a = \frac{7\hat{i} - 7\hat{i}}{1} = -7\hat{i}$$

$$a = 7 \text{ m/s}^2 \text{ South-East}$$

14. An object starts at the origin, has an initial velocity  $\vec{v}_i = (3\hat{i} - 4\hat{j})$  m/s, and has a constant acceleration  $\vec{a} = (-1\hat{i} + 4\hat{j})$  m/s<sup>2</sup>, the maximum positive x-coordinate that the object reached is

- (a)  $x_{\max} = 3.0$  m
- (b)  $x_{\max} = 4.5$  m
- (c)  $x_{\max} = 1.5$  m
- (d)  $x_{\max} = 0.5$  m
- (e)  $x_{\max} = 6.0$  m

$$a = -1$$

$$v_f = v_0 + at$$

$$0 = 3 - 1t \quad t = 3$$

$$dx = \frac{1}{2}(v_0 + v_f)t$$

$$dx = \frac{1}{2}(3 + 0)3 = 4.5$$

15. A car is driving along a straight horizontal road at a speed of 20.0 m/s. The driver applies the brakes and the car comes to a rest uniformly in a distance of 50 m. What was the coefficient of kinetic friction between the wheels of the car and the road?

- (a) 0.30
- (b) 0.25
- (c) 0.50
- (d) 0.40
- (e) 0.60

$$v = 20 \text{ m/s}, dx = 50$$

$$F_k = F = \frac{dx}{t}$$

$$dx = vt$$

$$20 = \frac{50}{t} \quad t = 2.5$$

$$F_k = F = ma$$

$$N \mu k = ma$$

16. The number of table tennis balls that can fit inside a one cubic meter barrel is approximately

- (a)  $2 \times 10^6$
- (b)  $2 \times 10^2$
- (c)  $2 \times 10^4$
- (d)  $2 \times 10^8$
- (e)  $2 \times 10^9$

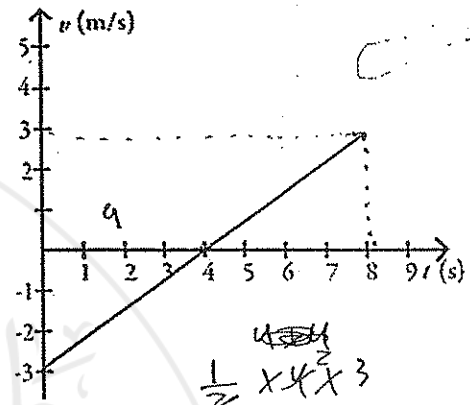
$\frac{3}{4} \pi r^3 = 1 \text{ m}^3$

2.94375

$\Delta n = \frac{1 \text{ m}^3}{8}$

17. The motion of a particle along the x-axis is described in the velocity versus time graph shown in the figure. If the particle starts at  $x=0$ , then the maximum distance reached in the negative x-direction is

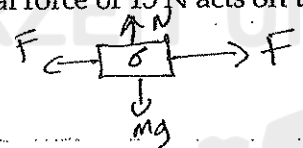
- (a) 3 m
- (b) 4 m
- (c) 8 m
- (d) 6 m
- (e) 2 m



$\frac{1}{2} \times 4 \times 3 = 6 \text{ m}$

18. An object of mass  $M = 6 \text{ kg}$ , rests on a horizontal rough surface that has  $\mu_s = 0.3$  and  $\mu_k = 0.2$ . An applied horizontal force of  $15 \text{ N}$  acts on the object. The magnitude of the frictional force is:

- (a) 18 N
- (b) 25 N
- (c) 9 N
- (d) 32 N
- (e) 15 N



$mg = N \Rightarrow N = 60$

$F_s = \frac{3}{10} \times 60 = 18$

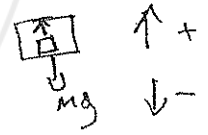
$F - f_s = ma$   
 $15 - \quad = \quad$

$F_s = 18$

19. A  $50 \text{ kg}$  girl stands on a scale inside a moving elevator. The scale reads  $450 \text{ N}$ . The acceleration of the elevator is

