

فيزياء ١٤١

الحل التفصيلي للدوائر الموجودة في

Test bank

إعداد الرباعي:

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للتسونا من صالح وحاتم بظهر الغيب

CHAPTER 1

1) **Ans: E** from the book "None"

2) **Ans: B** "ns" nanosecond = 10^{-9} s
from the book

3) **Ans: E** the speed of light
from the book

4) **Ans: C** The Def. relates the current ...

5) **Ans: C** 1 yard = $\frac{3600}{3937}$ meters

1 yard = 0.914 \approx 1 m.

6) **Ans: D** "can be expressed in terms of m^2 "

7) **Ans: C** kg

8) **Ans: B** 1 kg = 10^{-3} kg

9) **Ans: B** 1 pound = 0.453 kg
* "خطا" في الجواب \approx 0.5 كجم

10) **Ans: C** $(5.0 \times 10^4)(3.0 \times 10^6) =$
 $= (5.0 \times 3.0) 10^{6+4}$
 $= 1.5 \times 10^{10} = 1.5 \times 10^{10}$

11) **Ans: B** " 1.5×10^{-1} "
the same as 10

12) **Ans: E** $5.0 \times 10^5 + 3.0 \times 10^6 =$
 $= ~~5.0~~ 0.5 \times 10^6 + 3.0 \times 10^6 =$
 $= 3.5 \times 10^6$

13) **Ans: E** $(7.0 \times 10^6) / (2.0 \times 10^6) =$
 $(\frac{7.0}{2.0}) 10^{6-6} = 3.5 \times 10^{12}$

14) **Ans: B** 0.00150 "3" sign. nom.

15) **Ans: C** 15.0 "3" sign. nom.

16) **Ans: C** $3.2 \times 2.7 = 8.64$
 $8.64 \approx 8.6$

17) **Ans: B** $1.513 + 27.3 =$
 $= 28.813 \approx 28.8$ ^{least}

18) **Ans: B** 1 mi = 1609 m
55 = y m
 $y = 55 \times 1609 = 88.495$ ^{mi}
 $88.495 \text{ meter/h} = \frac{88.495 \text{ meter}}{3600 \text{ s}}$
 $= 24.58 \approx 25$

19) **Ans: A** $V_{\text{sphere}} = \frac{4}{3} \pi r^3$
 $= (\frac{4}{3})(3.14)(1.7 \times 10^{-2})^3$
 $= 26.569 \approx 2.7 \times 10^{-5}$ ^{m³}

20) **Ans: C** $A_{\text{sphere}} = 4 \pi r^2$
 $= (4)(3.14)(1.7 \times 10^{-2})^2$
 $= 3.6298 \approx 3.6 \times 10^{-3}$ ^{m²}

Ans: D

$$\begin{aligned}
 21) V_{\text{cylinder}} &= (\text{Area of base}) (\text{height}) \\
 &= (\pi r^2) (h) \\
 &= (\pi) (2.3 \times 10^{-2})^2 (1.4) \\
 &= 2.3 \times 10^{-3} \text{ m}^3
 \end{aligned}$$

Ans: D

$$\begin{aligned}
 A_{\text{cylinder}} &= 2 \text{ " Area base } + 2\pi r h \\
 &= 2\pi r^2 + 2\pi r h
 \end{aligned}$$

$$\begin{aligned}
 &= (2) (3.14) (2.3 \times 10^{-2})^2 + (2) (3.14) (2.3 \times 10^{-2}) (1.4) \\
 &= 5.344 \approx 5.3 \times 10^{-3} \text{ m}^2
 \end{aligned}$$

Ans: B

$$V_{\text{cube}} = L^3 = (1 \times 10^{-2})^3 = 10^{-6} \text{ m}^3$$

Ans: B

$$A_{\text{square}} = L^2 = (1 \times 10^{-2})^2 = 10^{-4} \text{ m}^2$$

Ans: B

$$\begin{aligned}
 1 \text{ m} &\rightarrow 3.281 \text{ ft} \\
 y \text{ m} &\leftarrow 1.5 \text{ ft} \\
 y &= \frac{1.5}{3.281} = 0.457 \\
 V_{\text{cube}} &= L^3 = (0.457)^3 = 0.0955 \\
 &\approx 0.096
 \end{aligned}$$

Ans: D

$$V = at^2 + bt^3$$

$\Rightarrow V$ is in m/s

So at^2 is in m/s

$$(a) (s^2) = \text{m/s}$$

$$a = \frac{s^3}{m}$$

$\Rightarrow bt^3$ is in m/s

$$(b) (s^3) = \text{m/s}$$

$$b = \frac{s^4}{m}$$

Ans: A

$$A = BC \Rightarrow B = \frac{A}{C}$$

$$B = \frac{L/m}{L/T} = T/m$$

Ans: D

$$A = B^n C^m$$

$$\begin{aligned}
 B &= L^2 T^{-1} / A = LT / C = LT^2 \\
 (L^2 T^{-1})^n (LT^2)^m &= L^1 T^1 \\
 L^{2n+m} &= L^1 \\
 T^{-n+2m} &= T^1
 \end{aligned}$$

$$\begin{aligned}
 2n+m &= 1 \quad \boxed{1} \\
 -n+2m &= 1 \quad \boxed{2}
 \end{aligned}$$

$$-2n+2m=1 \quad \boxed{2}$$

~~(2) - (1)~~

$$2 \times \boxed{1} - \boxed{2}$$

$$4n+2m=1$$

$$-(n+2m=1)$$

$$5n = 1 \quad n = \frac{1}{5}$$

$$(2) (\frac{1}{5}) + m = 1$$

$$m = 1 - \frac{2}{5} = \frac{3}{5}$$

$$m = \frac{3}{5}$$

1. $\Delta X = X_f - X_i$

So **E** because

$\Delta X = 4 - (-4) = 8$ is the largest.

2. $\Delta X = X_f - X_i$

B because

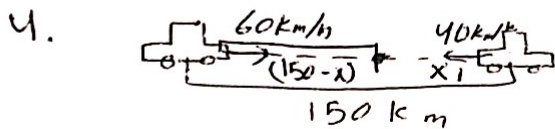
$\Delta X = -8 - (-4) = -4$

It is the only negative result.

3. $S_{avg} = \frac{\text{total distance}}{\Delta t}$

So **B** the distance

كل المسافة التي مشيتها
فترات الفترة على الفترة



~~So $\Delta X = 150 - 0 = 150$~~
 ~~$\Delta t = 0$~~

$v_1 = 40 \text{ km/h} = 11.1 \text{ m/s}$

$v_2 = 60 \text{ km/h} = 16.7 \text{ m/s}$

$x_1 = v_1 t + \frac{1}{2} a t^2$

$x_1 = 16.7 t$

$x_2 = 150 \times 10^3 - x_1$

$x_2 = 150 \times 10^3 - v_2 t - \frac{1}{2} a t^2$
 $= 150 \times 10^3 - 16.7 t$

$x_2 = 150000 - x_1$

$150000 - 16.7 t = 11.1 t$

$150000 = 27.8 t$

$t = \frac{54025}{3600}$

$= 1.5 \text{ h}$

5. $S_{avg} = \frac{\text{total distance}}{\Delta t}$

$s_1 = \frac{d_1}{t_1}$

$\Delta t_1 = \frac{d_1}{s_1} = \frac{40}{80} = \frac{1}{2} \text{ h}$

$\Delta t_2 = \frac{d_2}{s_2} = \frac{40}{40} = 1 \text{ h}$

the total time = $\frac{1}{2} + 1 = 1.5 \text{ h}$

على أننا كان الوقت من 40 و 40 ميلنا
1.5 ساعة 80 km

$S_{avg} = \frac{80}{1.5} = 53.3$

D



$v_{avg} = \frac{\Delta X}{\Delta t}$

و على انه زائد و موجب

لنفس التوجه

$\Delta X = 0$

$v_{avg} = 0$ اذن

$$7. \text{ Avg} = \frac{d}{\Delta t} = \frac{50+50 \text{ km}}{2 \text{ h}} = 50 \text{ km/h}$$

(B)

$$8. x(t) = 16t - 30t^3$$

$$v(t) = 0$$

$$v(t) = x' = 16 - 90t^2$$

$$16 - 90t^2 = 0$$

$$90t^2 = 16$$

$$t^2 = \frac{16}{90}$$

$$t = \frac{4}{3} = 1.33 \text{ s}$$

(B)

$$9. v = bt^2$$

$$v = \frac{dx}{dt}$$

$$\int_0^t dx = \int_0^t v dt$$

$$x = \int_0^t bt^2 dt$$

$$x(t) = \frac{b}{3} t^3$$

(B)

$$10. \frac{\Delta v}{\Delta t} = \frac{v(8) - v(3)}{8 - 3}$$

$$= \frac{0 - 20}{8 - 3} = -4 \text{ cm/s}^2$$

(B)

$$(11) \quad x = 7t - 3t^2$$

$$v_{\text{avg}} = \frac{\Delta x}{\Delta t} = \frac{x(4) - x(0)}{4}$$

$$= \frac{-20 - 0}{4} = -5 \text{ m/s}$$

(B)

$$(12) \quad v = 4t - 3t^2$$

$$x = \int v \cdot dt$$

$$\int 4t - 3t^2 \cdot dt$$

$$x = 2t^2 - t^3$$

$$v_{\text{avg}} = \frac{\Delta x}{\Delta t} = \frac{x(2) - x(0)}{2}$$

$$= \frac{8 - 8 - 0}{2} = \frac{0}{2} = 0$$

(A)

(B)

$$x = 4t^2 - 3t^3$$

$$v = 8t - 9t^2$$

$$\frac{\Delta v}{\Delta t} = \frac{\Delta v}{\Delta t}$$

$$= \frac{v(2) - v(0)}{2}$$

$$= \frac{16 - 36 - 0}{2}$$

$$= -10 \text{ m/s}^2$$

(C)

14. ~~14~~

16

particle 1, 2
 ثابت سرعت
 constant velocity

(3) $\Rightarrow 3.5 + 2.7t^2$

$v = 5.4t$

$a = 5.4 \text{ m/s}^2$

(4) $\Rightarrow 3.5 - 3.4t - 2.7t^2$

$v = -3.4 - 5.4t$

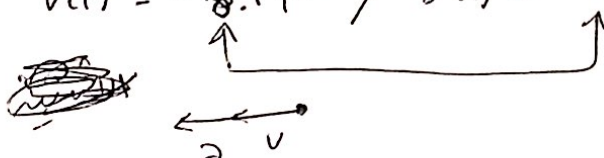
$a = -5.4 \text{ m/s}^2$

so only 3 and 4

(D)

15. particle 1 = $x(t) = 3.5 - 2.7t^3$

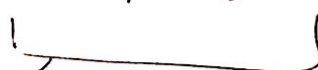
$v(t) = -8.1t^2$ / $a(t) = -16.2t$



⊖ انجم يتجه بالاتجاه السالب والسرعة سالبة و ان تاربع بتغير الاتجاه اذن عم تزداد سرعته

particle 2 $\Rightarrow x(t) = 3.5 + 2.7t^3$

$v = 8.1t^2$ / $a(t) = 16.2t$



⊕ تغير الاشارة بعد بالاتجاه الموجب

particle 3 = $3.5 + 2.7t^2$

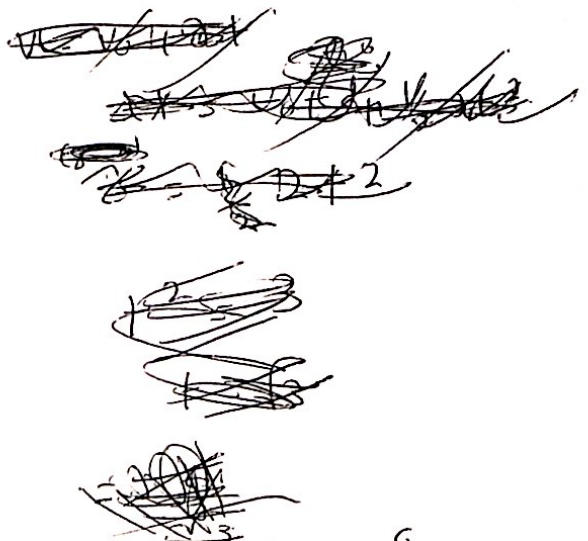
$v = 5.4t$ / $a = 5.4$

تغير اشارة السرعة وتكون سالبة

particle 4 = $3.5 - 3.4t - 2.7t^2$ (A) ←

$v_0 = 0$ constant $a = 4 \text{ m/s}^2$

$v_{avg} = \frac{\Delta x}{\Delta t}$



$x = v_0 t + \frac{1}{2} a t^2$

$2 = 2t + 2$

$t = 1.5$

$8 = 2t^2$

$t^2 = 24$

$t = 2$

$v_{avg} = \frac{\Delta x}{\Delta t}$

$= \frac{8 - 2}{2 - 1} = 6 \text{ m/s}$

17 (E)

متغير يكون جسم متحرك
 تغير بين سرعة بشكل
 ثابت
 اذن

$a = \frac{dv}{dt}$

(2)

18 | C | ~~←~~

S increase

(B) $a \neq 0$ and $a \neq v$
in the same direction

لأنه يتزايد لأنهم لا يكونوا بنفسه الاتجاه

والجواب هو الوصف الذي يلي

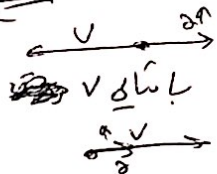
(C) negative & negative

و لأن speed ما يتغير على الاتجاه

فما يتبين الإشارة .

19 | 

(E) لا توجد



مثل شرط أن يكون

(E)

20 | $y = at - bt^2$

y position L

$a \rightarrow \frac{L}{T}$ $b \rightarrow \frac{L}{T^2}$

(C)

21

$x = 6t^2$

(E) لا توجد ولا صفر

~~$a = 6t$~~

تأثير العوائد سالب
مثل أن t^2 خارج
لا يكون سالب

(C) وبما أنه + خارج
يكون سالب لأن t^2 خارج
لا يكون سالب

$a = 9.8$

22

$x(t) = 27t - 4t^3$

$v = 27 - 12t^2$

$a = -24t$

$a(1) = -24 \text{ m/s}$

23

$x(t) = 27t - 4t^3$

$v(t) = 27 - 12t^2$

$v(0) = 27$

$a(t) = -24t$

$a(0) = 0$

(C)

24

$v = 16 \text{ m/s} \rightarrow t = 0$

$a = -0.5t$

$a = \frac{dv}{dt}$

$v = \int a dt$

$v = -0.5t^2 + c$

24) $v = -0.25t^2 + c$

$v(0) = c$

$c = 16$

$v = -0.25t^2 + 16$

$-0.25t^2 + 16 = 0$

$0.25t^2 = 16$

$t^2 = 64$

$t = 8$

D

25) نصف السوار

24

$v = -0.25t^2 + 16$

$x = \int_0^t v \cdot dt$

$\Delta x = \frac{-0.25}{3} t^3 + 16t$

$\Delta x = 58.7 = 59 \text{ m}$

E

26) نصف السوار

24, 52

It stopped at $t = 8$

so $\Delta x = \frac{-0.25}{3} t^3 + 16t = 85$

D

27) $v(t) = 98 - 2t^2$

$98 - 2t^2 = 0$

$2t^2 = 98$

$t^2 = 49$

$t = 7$

$a(t) = -4t$

$= -4 \times 7 = -28 \text{ m/s}^2$

D

28) $x(t) = 75t - t^3$

$v(t) = 75 - 3t^2$

$75 - 3t^2 = 0$

$3t^2 = 75$

$t^2 = 25$

$t = 5$

$a(t) = -6t$

$= -6 \times 5 = -30 \text{ m/s}^2$

C

29) 20 m in 4s

$\Delta x = v_0 t + \frac{1}{2} a t^2$

$20 = 0 + \frac{1}{2} a (16)$

$a = \frac{20}{8} = 2.5 \text{ m/s}^2$

C

(3)

$$\boxed{30} \quad v^2 = v_0^2 + 2ax$$

$$2500 = 100 + 2(60)a$$

$$2400 = 120a$$

$$a = 20 \text{ m/s}^2$$

$$v = v_0 + at$$

$$50 = 10 + 20t$$

$$40 = 20t$$

$$\boxed{t = 2 \text{ s}}$$

(A) ~~صحيح~~

(B) ~~صحيح~~

$$S_{\text{avg}} = \frac{d}{\Delta t}$$

$$\frac{10450}{2} = \frac{60}{\Delta t}$$

$$30 = \frac{60}{\Delta t}$$

$$\boxed{\Delta t = 2 \text{ s}}$$

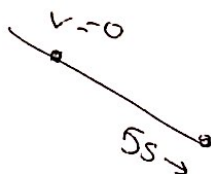
صحيح

$$\boxed{31} \quad a = 5 \text{ m/s}^2$$

$$v = v_0 + at$$

$$= 5 \times 5 = 25 \text{ m/s}$$

(C)



$\boxed{32}$

$$v_0 = 25 \text{ m/s} \quad \uparrow$$

$$a = 3 \text{ m/s}^2 \quad \downarrow$$

$$v = v_0 + at$$

$$v = 25 - 3(6)$$

$$25 - 18 = 7 \text{ m/s}$$

(A)

$\boxed{33}$

$$v_0 = 12 \text{ m/s} \leftarrow$$

$$a = 4 \text{ m/s}^2 \leftarrow$$

$$\Delta x = v_0 t + \frac{1}{2} a t^2$$

$$\Delta x = 12(3) + \frac{1}{2}(4)(3)^2$$

$$= 36 + 18 = 54 \text{ m}$$

(D)

$\boxed{34}$

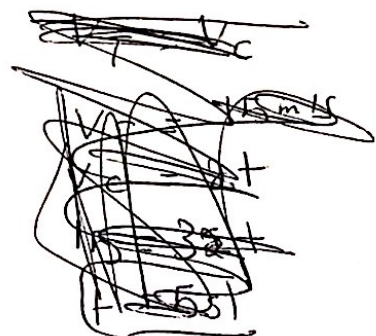
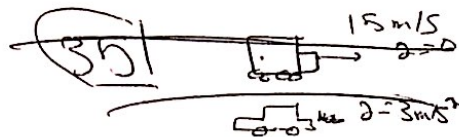
$$v_0 = 2 \text{ m/s} \quad t = 6 \text{ s}$$

$$a = 2 \text{ m/s}^2$$

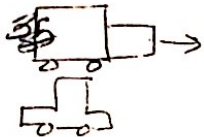
$$\Delta x = v_0 t + \frac{1}{2} a t^2$$

$$= 12 + 36 = 48 \text{ m}$$

(E)



(35)



$$X_T = X_C$$

~~$$v_T t + \frac{1}{2} a t^2 = v_C t + \frac{1}{2} a t^2$$~~

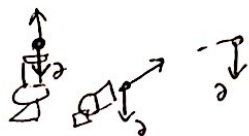
$$v_T t = \frac{1}{2} a t^2$$

$$15 = \frac{3}{2} t$$

$$t = \frac{30}{3} = 10s$$

(B)

(36)



downward

داعاً يكون
تتصلاً كان في الهواء
في انحدار. (A)

(37)

ascend
النور

$$\Delta X = x_2 - x_1$$

$$= x_2 - x_1$$

(x2 > x1)

descent

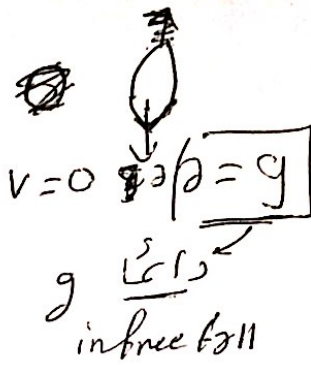
$$\Delta X = x_2 - x_1$$

$$= x_1 - x_2$$

$$= -$$

صعود بالصور والبال بالهبوط
(B)

(38)



(39)

$$v_{avg} = \frac{\Delta x}{\Delta t}$$

$$\Delta x = v_0 t + \frac{1}{2} g t^2$$

$$\Delta x = 4.9 t + \frac{1}{2} g t^2$$

~~$$\Delta x = 4.9 t + \frac{1}{2} g t^2$$~~

$$\Delta x(t) = 4.9 t$$

$$v_{avg} = \frac{4.9 t - 0}{t} = 4.9 \text{ m/s}$$

(A)

لا نواكس
تتبط كل ثانية بمقدار 4.9

(C) acceleration is constant and equal to 9.8
ما يتغير كل ثانية بمقدار 9.8

(D) يمتد بمقدار 4.9m في كل ثانية بمقدار 9.8m

(E) 2 constant
والتسارع ثابت
g = g
والتسارع ثابت للوزن
بالجاذبية.

(C)

40 [C] $a = 9.8 \text{ m/s}^2$

ازن السرى رح تزداد
 دل تايه بقدر 9.8

$$v = 0 + 9.8t$$

$$v = 9.8t$$

و جايانه سقوط ازن

رح يهون ايجاه السرى للاسفل عشان
 فصل درج تزايدى فى سباق

زكى جويان [E]

41

↓ 1 m/s

$$\Delta x = v_0 t + \frac{1}{2} g t^2$$

$$= 1(5) + \frac{1}{2} 9.8(5)^2$$

$$= 5 + 122.5$$

$$= 127.5 \text{ m}$$

ة نو v_0 و a بنفسه الالباه
 بتكون الالباه (+)

[B]

45

↑ 35 m/s

$$v = v_0 + at$$

$$v = 35 - 10(5)$$

$$= 35 - 50 = -15 \text{ m/s}$$

15 down

[B]

41

↑ v
 ↓ a

[B]

↑ v

↓ a

رائعاً بتكون للاسفل

42

↑ 50 m/s

46 (level ground)

$$\Delta x = v_0 t - \frac{1}{2} g t^2$$

$$x = 50(1) - 5(1)$$

$$= 45 \text{ m}$$

[B]

سباق السودان [42]

43

$$x = 50(8) - 5(8)^2$$

$$= 300 - 180$$

$$= 120 \text{ m}$$

[E]

و 80 م

46

[C]

لا تزداد رح

دائماً بقدر تايه بالسقوط لكر

47

$$\Delta x = v_0 t + \frac{1}{2} g t^2$$

~~$$\Delta x = 9.8(5) + \frac{1}{2} 9.8(5)^2$$~~

~~$$= 49 + 122.5$$~~

~~$$= 171.5$$~~

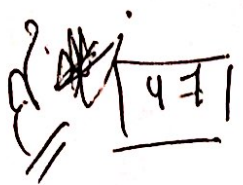
~~$$\Delta x = 9.8(2)^2$$~~

~~$$= 39.2$$~~

~~$$\Delta x = 34.1$$~~

~~$$\Delta x = 4.9(2)^2$$~~

~~$$= 19.6$$~~



$$v(1) = v_0 + gt = g$$

$$v(2) = v_0 + g(2) = 2g$$

$$v_{avg} = \frac{2g + g}{2} = \frac{3g}{2}$$

Distance moved in second

$$\text{second is } \frac{3g}{2} \times 1 = \frac{3g}{2} = \frac{3 \times 10}{2} = 15 \text{ m}$$

$$v_{avg} = \frac{\Delta x}{\Delta t}$$

$$v_{avg} \Delta t = \Delta x$$

(C)

الارتفاع

481 $v_0 = 0$

$$v(4) = v_0 + g(4) = 4g$$

$$v(3) = 3g$$

$$v_{avg} = \frac{(4+3)g}{2} = \frac{7}{2}g$$

$$v_{avg} = \frac{d}{\Delta t}$$

$$d = v_{avg} \cdot \Delta t$$

$$= \frac{7}{2}g \times (4-3) = 34.3 \text{ m}$$

(D)

491



عالية الصاروخ
تزداد مع الزمن

بالساعة لا يوقف

الارتفاع الذي يتحرك فيه الصاروخ

(5)

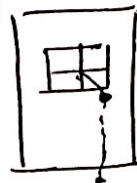
501



عالية الارتفاع
من البالون ظهر
يتكون بنفسه $v_0 = 10 \text{ m/s}$

$$v = v_0 + gt = 10 + 9.8(20) = 206 \text{ m/s}$$

511



$$\Delta x = v_0 t + \frac{1}{2}gt^2 = 0 + \frac{1}{2}(9.8)(12)^2 = 705.6 \text{ m}$$

(E)

521

$$\Delta x = v_0 t + \frac{1}{2}gt^2$$

$$175 = \frac{1}{2}(9.8)t^2$$

$$t^2 = 35.7$$

$$t = 5.9 = 6 \text{ s}$$

(C)

531

$$v_0 = 19.5 \text{ m/s}$$

$$\Delta x = v_0 t + \frac{1}{2}gt^2$$

$$\Delta x = 19.5t - 4.9t^2$$

$$v_{at \text{ the top}} = 0$$

$$v = v_0 + gt$$

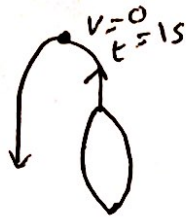
$$v_0 = gt$$

$$t = \frac{19.5}{9.8} = 2 \text{ s}$$

(C)

$$\Delta x = 39 - 19.6 = 19.4$$

54



25

~~v = gt~~



~~v = v_0 + gt~~

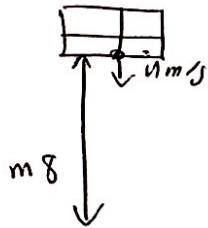
~~v_0 = 9.8(1) = 9.8 m/s~~

~~Δx = v_0 t - 1/2 g t^2~~

~~Δx = 9.8 t - 4.9 t^2~~
~~= 9.8(1) - 4.9(1) = 4.9~~

(A)

55



~~Δx = v_0 t + 1/2 g t^2~~

~~8 = 4t + 4.9 t^2~~

~~4.9 t^2 + 4t - 8 = 0~~

~~t = $\frac{-4 \pm \sqrt{16 + 156.8}}{9.8}$~~

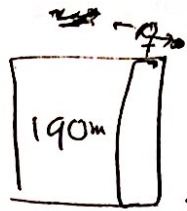
~~t = $\frac{-4 \pm 13.145}{9.8}$~~

~~t = 9.3~~

~~t = -X~~
لا نه ساله

(B)

56



~~v = gt~~

~~v^2 = v_0^2 + 2gX~~

~~v^2 = 0 + 2g(190)~~

~~v = 61 m/s~~

(B)

57



$a_n = 19.6 = 2g$

~~Δx_n = v_0 t - 1/2 g t^2~~

~~v = v_0 - g t~~

~~v_0 = 2g t~~

~~= 2g t^2 - g t^2~~

~~Δx_n = g t^2~~

but ~~v_0 = 2g t~~

~~Δx_e = v_0 t - 1/2 g t^2~~

~~= 2g t^2 - 1/2 g t^2~~

~~Δx_e = 3/2 g t^2~~

$Δx_n = v_0 t - \frac{1}{2} a_n t^2$

$Δx_n = v_0 t - g t^2$ Where $a_n = 2g$

$Δx_e = v_0 t - \frac{1}{2} g t^2$

السنه

في الارض راج يتنوع اعلى من سرعة سقوط الكواكب
بانه في بائس كواكب راج يتنوع بعد الارتفاع اي يرتفع في الارض اذا كل الهم نفس السرعة
الاستراتيجية

$$\boxed{58.} \quad v_f^2 = v_i^2 - 2gx$$

case 1 $0 = v_i^2 - 2(100)g$

① $v_i^2 = 200g$

case 2

$$v^2 = (2v_i)^2 - 2gx$$

$$0 = 4v_i^2 - 2gx$$

$$4v_i^2 = 2gx$$

$$x = \frac{4(200g)}{2g}$$

$$= 400 \text{ m}$$

(E)

$\boxed{59}$

$\uparrow 100 \text{ m/s} \quad \uparrow 10 \text{ m/s}$

$$v_f^2 = v_i^2 - 2gx$$

~~0~~

$$x = \frac{v_i^2}{2g}$$

$$x_1 = \frac{10000}{2g}$$

$$x_2 = \frac{100}{2g}$$

$$\frac{x_1}{x_2} = 100$$

(B)

$\boxed{60}$

~~$$v = \frac{dx}{dt}$$~~

~~$$\int dx = \int v dt$$~~

$$\boxed{x = \int v dt}$$

displacement

$\boxed{61}$

(D) ^A تفکره

$\boxed{62}$

$$a = 3 \text{ m/s}^2$$

~~$$a = \frac{dv}{dt}$$~~

$$dv = a dt$$

$$v = \int_0^t 3 dt$$

$$v = 3t$$

but $v = \frac{dx}{dt}$

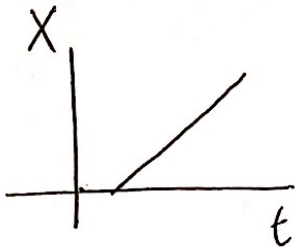
$$x = \int_0^t v dt$$

$$= \int_0^t 3t dt$$

$$x = \frac{3}{2} t^2$$

So it is increase with time.

63



slope = ~~dx/dt~~ = $\frac{dx}{dt}$

$v = \frac{dx}{dt}$

و بجایه straight line
از آن رخ توی v
ثابته لانوسه
معالیه اولیه تعریف رقم.

64 B سفر العکسه

constant
از آن رخ توی العکسه
non zero
انقره ادمسودن
فاضل غیر B

65 ~~is~~ constant velocity

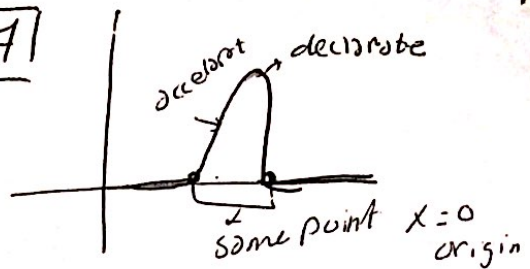
means $a = 0$
so E

66 speed increasing

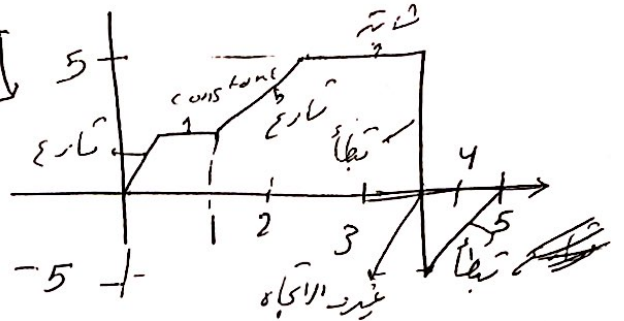
از آن فقط مستقیم
عینله عصبه

A

67



68



~~Handwritten scribbles and equations, including $v = 5x + 11$ and $v = -5x + 11$.~~

~~$v = 5x + 11$~~

~~Handwritten scribbles.~~

~~Handwritten scribbles.~~

ازا كانه $v = 0$ لازم يكون
ماشي باعده تارعه والا غير صير يكون
في عينا سره E

69

هو البرقي به ينزله رخ يكون
بلله لدره ينزله
ننه سره المصعد بانسولين
رخ يتنوع شترن ويريم

ينزل $\Delta x = v_0 t - \frac{1}{2} g t^2$

تفكره سؤال [76] [75]

تجربا الجواب

[C] كلو

$v \propto t$
بتزداد مع الزمن

[77] ↑

$$v = u + gt$$

When $t = 0$

$$v = u$$

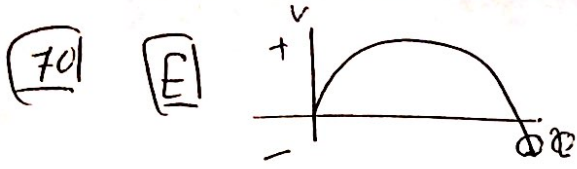
والرسمه الوصيه
اي متر ببله

من نقطه الاصل

[C]

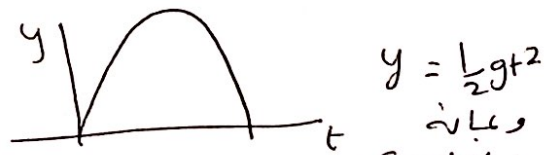
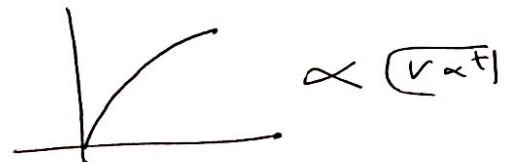
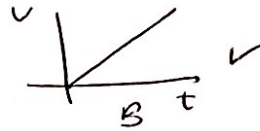
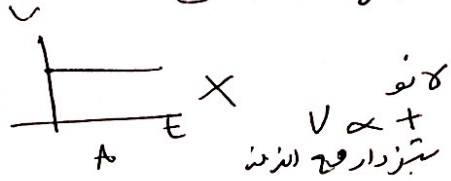
وصي





يكون اشارة \oplus باساره
عشان صيرد بتجملا سرته ولان
بالا اتجاه العكسي

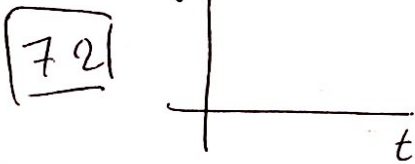
75 $v_i = 0$
 (a) $v = gt$
 (b) $y = \frac{1}{2}gt^2$
 (c) $v^2 = 2gx$



الاسمى موجب اول اولاد
 يكون القطع المتكافئ لانه
 وانه يكون نفسه فقط

B

71 C باتسارع
 لان الميل موجب



$\Delta x = v \cdot t$

$\Delta x = \int v \cdot dt$
 = Area under the curve

= $3 \times 12 = 36 \text{ m}$

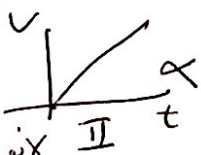
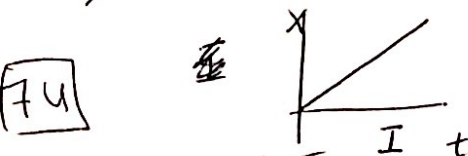
D

73 A لانو بتسارع

لعدنه نفس سرته لانه وسه يتبين

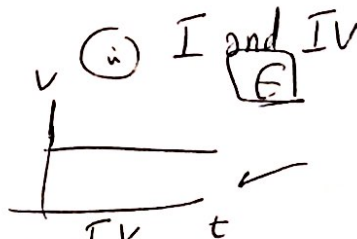
$a = \frac{dv}{dt} = \frac{12-0}{2-0} = 6 \text{ m/s}^2$

74



لانو اسرته
 بتزداد مع الزمن

لانو اسرته
 بتسارع ويبقى اسرته ثابتة



اسرته ثابتة مع الزمن



تسارعه ثابتة لانه سرته بتزيد
 بتسارعه ثابتة

By: Lara Sami

Chapter 3: Vectors

Test bank solutions

1 Ans: B

→ ∞

2 Ans: D

3 Ans: A

→ ∞

4 Ans: C

→ ∞

The magnitude of the resultant must be some where between 5 and 45 only 12 satisfy this.

5 Ans: A

Because

$$T+6 > 12$$

so $T > 6$

$$\text{and } T-6 < 12$$

so $T < 18$

6 Ans: D

7 Ans: ~~B~~ C

$$\vec{V}_1 + \vec{V}_3 = \vec{V}_2 \quad \text{so } \vec{V}_3 = \vec{V}_2 - \vec{V}_1$$

8 Ans: E

9 Ans: A

10 Ans: B

11 Ans: B

→ ∞

12 Ans: C

13 Ans: D

$$y = 12 \sin 30$$

component = -6

14

Ans: A

15 Ans: D

$$4 \times \sqrt{100} = 4 \times 10 = 40$$

$$\{16\} \text{ Ans: B } \neq \sqrt{(10)^2 + (10)^2 + (5)^2}$$

$\neq 15$

17

$$\text{Magnitude} = \sqrt{(2)^2 + (6)^2 + (6)^2} = 7 \text{ Ans: C}$$

18

$$25 \cos \theta = 12 \Rightarrow \theta = 61^\circ \text{ Ans: C}$$

19

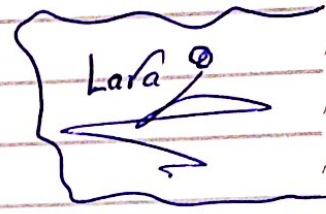
$$\theta = \tan^{-1} \frac{45}{25} = 61^\circ \text{ Ans: B}$$

20

$$\theta = \tan^{-1} \frac{45}{25} = 61^\circ \Rightarrow \theta = 180 - 61 = 119 \text{ Ans: C}$$

21 Ans: A $S = (2+4)\hat{i} + (6+2)\hat{j} + (-3+1)\hat{k}$

22 Ans: B $D = (2-4)\hat{i} + (6-2)\hat{j} + (-3-1)\hat{k}$
 $= -2\hat{i} + 4\hat{j} - 4\hat{k}$



23 ans: A $= (2\hat{i} - 3\hat{j}) - (2(1)\hat{i} - 2(2)\hat{j})$
 $= 2\hat{i} - 3\hat{j} - 2\hat{i} + 4\hat{j} = +1\hat{j}$

24 Ans: C $(A+B)_x = A \cos \theta + B \cos \theta = 12(\cos 45) + B(\cos 60) \approx 12$

25 $A \cos \theta = 4 \quad \text{--- (1)} \quad \tan \theta = \frac{10}{4} \quad \theta = 68^\circ$
 $A \sin \theta = 10 \quad \text{--- (2)} \quad \text{Then } A = \frac{4}{\cos \theta} = 10.7$

Finally $A \cos \theta_2 = 8 \Rightarrow (10.7) \cos \theta_2 = 8 \Rightarrow \cos \theta = \frac{8}{10.7} \Rightarrow \theta_2 = 41.6$

So the y component $= A \sin \theta_2 = 10.6 \sin 41.6 \approx 7.2$

Ans: B

26 Ans: C $A \cdot B = |A| |B| \cos \theta = (L)(L) \left(\frac{\sqrt{3}}{2}\right) = \frac{\sqrt{3} L^2}{2}$

27 Ans: D $\vec{A} \cdot \vec{B} = (2)(4) + (6)(2) + (-3)(1) = 17 \text{ m}^2$

28 Ans: C $A \cdot B = (10)(15) \cos 65^\circ = 63 \text{ m}^2 ?$

29 Ans: D $AB \cos \theta = A \cdot B$
 $(3)(5) \cos \theta = (1)(3) + (2)(4) = 11 \Rightarrow \cos \theta = \frac{11}{15}$
 $\theta = \cos^{-1} \frac{11}{15}$

30 Ans: D $\cos(B) = -\cos(B+20)$ so $B + B + 20 = 180$
 $2B = 160$
 $B = 80^\circ$

31 Ans: A 32 Ans: E 33 Ans: C $AB \sin \theta$

34

Ans: B

$$\sin(\theta + 20) = 2 \sin \theta$$

بتجربوا الخيارات بالآلة الحاسبة

والخيار الذي يربط بتخاروه وهون 18°

الصح

35

Ans: E

36

\hat{i}	\hat{j}	\hat{k}
3	-2	0
2	3	-2

$$= \hat{i}(4-0) + \hat{j}(-6-0) + \hat{k}(9-4)$$

$$= 4\hat{i} - 6\hat{j} + 5\hat{k}$$

Ans: A

37

Ans: E

38

Ans: B

$$\hat{i} \cdot (\hat{j} \times \hat{k}) = \hat{i} \cdot \hat{i} = 1$$

39

Ans: A

$$\hat{k} \cdot (\hat{k} \times \hat{i}) = \hat{k} \cdot \hat{j} = 0$$

لا تنسونا من دعائكم بفاهر
الغيب

Lara



Chapter 4

اعداد وناام ساويه

1. $v = \frac{dx}{dt} = \frac{ax}{at}$

معدل التغير في الازمان
بالنسبة لزمانه (A)

7



2. $a = \frac{dv}{dt}$

معدل التغير في السرعة
بالنسبة لزمانه (C)



3. speed (non vector quantity)
قياسه

4. (E) ولة وحدة
كحد متجه

5. (E) الحركة الاقترية

المختزونات دائما يتكون
تقسيم السرعة والسرعة ثابتة

اذن (السرعة)

6. $r = -2\hat{i} + 3\hat{j} + 1\hat{k}$
to
 $r = 3\hat{i} - 1\hat{j} + 4\hat{k}$

$\Delta r = r_2 - r_1$

$\Delta r = 5\hat{i} - 4\hat{j} + 3\hat{k}$

(B)

$\cos 30 = \frac{H}{Y}$

Y it is the distance that sound waves have traveled

$Y = \frac{H}{\cos 30}$

$Y = \frac{H}{\frac{\sqrt{3}}{2}}$

$Y = \frac{2}{\sqrt{3}} H$

but

X is the distance that plane have traveled

$\tan 30 = \frac{X}{H}$

$X = \tan 30 H$

(1)

رعانه

$$\delta = \frac{d}{dt}$$

وقطع السرعة والطياره عند الكنته
بغير الانسازن

$$X = \frac{1}{\sqrt{3}} H$$

$$Y = \frac{2}{\sqrt{3}} H$$

$$\frac{X}{Y} = 2$$

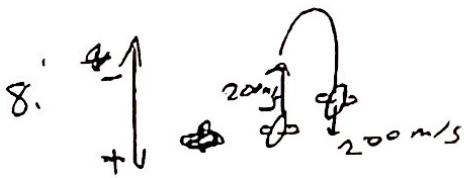
plane

$$X = \frac{1}{2} Y$$

$$\frac{1}{\sqrt{3}} = \frac{2}{\sqrt{3}}$$

$$\frac{1}{\sqrt{3}} \times \frac{\sqrt{3}}{2} = \frac{1}{2}$$

(B) half the speed of sound.

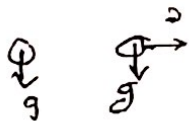


$$\Delta V = V_2 - V_1$$

$$= 200 - (-200)$$

$$= 400 \text{ m/s south}$$

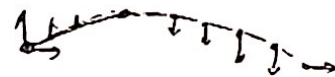
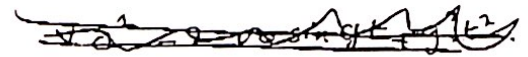
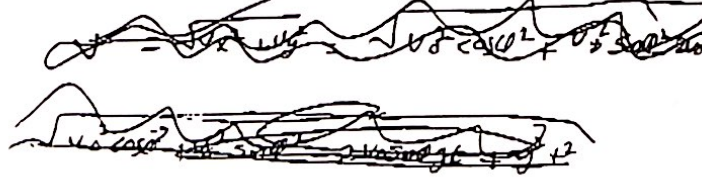
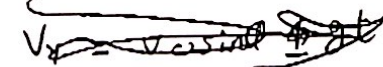
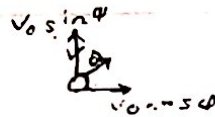
(9)



بمانه السارح الاله الفضايا
كان انقى اذن قابا تر علوه
ضرب بالاربعه نرح يضربوا على
الناس

(A)

(10)



(D) constantly increasing downward velocity (gt)

- because the gravity will accelerate the object down which increase downward velocity. $V = U + gt$

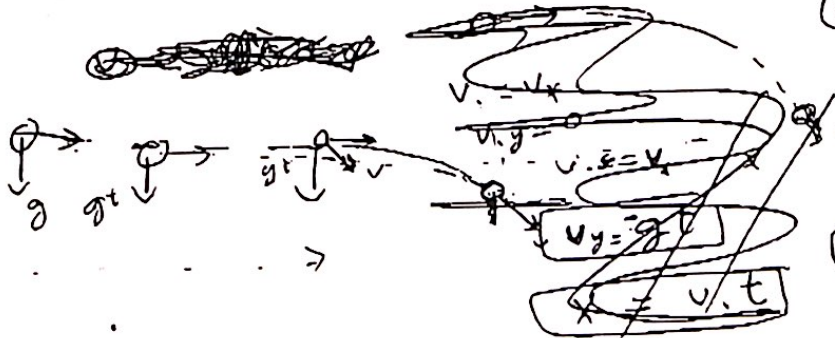
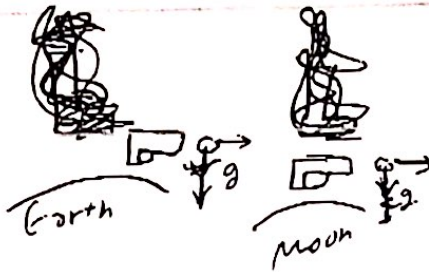
~~...~~

(11)



كسوره

12

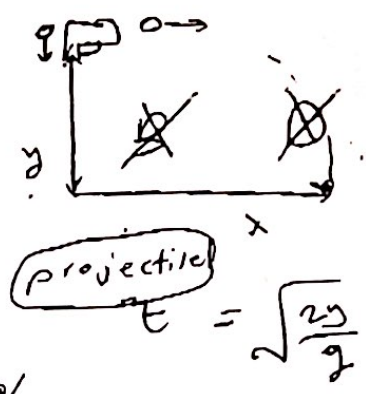


عبارته الصفحات روح رياضيوا
 بعدا ذيه يتكون الجاذبية بالسر
 اقتصرها الارض من
 امكنه السير ينقطع الصفحات
 للسر يكون ايجر من المانه
 من الارض والذفا اكر
 كمان I and II

$v_x = v_x$
 $v_{y0} = 0$
 $v_x = v$
 $v_y = -gt$
 $y = \frac{1}{2}gt^2$
 $t = \sqrt{\frac{2y}{g}}$

بما انه لا قاده
 في الحالة

14

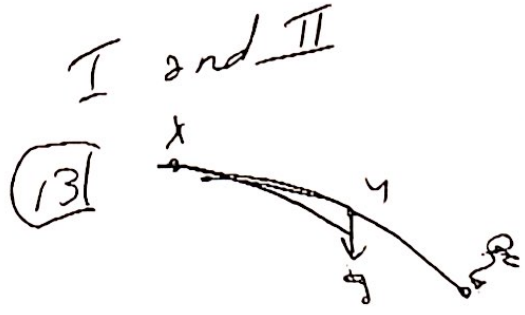


$E = \sqrt{\frac{2y}{g}}$
 $y = \frac{1}{2}gt^2$
 $t = \sqrt{\frac{2y}{g}}$

$x = v_x t$
 $x = v_x \sqrt{\frac{2y}{g}}$

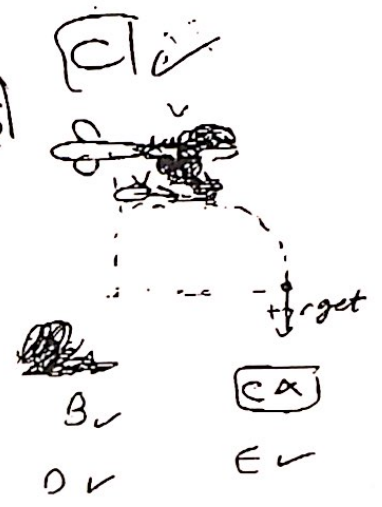
$x_m = v_x \sqrt{\frac{2y}{g}}$
 $x_m > x_e$

$t = \sqrt{\frac{2y}{g}}$
 $t_m = \sqrt{\frac{2y}{g}}$
 $t_m > t_e$



(A)

15



$x = v_0 t = v_0 \sqrt{\frac{2y}{g}}$
 $t = \sqrt{\frac{2y}{g}}$
 $v = v_0$
 $x = v_0 t - \frac{1}{2}gt^2$
 $x = v_0 \sqrt{\frac{2y}{g}}$

ازن الجوان (C)