- (a)  $2.0 \text{ m/s}^2$  downward
- (b)  $1.0 \text{ m/s}^2$  upward
- (c)  $1.0 \text{ m/s}^2$  downward
- (d)  $2.0 \text{ m/s}^2$  upward
- (e)  $0.0 \text{ m/s}^2$

$N - mg = ma$   
 $450 - 50 \times 10 = 50 \times a$   
 $450 - 500 = 50a$   
 $-50 = 50a$   
 $a = -1$



20. A package is dropped from a helicopter flying horizontally. the package took  $12 \text{ seconds}$  to hit ground, how high above the ground was the package when it was released

- (a) 1200 m
- (b) 810 m
- (c) 520 m
- (d) 1040 m
- (e) 720 m

$t = \sqrt{\frac{2y}{g}}$

$12 = \sqrt{\frac{2 \times y}{10}}$

$12 = \sqrt{\frac{y}{5}}$

$\frac{144}{1} = \frac{y}{5}$

$y =$

April 3<sup>rd</sup> 2016  
 Key Phy 141

مركز تطوير العلوم

Q1  $r = 0.1 \text{ m}$ ,  $t = 4$ ,  $v = \frac{2\pi r \cdot 0.1}{4} = 0.2 \text{ m/s}$ ,  $a = \frac{(0.2)^2}{0.1} = 0.4 \text{ m/s}^2$

Q2  $3 + 4 = 7$  (أقصى قدر ممكن الزاوية)  $\rightarrow 3 \rightarrow 4$   
 ∴ cant have بين الـ 3 و الـ 4  
 magnitude  $> 7$  unit

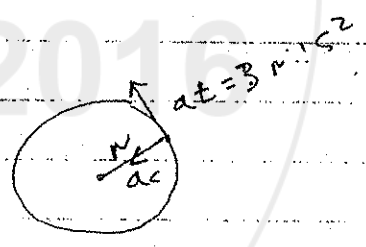
Q3  $v_{max} = \sqrt{\tan \theta \cdot r \cdot g} = \sqrt{\tan 22 \times 0.1 \times 10}$   
 $= 1.9 \text{ m/s}$   
 $1.9 \times 3.6 = 50 \text{ km/h}$

Q4  $F_d = \frac{1}{2} C_p A v^2$ ,  $\frac{v_1}{v_2} = ?$   
 ثابت  $C_p$  و  $A$

$D = 0.1 A v^2 = v^2 = \frac{D}{0.1 A}$  //  $v_1 = \sqrt{\frac{D}{0.1 A}}$

$v_2 = \sqrt{\frac{D}{0.2 A}} = \frac{1}{\sqrt{2}} \times \sqrt{\frac{D}{0.1 A}} =$   
 $= 0.71 \times \text{time as much}$

Q5  $r = \frac{H}{2}$ ,  $a_t = 3.0 \text{ m/s}^2$   
 $a_c = \frac{v^2}{r}$ ,  $v = ?$



$v^2 = v_0^2 + 2a \Delta s$ ,  $\Delta s = 2\pi r$

$v^2 = 0 + 2 \times 3 \times 2\pi \times \frac{H}{2}$

$v^2 = 6\pi^2 H^2 \Rightarrow a_c = \frac{6\pi^2 H^2}{\frac{H}{2}} = 6\pi^2 H \times \frac{2}{H} = 12\pi H$

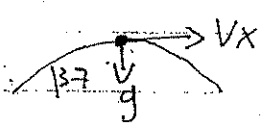
$a = \sqrt{(a_c)^2 + (a_t)^2} = \sqrt{(12\pi)^2 + (3)^2} = 37.8 \text{ m/s}^2$

لا يوجد إجابات

Q6  $x = bt \Rightarrow m = b s \Rightarrow b = m/s$

$x = ct^3 \Rightarrow m = c s^3 \Rightarrow c = m/s^3$

Q7  $t_F = \frac{v_0 \sin 37}{g}$



$= \frac{5g \sin 37}{1g} = 3.5$

هذا يكون  $v \perp a$



Q8)  $a t = 2t$ ,  $s(0) = 0$ ,  $v(5) = ?$

$$v = \int a dt = \int_0^t 2t dt$$

$$v = t^2 \Big|_0^5 = t^2 \quad // \quad v(5) = 5^2 = 25 \text{ m/s}$$

Q9  $\vec{v}_{sg} = \vec{v}_{sw} + \vec{v}_{wg}$

$$25 = 9 + v^2$$

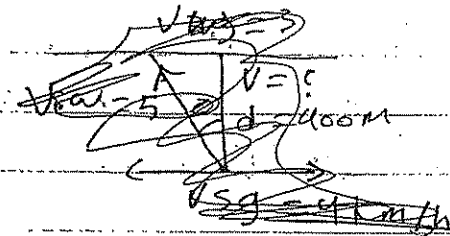
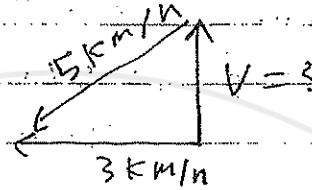
$$v^2 = 16$$

$$v = 4 \text{ km/h}$$

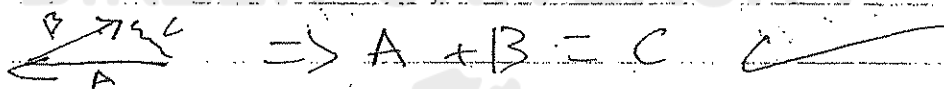
$$v = \frac{d \text{ km}}{t} \Rightarrow \frac{4}{1} = \frac{400 \text{ m}}{t} \Rightarrow 400 \text{ m} = 4t$$

$$\frac{400 \text{ km}}{1000} = 4t \text{ (h)}$$

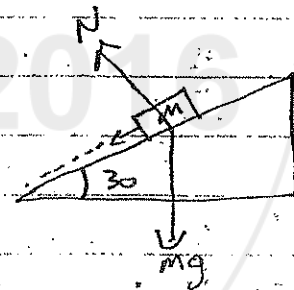
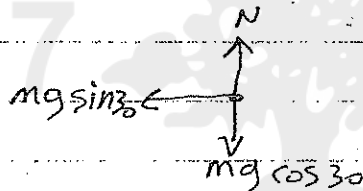
$$t = \frac{400}{4 \times 1000} = \frac{1}{10} \text{ hour (h)}$$



Q10



Q11)



$$\sum F = ma$$

$$mg \times \frac{1}{2} = ma \Rightarrow a = 5 \text{ m/s}^2$$

$$\Delta z = 2.5 \text{ m} \Rightarrow \text{UF?}$$

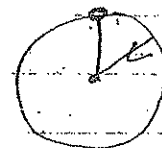
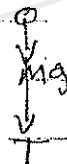
$$v^2 = 0 + 2 \times 5 \times 2.5$$

$$= 25 \Rightarrow v = 5 \text{ m/s}$$

Q12

$$mg + T = ma$$

$$mg + T = m \frac{v^2}{r}$$



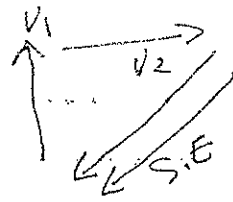
$$T = m \left( g + \frac{v^2}{r} \right)$$

$$= 9 \left( 10 + \frac{25}{2} \right)$$

$$= 9(2.5)$$

$$10 \text{ N} \quad !C$$

Q13  $\Delta v = v_2 - v_1$   
 $\Delta v = 7\hat{i} - 7\hat{j}$ ,  $\Delta t = 1$   
 $a = \frac{\Delta v}{\Delta t} = 7\hat{i} - 7\hat{j}$   
 $|a| = \sqrt{49 + 49} = 7\sqrt{2} \approx 9.8 \approx 10 \text{ m/s}^2 \text{ S.E}$



Q14  $\vec{v} = v_0 + \vec{a}t$   
 $= (3\hat{i} - 4\hat{j}) + (9\hat{j} - \hat{i})t$  //  $\hat{i} \Rightarrow x_P, \hat{j} \Rightarrow y_P$

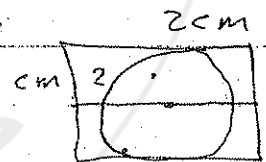
at max  $v = 0$

$v_x = 0 \Rightarrow 3\hat{i} - \hat{i}t = 0$   $t = 3 \text{ sec}$

$x = x_0 + v_{0x}t + \frac{1}{2}a_x t^2$   
 $x = 0 + 3 \times 3 + \frac{1}{2}(-1)(3)^2$   
 $= 9 - 4.5 = 4.5 \text{ M}$