16

$$y = v_0 \sqrt{\frac{2y}{g}}$$

$$x = \frac{1500}{36} \sqrt{\frac{2500}{10}}$$

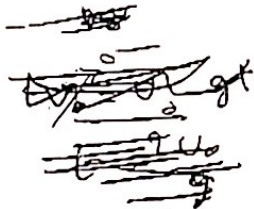
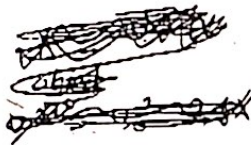
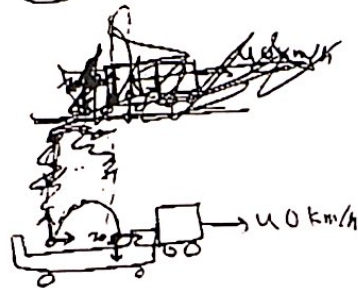
$$x \approx 41.7 \times 10$$

$$x = 417 \text{ m}$$

C) $\approx 420 \text{ m}$

17

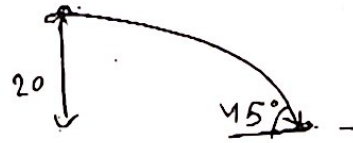
17



C

On the flat car because the object has both horizontal and vertical components
 subject اگر جسم افقی سرعت
 فقط horizontal
 ان دن ایسا اعطیسا ارتفاع و زمان
 ان دن ایسا اعطیسا

18



$$v_x = v_y$$

$$v \sin 45 = v \cos 45$$

$$v_x = v_y$$

I need to find v_y

$$v_{0y} = 0$$

$$v_y^2 = v_{0y}^2 - 2gy$$

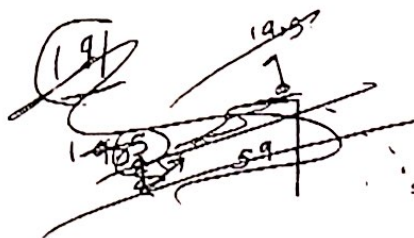
$$v_y^2 = 0 - 2g(20)$$

$$v_y^2 = \sqrt{400}$$

$$= 20 \text{ m/s}$$

$$v_x = v_0 = 20 \text{ m/s}$$

19



~~$$v_y^2 = v_{0y}^2 + 2gy$$~~

~~$$v_y^2 = 38.025 + 118.8$$~~

~~$$v_y = 39.46$$~~

~~$$v_y = v_0 = 20$$~~


~~$$39.9 = 19.5 - 10t$$~~

~~$$\frac{20}{10} = t$$~~

~~$$t = 2 \text{ s}$$~~

~~19~~ 19 $y = v_y t - \frac{1}{2} g t^2$

$$y = 19.5 t - 5 t^2$$

 - 59.4 = 19.5 t - 5 t^2

$$5 t^2 - 19.5 t + 59.4 = 0$$

$$1 - 2 \cdot 3.9 t + 11.8 = 0$$

~~3.9 t + 11.8~~

$$3.9 \pm \sqrt{15.21 + 47.2}$$

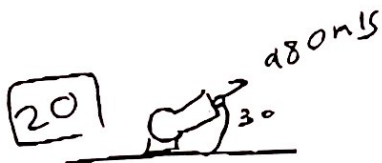
2

$$\frac{3.9 \pm 7.9}{2}$$

↙ ↘

$t = 5.9$ ~~$x = -$~~

$t = 6$



$$v_x = 980 \times \cos 30 = 848.7 \text{ m/s}$$

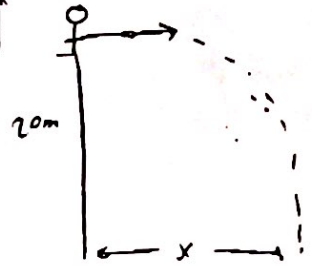
$$R = v_x t$$

6H

$$0 = v_y \sin \theta - g t$$

$$t = \frac{980 \sin 30}{g} \Rightarrow t = 2 \times 50 = 100 \text{ (3)}$$

21



$$y = 20$$

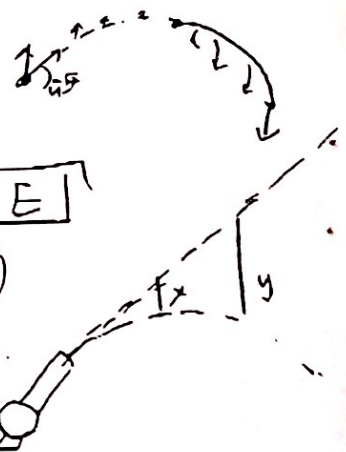
$$y = v_0 y t - \frac{1}{2} g t^2$$

$$20 = \frac{1}{2} g t^2$$

$$t = 2 \text{ s}$$

$$x = v_0 t = 20 \times 2 = 40 \text{ m}$$

22



بقایا کاز

$$v_x = v_0 \cos \theta$$

$$v_y = v_0 \sin \theta$$

بوجود کاز

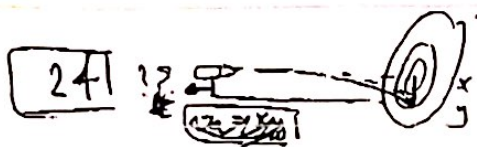
$$v_y = v_0 \sin \theta - g t$$

$$y = v_0 y t - \frac{1}{2} g t^2$$

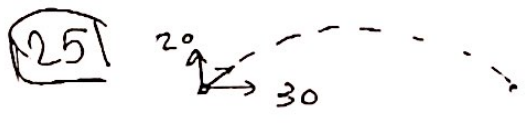
$$y = \frac{1}{2} v_0 y t$$

$$v_{\text{not}} \cdot y = \frac{1}{2} g t^2$$

$$x = \frac{1}{2} \times 10 \times 5 \text{ m}$$



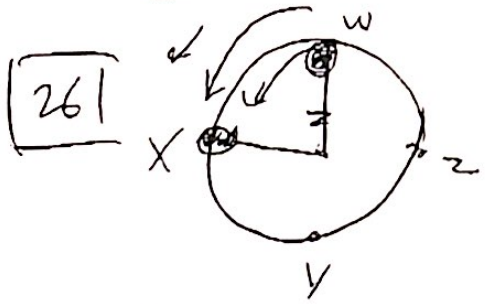
24 | $t = 0.5$
 $y = \frac{1}{2}gt^2$
 $y = \frac{1}{2}10(0.5)^2$
 $y = 0.05 \text{ m}$



25 | $v_y = v_{0y} - gt$
 $0 = 20 - 10t$

$t = 2 \text{ s}$
 $t_x = 2 \times 2 = 4 \text{ s}$
 $= 2 \times 2 = 4 \text{ s}$

$x = v_x t$
 $= 30 \times 4 = 120 \text{ m}$



27 | $x = 0$ $y = 3 \text{ m}$
 $v = 6 \text{ m/s}$

31 | $v = 6 \hat{j} \text{ m/s}$

~~$a = \frac{v^2}{R}$~~
 $= 2 \cdot 17 \text{ m/s}^2$



$v = 200 \text{ m/s}$

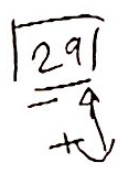
$a_{avg} = \frac{v_2 - v_1}{\Delta t}$

~~$= \dots$~~

$\frac{200 \hat{j} + 200 \hat{i}}{\Delta t}$

$= \frac{\sqrt{240000}}{20}$

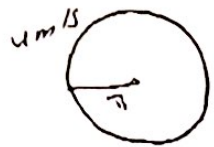
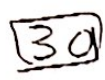
$= 14 \text{ m/s}^2$



$a_{avg} = \frac{500 + 500}{40}$

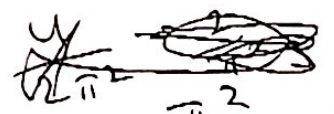
$= \frac{1000}{40}$

$= 25 \text{ km/h}^2$

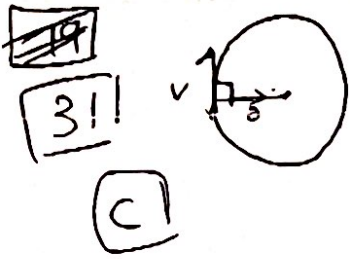


$v = r \frac{\Delta \theta}{\Delta t}$

$\Delta t = \frac{\Delta v}{a_x} = \frac{v}{a_x} = \frac{2\pi r}{a_x}$



$\Delta t = \frac{\pi^2}{2} \text{ s}$



(C)



$v_2 = 2v_1$

R same

$a_1 = \frac{v^2}{R}$

$a_2 = \frac{v_2^2}{R}$

$\frac{a_1}{a_2} = \frac{v^2}{4v^2}$

$4a_1 = a_2$

(C) ✓

(33) a) have same a

$v_A = 2v_B$

$a_A = a_B$

$\frac{v_A^2}{R_A} = \frac{v_B^2}{R_B}$

~~$\frac{4v_B^2}{R_A} = v_B^2$~~

$\frac{4v_B^2}{R_A} = \frac{v_B^2}{R_B}$

$4R_B = R_A$

34



$v = 4 \text{ m/s}$

~~$a = \frac{v^2}{R}$~~

$a = \frac{v^2}{R} = \frac{16}{25} = 32 \text{ m/s}^2 \text{ down}$

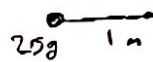
35

$a = \frac{v^2}{R} = \frac{16}{25} = 32 \text{ up m/s}^2$

36

$a = \frac{v^2}{R} = \frac{100}{20} = 5 \text{ m/s}^2$

37



$a = \frac{v^2}{R}$

$a = 28g$

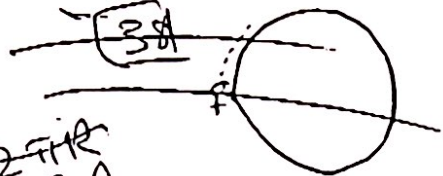
~~$T = \frac{2\pi R}{v}$~~

~~$a = \frac{v^2}{R}$~~

$v^2 = aR$

$v = \sqrt{25g} = 16 \text{ m/s}$

38



~~$a = \frac{2\pi R}{v}$~~
 ~~$25 = \frac{v^2}{R}$~~

$a = \frac{v^2}{R}$

$= \frac{400}{15.9} = 25.15 \text{ m/s}^2$

~~$\frac{1}{4} \cdot 2\pi = \frac{1}{2}$~~

~~$25 = \frac{v^2}{R}$~~

~~$R = \frac{50}{v^2}$~~

~~$R = 15.9$~~

~~$T = \frac{2\pi R}{v}$~~

~~$v = 50$~~

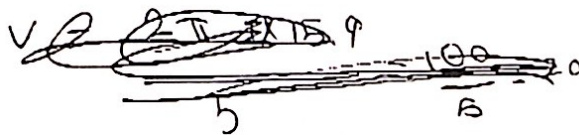
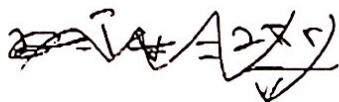
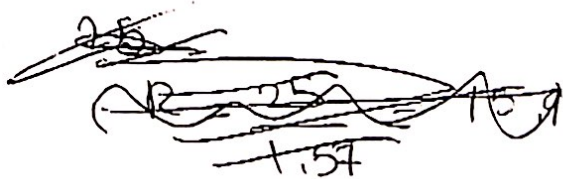


39



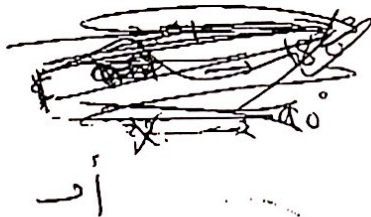
~~$s = r \theta$~~

~~$\theta = \frac{7}{2} \Rightarrow \omega = \frac{3.14}{2} = 1.57 \text{ rad}$~~



$\omega = \frac{\pi}{2T} = \frac{\pi}{27} = 0.314 \text{ rad/s}$

$a = r \omega^2 = 15.9 (0.314)^2 = 1.57 \text{ m/s}^2$
 $= 1.6 \text{ m/s}^2$



$v = \frac{25}{5} = 5 \text{ m/s}$

$a = \frac{v^2}{R} = \frac{25}{15.9} = 1.57 \text{ m/s}^2$

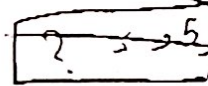
$2\pi R = 25$
 $R = 15.9$



~~$v = 2 \times 3.14 \times 1.5$~~
 ~~$= 9.42$~~

~~$a = \frac{v^2}{R} =$~~

~~$\frac{4\pi}{2\pi} \rightarrow \frac{15}{?}$~~



~~$\frac{2\pi R}{v}$~~

$v = \frac{2\pi R}{T}$
 $= \frac{2 \times 3.14 \times 15}{25}$
 $= 18.84 \text{ m/s}$

$a = \frac{v^2}{R} = 237$
 $= 240 \text{ m/s}^2$

40

$R = 8$

~~$T = 10s$~~

$T = 10s$



$T = \frac{2\pi R}{v}$

$v = \frac{2\pi R}{T}$

$= \frac{2 \times 3.14 \times 8}{10}$

$= 5 \text{ m/s}$



$R = vt$

but

$y = \frac{1}{2}gt^2$

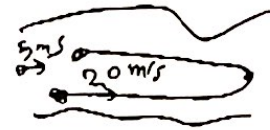
$\frac{2 \times 16}{g} = t^2$

$t = 1.8 \text{ s}$

$R = 5 \times 1.8$

$= 9.1 \text{ m}$

41



~~$t_1 = \frac{x}{v}$~~

$t = \frac{3000}{(v_{boat} + v_c)}$

$\frac{3000}{25} = 120s$

$t_2 = \frac{x}{v} = \frac{3000}{20-5} =$

$t = t_1 + t_2 = 320s$

~~42~~

~~$v_{BR} = 14 \text{ km/h}$~~

~~$v_{RC} = 6 \text{ km/h}$~~

~~$v_{mb} = 6 \text{ km/h}$~~



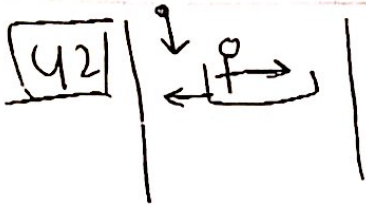
~~$v_{mR} = v_{mb} + v_{BR}$~~

~~$= 6 + 14$~~

~~$= 20 \text{ km/h}$~~

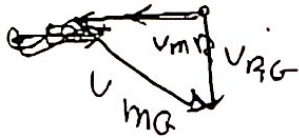
~~$v_{mC} = v_{mR} + v_{RC}$~~

~~$= 20 + 6 = 26 \text{ km/h}$~~



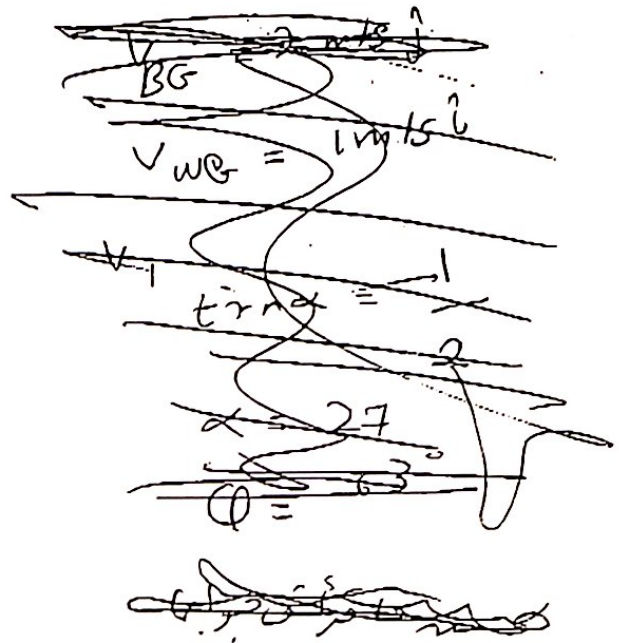
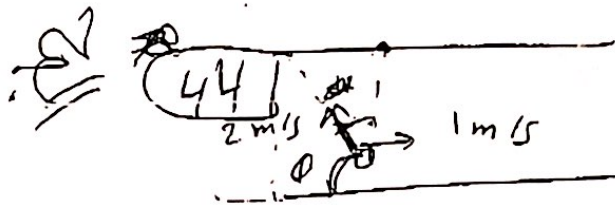
$$V_{MR} = V_{BR} - V_{MB}$$

$$V_{MR} = 14 - 6 = 8 \text{ km/h}$$

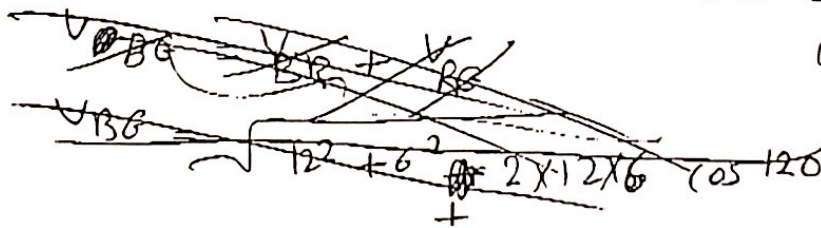


$$V_{MG} = \sqrt{6^2 + 8^2}$$

$$= 10 \text{ km/h}$$



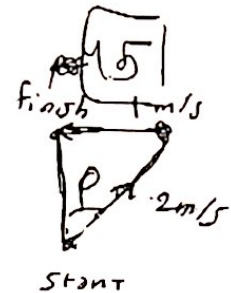
43



ازا كان القارب مع بصر 30°
من النجان نحو النهر اذن هم
عم يقص منظمه فرائسها
و عم يرد ع صيرة كان
السيار

90° لانو

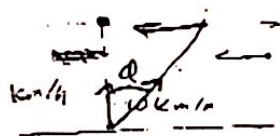
لما لب اكد وقد لفت
شرف بفروره لوصول
اسرر سير عنوا
و من لما لب طول الحان
90° صيرة



$$\sin \phi = \frac{1}{2}$$

$$\phi = 30^\circ$$

46



$$\tan \theta = \frac{5}{10} = \frac{1}{2}$$

$$\theta = 30^\circ$$

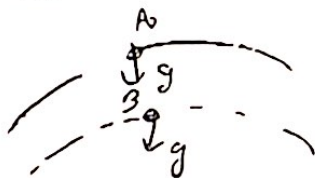
من الجواب

W of N



(B)

47



$$\begin{aligned} \theta_{AB} &= \theta_{AO} - \theta_{BO} \\ &= g - g = 0 \end{aligned}$$

تم الحساب

وأضرباً مكان

اعداد: و ناس حاويه

Chapter 5

14 B

1. B
كانوا ازانانين
تده تاثير علم الجسم

9. D net force
 $F_{net} = ma$

$W = mg$
 $F = ma$

$F = \Sigma ma$ اذن
 $\theta = 0$ وعليه ايا يكون يا ساكن

ثابتة وقوة
اذن F و g
same direction

15
الكتلة تتحرك
ويبدأ بحركة

ويفضل ساكن ادرج يتحرك
سرعته ساكنة ويفضل نفس الاصل
وهذا يعني تقديرة العصور الماز

10 B
الكتلة
لكن نسبة فاسان
Inertia العصور انما لانها

وهي اس
free fall

2
نفس الزكرة
ز 2 آت

عامة لتعني حركتها التي
خاوا اثرها على جسم بقوه

16
 $w = 9.8 m$

$F_{net} = 0$

$F = ma$
فكل ما زاد m

$\frac{W}{m} = 9.8$
وهي g يعني

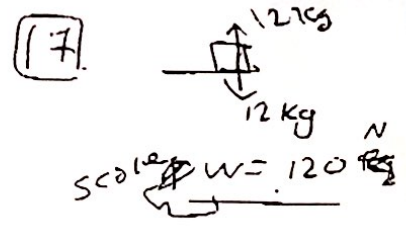
3
 $F = ma$
so D

لانهم تزيد القوة
عامة فكل ما زاد a يتر
ما اتا هو

الصم
لننا انهم فكل واحد
صم فجميعهم زينة لكانت

4 A Mrs

11 C
يبلغ
اي بيبي



5 D
 $F = kg \frac{m^2}{s^2}$

كان ساكنة و يتحرك
د بالحق

$M = \frac{W}{g} = \frac{120}{10} = 12$

6 و 7
ننا لفره

12 C
لانها
مع لكانت

$m = 12 kg$

8
 $F = ma$

فصوور سة كتلتها
بجدة انه لو اخلت
القوة رح يتاثر بس
الخطوات تصاري بوز
فانما اثر الطلاب

~~$W = mg$~~
 $= 12 \times \frac{1}{6}$
 $g = 2$

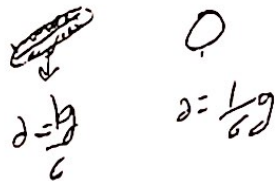
$F = 5.6 \times 1$
 $= 5.6 m/s^2$

13
 $1 kg \rightarrow 5 m/s^2$
 $2? \rightarrow 1 m/s^2$

$F_a = F_b$
 $m_a a_a = m_b a_b$

(18) $m_1 = 3m_2$
 $v = gt + v_0$
 الجواب في السؤالين

(19) $a = \frac{F}{m} = \frac{mg}{m}$



(B) the same

(20) $a = 0$
 $F \neq mg$

$F = 0$
 $5 - 3 - f = 0$
 $f = 5 - 3$
 $f = 2N$
 left word

(B)

(21) (A)

$5 - 3 = 2$
 $F = 2N$

22: 1- $N = mg$
 2- $N \sin \theta + 10 \sin \theta = mg$
 3- $N + 10 = mg$

$3 < 2 < 1$

(23) $N_i = mg$
 $N_{ii} = mg \cos \theta$

(C) (less)

(24) $m_B = 3m_A$

$F_B = F_A$

$m_B a_B = m_A a_A$

$3m a_B = m a_A$

$3a_B = a_A$

(A)

(25) zero
 $a = 0$

Frict $\rightarrow a$
 $F = 8N$

(26) u_s
 $16kg$

$(\frac{F}{m})a = \frac{\Delta v}{\Delta t}$
 $(4s) \frac{8}{16} = \Delta v$

$\Delta v = 2 m/s$

(B)

$\Delta v = 0.5$
 in this case



(A) $a = F$
 $= 2 m/s^2$
 North

على انك من بعد الاجابة
 زنا ما مضى الزمان
 بس هو

(28) $w = 9000N$
 $F = 500N$

$F = ma$
 $a = \frac{F}{m}$

$= \frac{500}{9000}$
 $= .55$ (B)

(29) a always
 $F = ma$

$F_{app} - 0 = ma$
 الجواب

(30) $A = 25tg$
 $f = 20N$ 20°


$a = \frac{F \cos 20^\circ}{m} = \frac{20 \times \frac{4}{5}}{25} = \frac{16}{25} = .64$
 $\rightarrow 75 m/s$

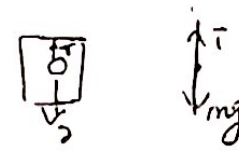
(31) $w = 1.5N$
 30°
 $v_0 = 12 m/s$
 $F = mg = 1.5N$
 down

(32) 5 kg




$F_{net} = \sqrt{8^2 + 6^2}$
 $= 10N$

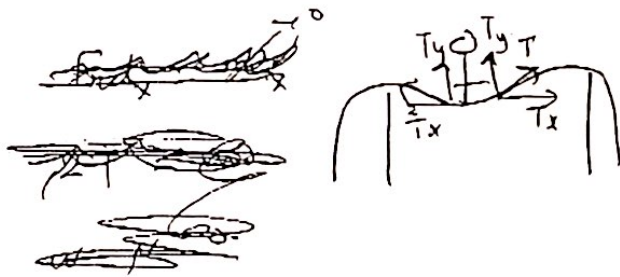
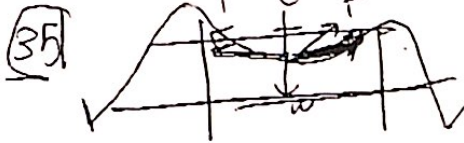
33 
 $T = 400 \text{ N}$
 $T = mg = W = 400$

37 
~~Handwritten scribbles and crossed-out text.~~

34 $A = \text{Zero}$


 لا يوجد
 الحركة عمودي
 بين السطحين

~~Handwritten scribbles and crossed-out text.~~
 $T = m(g + a)$
 $= 25(9.8 + 3)$
 $= 64 \text{ N}$



$T = ma + mg$
 $T = m(2 + 9)$
 $= m(11)$
 $= 34 \text{ N}$

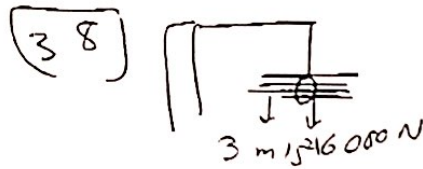
ممكن لانها تالوا

Component x و y

كيفة الف

$T_y = mg$

و يمكن ان كان x
 component فتناقص
 بتكون اكبر من w



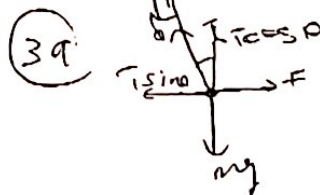
$T - mg = -ma$
 $T = mg - ma$
 $T = 16000(9.8 - 3)$
 $= 11000 \text{ N}$

36 1000 kg
 $s \uparrow$

$a = 3 \text{ m/s}^2$

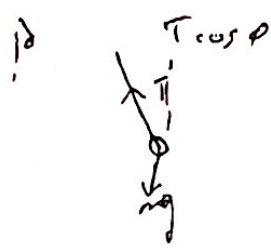
$F_{\text{net}} = ma$

$T - mg = ma$

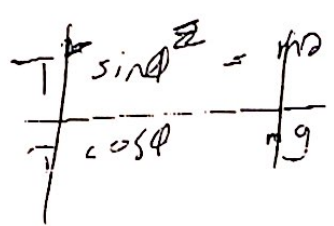


$T^2 \cos^2 \theta = mg^2$
 $T^2 \cos^2 \theta = 1$
 $T^2 \sin^2 \theta = 4$

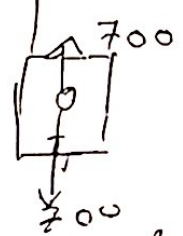
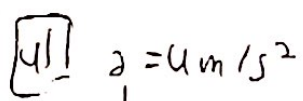
Handwritten notes and scribbles at the bottom of the page.



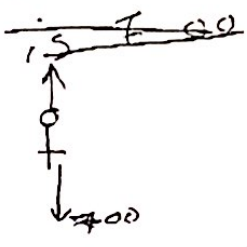
$F_{net} = ma$
 $T \sin \phi = ma$
 $T \cos \phi = mg$



$\tan \phi = 0.306$
 $\phi = 17^\circ$



~~an train from station~~



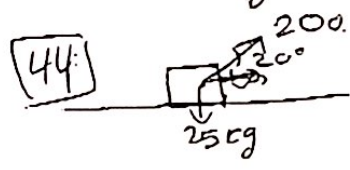
$N - 700 = ma$
 $N = ma + 700$
 $= 285.7 + 700$
 $= 985.7$
 $\approx 990 \text{ N}$



- (A) $T = m(g+a)$
- (B) $T = m(g-a)$
- (C) $T = mg$
- (D) $T = m(g-a)$
- (E) $T = mg$



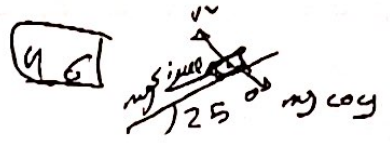
- (A) $N = m(g-a)$
- (B) $N = m(g+a)$
- (C) $N = mg$
- (D) $N = m(g-a)$
- (E) $N = mg$



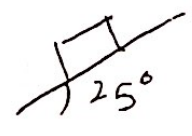
$N = mg \cos 20$
 $= 245 + 68.4$
 $= 313$
 $\approx 310 \text{ N}$



$mg \sin \theta = ma$
 $a = 4.9 \text{ m/s}^2$
 490 cm/s^2



$N = mg \cos \phi$
 $= 25 \cos 25$
 $= 22.6$
 $\approx 23 \text{ N}$

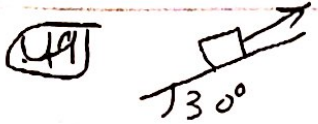


$F - mg \sin \theta = 0$
 $F = mg \sin \theta$
 $= 15 \sin 25$
 $= 10.5 \text{ N}$



$N = mg \cos \theta$
 $= 23 \text{ N}$



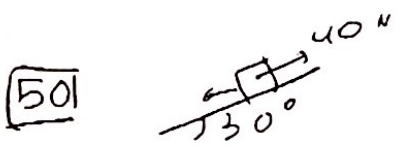


$$F - mg \sin \theta = ma$$

$$32 - 4.9m = 0$$

$$4.9m = 32$$

$$= 6.5 \text{ kg}$$



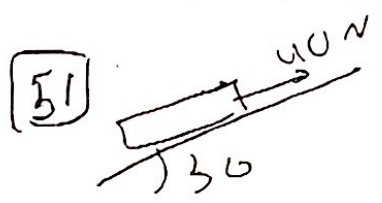
$$mg \sin \theta = F$$

$$4.9m - 40 = 2m$$

$$2.9m = 40$$

$$m = 13.79$$

قوة
(E)



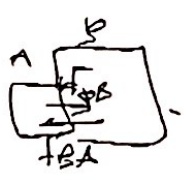
$$F - mg \sin \theta = ma$$

$$40 - 4.9m = 2m$$

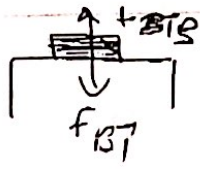
$$40 = 6.9m$$

$$m = \frac{40}{6.9} = 5.8 \text{ kg}$$

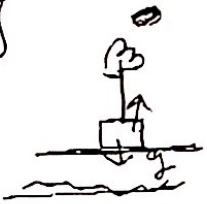
(B)



53

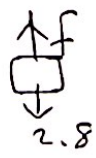


54



The block on Earth

55



$$F - mg = ma$$

$$F = mg + ma$$

$$F = 35 \text{ N up}$$

$$F_{RB} = 35 \text{ N down}$$

$$F_{BR} = 35 \text{ N up}$$

56



$$F = mg$$

$$= 90 \times 9.8$$

$$= 882 \text{ N}$$

57



$$F - mg = ma$$

$$F = m(g + a)$$

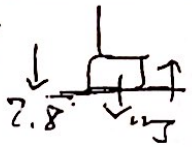
$$F = 90(10 + 1)$$

$$= 990$$

$$= 774$$

$$= 760 \text{ N}$$

58

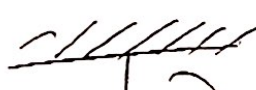


$$F_{BG} = mg$$

$$= 49 \text{ N}$$

$$F_{GB} = 49 \text{ N}$$

59



$$40g = 392$$

$$110g = 1078$$

$$W = 882$$

$$W = 1078$$

$$1078 - T = 110a$$

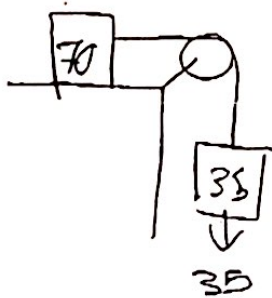
$$T - 392 = 40a$$

$$1078 - 882 = 150a$$

$$a = 1.97$$

$$T = 698 \text{ N}$$

60



$$35 - T = 3.8a$$

$$T = 7.14a$$

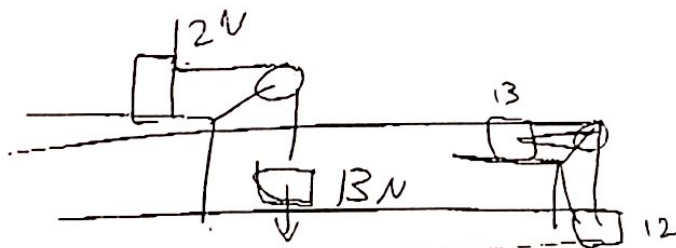
$$35 - 7.14a = 3.62$$

$$35 = 10.7a$$

$$a = 3.25 \text{ m/s}^2$$

$$= 3.3$$

61

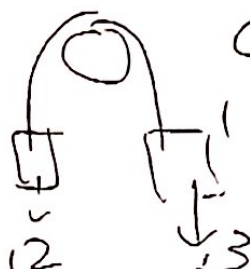


$$13 - T = 1.3a$$

~~$$T = 1.2a$$~~

~~$$13 - 1.2a = 1.3a$$~~
~~$$a = 2.5a$$~~

~~$$a = 2.5a$$~~



$$13 - T = 1.3a$$

$$T - 12 = 1.2a$$

62



$$5kg \quad 4kg$$

$$5g - T = 5a$$

$$T - 4g = 4a$$

$$1g = 9a$$

$$a = \frac{g}{9}$$

63

$$350 - T = 35a$$

$$T - 250 = 25a$$

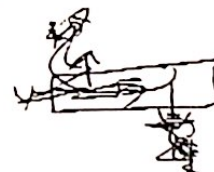
$$100 = 60a$$

$$a = 1.66 \text{ m/s}^2$$

$$T = 41.7 + 25a$$

$$= 290 \text{ N}$$

64



zero

لا نولو كان
الذراع
يكون اوتار
ذراع مع تردد
لبس هو ثابتة

65 but bar free falling body

$$a = 2g$$

$$= 9.8$$

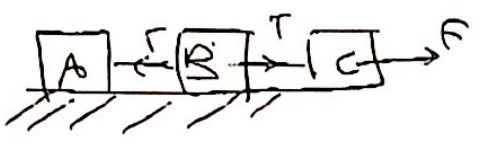
$$\frac{54}{98} \approx \frac{1}{25}$$

65



لا فوسه 9 = Xoy

(66)



$$F - T_1 = M a$$

$$T_1 - T_2 = M a$$

$$T_2 = M a$$

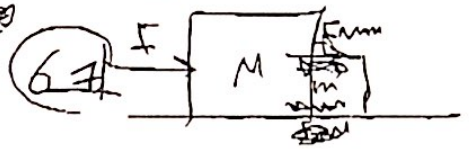
~~$$a = \frac{F}{3M}$$~~

~~T~~

$$F = 3 M a$$

if $a =$

$$F_{net} = M a$$



~~$$F - F_{nm} = M a$$~~

~~$$F - F_{nm} = M a$$~~

~~$$2 F_{nm} = (m + M) a$$~~

~~$$F_{nm} = \frac{(m + M) a}{2}$$~~

$$F - F_{nm} = M a$$

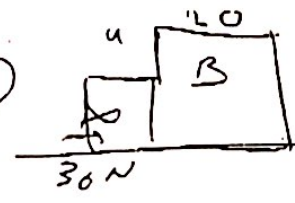
$$F_{nm} = m a$$

$$F = (M + m) a$$

$$F_{nm} = m a$$

$$F_{nm} = \frac{m F}{(m + M)}$$

(68)



$$F - F_{AB} = m a$$

$$F_{AB} = M a$$

~~F~~

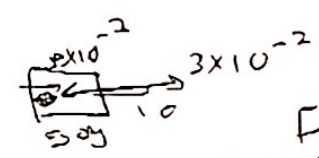
$$F = (m + M) a$$

$$36 N = 24 a$$

$$a = 1.5 \text{ m/s}^2$$

$$F_{AB} = 1.5 \times 20 = 30 N$$

(69)



$$F - F_{ST} = m a$$

$F = M a$
 $3 \times 10^{-2} = 500 a$
 $a = 0.06$

$$F_{ST} = F - m a$$

$$= 3 \times 10^{-2} - m a$$

$$= M a - m a$$

$$= (500 - 10) a$$

$$= 490 \times 0.06$$

$$= 2.94 \times 10^{-2}$$

$$= 2.94 \times 10^{-2}$$

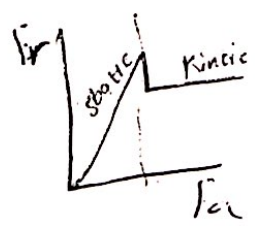
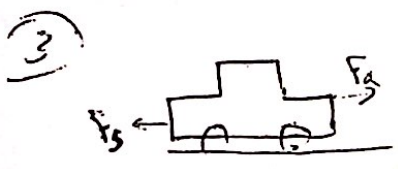
2.94

Chapter 6

اعداد: محمد
الهدل

① $F_s = M_s N = M_s mg$
تتبع زيادة الكتلة يؤدي الى زيادة F_s

② μ_k : ليس له وحدة
(2) ليس له اتجاه



The greatest retarding force $f_r = F_{smax}$
وذلك قبل بدء الانزلاق



$F = \mu_k N$

$\mu_k = \frac{f}{N} = \frac{12}{240} = 0.05$



$F_s = ma$
 $\mu_k N = ma$
 $\mu_k mg = ma$

$\mu_k = \frac{a}{g} = \frac{0.16}{4.8} = 0.0622$

⑥ $F_s = 10N$ في الحالة الاولى
 $F_s = (10N) \cos \theta$ في الحالة الثانية
 $F_s = 20N$ في الحالة الثالثة

$1 > 2 > 3$



$F = M_s N = M_s (mg - F')$
 $F = (0.4)(50 - F')$
 $F' = 50 - 25 = 25$

⑧ اذا كانت $F > F_{smax}$ تكون

$F_s = \mu_k N$

اما اذا كانت $F < F_{smax}$ تكون

$F_s = F$

~~F_{smax}~~ $F_{smax} = M_s N = (0.5)(40) = 20N$
 $F_{smax} > F$

$F_s = F = 12N$ يتالى

⑨ (نفس فكرة السؤال 8)

$F_{smax} = M_s N = (0.5)(40) = 20N$

$F > F_{smax}$

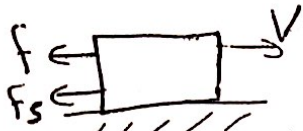
$F_s = \mu_k N = (0.4)(40) = 16N$

⑩ $F_{smax} = 200N$

$M_s N = 200$

$M_s = \frac{200}{800} = \frac{200}{800} = 0.25$

(11) f / f_{smax} (مطلوبات)



بما ان القوة اثرت باتجاه يعاكس اتجاه الحركة يتالي سرعة الجسم سوف تقل حتى تصبح صفر ثم تزداد بعد ذلك

(12) $F = f_{smax} = \mu_s N = 0.5mg$

$F - f_k = ma$
 $0.5mg - 0.4mg = ma$
 $a = 0.1g = (0.1)(9.8)$
 $a = 0.98$

(13) $v_f = v_i + at$

$0 = 15 + a(4)$

$a = \frac{-15}{4} = -3.75 \text{ m/s}^2$

$f_k = \mu_k N = \mu_k mg$

لحظة توقف الاجسام عن الدوران

$f_k = ma$



$\mu_k mg = ma$

$\mu_k = \frac{a}{g} = \frac{3.75}{9.8} = 0.382$

(14) فيما ان السرعة ثابتة يتالي التسارع يسا صفر

$P - F = ma = 0$

$P = F$

$N - fg = 0$

$N = F_g$

(15) $P \cos \theta - f = ma = 0$

$P \cos \theta = f$

بما ان $-1 < \cos \theta < 1$ يتالي

$P > f$

$P \sin \theta + N - fg = 0$

$N = fg - P \sin \theta$

$N < fg$

بما ان الجسم يتحرك بسرعة ثابتة

(16)

$F \cos \theta - f_k = ma = 0$

$F \cos \theta = f_k$

$F \cos \theta = \mu_k N = \mu_k (mg - f \sin \theta)$

$(0.8)F = (0.4)(400 - (0.6)F)$

$(0.8)F = 160 - (0.6)(F)(0.4)$

$(0.8)F + (0.24)F = 160$

$(1.04)F = 160$

$F = \frac{160}{1.04} = 153.8 \approx 150 \text{ N}$

(17)

بما ان الجسم يتحرك بسرعة ثابتة

$T \cos \theta - f_k = ma = 0$

$f_k = T \cos \theta$

(18)

$T \sin \theta + N - mg = 0$

~~$T \sin \theta = mg - N$~~

(المركبة العمودية للقوة التماسية)

~~$N = mg - T \sin \theta$~~

المطلوب

(19)

اقبال قوة التماسية لتتوازي الجسم

~~$F \cos \theta = f_{smax}$~~

~~$F \cos \theta = \mu_s N = \mu_s (mg + F \sin \theta)$~~

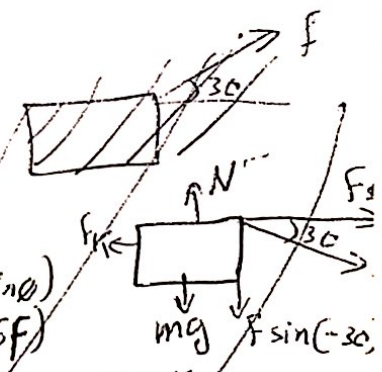
~~$F \cos(30) = (0.4)((12)(9.8) + (0.5)F)$~~

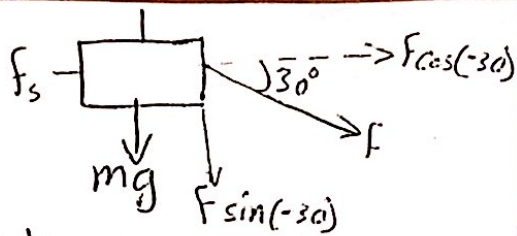
~~$F = \frac{47.04}{\cos 30} = 54.317 \text{ N} \approx 54$~~

~~$F \cos 30 = 47.04 + (0.5)F$~~

~~$F \cos 30 - (0.5)F = 47.04$~~

~~$F = \frac{47.04}{\cos 30 - \sin 30}$~~





أقل قوة تلزم لتريك الجسم عندها تكون

$$F \cos(-30) = F_{s \max} = \mu_s N = \mu_s (mg + F \sin(-30))$$

$$F \cos 30 = (0.4)(12)(0.8) + (0.5)F$$

$$F \cos 30 = 47.04 + (0.5F)(0.4)$$

$$F' = \frac{47.04}{\cos 30 - 0.2} = \frac{47.04}{0.366}$$

$$F \cos 30 = 0.2F = 47.04$$

$$F = \frac{47.04}{\cos 30 - 0.2} = 70.627 \text{ N}$$

20) $\tan \theta = \mu_s$

$$\theta = \tan^{-1}(0.4) = 22^\circ$$

21) $\tan \theta = \mu_s$

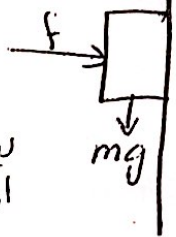
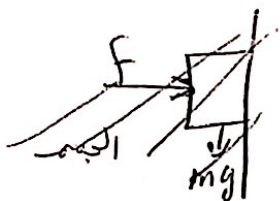
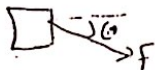
$$\theta = \tan^{-1}(0.5)$$

$$\theta = 26.6 \approx 27^\circ$$

عند هذه الزاوية تكون الكبرقوة وبتالي اعلى تسارع

22) تزداد قوة الاحتكاك عند تسارع الجسم بقوة تصلح زاوية تحت الاتجاه الافقي نتيجة زيادة N

$$F_s = \mu_s N$$



ليتحرك الجسم للأسفل
ان اعمت
 $mg > F_{s \max}$

$$F_{s \max} = \mu_s N = \mu_s F = (0.6)(12) = 7.2$$

$$F_{s \max} > mg$$

بتالي:

$$F_s = mg = (0.5)(9.8) = 4.9$$

24)

نبحث اذا كان الجسم تحرك للأسفل ام لا

$$mg = (0.5)(9.8) = 4.9 \text{ N}$$

$$F_{s \max} = \mu_s F = (0.6)(5) = 3 \text{ N}$$

$$mg > F_{s \max}$$

بتالي تحرك الجسم للأسفل

$$F_s = \mu_k N = \mu_k F = (0.8)(5) = 4 \text{ N}$$

25)

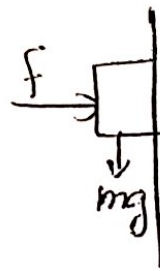
نبحث اذا كان الجسم قد تحرك ام لا

$$mg = (0.5)(9.8) = 4.9$$

$$F_{s \max} = \mu_s F = (0.6)(12) = 7.2$$

$$F_{s \max} > mg$$

و بتالي الجسم لم يتحرك التسارع يساوي صفر



(26)

$$mg = 4.9$$

$$f_{smax} = (0.6)(5) = 3$$

$$mg > f_{smax}$$

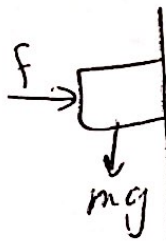
بئالي الجسم - تترك للاسفل

$$mg - f_k = ma$$

$$mg - \mu_k f = ma$$

$$4.9 - (0.8)(5) = (0.5)a$$

$$a = \frac{0.9}{0.5} = 1.8$$



(30)

$$mg \sin \theta - f_k = 0$$

$$mg \sin \theta = (\mu_k)(mg \cos \theta)$$

$$\mu_k = \tan \theta = 0.577$$

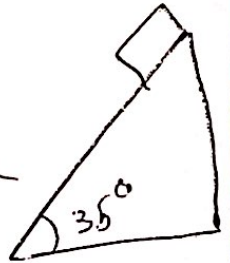


(31)

$$mg \sin \theta - f_k = ma$$

$$mg \sin \theta - \mu_k (mg \cos \theta) = ma$$

$$g \sin 35 - (0.4)(g)(\cos 35) = a$$



$$a = 2.409$$

(27)

$$F_1 = F_2 + ma$$

من اى اى الالات

من اى اى الالات

$$F_2 = F_2 + mg \sin \theta + ma$$

بئالي

$$F_1 = F_2$$

$$F_{s1} + ma = F_{s2} + mg \sin \theta + ma$$

$$F_{s1} = F_{s2} + mg \sin \theta$$

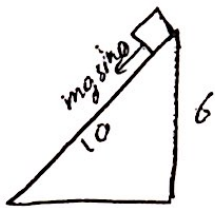
$$mg \sin \theta > 0$$

بئالي

بئالي

$$F_{s1} > F_{s2}$$

(28)



$$mg \sin \theta = f_s = \mu_s N$$

$$mg \sin \theta = \mu_s (mg \cos \theta)$$

$$\mu_s = \tan \theta$$

$$\mu_s = \tan(37^\circ) = 0.75$$

(32)

نبحث اذا تترك الجسم للاسفل
ام لا

$$mg \sin \theta = (49)(\sin 25) = 20.7 \text{ N}$$

$$f_{smax} = \mu_s N = \mu_s mg \cos \theta = (0.5)(44.4)$$

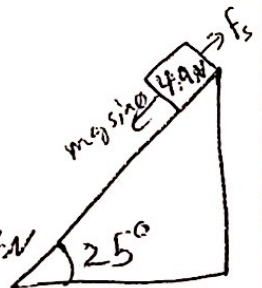
$$f_{smax} = 22.2$$

$$f_{smax} > mg \sin \theta$$

بئالي الجسم - لا يتحرك

~~بئالي الجسم - لا يتحرك~~

$$f_s = mg \sin \theta = 20.7 \approx 20$$



(33)