Q15  $v^2 = v_0^2 + 2ax$   $\Rightarrow 0 = (20)^2 + 2 \times a \times 50$   
 $\Rightarrow 0 = 400 + 100a$   
 $\Rightarrow a = -4 \text{ m/s}^2$   $\hat{a}$   $\text{as m/s}^2$   
 $\text{MK } g = a \Rightarrow \text{MK} = \frac{a}{g} = \frac{4}{10}$

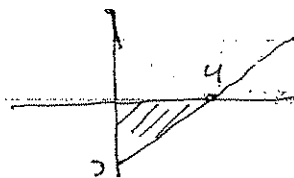
Q16  $\frac{1}{8 \times 10^{-6}}$   
 $= 0.125 \times 10^6$   
 $= 125000$   
 $a \times 10^5$   $\hat{a}$   $\text{في فراغات}$   
 $\text{فاية جرابا جيفار بور اول بيتوي}$   
 $a \times 10^4$



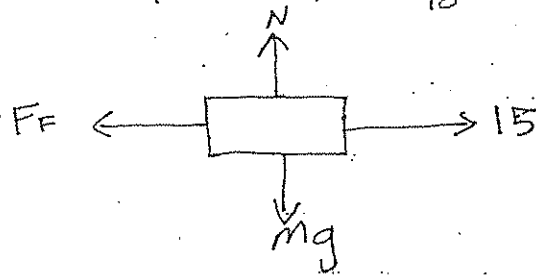
$V_b = (2)^2 \text{ cm}$   
 $= 8 \text{ cm}^3$   
 $= 8 \times 10^{-6}$

Q17 المسافة السالبة تحت المحور  
 المساحة التي تحت المحور  
 مساحتها

$M = \frac{1}{2} \times 3 \times 2$   
 $= 3 \text{ M}$



Q18)  $M = 6 \text{ kg}$ ,  $M_s = \frac{3}{10}$ ,  $M_k = \frac{2}{10}$ ,  $F_{APP} = 15 \text{ N}$   
 $f_{friction} = ?$



$$N = mg \quad \text{--- (1)}$$

① أولاً نفحص قوة الإحتكاك الساكنة إذا كانت أكبر من القوة المؤثرة على الجسم فإن الجسم يتحرك ويكون له قوة الإحتكاك مخالفة بمقدار القوة المؤثرة. أما إذا كانت قوة الإحتكاك الساكنة أقل من القوة المؤثرة على الجسم فإن الجسم لا يتحرك وتكون قوة الإحتكاك المعاكسة للقوة مساوية للقوة المؤثرة. مقارناً ومعاكسة كما في الإجابة

$$F_s = N M_s = mg \times \frac{3}{10} = 6 \times 10 \times \frac{3}{10} = 18 \text{ N}$$

$$F_s > F_{APP} \Rightarrow F_{friction} = \boxed{15 \text{ N}}$$

$$F_f - F_{APP} = ma \Rightarrow a = 0 \text{ لأن الجسم لا يتحرك}$$

$$F_f = F_{APP} = 15 \text{ N}$$

مع كتابة قيمة الأخطاء لكي لا تخطوا على السيد الفقيه بالله

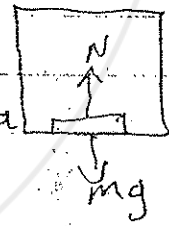
Q19)

$$M_{girl} = 50 \text{ kg} // \text{ } g(50) = N \text{ قس}$$

$$N - mg = ma \Rightarrow 450 - 50 \times 10 = ma$$

$$-50 = 50a$$

$$a = -1 \text{ m/s}^2$$



بما أن التسارع سالب فهذا يعني أن التسارع للأسفل (D)

Q20)  $t = 12 \text{ s}$

$$t = \sqrt{\frac{2g}{g}} \Rightarrow 12 = \sqrt{\frac{2g}{5}} \Rightarrow (12)^2 = \left(\sqrt{\frac{g}{5}}\right)^2$$

$$5/144 = \frac{g}{5}$$

$$g = 720 \text{ m}$$

*Handwritten signature:*  
 Engineer