نبحث اذا تترك الجسم
للاسفل ام لا

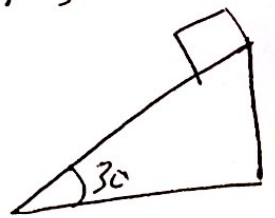
$$mg \sin \theta = 24.5 \text{ N}$$

$$f_{smax} = (0.5)(49)(\cos 30) = 21.2$$

$$mg \sin \theta > f_{smax}$$

بئالي الجسم - تترك للاسفل

$$f_k = \mu_k N = (0.4)(49)(\cos 30) = 17 \text{ N}$$



$$mg \sin \theta = 24.5 \text{ N}$$

$$f_{s \max} = 21.2 \text{ N}$$

$$mg \sin \theta > f_{s \max}$$

بما ان الجسم يتحرك للأسفل
ولكنه يثبت الجسم يجب ان
تؤثر القوة باتجاه يعاكس لاجي
 $mg \sin \theta$

$$mg \sin \theta - F - f_s = ma = 0$$

$$= mg \sin \theta - \mu_s (mg \cos \theta)$$

$$= 24.5 - 21.2$$

$$F = 3.3 \text{ N}$$

$$(35) mg \sin \theta = 24.5 \text{ N}$$

$$f_{s \max} = 21.2$$

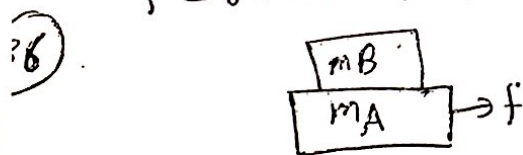
$$mg \sin \theta + f_s - F = ma = 0$$

$$F = mg \sin \theta + f_{s \max}$$

$$= 24.5 + 21.2$$

$$= 45.7 \text{ N}$$

وصفنا f_s باتجاه $mg \sin \theta$ لان ايس زياد
في قليلة في F سوف تؤدي الى حركة
الجسم للأسفل وبالتالي يكون الاحتكاك
باتجاه يعاكس ل F



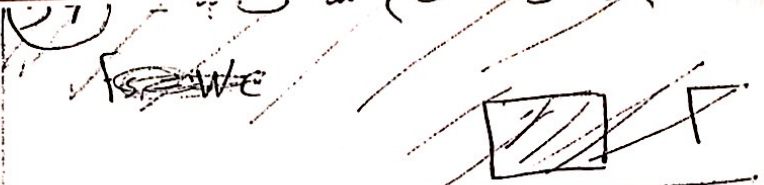
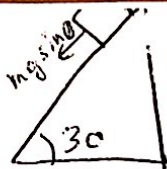
ملاحظة: اذا كانت
 $F \leq f_{s \max} \rightarrow$ بين A و B

لا ينضصل الجسمان
لذا ان كانا كانت

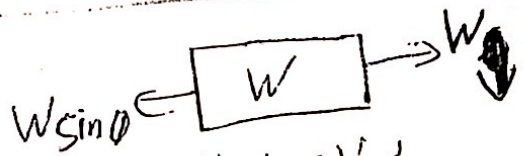
$$F > f_{s \max}$$

ينضصل الجسمان

$$f_{s \max} = \mu_s N = \mu_s (m_A + m_B)g$$



(37)



بما ان النظام ساكن

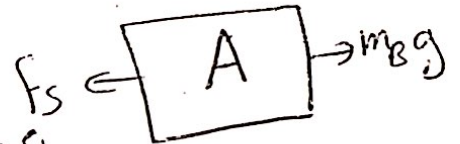
$$W \sin \theta + f_s - W \cos \theta = 0$$

$$f_s = W - W \sin 37$$

$$= 20 - 20 \left(\frac{3}{5} \right)$$

$$f_s = 8 \text{ N}$$

(38)



لكون الجسم على وشك ان
يتحرك الى اليمين

$$m_B g = f_{s \max}$$

$$f_{s \max} = \mu_s N = (0.4)(490) = 196$$

$$m_B g = f_{s \max} = 196$$

$$m_B = \frac{196}{9.8} = 20 \text{ kg}$$

(39)



$$m_A g \sin \theta - f_s - m_B g = 0$$

$$m_B = \frac{m_A g \sin \theta - f_s}{g} = \frac{m_A g \sin \theta - \mu_s m_A g \cos \theta}{g}$$

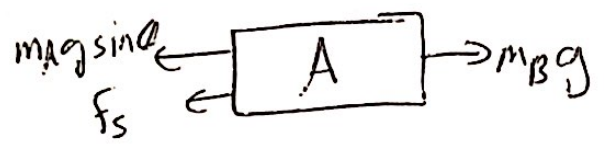
$$m_B = (10)(9.8)(\sin 35) - (0.4)(10)(\cos 35)$$

$$\leftarrow 200.75 \rightarrow$$

$$m_B = 5.735 - 3.276$$

$$m_B = 2.458 \approx 2.5$$

40

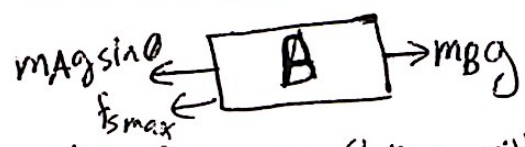


$$mBg = mAg \sin \theta + F_s = mAg \sin \theta + \mu_k (mAg \cos \theta)$$

$$mBg = (10)(9.8)(\sin 35) + (0.4)(10)(9.8)(\cos 35) = 88.32$$

$$m_B = \frac{88.32}{9.8} = 9.01 \text{ Kg}$$

41



$mAg \sin \theta = 49 \text{ N}$
 $mBg = 78.4$
 لأن mBg أكبر من $mAg \sin \theta$ بالتالي تكون الحركة باتجاه mBg والاحتكاك باتجاه $mAg \sin \theta$

$$F_k = \mu_k N = (0.2)(mg \cos 30)$$

$$F_k = (0.2)(98)(\cos 30) = 16.7 \text{ N}$$

$$mBg - mAg \sin \theta - F_k = m_{(A+B)} a$$

$$12.7 = (18) a$$

$$a = 0.705$$

باتجاه mBg

42

$mAg \sin \theta = 49$
 $mBg = 29.4$
 لأن $mAg \sin \theta$ أكبر من mBg بالتالي تكون الحركة باتجاه $mAg \sin \theta$ وتكون F_s باتجاه mBg



$$mAg \sin \theta - mBg - F_k = m_{(A+B)} a$$

$$49 - 29.4 - 16.7 = (13) a$$

$$a = 20$$

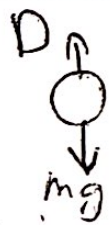
باتجاه $mAg \sin \theta$

Up

43

$f = ma$
 بيان السرعة ثابتة بتالي التسارع يساوي صفر $f = ma$ ستساوي صفر

44

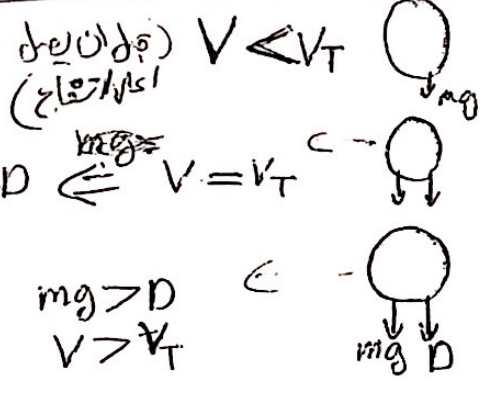


لأن مقاومة الهواء لسقوط الكرة تقل إلى قيمتها العظمى عند تسارع يساوي (mg) ولا يمكن أن تزيد عن هذا المقدار.

45


ما إن سرعته البدائية تساوي ثلاث أضعاف v_t بتالي فإن سرعته سوف تقل حتى تصبح تساوي v_t ومن ثم تثبت وبما أن السرعة تقل بتالي التسارع سالب حيث يكون اتجاهه للأعلى وبما أن اتجاه التسارع للأعلى $a > g$

46

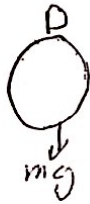


$v < v_t$
 $mg > D$
 $v > v_t$
 $mg < D$

$D=0$

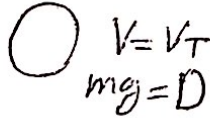


$mg = D$
 $v = v_T$



$v < v_T$
 $mg > D$

$v > v_T$
 $D > mg$



$v = v_T$
 $mg = D$

(44) $a = \frac{v^2}{R}$

بما ان السرعة ثابتة وكذا ذلك
المسافة نصف قطر الدائرة ثابت
فان التسارع يتحرك بتسارع ثابت

(50) $a = \frac{v^2}{R}$

لا تقدر على كتابة الجواب

(54) $T_1 = \frac{mv^2}{R}$

$T_2 = \frac{mv^2}{2R} = \frac{1}{2} \frac{mv^2}{R} = \frac{1}{2} T_1$

$T_2 = \frac{1}{2} T_1$

(51) $F = \frac{mv^2}{R}$

$F = \frac{(0.04)(0.0)^2}{1}$

$F = 0.0144 \text{ N}$

(55) $T_1 = \frac{mv^2}{R}$

$T_2 = \frac{(3m)(\frac{1}{2}v)^2}{R} = (3)(\frac{1}{4}) \frac{mv^2}{R} = \frac{3}{4} T_1$

(52) $T = \frac{mv^2}{R}$

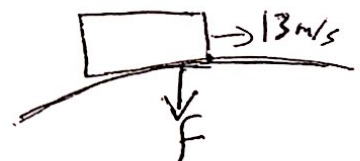
$V = 150 \text{ rev/min} = \frac{150(2\pi R)}{60} \text{ m/s}$

$V = 9.42$

$T = \frac{(0.2)(9.42)^2}{0.6} = 30 \text{ N}$

(56) التسارع من الكسار الدائري يكون
دائماً باتجاه المركز

(57)



لكي يفتح الباب يجب ان تكون
السرعة 13 m/s

$F = \frac{mv^2}{R}$

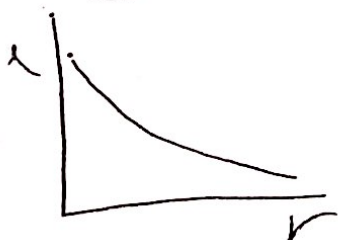
$200 = \frac{(800)}{10} (13)^2 \Rightarrow R = 67.6$

لكي يفتح الباب يجب ان تكون
السرعة 800 N

$800 = \frac{(80)(v^2)}{67.6} \Rightarrow v = \sqrt{676} = 26$

(53) $a = \frac{v^2}{R}$

بما ان السرعة ثابتة وبالتالي فان زيادة
تؤدي الى نقصان قيمة التسارع



$$(58) F = \frac{mv^2}{r}$$

$$r_1 = \frac{mv^2}{F}$$

$$r_2 = m \frac{(2v)^2}{F} = 4 \frac{mv^2}{F}$$

$$r_2 = 4r_1$$

$$(59) F_s = MBN = \frac{mv^2}{r}$$

$$(0.5)mg = \frac{mv^2}{30}$$

$$v^2 = 147$$

$$v = 12 \text{ m/s}$$

$$(60) F_s = \frac{m v_{\max}^2}{R}$$

$$v_{\max}^2 = \frac{(F_s)(R)}{m} = \frac{(900)(1000)}{1000} = 900$$

$$v_{\max} = \sqrt{900} = 30 \text{ m/s}$$

تبقى السيارة تتحرك على المنحنى بحداد
سرعتها أقل أو تساوي v_{\max} وبما أن
السيارة دخلت المنحنى بسرعة أكبر
من 30 m/s وهي 40 m/s يتأرجح
السيارة من المنحنى

$$(61) a = \frac{v^2}{R}$$

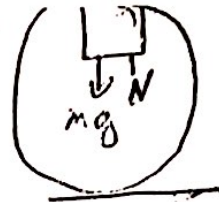
$$a = \frac{(18)^2}{75} = 4.32 \text{ m/s}^2$$

$$\tan \theta = \frac{a}{g} = \frac{4.32}{9.8} \frac{\Delta g}{a}$$

$$\theta = \tan^{-1} \left(\frac{4.32}{9.8} \right)$$

$$\theta = 23.788 \approx 24^\circ$$

(62)



$$\Sigma F = mg + N$$

$$N = mg$$

$$\Sigma F = 2mg$$

من السؤال السابق

$$\Sigma F_{\text{net}} = 2mg = ma$$

$$a = (2)(9.8) = 19.6 \text{ m/s}^2$$

$$a = \frac{v^2}{R}$$

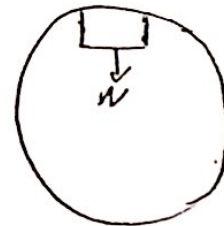
$$v^2 = (a)(R) = (19.6)(20) = 392$$

$$v = 19.8 \approx 20$$

(64)

$$F_g = N = mg$$

$F_b = 0 \rightarrow$
تبقى منحنى بحداد الحداد
يدور



حداد

$$F_s = 0$$

(65)

$$T - mg = ma$$

$$T = mg + ma$$

$$= (2)(9.8) + (2) \left(\frac{v^2}{R} \right)$$

$$= 19.6 + 2 \left(\frac{16}{1} \right)$$

$$= 19.6 + 32$$

$$= 51.6 \approx 52 \text{ N}$$



33

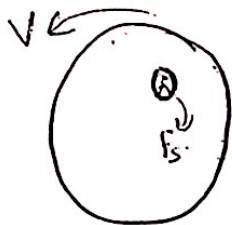
$$T - mg = ma$$

$$T - m\left(\frac{v^2}{R}\right) - mg$$

$$= 32 - 19.6$$

$$= 12.4 = 12 N$$

7



$$N = mg = \text{constant}$$

$$s_{max} = \mu_s N$$

بجانب N ثابت بتالي

$$f_{s max} = \text{ثابت}$$

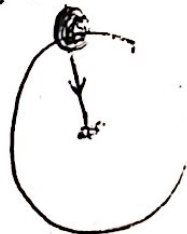
$$s = ma = m \frac{v^2}{R}$$

بتالي f تزيد مع تسارع

f s max و اسي زيادة بعد ذلك
تكون في اثنائها العلاقة العكس

8

$$T = mg$$



$$\frac{mv^2}{R} = mg$$

$$v^2 = (0.7)(9.8)$$

$$v^2 = 6.86$$

$$v = 2.61 \text{ m/s}$$

69

$$a = \frac{V}{R} = \frac{(22)^2}{45} = 10.755$$

$$\tan \theta = \frac{a}{g}$$

$$= \frac{10.755}{9.8}$$

$$\theta = 47.66$$



70

$$a = \frac{v^2}{R}$$

$$R = \frac{v^2}{a}$$

بما ان السرعة ~~تزداد~~ زادت اى

$$(4v)^2 = 4v^2$$

~~بتالي~~ بتالي $2V$

بتالي R تزداد اربع اضعاف

71



$$mg \sin \theta = ma$$

$$mg \sin \theta = \frac{mv^2}{R}$$

$$\theta = \sin^{-1} \frac{v^2}{(g)(R)}$$

$$\theta = 17^\circ$$

erg \checkmark الأرع \checkmark وحدة قياس الطاقة
 $W = \Delta K.E$ \checkmark \checkmark \checkmark

Ft lb \checkmark وحدة قياس القوة

Natt \times وحدة قياس القوة

$1, m \Rightarrow W = F \cdot d = N \cdot m$

Joule $\Rightarrow W = \Delta K.E = J$

Scalar quantity

Power / speed

energy / distance / time

vector quantity

velocity force displacement

acceleration / force / weight

Weight

3) $W = \vec{F} \cdot \vec{d}$
 بما ان الازمان تتساوى في
 اتجاهي الشكل يساوي في

1) $W = F \cdot d = (10)(10) = 100$
 في الاتجاه الاخر
 في الاتجاه الاخر

$W = (F \cos \theta)(10) < 100$
 في اتجاه الاخر

$W = (F)(d)(\cos 90) = 0$

$\theta > 273$

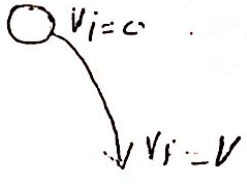


شدة القوة المركزية يساوي صفر
 لان الزاوية بين (F) و (d)
 دائماً يساوي 90 و $\cos 90 = 0$
 $w = 0$

(6) $W = 0$ (نفس فكرة سوال 5)

(7) $W_{mag} = \Delta K$

V_f دائماً موجبة كان
 V_i اكبر من



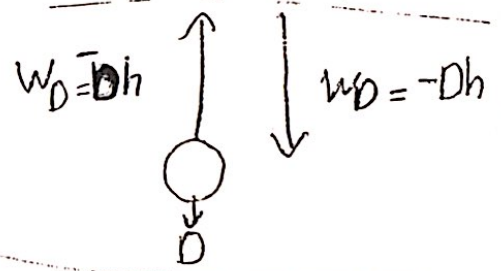
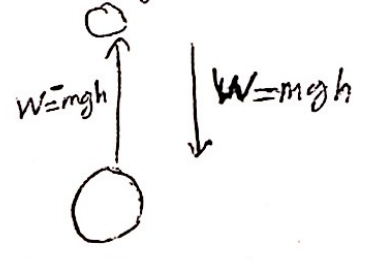
(8) ~~$W_{mag} = \Delta K$~~ $W = mgh$

V_f اكبر من V_i تكون ΔK سالبة



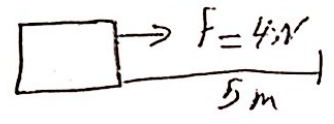
(9) $W_{mag} = mgh - mgh = 0$

$W_D = -Dh - Dh = -2Dh$



(10)

$W_f = F \cdot d = (4)(5) = 20 J$

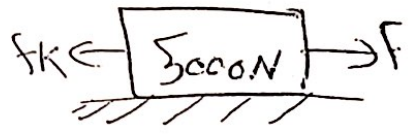


(11)

بما ان السرعة ثابتة يتاكد
 التسارع يساوي صفر

$F - f_k = ma = 0$

$F = f_k = \mu_k N = (0.05)(5000) = 250 N$



$W_f = F \cdot d = (250)(1000) = 2.5 \times 10^5 J$

(12) $f_k \leftarrow \boxed{6000\text{ N}} \rightarrow f$
 عند التسارع يساوي القوة
 $F = F_k = \mu_k N = (0.05)(6000) = 300$
 $W_f = f \cdot d = (300)(1000) = 3 \times 10^5$

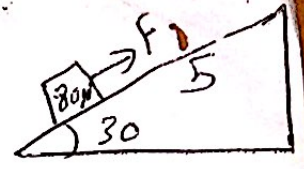
(13) $f_k \leftarrow \boxed{6000} \rightarrow f$
 $a = 0.2 \text{ m/s}^2$
 $F - f_k = ma$
 $F = F_k + ma = 300 + \frac{6000}{10}(0.2)$
 $F = 420 \text{ N}$
 $W_f = F \cdot d = (420)(1000) = 4.2 \times 10^5$

(14) $F_b = mg = (1)(10) = 10 \text{ N}$
 $W_b = f \cdot d = (10)(1) = 10 \text{ J}$

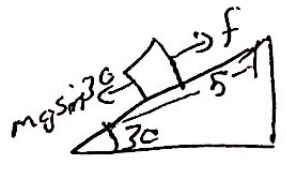
(15) $d = \text{one revolution}$
 $= 2\pi r = 15.7 \text{ m}$
 $W_f = F \cdot d = Fd \cos \theta$
 $= (3)(15.7) = 47.1$

(16) $mg \sin 30^\circ$
 عند التسارع ثابت
 يتساوى التسارع
 يساوي التسارع
 $F_m - mg \sin 30 = 0$
 $F_m = mg \sin 30 = (100)(0.5) = 50 \text{ N}$
 $W_m = F_m \cdot d = (50)(10) = 500 \text{ J}$

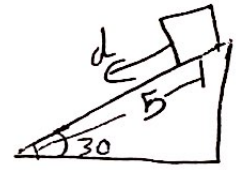
(17) $a = 1.5 \text{ m/s}^2$
 $F - mg \sin 30 = ma$
 $F = mg \sin 30 + ma = (80)(0.5) + \frac{80}{10}(1.5)$
 $F = 28 \text{ N}$
 $W_f = f \cdot d = (28)(5) = 140 \text{ J}$



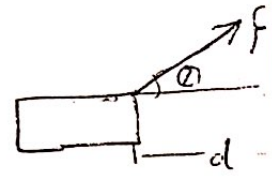
(18) $F - mg \sin 30 = 0$
 $F = (80)(0.5) = 40 \text{ N}$
 $W_f = (40)(5) = 200 \text{ J}$



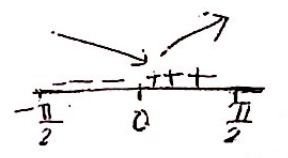
(19) $W_{mg} = mg \cdot d$
 $= (mg)(d)(\cos 90 + \theta)$
 $= (mg)(d)(\sin 30)$
 $= (80)(5)(0.5)$
 $= 200 \text{ J}$



(20) $W = fd \cos \theta$



(21) $F_k = \mu_k N = \mu_k (mg + F \sin \theta)$
 $F \sin \theta = 0$
 $\sin \theta = 0$
 $\theta = 0$
 $W_f = Fd \cos \theta$
 $dW = Fd \sin \theta = 0$
 $0 = 0$



نشفل مركبة القوة على x و y وعلى z -axis
 الحالة تكون 90° بين F و d
 ونتيجة لذلك يكون شغل F

$$W_f = F_x \cdot d = (4)(5)(1) = 20 \text{ J}$$

23) $W_s = \frac{1}{2} K (x_i^2 - x_f^2)$

يكون W_s موجب اذا كان

$$x_i^2 > x_f^2$$

24) $F = -K \Delta x$

من الحالة الاولى

$$00 = -K(40 - x_0) \quad \text{--- (1)}$$

$$200 = -K(60 - x_0) \quad \text{--- (2)}$$

يحل (1) و (2) من خلال طرح (1) من (2)

~~$$100 = 40K - Kx_0 + 60K - Kx_0$$~~

~~$$100 = 40K - Kx_0 + 60K - Kx_0$$~~

$$20 - 100 = K(60 - x_0) - K(40 - x_0)$$

$$100 = 60K - Kx_0 - 40K + Kx_0$$

$$100 = 20K$$

$$K = 5$$

بمعرفتي (1)

$$100 = 5(40 - x_0)$$

$$x_0 = 20$$

من الحالة الثانية

$$100 = K(30 - x_0)$$

$$= 5(30 - 20)$$

$$= 50$$

25) $F = K \Delta x$

$$-mgy = -Kx$$

من الحالة الاولى

$$(4)(10) = K(3 \text{ cm})$$

$$K = \frac{40}{3} \text{ N/cm}$$

من الحالة الثانية

$$60 = \left(\frac{40}{3}\right)(\Delta x)$$

$$\Delta x = 4.5 \text{ cm}$$

وبما انه يوجد زبرك z ونيزك y

فان كل منهما يتحرك بمقدار 4.5 cm

$$\Delta x = 4.5 + 4.5 = 9 \text{ cm}$$

26) $W = \int f dx = \int_0^L Ax dx$

$$W = \frac{Ax^2}{2} \Big|_0^L = \frac{AL^2}{2} - 0 = \frac{AL^2}{2}$$

27) $W = \int f dx = \int_0^L ax + bx^2$

$$= \frac{ax^2}{2} + \frac{bx^3}{3} \Big|_0^L = \frac{aL^2}{2} + \frac{bL^3}{3}$$

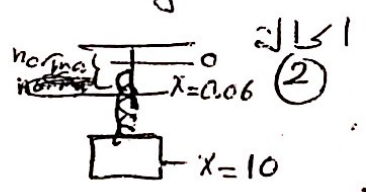
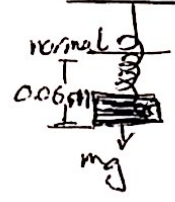
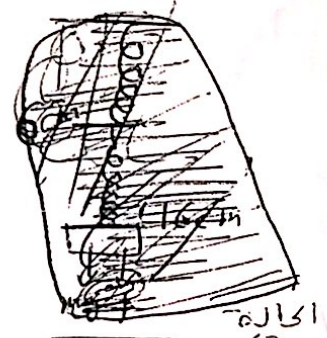
28) $mg = K \Delta x$

$$20 = K(0.06) \Rightarrow K = \frac{20}{0.06} \text{ N/m}$$

$$W = \frac{1}{2} K (x_i^2 - x_f^2)$$

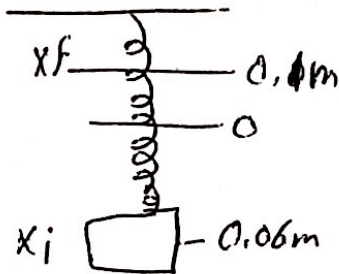
$$= \frac{1}{2} \left(\frac{20}{0.06}\right) ((0.06)^2 - (0.16)^2)$$

$$= -3.66$$



(29) $k = \frac{20}{0.06}$

$w = \frac{1}{2} k (x_i^2 - x_f^2)$
 $= \frac{1}{2} \left(\frac{20}{0.06} \right) (0.06^2 - 0.1^2)$
 $= -1.06 \text{ J}$



(30) الجسم الأول: $K_1 = \frac{1}{2} m v^2 = \frac{1}{2} (3M)(v)^2 = \frac{3}{2} M v^2$

الجسم الثاني: $K_2 = \frac{1}{2} (3M)(2v)^2 = \frac{1}{2} (3M)(4v^2) = 6 M v^2$

الجسم الثالث: $K_3 = \frac{1}{2} (2M)(3v)^2 = 9 M v^2$

الجسم الرابع: $K_4 = \frac{1}{2} (M)(4v)^2 = 8 M v^2$

~~الجسم الخامس: $K_5 = \frac{1}{2} (M)(4v)^2 = 8 M v^2$~~

الجسم الثالث له أكبر طاقة حركية

$K_3 > K_4 > K_2 > K_1$

(31) $V_x = \frac{1}{2} m v_x^2 = \frac{1}{2} (500) v^2 = 250 v^2$

$V_y = \frac{1}{2} m v_y^2 = \frac{1}{2} (2000) v^2 = 1000 v^2$

$V_x = \frac{1}{4} V_y$

$V_y : V_x$
 $4 : 1$

$V_i = 12 \text{ m/s}$ $V_f = 0$
 8000 N \square

(32)

$\Delta K = K_f - K_i$
 $= \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2$
 $= 0 - \frac{1}{2} \left(\frac{8000}{9.8} \right) (12)^2$
 $= -58775.5$
 $= -5.9 \times 10^4 \text{ J}$

(33) $w = \Delta K \cdot \epsilon$

~~$w = \Delta K \cdot \epsilon$~~

$w = \frac{1}{2} m (v_f^2 - v_i^2)$

يكون الشغل موجب عندما تكون

$v_f^2 > v_i^2$

(34) $T = \frac{mv^2}{R}$

الجهد ينقطع اذا زادت (T) عن (16M) أكبر طاقة حركية يمكن الحصول عليها تكون عند أكبر سرعة / أو أكبر سرعة يمكن الحصول عليها بحيث لا ينقطع الجهد عندما تكون

$T = 16$

$T = 16 = \frac{mv^2}{0.5}$

$v^2 = \frac{8}{m}$ (1)

$K_{\text{max}} = \frac{1}{2} m v^2 = \frac{1}{2} m \left(\frac{8}{m} \right) = \frac{8}{2} = 4 \text{ J}$

(35) بما ان الطاقة الحركية لا تعتمد على التسارع بتالي تكون متساوية للجسمين لهما نفس الكتلة ويتحركان بنفس السرعة حتى كوكبين مختلفين

$K_{\text{moon}} = \frac{1}{2} m v^2$

$K_{\text{Earth}} = \frac{1}{2} m v^2$

$K_{\text{moon}} : K_{\text{Earth}}$
 $1 : 1$

نظرة: الكتلة تختلف كوكب لآخر اختلاف في الوزن لا يختلف من ذلك لآخر

(36) الجواب C

$K = \frac{1}{2} m v^2 = k g m^2 = \frac{M L^2}{s^2}$ $\frac{M L^2}{T^2}$ \rightarrow مسافة \rightarrow زمن

(37)



$w = \Delta K \cdot \epsilon$

$w = K_f - K_i = 0 - K_i$

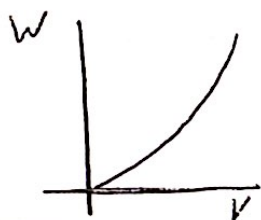
$w = -\frac{1}{2} m v^2 = \text{Kinetic energy of the object}$

38) $W_{net} = \Delta K_{m.t} = K_f - K_i$
 $= \frac{1}{2} m (v_f^2 - v_i^2)$
 $= \frac{1}{2} (5) ((10)^2 - (6)^2)$
 $= 160 \text{ J}$

9) $W = \Delta K.E = K_f - K_i = K_f - 0$
 $W = \frac{1}{2} m v^2$

$W \propto v^2$

النتيجة يتناسب طردياً مع v^2



40) $W = F_r \cdot d$

نحتاج لمعرفة d كما ان
 F_r تكون متغيرة حتى
 تصبح $V = V_f$ ومن ثم تثبت
 ونقيس مسافة mg يتالي نحتاج
 الى منحنى F_r vs t

1) $W = \Delta K = \frac{1}{2} m (v_f^2 - v_i^2)$
 $= \frac{1}{2} (4) (0 - (3)^2)$
 $= -18 \text{ J}$

2) $W = F \cdot d = \Delta K.E = K_f - K_i$

$(F_1)(d_1)(1) = 0 - K_{i1}$ للجسم الاول

$F_2(d_2)(1) = 0 - K_{i2}$ للجسم الثاني

$F_1 = F_2$ بها ان

$K_{i1} = K_{i2}$ @

$d_1 = d_2$ يتالي

43) $W = f \cdot d = \Delta K = K_f - K_i$

$(F)(d)(-1) = 0 - \frac{1}{2} m v^2$

$f d = \frac{m v^2}{2} \Rightarrow f = \frac{m v^2}{2 \cdot d}$

44

$W = f \cdot d = \Delta K.E = K_f - K_i$

$(3)(2\pi R^2) = \frac{1}{2} m v^2 - 0$

$v = \sqrt{\frac{(3)(2\pi R^2)(2)}{m}}$

$= \sqrt{\frac{6(2\pi(2.5))}{0.5}}$

$v = \sqrt{188.5} = 13.7 \text{ m/s} \approx 14$



45

المطلوب حساب قوة الشد

$T = \frac{m v^2}{R} = \frac{(0.5)(13.7)^2}{2.5} = 37.7 \text{ J}$

46

$\Delta E_{m.t} = \Delta K + \Delta U = 0$

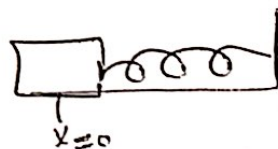
$K_f - K_i + U_f - U_i = 0$

$0 - \frac{1}{2} m v_i^2 + \frac{1}{2} k x_f^2 - 0 = 0$

$\frac{1}{2} m v_i^2 = \frac{1}{2} k x_f^2$

$x_f = \sqrt{\frac{m v_i^2}{k}}$

$= \sqrt{\frac{(2)(25)}{200}} = \sqrt{0.25} = 0.5 \text{ m}$



(47) ~~بما ان~~ الطاقة الحركية تزيد ان تزداد بالسرعة بشكل منتظم مع مرور الوقت بتالي

$$K.E(t) = ct$$

$$\frac{1}{2}mv^2 = ct \Rightarrow v = \sqrt{\frac{2ct}{m}} = \sqrt{\frac{2c}{m}} \sqrt{t}$$

$$a = \frac{dv}{dt} = \sqrt{\frac{2c}{m}} \frac{1}{2\sqrt{t}}$$

$$F = ma = \left(\frac{m}{2} \sqrt{\frac{2c}{m}}\right) \frac{1}{\sqrt{t}}$$

$$F \propto \frac{1}{\sqrt{t}}$$

(48) $v_i = \sqrt{(4)^2 + (3)^2} = 5$

$$v_f^2 = (2)^2 + (3)^2 = 13$$

$$W = \Delta K = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2 = \frac{1}{2}(2)(13) - \frac{1}{2}(2)(25) = 13 - 25 = -12J$$

(49) $F = ct$

$$ma = ct$$

$$a = \frac{ct}{m}$$

$$v = \int_0^t a dt = \int_0^t \frac{c}{m} t dt$$

$$v = \frac{c}{2m} t^2$$

$$K.E = \frac{1}{2}mv^2 = \frac{1}{2}m \left(\frac{c}{2m} t^2\right)^2$$

$$K.E = \left[\frac{c^2}{4m}\right] t^4$$

$$K.E \propto t^4$$

(50) reading of scale = $F = kx$

$$v_f^2 = v_i^2 + 2gy$$

$$v_f^2 = 0 + (2)(10)(2)$$

$$v_f^2 = 40$$

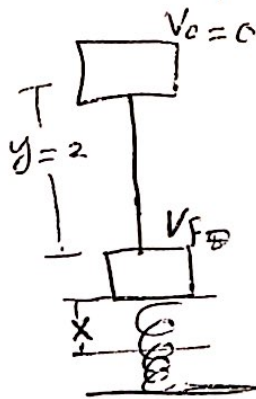
من قانون حفظ الطاقة الميكانيكية

$$\Delta K = \Delta U$$

$$\frac{1}{2}mv_f^2 = \frac{1}{2}kx^2$$

$$x = \sqrt{\frac{40}{105}} = 0.02$$

$$F = kx = (1.5 \times 10^5)(0.02) = 3 \times 10^3 N$$



(51) $W = F \cdot d = \frac{1}{2}mv^2$

$$F = \frac{mv^2}{2d} = \frac{m}{L} \frac{L^2}{t^2} = \frac{mL}{t^2}$$

$$F = F_0 e^{-kx}$$

$$F_0 = \frac{mL}{t^2}$$

$$k = \frac{L}{x} = \frac{1}{L}$$

$$k.E = \frac{mL^2}{t^2}$$

$$k.E = \frac{mL^2}{t^2}$$

يتغير مع الإزاحة بتغير في الإجابة

(a) $\frac{F_0}{k} = \frac{mL}{\frac{1}{L} t^2} = \frac{mL^2}{t^2} = K.E$ ✓

(b) $\frac{F_0}{e^{kx}}$ ✗ (لا يجوز ان تكون e^{kx})

(c) $kF_0 = \left(\frac{1}{L}\right) \left(\frac{mL}{t^2}\right) = \frac{m}{t^2} \neq K.E$ ✗

(d) $\frac{1}{2(kF_0)^2} = \frac{1}{\left(\frac{m}{t^2}\right)^2} = \frac{t^4}{m^2} \neq K.E$ ✗

(e) $k e^{kF_0}$ ✗ (لا يجوز ان تكون e^{kF_0})

النسبة بين القوة التي بذلها الارتفاع إلى القوة التي تؤثر بها

بما أن الارتفاع المواد رفع الجسم إليه يساوي عن الحالتين يتالي فإن وضع الجسم بشكل عمودي يحتاج إلى قوة أكبر من القوة اللازمة لرفع عن

4) Watt
 وحدة قياس Power
 $= f \cdot v = (ma) \cdot v$
 $= \text{kg} \left(\frac{\text{m}}{\text{s}^2} \right) \left(\frac{\text{m}}{\text{s}} \right)$
 $= \text{kg} \cdot \text{m}^2 / \text{s}^3$

من السؤال السابق
 $= \text{kg} \cdot \text{m}^2 / \text{s}^3$
 $= \text{mL}^2 / \text{T}^3$

6) watt → وحدة قياس القدرة
 أما باقي الوحدات لطاقته

7) $ma = F = \text{Newton}$

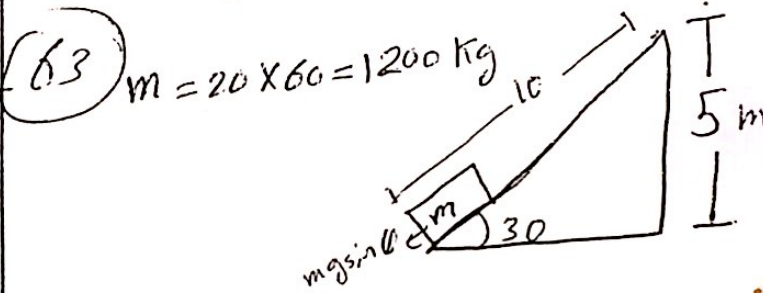
8) $\text{Watt} \cdot \text{second} = (P)(t) = \frac{W}{t}(t) = W$
 $= \text{Energy}$

7) Kibwatt - hours
 وحدة قياس الطاقة
 وبتساوي work

11) $h = 2R = 40 \text{ m}$
 $m = 0.01 \text{ kg}$
 $W = (0.01)(40)(40) = 4 \text{ J}$

ملاحظة: الشغل لا يعتمد على الوقت وبتالي (0.75 min) لا فائدة منها
 Power لأنه يعتمد على الوقت
 $P = \frac{W}{\Delta t}$

62) الشغل لا يعتمد على الوقت وإنما يعتمد على مقدار القوة ويعتمد أيضاً على نقطة البداية ونقطة النهاية (الازاحة)



$P = F \cdot v = (mgsin\theta) \left(\frac{10\text{m}}{60\text{s}} \right)$
 $= (6000) \left(\frac{10}{60} \right) = 1000 \text{ watt}$

64) $P = \frac{W}{\Delta t} = F \cdot v$

$P = \frac{(80)(2)}{30} = 5.3 \text{ watt}$

65) $F = ma$
 $50 = 2a \Rightarrow a = 25 \text{ m/s}^2$
 $v_0 = 0 \Rightarrow f = 50 \text{ N}$

$d = v_0 t + \frac{1}{2} a t^2$
 $= 0 - \frac{1}{2} (25) (2)^2 = 50 \text{ m}$
 $v_f = v_0 + at = 0 + 25(2) = 50$
 $v_f = 10(2) = 20$

$\text{Work} = f \cdot d = 50 \times 50 = 2500 \text{ J}$

rate of work $K \frac{\Delta W}{\Delta t} = \frac{2500}{2} = 1250 \text{ watt}$

(66) $F = ma \Rightarrow a = \frac{F}{m}$
 $a = \frac{50}{2} = 25 \text{ m/s}^2$ $p = (v) \cdot t$
 ~~$d = vt = \frac{1}{2} at^2$~~ $v^2 = v_0^2 + 2ax$
 ~~$2 = 0 + \frac{1}{2}(25)t^2$~~ $v = \sqrt{\frac{1}{2}(25)(2)}$
 ~~$t = \sqrt{0.16} = 0.4 \text{ s}$~~
 $w = f \cdot d = 50 \times 2 = 100$
the rate $\frac{w}{\Delta t} = \frac{100}{0.4} = 250 \text{ watt}$

(66) $F = ma$
 $a = \frac{F}{m} = \frac{50}{2} = 25 \text{ m/s}^2$
 $v^2 = v_0^2 + 2ax$
 $v^2 = 0 + 2(25)(2) = 100$
 $v = 10$
 $P = \frac{dw}{dt} = F \cdot v = (50)(10)(1) = 500 \text{ watt}$

(67) $\frac{w}{t} = ct$ $w = pt$
 $w = ct^2$ $w = \frac{1}{2} mv^2$
 $\frac{1}{2} mv^2 = ct^2$
 $v^2 = \frac{2c}{m} t^2$
 $v = \sqrt{\frac{2c}{m}} t$
 $v \propto t$

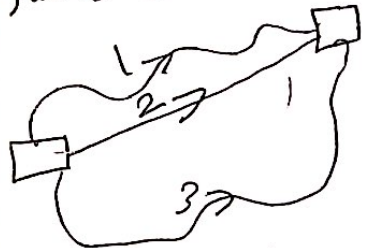
(67)

Chapter 8

إذا أثرت قوة محافظة على جسم فإن مجموع الشغل لمسار متعلق بسطح

إعداد: محمد الهدلج

إذا كانت القوة محافظة فإن شغلها يعتمد على المسافة بين نقطة البداية والنهاية ولا يعتمد على المسار



$W_1 = W_2 = W_3$

بما أن كلا الجسمين عادا إلى نفس النقطة انطلقا منها فإن طاقة الوضع تكون نفسها (لأنها عادا إلى نفس الارتفاع)

$W = -\Delta K.E = -f \cdot d$

التغير في طاقة الوضع يساوي شغل القوة المؤثرة على الجسم

$E_m = K + U$

ولها أن سرعة كل من الجسمين قلت بتالي الطاقة الحركية للجسم قلت وبما أن $\Delta E_m \neq 0$ يتالي وجود تحول لطاقة أي أثرت قوة غير محافظة

$E_m = K + U$

بما أن $E_m = K + U$ تقل لأن السرعة بتالي تقل E_m

السرعة كبيرة جداً وبما أن $K.E = \frac{1}{2} m v^2$ يتالي تكمن الطاقة الحركية كبيرة جداً

8

في حالة التمدد الساكن تكون $v = 0$ وبما أن

$K.E = \frac{1}{2} m v^2$

$K.E = 0$

لا يوجد طاقة حركية

9

النار في الملقوف في الساعة ليملك طاقة وضغ ولا يملك طاقة حركة

10

الجسم الساكن في نظام بإمكانه أن يبدل شغل إذا كان بإمكانه الحركة بحيث تقل طاقة الوضع الخاصة به أي تزداد الطاقة الحركية له صبي أن

$W = \Delta K.E$

11

$U = -W_f = F d \cos \theta$

$d = v t$

$U = F v t$

$U = F v t$

13

$U = -W_f = -\int F dx = -(\text{مسافة})$

مسافة 1 $= \frac{1}{2} x_1 f_1 \Rightarrow U_1 = -\frac{1}{2} x_1 f_1$

مسافة 2 $= x_1 f_1 \Rightarrow U_2 = -x_1 f_2$

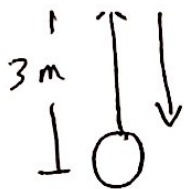
مسافة 3 $= \frac{1}{2} x_1 f_1 \Rightarrow U_3 = \frac{1}{2} x_1 f_1$

$U_3 > U_2$

الترتيب من الأكثر سالبية

$2 > 1 > 3$

(14)



اكثر طاقة وضع تكون عند اعلى ارتفاع حيث تكون الطاقة الحركية تساوي صفر ($v=0$) وذلك لأن

$$U = mgh$$

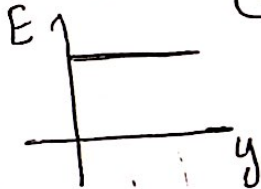
↑
الارتفاع ثابت

(15)

بما ان مقاومة الهواء يمكن تجاهلها يتالي

$$\Delta E_m = 0$$

اي ان الطاقة الميكانيكية محفوظة (تبقى ثابتة)



(16)

$$v_{60m}^2 = v_0^2 + 2gh$$

$$v^2 = 0 + (2)(10)(60) = 1200$$

$$v^2 = 1200$$

$$K.E = \frac{1}{2}mv^2 = \frac{1}{2}(6)(1200) = 3600$$

او بطريقة اخرى

at height 80 m

$$E_m = U + K = U + 0 = mgh = (6)(10)(80) = 4800$$

at height 60

$$\Delta E_m = 0$$

$$E_m = E_m$$

$$4800 = U + K = mgh + K = (6)(10)(60) + K$$

$$K = 4800 - 1200 = 3600$$

(17)

المطلوب! متى تكون $\Delta U = 500 J$

~~$$U = mgh = (2)(9.8)(20) = 392 J$$~~

$$\Delta U = U_f - U_i = 500$$

$$mg(h_f - h_0) = 500$$

$$h_f - h_0 = \frac{500}{mg} = \frac{500}{19.6} = 25.5$$

$$h_f = h_0 + 25.5$$

$$= 20 + 25.5 = 45.5$$

(18)

بما ان المصعد يرتفع بسرعة ثابتة فان تسارعه يساوي صفر

$$a = \frac{v}{t} = 0$$

الطاقة الحركية له ثابتة

$$\Delta K = mg(v_f - v_i) = mg(0) = 0$$

وبما ان المصعد يتحرك بسرعة ثابتة فان القوة المؤثرة عليه تكون ثابتة

(19)

$$K.E \text{ (vertical component)} =$$

$$= \frac{1}{2}m(v \sin 60) = \frac{1}{2}(\frac{1}{2})(8.6)$$

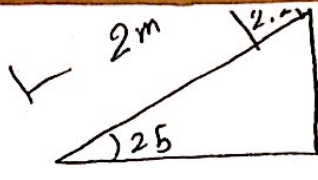
$$= \frac{75}{4} = 18.75$$

(20)

لكي يصل إلى ارتفاع h يجب ان يمتلك على الأقل طاقة حركية تساوي طاقة الوضع عند ارتفاع h

$$K = U = mgh$$

1) $\mu_k = .25$



$\Delta E_m + \Delta E_{bh} = 0$

$E_m = \Delta E_{bh} = W_{f_k} = (\mu_k N) d \cos 180$
 $= -\mu_k (mg \cos 25) (2)$
 $= -(0.25)(2.2)(9.8)(\cos 25)(2)$
 $= -9.8$

2) $U = K$
 $mgh = \frac{1}{2} m v^2$

$v^2 = 2gh$
 $v = \sqrt{2gh}$
 $= \sqrt{(2)(9.8)(1.85)}$
 $= 6.02 \text{ m/s}$

3) $\Delta E_m = 0$
 $E_{mf} = E_{mi}$

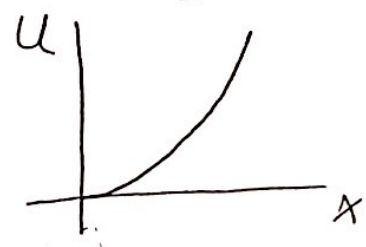
~~$E_f = K_f + U_f$~~
 $K_f + U_f = K_i + U_i$
 $\frac{1}{2} m v_f^2 + 0 = \frac{1}{2} m v_i^2 + mgh$
 $v_f^2 = (\frac{1}{2})(3)^2 + (9.8)(0.5)$
 $v_f^2 = 4.5 + 4.9 = 9.4$
 $v = \sqrt{(2)(9.4)} = 4.3 \text{ m/s}$

4) $f = -\frac{du}{dx} \Rightarrow du = -f dx$
 $\int du = \int f dx$
 $U - U_0 = -\int 8x^3 dx = -2x^4$
 $U - 0 = -2x^4$
 $U = -2x^4$

25) at $x=1 \Rightarrow U(1) = 80$
 $K(1) = \frac{1}{2} m v^2 = \frac{1}{2} (0.2)(5)^2 = 2.5$

at $x=1$ $E_m = U(1) + K(1) = 12.5$
 $\Delta E_m = 0$
 $E_{m0} = E_{m1}$
 $K_0 + U_0 = 12.5$
 $\frac{1}{2} m v^2 + 0 = 12.5$
 $v = \sqrt{125} = 11.1 \text{ m/s}$

26) $U = \frac{1}{2} k x^2$
 اقتران تربيعي



27) $U = \frac{1}{2} k x^2$
 $f = -\frac{du}{dx} = -kx$

$10 = -20x \Rightarrow x = -\frac{1}{2}$

$U = \frac{1}{2} (20) (\frac{1}{2})^2 = \frac{20}{8} = 2.5$

28) طاقة الوضع تتحول الى طاقة حركية

~~$U = K$~~
 $\frac{1}{2} k x^2 = \frac{1}{2} m v^2$

$(\frac{1}{2})(20)(0.07)^2 = \frac{1}{2} (0.015) v^2$

$v = \sqrt{6.533} = 2.556$

$K.E = \frac{1}{2} m v^2 = \frac{1}{2} (0.015) (2.556)^2$
 $= 0.049$

(29) $E_m = U + K = U + 0$
 $0.12 = \frac{1}{2} k x^2$
 $x = \sqrt{\frac{(2)(0.12)}{80}} = 0.054$

(30) $E_m = U + K = 0 + K$
 $0.12 = \frac{1}{2} m v^2$
 $v = \sqrt{\frac{(2)(0.12)}{0.5}} = 0.692 \text{ m/s}$

(31) when the spring is 4 cm
 $E_m = U + K = \frac{1}{2} k x^2 + \frac{1}{2} m v^2$
 $E_m = (\frac{1}{2})(80)(0.04)^2 + \frac{1}{2}(0.5)(0.5)^2$
 $E_m = 0.064 + 0.0625 = 0.1265 \text{ J}$
 $\Delta E_m = 0$
 $E_{m_0} = E_m$

$0.1265 = K + U = K + 0$

$0.1265 = \frac{1}{2} m v_{\text{max}}^2$

$v_{\text{max}} = \sqrt{\frac{(2)(0.1265)}{(0.5)}} = 0.71 \text{ m/s}$

(32) طاقة الحركة تتحول لاجل
 طاقة وضع

$\frac{1}{2} m v^2 = \frac{1}{2} k x^2$

$(\frac{1}{2})(\frac{1}{2})(2)^2 = \frac{1}{2}(800)^2 x^2$

$x = \sqrt{\frac{1}{400}} = 0.05 \text{ m} = 5 \text{ cm}$

(33) $K.E = U$
 $\frac{1}{2} m v^2 = \frac{1}{2} k x^2$

$x^2 = \frac{m v^2}{k} \Rightarrow x = v \sqrt{\frac{m}{k}}$

~~$\frac{1}{2} k x^2 = \frac{1}{2} m v^2$~~

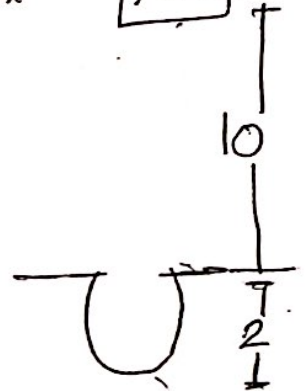
(34)

$mgh = \frac{1}{2} k x^2$

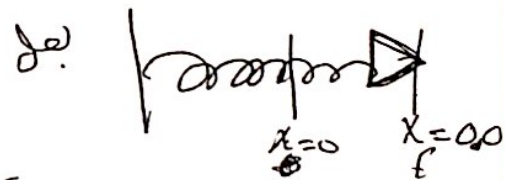
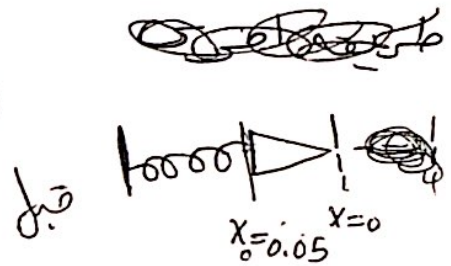
$(700)(12) = \frac{1}{2} k x^2$

$\frac{1}{2} k x^2 = 8400$

700 N



(35)



$\Delta E_m = 0$

$E_{m_0} = E_{m_f}$

$U_0 + K_0 = U + K$

$\frac{1}{2} k x_0^2 + 0 = \frac{1}{2} k x_f^2 + \frac{1}{2} m v^2$

$v^2 = \frac{k x_0^2 - k x_f^2}{m}$

$v^2 = \frac{(10)(0.05)^2 - (10)(0.01)^2}{(0.005)}$

$v^2 = 4$

$v = 2$

$$36) mgr = \frac{1}{2} mv^2$$

$$v^2 = 2gr$$

$$\Sigma F = ma = \frac{mv^2}{r} = \frac{m(2gr)}{r} = 2mg$$

$$\Sigma F = T - mg = 2mg$$

$$T = 3mg$$



$$37) mgh = \frac{1}{2} mv^2$$

$$h = r$$

$$v^2 = 2gr = 2(9.8)(0.5)$$

$$v = \sqrt{9.8} = 3.13 \text{ m/s}$$

$$38) \Delta E_m = 0 \quad E_{m1} = E_{m2}$$

$$mgh_1 = mgh_2 + \frac{1}{2} mv^2$$

$$= 2g(h_1 - h_2)$$

$$= \sqrt{2g(h_1 - h_2)}$$

~~$$1) mgh(2r+h) = mgr + \frac{1}{2} mv^2$$~~

لا نعلم الطاقة الميكانيكية محفوظة النسبة المتغيرة

~~$$mgh(2r+h) = mgr + \frac{1}{2} mv^2$$~~

$$gh = \frac{v^2}{2} \quad \text{--- (1)}$$

نعم

$$\Sigma F = ma$$

~~$$mg = \frac{mv^2}{r}$$~~

~~$$v^2 = gr$$~~

~~$$\text{--- (1)}$$~~

~~$$gh = \frac{gr}{2}$$~~

~~$$|g = \frac{r}{2}|$$~~

$$40) F = ma = \frac{mv^2}{r}$$

~~$$mg = \frac{mv^2}{r}$$~~

~~$$v = \sqrt{gr} = \sqrt{\left(\frac{3}{2}\right)(9.8)} = 3.8 \text{ m/s}$$~~

41) عند أعلى ارتفاع (Point 3) يكون
السرير يمتلك أقل طاقة حركية
وأكثر طاقة وضع وبما أن

$$\Delta E_m = 0$$

~~$$E_{m1} = E_{m2}$$~~

~~$$\Delta K_1 + \Delta U_1 = \Delta K_2 + \Delta U_2$$~~

~~$$K_1 + U_1 = K_2 + U_2 = E_m$$~~

~~$$E_{m1} = K_2 + U_2$$~~

$$E_{m1} = E_{m2} = U + K$$

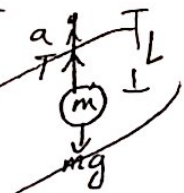
$$E_m = mgh + \frac{1}{2} mv^2$$

عند أعلى ارتفاع يكون هذا
السرير أكبر ما يمكن
وبما أن تكون الطاقة الحركية
أقل ما يمكن وبما أن
 $K.E = \frac{1}{2} mv^2$
تكون السرعة أقل ما يمكن

42) at the bottom of circle

~~$$\Sigma F = ma = \frac{mv^2}{L}$$~~

~~$$T - mg =$$~~



(42)

$$\Delta E_m = 0$$

$$E_{m_{top}} = E_{m_{bottom}}$$



$$K + U = K + U$$

$$\frac{1}{2} m v_{top}^2 + m g (2L) = \frac{1}{2} m v_{bottom}^2 + 0$$

$$\frac{v_{top}^2}{2} + 2gL = \frac{v_{bottom}^2}{2} \rightarrow (1)$$

at the top

$$\Sigma F = ma = \frac{m v^2}{r}$$

$$\Rightarrow m g = \frac{m v^2}{L}$$

$$v^2 = gL$$

من المعادلة 1

$$\frac{gL}{2} + 2gL = \frac{v^2}{2}$$

$$v^2 = 5gL$$

$$v = \sqrt{5gL}$$

ملاحظة:
عند أقصى ارتفاع السلسلة يساوي صفر

(44)

the limits of motion are when $U = E_m$
when K.E = zero

$$8x^2 + 2x^4 = 9$$

بالجريب

$$8(0.96)^2 + 2(0.96)^4 \stackrel{?}{=} 9$$

$$a = 9$$

بإلى الجواب

$$(-0.96 \text{ m}, 0, 0.96 \text{ m})$$

$$-0.96 \quad 0 \quad 0.96$$

أيضا يمكن أن يكون x أو $-x$

(45)

$$K(1) = \frac{1}{2} m v^2 = \frac{1}{2} (0.2) (20)^2 = 20$$

$$U(1) = 8 + 2 = 10$$

$$E_{m1} = 10 + 20 = 30$$

~~when it stop~~

$$\Delta E_m = 0$$

$$E_m = E_m$$

$$K(1) + U(1) = K + U$$

when it stop

$$K(1) + U(1) = 0 + U$$

$$E_{m1} = U$$

$$8x^2 + 2x^4 = 30$$

بالجريب

$$8(1.1)^2 + 2(1.1)^4 \stackrel{?}{=} 30$$

$$30 = 30$$

وبما انه كان يتحرك على محور السينات الكوسايد (صهبات) بإلى قارة يسكن عسلا

$$x = +1.1$$

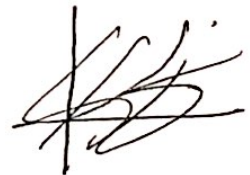
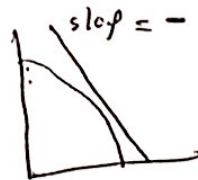
(46)

$$F = -\frac{du}{dt}$$

(F) is positive when

$\frac{du}{dt}$ is ~~positive~~ negative $F = (-)(-) =$

that when U is decreasing function



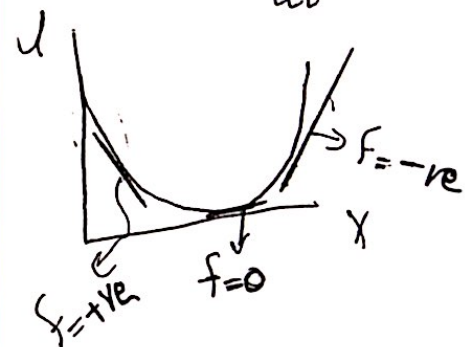
$$F = -\frac{du}{dx}$$

$$|F| = \left| \frac{du}{dx} \right|$$

AB < CD
 (أقل انحدار)
 منحنى: $F = -\frac{du}{dx}$

CD > AB > BC
 منحنى: $F = -\frac{du}{dx}$

48) $F = -\frac{du}{dx}$

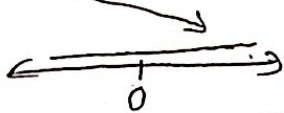


بما ان اقتران (U-x) يشبه اقتران الترسيع

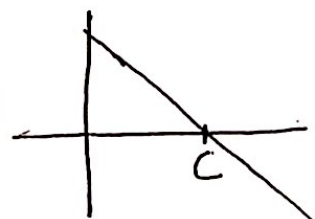
$$U = (x-c)^2$$

$$F = -\frac{dU}{dx} = -2(x-c) \Rightarrow x=c$$

$$\frac{dF}{dx} = -2$$

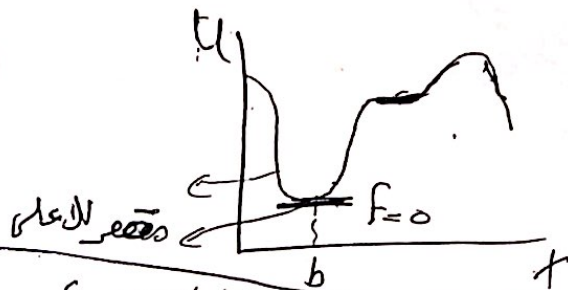


F decreasing (منهجه)



49) The point of stable equilibrium
 نقطة تكون عندها $F=0$ والاقتزان
 مع تغير (U-x)

only b



50) The point of ~~stable~~ unstable equilibrium

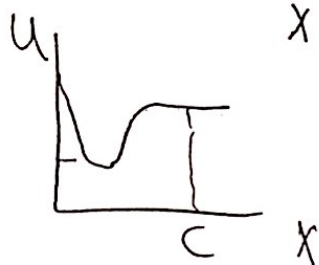
نقطة تكون عندها $F=0$ والاقتزان
 مع تغير (U-x)

only d



51) The point of neutral equilibrium

نقطة تكون عندها مقدار U ثابت
 مع تغير x



only c

52) $U = -mgx + \frac{1}{2}kx^2$

$$F = -\frac{dU}{dx} = -(mg + kx)$$

$$F = mg - kx$$

(53) $f = ma_1 = -\frac{du}{dx}$
 $\left. \frac{du}{dx} \right|_{x=1} = 16x + 8x^3 = 16 + 8 = 25$
 $F = -25 = m \cdot a$
 $a = \frac{-25}{m} = \frac{-25}{0.2} = -125$

(53) لوجد خطأ مني السؤال التصحيح:

$$U(x) = 8x^2 - 2x^4$$

$$F = -\frac{du}{dx} = ma$$

$$\left. \frac{du}{dx} \right|_{x=1} = 16x - 8x^3 = 16 - 8 = 8$$

$$F = -8 = ma$$

$$a = \frac{-8}{m} = \frac{-8}{0.2} = -40 \text{ m/s}^2$$

(54) $U = Ax^{-12} - Bx^{-6}$

$$F = -\frac{dU}{dx} = -\left(\frac{-12A}{x^{13}} + \frac{6B}{x^7} \right)$$

$$= 12A/x^{13} - 6B/x^7$$

(56)

(57)

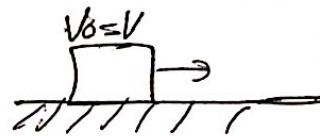
(58)

$$\Delta E_m + \Delta E_{int} = 0$$

$$\Delta K + \Delta u + \Delta E_{th} = 0$$

$$\Delta K + 0 + \Delta E_{th} = 0$$

$$\Delta K + \Delta E_{th} = 0$$



السائل الذي يبذل الاحتكاك يغير الطاقة الحركية والطاقة الداخلية فقط

(59)

$$\Delta E_m + \Delta E_{int} = 0$$

$$\Delta K + \Delta u + 15 = 0$$

$$K_f - 0 + 0 - U_i + 15 = 0$$

$$\frac{1}{2}mv^2 - mgh + 15 = 0$$

$$\frac{1}{2}mv^2 = mgh - 15 = 19.6 - 15 = 4.6$$

$$v^2 = \frac{(2)(4.6)}{0.025} = 368 \Rightarrow v = 19.1 \text{ m/s}$$

$$v_0 = 0.025$$

(60)

$$\Delta E_m + \Delta E_{th} = 0 \Rightarrow \Delta E_{th} = -\Delta E_m$$

$$\Delta E_{th} = \Delta E_m = -\Delta K + \Delta U = -\Delta K + \Delta U$$

$$\Delta E_{th} = -\Delta K = \frac{1}{2}m(v_i^2 - v_f^2) = \frac{1}{2}(5)(200^2 - 15^2)$$

$$\Delta E_{th} = 44000 \text{ J}$$

(61)

$$\Delta E_m + \Delta E_{int} = 0 \Rightarrow \Delta E_{int} = -\Delta K + \Delta U$$

$$\Delta E_{int} = K_i - K_f + U_f - U_i = \left(\frac{1}{2}mv^2 = 0 + 0 - \frac{1}{2}Kx^2 \right)$$

$$\Delta E_{int} = -\left(\frac{1}{2}(0.75)(3.5)^2 - \frac{1}{2}(1200)(0.057)^2 \right) = 2.6$$

CHAPTER 9

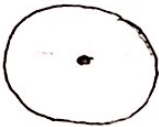
1) **Ans: E** "None of these"

2) **Ans: C** $6\text{ kg}(1,3)\text{m} / 4\text{ kg}(0,0)\text{m} / 5\text{ kg}(3,2)\text{m}$

$$X_{\text{com}} = \frac{m_1 x_1 + m_2 x_2 + m_3 x_3}{\Sigma M}$$

$$= \frac{4(0) + 6(1) + 5(3)}{15} = 1.4$$

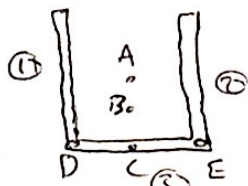
Y_{com} the same 1.9
 $Y_{\text{com}} = 1.9\text{ m}$
 Com (1.4, 1.9)

3) **Ans: E** the center of the circle 

4) **Ans: B** Closer to the sun than the Earth or Mars because the mass of the sun is very large $M_{\text{sun}} \gg (M_{\text{Earth}} + M_{\text{Mars}})$

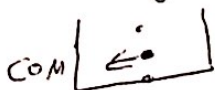
5) **Ans: D** "near the center of Earth"

6) **Ans: B**
 The center of 1, 2, 3 is in the midway between the ends across the thickness

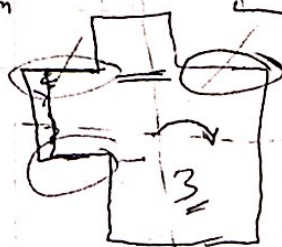
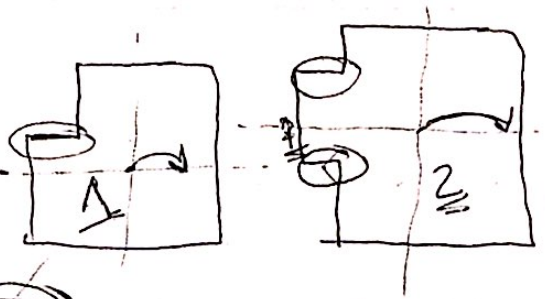


the center between 1, 2 in the mid way between

the center "1, 2" and "3" them is in the midway between them



7) **Ans: E**



the loss in X in 1 is the same as 3 because in 3 there is a cut from both right and left sides. But in 2 the loss is greater because there is a cut from the left side only.

8) **Ans: B**
 $V_{\text{com}} = \frac{V_1 m_1 + V_2 m_2}{M}$

$$= \frac{(4)(2) + (8)(3)}{12} = 7.3\text{ m/s}$$

9) **Ans: D** we find the height of the two balls after 2 s by $y = v_0 t + \frac{1}{2} a t^2$

$$H_1 = 25 - y_1 \Rightarrow H_1 = 25 - 19.6 = 5.4\text{ m}$$

$$+ H_2 = y_2 = 10.4\text{ m}$$

$$H_{\text{com}} = \frac{m_1 h_1 + m_2 h_2}{M} = \frac{(5.4)(0.5) + (10.4)(0.25)}{0.75}$$

$$\approx 7.1\text{ m}$$

10) **Ans: C** we first find V after 2 sec.

$$\text{by } V_2 = v_0 + at \Rightarrow V_1 = 19.6 / V_2 = 4.6$$

$$V_{\text{com}} = \frac{V_1 m_1 + V_2 m_2}{M} = \frac{(19.6)(0.5) + (4.6)(0.25)}{0.75}$$

$$= 15.026 \approx 15\text{ m/s}$$

11) **Ans: D** $a = g$ the acceleration never changes when the particles moves within the range of the Earth

12) **Ans: E** None of these

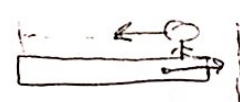
13) **Ans: B** since the two objects are the same with the same initial conditions the center of mass displacement is the displacement of one of them.

In this question we are considered in vertical D, as the v_y at "L" is zero, the question is free fall: $y = v_0 t + \frac{1}{2} a t^2 \Rightarrow = 0 + \frac{1}{2} (10)(4) = 20$

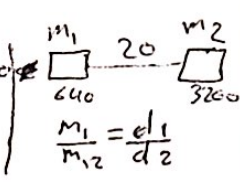
14) **Ans: B** $\Sigma F_{ext} = 0$

15) **Ans: A** $v = 0$ & $\Sigma F_{ext} = 0$

16) **Ans: E** is rearward of its original place of not moving.



17) **Ans: B** since the bear will move $\frac{1}{5} * 20 = 3.3 m$



18) **Ans: A** the same as 17 the 60 kg boy will move $\frac{10}{2.5} = 4 m$

19) **Ans: C** $\vec{F} = \Sigma F_{ext}$ / $m = m_{system}$

20) **Ans: B** the same as 17 & 18 so $v_1 = 2v_2$ for the Hz comp. $v_2 = \frac{6}{2} = 3 m/s$

21) **Ans: D** the motion was started with at least one of masses moving

22) **Ans: B** $E = \Sigma E_k = \frac{1}{2} k x^2 = (\frac{1}{2})(100)(0.1)^2 = 0.5$
 $\Sigma E_k = \frac{1}{2} m v^2 = (\frac{1}{2})(2)(0.3)^2 = 0.18$
 $\Delta E_k = 0.18 - 0.5 = -0.32$

23) **Ans: C** $dp = j \Rightarrow j = \Delta p = F \cdot t$

24) **Ans: E** acceleration

25) **Ans: D** $p = \sqrt{2 km}$ $m_A = 9 mb$

$$\frac{p_A}{p_B} = \frac{\sqrt{2 k m_A}}{\sqrt{2 k m_B}} \Rightarrow \frac{p_A}{p_B} = \sqrt{\frac{m_A}{m_B}} = \sqrt{\frac{9 mb}{1 mb}} = 3$$

$$\frac{p_A}{p_B} = \frac{3}{1}$$

26) **Ans: B** "is moving faster"

27) **Ans: B** F is the slope in P_V vs t graph

28) **Ans: D** $dp = m \Delta v = 1(1.5 - -2) = 3.5$ away

29) **Ans: D** $\Sigma F_{ext} \neq zero$

30) **Ans: B** "the force of friction of the vertical"

31) **Ans: A** $v = v_0 + at \Rightarrow v = 39.2$
 $P = mv = (39.2)(2.5) = 98$

41) **Ans: D** $P_b = P_a \Rightarrow m_1 v_1 = (m_1 + m_2) v$
 $2000 \times 3 = (2000 + 500) v \Rightarrow v = 2.4 \text{ m/s}$

32) **Ans: B** $m_1 v_{1b} + m_2 v_{2b} = m_1 v_{1a} + m_2 v_{2a}$
 $0 = (24)(0.0017) + 0.1 v_{2a}$
 $v_{2a} = -1.1$

42) **Ans: E** "Zero"

43) **Ans: B** "the force of the existing fuel gases"

33) **Ans: C** the same as 32 $v = 8.3 \times 10^{-2}$ 44) **Ans: C** Thrust = $v_{rel} \frac{dM}{dt} = (1500)(100) = 1.5 \times 10^5$

34) **Ans: B** the same as 32, 33 $v = 0.38 \text{ m/s}$ 45) **Ans: B** $v_f - v_i = v_{rel} \ln \left(\frac{M_i}{M_f} \right)$
 $\Rightarrow v_f = 1500 \ln \left(\frac{1}{0.2} \right) = 2414 \approx 2400 \text{ m/s}$

35) **Ans: A** P is conserved in explosion

36) **Ans: C** $\frac{P_b^0}{P_a} = P_a \Rightarrow 0 = M v_1 + m_2 v_2$
 $v = \frac{-m_2 v_2}{M}$

46) **Ans: B** $v_f - v_i = v_{rel} \ln \left(\frac{M_i}{M_f} \right)$
 $\frac{70}{1500} = \ln \left(\frac{M_i}{M_f} \right) \Rightarrow 1.004 = \ln \left(\frac{M_i}{M_f} \right)$

$M_f = \frac{1000}{1.004} = 996 \Rightarrow 1000 - 996 = 4 \text{ kg}$

37) **Ans: C** $\frac{P_b^0}{P_a} = P_a \Rightarrow 0 = M v + m_b v$
 $\frac{P_{G1}}{P_{G2}} = \frac{m_{bullet 1} v}{m_{bullet 2} v} = \frac{2m_1}{m_2} = \frac{2}{1} (2 \times 1)$

47) **Ans: D** $J = \Delta p$

48) **Ans: D** $J_{ext} = 0 \Rightarrow F_{ext} = 0$

38) **Ans: A** Area under $(F vs t)$ graph = J
 $\Rightarrow J = \Delta p \Rightarrow \left(\frac{1}{2} \right) (4) (2) = m \Delta v$
 $\frac{4}{5} = v = 0.8$

49) **Ans: E** $J_{xy} = -J_{yx}$

50) **Ans: E** the same momentum for the other

39) **Ans: D** $F = \frac{\Delta p}{\Delta t}$

40) **Ans: B** $v_{comb} = v_{com after}$
 $v_{com} = \frac{m_1 v_1 + m_2 v_2}{M} = \frac{0.2 \times 3 + 0.4 \times 2}{0.6}$

51) **Ans: A** $J = \Delta p = m \Delta v$
 $= 0.2(20 - -30) = 10 \text{ upward}$

52) **Ans: C** $F_{ext} = \Delta p \Rightarrow 1 \times 1 = P_f \frac{t}{m}$
 $P_f = 1 \text{ kg} \cdot \text{m/s}$

≈ 0.33
Ans: C

53) (Ans: C) ~ max in straight line

54) (Ans: C) $J = \rho p = +50$

55) (Ans: D) the airbags make it larger ~~and~~
so ~~J will be smaller~~ will be smaller
"exerts a much smaller force"

56) (Ans: C) $\vec{O}P_x = P_x - P_{y2} \Rightarrow \vec{0}$ same direction
 $\vec{O}P_y = P_y - P_{y2} = 2P_y \neq 0$

57) (Ans: B) $J = F \cdot t \Rightarrow F = \frac{J}{t}$
 $F = \frac{mV}{t}$

58) (Ans: E) "Impossible to determine for given data"

59) (Ans: E) "None of the choices"

60) (Ans: D) "a frame for which the total momentum of the two objects is zero"

61) (Ans: D) P is conserved if K is Not

62) (Ans: A) $P_{before} = P_{after}$
 $m_1 v_1 = (m_1 + m_2) V$
 $V = \frac{1 \cdot 2}{1 + 2} = 1 \text{ m/s}$

63) (Ans: B) the same as 62
 $V = \frac{m_1 v_1}{(m_1 + m_2)} = \frac{0.399}{1.4} = 0.285$

64) (Ans: B) $P_b = P_{after} \Rightarrow m_1 v_1 = (m_1 + m_2) V$
 $V = 1.8$ $J = 0 P$
 $OP_2 = (1)(4) = 4 \text{ N.s}$

65) (Ans: B) $m_1 v_1 = (m_1 + m_2) V \rightarrow \sqrt{2gh}$
 $V = 0.245$ $V_1 = \frac{2.450}{0.003} = 816 \approx 8 \times 10^2$

66) (Ans: C) ~~$\frac{1}{2} m v^2$~~ $K = \frac{1}{2} m v^2$
 $40 = \frac{1}{2} (5) v^2$
 $V = 4 \text{ m/s}$

67) (Ans: C) $m_1 v_1 + m_2 v_2 = (m_1 + m_2) V_f$
 $V_f = 0 \Rightarrow 0K = K_f - K_i$
 $0K = \frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2 = 3750 \text{ J}$

68) (Ans: C) $\frac{1}{2} M_{total} V_{com}$

69) (Ans: D) $(m_1 + m_2) V_f = m_2 v_2$
 $V_f = \frac{(105)(2)}{30} = 7$ $0V = 7 - 2 = 5 \text{ m/s}$

70) (Ans: C) P & K are conserved

71) (Ans: E) Before: A (m) moving right with velocity v, B (m) at rest. After: A (m) moving right with velocity v, B (m) moving right with velocity v. The whole speed of elastic A goes to B for elastic \Rightarrow proved by $(P_b = P_a) \& \left(\frac{v_2 - v_1}{v_1 - v_2} = 1 \right) \Rightarrow$ for B to have the greatest K $m_B v_B^2 = m_A v_A^2$

72) (Ans: C) " " it likes when a ball strikes a wall in an elastic collision so the ball will rebound with same speed & the opposite direction $V_{after} = -5 \text{ m/s}$

$$V_{1a} = \frac{m_1 - m_2}{m_1 + m_2} (V_{1b}) + \frac{2m_2}{m_1 + m_2} (V_{2b})$$

$$\text{SS} = 0 + \frac{2m_2}{m_2} 10 = 20 \text{ m/s}$$



$$P_{\text{before}} = P_{\text{after}}$$

$$m_A V = m_A V_A + m_B V_B \Rightarrow mV = mV_A + 2mV_B$$

$$V = V_A + 2V_B \quad (1)$$

$$\Rightarrow \frac{V - 0}{V_B - V_A} = 1 \Rightarrow V = V_B - V_A \quad (2)$$

$$V_B - V_A = V_A + 2V_B \Rightarrow -V_B = 2V_A \quad \text{so } V_A = -\frac{1}{2}V_B$$

$$\Rightarrow V_A = -\frac{V}{3} \quad | \quad V_B = \frac{2V}{3}$$

75) (Ans: A) By using $\Delta P = 0$ $\cancel{V_{2a} - V_{1a} = V_{1b} - V_{2b}}$

26

76) (Ans: E) "the incident and target particle have the same mass" the same as 71

77) (Ans: D) $x = \frac{2}{5}y \Rightarrow K = \frac{1}{2}mv^2 \Rightarrow K(x) = 50$ so $K(y) = 50 \times \frac{5}{2} = 125 \text{ J}$

78) (Ans: E) "the kinetic energy of the system is at a minimum"

79) (Ans: B) "if some other form of energy were changed to kinetic during the collision the report could be true" Because the K_{after} is larger than K_{before} and that impossible is if there is no other source of energy.

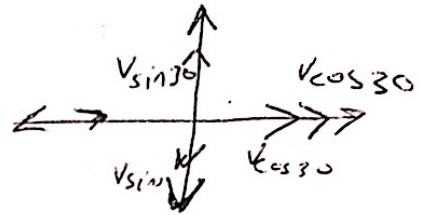
80) (Ans: A) $p_b = p_a \Rightarrow mV_0 = mV_1 + mV_2 \Rightarrow V_0 = V_1 + V_2$

$2K_b = K_a \Rightarrow 2\left(\frac{1}{2}mV_0^2\right) = \frac{1}{2}mV_1^2 + \frac{1}{2}mV_2^2 \Rightarrow 2V_0^2 = V_1^2 + V_2^2$

$\Rightarrow (5 = V_1 + V_2) \quad (50 = V_1^2 + V_2^2)$ By solving these simultaneously

$\Rightarrow V_1 = 1.83 \text{ m/s}$

81) (Ans: B)



like same as [56] $\Rightarrow \Delta p_x = 0 \quad \Delta p_y = 2py$

$= 2mV \sin 30$

اعداد: 10 اسباق سے زائد

Chapter 10: Rotation

Test bank Answers

1 $\pi \rightarrow 180^\circ$
 $1 \rightarrow ??X$

$$X = \frac{180^\circ}{3.14} = 57.3^\circ \quad \text{ans: D}$$

2 ans: E } 3 $\frac{1 \text{ rev}}{\text{min}} = \frac{2\pi \text{ rad}}{1 \times 60 \text{ s}} = 0.105 \text{ rad/s} \quad \text{ans: B}$

4 ans: C } 5 $T = \frac{2\pi}{\omega} = \frac{2\pi}{3} \approx 2.09 \approx 2.1 \text{ s} \quad \text{ans: E}$

6 $\omega = \frac{100 \times 2\pi}{10} \approx 63 \text{ rad/s} \quad \text{ans: E}$ } 7 The second hand complete 1 rev/min
so $\omega = \frac{2\pi}{60} \text{ rad/s} = \frac{\pi}{30} \text{ rad/s}$
ans: C

8 $\Delta\theta = \omega t + \frac{1}{2} \alpha t^2 \Rightarrow \alpha = \frac{2(\Delta\theta - \omega t)}{t^2} = \frac{2(450 - 20 \times 9)}{81} \approx 6.7 \text{ rad/s}^2$
ans: D

9 The min hand complete one rev/hour so $\omega = \frac{2\pi}{60 \times 60} = \left(\frac{\pi}{1800}\right) \text{ rad/s}$
ans: D

10 $\alpha_{\text{Avg}} = \frac{\Delta\omega}{\Delta t} = \frac{300(2\pi)}{60 \times 10} = 3.14 \text{ rad/s}^2 \quad \text{ans: A}$

11 $\omega_f^2 = \omega_i^2 + 2\alpha \Delta\theta \Rightarrow \omega_i = \sqrt{4\pi^2 - 2\pi^2} = \sqrt{2} \pi \text{ rad/s}$
ans: D

12 $\alpha_{\text{Avg}} = \frac{\Delta\omega}{\Delta t} = \frac{0 - 24\pi}{6} = -4\pi \text{ rad/s}^2 \quad \text{ans: D}$

13 $\alpha_{avg} = \frac{\Delta\omega}{\Delta t} = \frac{0 - 0.75 \times 2\pi}{30} = \frac{-1.5\pi}{30} = \frac{-\pi}{20}$ ans: D

14 Given that the time taken is $t = 1 \text{ min} = 60 \text{ s}$ $\omega_i = 0$ $\omega_f = 4\pi \text{ rad/s}$
 $\alpha_{avg} = \frac{\Delta\omega}{\Delta t} = \frac{4\pi}{60} = \frac{\pi}{15} \text{ rad/s}^2$ ans: D

15 The time taken for angular velocity 18 rad/s to zero is $\omega_f = \omega_i + \alpha t$
 $0 = 18 - 2t = 9 \text{ s}$ and The time for angular velocity zero to 18 is also 9s
 Total time is $t = 9 + 9 = 18 \text{ s}$ Hence we get by it ans: D

16 $\alpha = \frac{\omega_f - \omega_i}{t} = \frac{+24 - 36}{6} = -2 \text{ rad/s}^2$ Ans: B

17 $\alpha = \frac{\omega_f - \omega_i}{t} = \frac{-24 + 36}{6} = 2 \text{ rad/s}^2$ Ans: A

18 $\omega_f^2 = \omega_i^2 + 2\alpha\Delta\theta \Rightarrow 0 = (18)^2 + 2(-2)\Delta\theta \Rightarrow \Delta\theta = 81$ Ans = A

19 $\omega_f^2 = 0 + 2(4)(20\pi) \Rightarrow \omega_f = 22 \text{ rad/s}$ ans: B

20 $\Delta\theta = \omega t + \frac{1}{2}\alpha t^2 \Rightarrow t^2 = \frac{2(20\pi - 0)}{4} = 10\pi$ $t = \sqrt{10\pi} = 5.6 \text{ s}$ Ans: E

21 $\alpha(t) = (6t^2)$ $\frac{d\omega}{dt} = 6t^2 \Rightarrow \omega = \int 6t^2 dt = \frac{6t^3}{3} = 2t^3 + C$ (zero)
 $\Rightarrow \frac{d\theta}{dt} = 2t^3 \Rightarrow \theta = \int 2t^3 dt = \frac{1}{2}t^4 = ((1/2)t^4) \text{ rad}$ ans: C

22 from ~~the~~ Q 21 we found that $\theta = \frac{1}{2}t^4 \Rightarrow 10 \times 2\pi = \frac{1}{2}t^4$

$t = \sqrt[4]{125.6} = 3.3$

ملاحظة استخدمنا العلاقة من الدائرة السابقة فقط لأنه الساري البعدي هو نفسه أي ان هذه العلاقة ليست هي المطلوبة للإيجاد الزمن.

ans: B

23 Using Q 21 and Q 22 $\omega = 2t^3 \Rightarrow$ when $\theta = 10 \text{ rev}$ $t = 3.3$
 So $\omega = 2(3.3)^3 \approx 75 \text{ rad/s}$ ans: B

24 $\int d\omega = \int -3t^2 \Rightarrow \omega = -t^3 + C$ but $\omega(0) = 27 \Rightarrow 27 = 0 + C \Rightarrow C = 27$
 $\omega = -t^3 + 27$ when $\omega = 0$ $t = 3 \text{ second}$ Ans: C

العلاقة فونج تقصر على نصفها البعض

25 ans: B



26 Ans A (دائرة جيدة)

27 $\theta = \frac{s}{r} = \frac{3000}{20} = 150 \text{ rad}$ ans: C

28 $v = \omega r = 0.7(10) = 7$ Ans A 29 Ans: D

20 $\Delta\theta = \omega t + \frac{1}{2} \alpha t^2$ But $\Delta\theta = \frac{s}{r} = \frac{4}{0.015} = 266$
 $266 = 0 + \frac{1}{2} (2) t^2$ ~~$t = \sqrt{266}$~~ $t = \sqrt{266} \approx 16 \text{ s}$ ans: D
 $r = \frac{0.03}{2} = 0.015$

31 Because ω is constant the particle has a_r and doesn't have a_t so $a = a_r = \omega^2 r = (5(2\pi))^2 (0.1) = 10\pi^2 \text{ m/s}^2$ ans: E

32 ans: A دائرة متساوية

33 to find how many revolutions the tube made $r = 0.05 \text{ m}$

~~so the tube complete one revolution~~ so the tube complete one revolution when and the tube circumference $= 2\pi r = 2\pi(0.05) = 0.1\pi$

الأنبوب يقطع 10 سم كل ثانية ولذا في 10 سم 10 ثواني
 ويكون ذلك عدد الدورات في الثانية
~~to make one revolution~~
 $\frac{10 \times 10^{-2}}{0.1\pi} = 0.31847$ revolution the tube made every second

so $\omega = 0.318 \text{ rev/s} = 0.318(2\pi) \text{ rad/s} = 2 \text{ rad/s}$ Ans: A

34 from Question 33 we notice that $\omega = 2 \text{ rad/s}$
 here $a = a_r = \omega^2 r = (2)^2 (0.05) = 0.2 \text{ m/s}^2$

35 $a_t = \alpha r = 5 \times 0.6 = 3$ ans B

36 $v_1 = \omega r_1 = \omega r$ $v_2 = \omega \frac{r}{2} \Rightarrow \frac{v_1}{v_2} = \frac{\omega r}{\omega \frac{r}{2}} = 2$ (point 1) $\left(\frac{r}{2}\right)$ (point 2) ans: B

37) $360^\circ \text{ to } 2 \text{ wais} \Rightarrow a_{t1} = \alpha r \quad a_{t2} = \alpha \frac{r}{2} \quad \frac{a_{t1}}{a_{t2}} = 2$
ans: B

38) $37, 36^\circ \text{ to } 2 \text{ wais} \Rightarrow a_{t1} = \omega^2 r \quad a_{t2} = \omega^2 \frac{r}{2} \quad \frac{a_{t1}}{a_{t2}} = 2$
Ans B

39) $\omega_B = 2\omega_A \Rightarrow a_{tA} = \omega_A^2 r \quad a_{tB} = 4\omega_A^2 r \quad \frac{a_{tB}}{a_{tA}} = 4$
Ans D

40) Ans: D $\omega_f = \omega_i + \alpha t \Rightarrow \omega_f = \alpha t$ (constant) $\Rightarrow \omega_f$ increases $\Rightarrow \omega_f$ increase
 $a_t = \alpha r$ (constant) $a_r = \omega^2 r$ (constant) increases
 Vector $|a| = \sqrt{(a_r)^2 + (a_t)^2}$ (increasing constant)
 So \vec{a} increases in magnitude and becomes more radial

41) $|\vec{a}| = \sqrt{(a_t)^2 + (a_r)^2} \quad |\vec{a}_f| = \sqrt{(a_t)^2 + (a_r)^2}$

$a_{t \text{ final}} = 4 a_{t i}$
 $\alpha_{t \text{ final}} = 4 \alpha_{t i}$
 $\alpha_f = 4 \alpha_i$

$|\vec{a}_f| = 4 \sqrt{(a_t)^2 + (a_r)^2}$
 $= \sqrt{16(a_t)^2 + 16(a_r)^2}$
 $= \sqrt{(4a_t)^2 + (4a_r)^2}$
 $= \sqrt{(4\alpha_i t)^2 + (4\omega^2 r)^2}$

$a_{r \text{ final}} = 4 a_{r i}$
 $\omega_f^2 r = 4 \omega_i^2 r$
 $\omega_f = 2 \omega_i$

answer is E

42) $I_1 = m(1)^2 = m$
 $I_2 = m(2)^2 = 4m$
 $I_3 = m(3)^2 = 9m$
 $I_1 < I_2 < I_3$
Ans: A

$$43 \quad I = 2(0)^2 + 2(0)^2 + 2(1)^2 + 2(1)^2 = 4 \quad 12 \text{ kg} \cdot \text{m}^2$$

المسافة r في الاتجاه
السويحي

$$44 \quad I = 3(0)^2 + 2\left(\frac{L}{2}\right)^2 + M(L)^2$$

$$= \frac{1^M}{2} L^2 + \frac{2ML^2}{2} = \frac{3ML^2}{2}$$

Answer is C

منه عارفة ليس بال Test Bank معلومة E لـ L متاخرة من الجواب

45 Ans: D thin \rightarrow استاذك اذ لك
Hoop نصف \rightarrow نصف \rightarrow نصف \rightarrow نصف

46 Ans: D

$$47 \quad I_1 = \frac{2}{5} MR^2 \quad I_2 = \frac{2}{3} MR^2 \quad I_3 = \frac{MR^2}{2} \quad I_4 = MR^2$$

suppose that $X = MR^2$

the $I_4 > I_2 > I_3 > I_1$

\Rightarrow

1, 3, 2, 4

Ans: C



بصراحة سؤاله مستفز! لازم نحفظ القوانين

$$48 \quad I = \frac{1}{2} MR^2$$

~~Mass = pV~~

$$\text{Mass} = pV$$

$$V_A = \pi r^2 h$$

$$V_B = \pi (2r)^2 2L = 8V_A$$

$$I_A = \frac{1}{2} p \pi r^2 L R^2 \quad \text{--- } \textcircled{D}$$

$$I_B = \left(\frac{1}{2} p \pi (2r)^2 L (4r^2) \right) = 32 I_A$$

$$\frac{I_B}{I_A} = \boxed{32}$$

Answer: E

49 ans A

سؤال بسيط

50

$$V = \frac{m}{\rho} \leftarrow \text{constant}$$

Lava



الحجم يزداد عندما تقل الكثافة ويقل عندما تزداد

I (بتقليل الكثافة) عندما يزداد الحجم تزداد أبعاد الشكل بالتالي تزداد I

(بزيادة الكثافة) عندما يقل الحجم تقل أبعاد الشكل بالتالي تقل I

50

في نفسه صواب سؤال 49

لما كانت كثافة الـ lead < من كثافة الـ Wood

$$I_{\text{wood}} > I_{\text{lead}}$$

لذا "يخبو" تحت الماء

51

ans B



عند رجاء "ترى عجباً"

52

$$I_{\text{new}} = I_{\text{disk}} + Mr^2$$

$$= 0.7 + 0.32 = 1.02 \quad \text{ans: E}$$

53

$$I = I_{\text{cm}} + Mh^2 = \frac{1}{12} ML^2 + M\left(\frac{1}{2}L\right)^2 = \frac{1}{3} ML^2 \quad \text{ans: C}$$

54

$$I = \frac{2}{5} MR^2 + MR^2 = \frac{7}{5} MR^2$$

answer: E

55

$$I = I_{\text{cm}} + Mh^2 = \frac{2}{5} MR^2 + M(4R)^2$$

$$= \frac{2}{5} MR^2 + 16MR^2 = \frac{2}{5} MR^2 + \frac{16 \times 5}{5} MR^2$$

$$= \frac{82}{5} MR^2$$

where $h = 4R$

is the distance between the center of the sphere and the point of suspension

56

ans: D

57

Ans: E

$$\text{Torque} = FR \sin \theta$$

$$\sum \vec{F}_2 = \sum \vec{F}_3 = 0$$

$$r=0 \quad \theta=180$$

$$F_4 \sin \theta$$

$$\sin 90$$

$$\sum \vec{F}_1 = \sum \vec{F}_3$$

$$58: \tau_1 = F_1 \times r_1 = F_1 r_1 \sin \theta_1 = 5(4)(\sin 150) = 10 \text{ N.m}$$

$$\tau_2 = F_2 \times r_2 = F_2 r_2 \sin \theta_2 = 5(2)(\sin 150) = 5 \text{ N.m}$$

$$\tau_{\text{total}} = \tau_1 + \tau_2 = 10 + 5 = 15$$

Ans: D

59 ans: D 60 ans: A

61 $\tau = r \times F = I \alpha$ $\alpha = \frac{r F \sin \theta}{I}$

$$I_{\text{Disk}} = \frac{1}{2} M r^2, \quad I_{\text{Hoop}} = M r^2, \quad I_{\text{sphere}} = \frac{2}{5} M r^2$$

$$\alpha_{\text{Hoop}} < \alpha_{\text{Disk}} < \alpha_{\frac{2}{5} M r^2} \quad \text{Ans: D}$$

62 Ans: B 63 $\alpha = \frac{(0.1)(1)}{0.020} = 5 \quad \text{Ans: B}$

64 $\alpha = \frac{(5)(0.4)}{2} = 1 \quad \text{Ans: C}$

65 ans: A Because the force is applied along the rotation axis
 $\tau = 0$ so $\alpha = 0$

66 $\tau = F \times r = I \alpha$
 $F r \sin \theta = I \alpha$
 $\frac{(8)(0.25)(1)}{5} = \alpha$
 $\Rightarrow \alpha = 0.4 \text{ rad/s}^2$

then:
 $\omega_f^2 = \omega_i^2 + 2 \alpha \Delta \theta$
 $\omega_f^2 = 0 + 2(0.4)\pi$

$$\omega_f = \sqrt{0.8\pi} \approx 1.6$$

$\Delta \theta = \text{half revolution}$
 $= \frac{1}{2} \cdot 2\pi$
 $= \pi$

Ans: D

67 $I_{\text{Hoop}} = M r^2 = 1(2)^2 = 4 \text{ kg.m}^2$
 $\tau = \alpha I = (7)(4) = 28 \text{ N.m} \quad \text{Ans: c}$

68

$$w_f^2 = w_i^2 + 2\alpha \Delta\theta$$

← torque constant and I constant so α is constant

$$(6)^2 = (5)^2 + 2\alpha(10\pi)$$

$$\alpha = 0.175 \Rightarrow \tau = I\alpha = 12(0.175) = 2.1$$

Ans: D

69

$$I = 0.5 \text{ kg}\cdot\text{m}^2$$

We know that $\tau = I\alpha = Fx\vec{r}$

$$\tau = I\alpha = \text{Tension } r(1)$$

so Tension = $\frac{I\alpha}{r}$

And $F_{\text{net}} = W - T$

$$ma = mg - \left(\frac{I\alpha}{r}\right) \dots (1)$$

But we know that $a = r\alpha \Rightarrow \alpha = \frac{a}{r} \dots (2)$

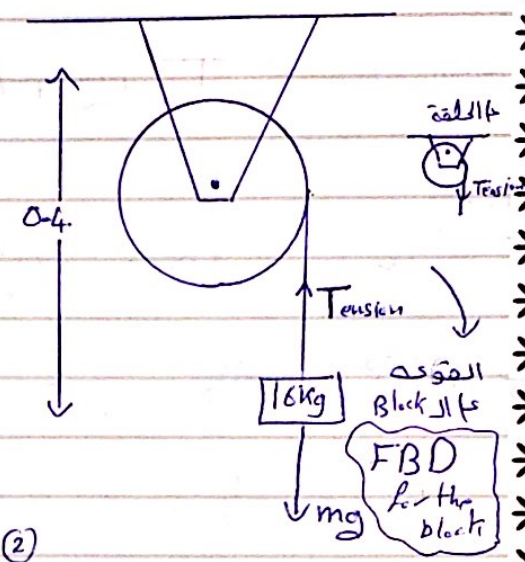
By substituting (2) in (1)

$$ma = mg - \frac{Ia}{r^2} \Rightarrow \text{now we must solve for } a \text{ so}$$

$$ma + \frac{Ia}{r^2} = mg$$

$$a = \frac{(mg)}{\left(m + \frac{I}{r^2}\right)} \Rightarrow a = \frac{16 \text{ g}}{16 + \frac{0.5}{(0.2)^2}} = 0.56 \text{ g}$$

Ans is B



70

$$R = 8.0 \text{ cm} = 8 \times 10^{-2} \text{ m} \quad \{ I = 0.12 \text{ kg}\cdot\text{m}^2 \quad \{ m = 10 \text{ kg} \} \quad \tau = 9 \text{ N}\cdot\text{m}$$

~~$\tau = I\alpha = \text{Tension } R(1)$~~

~~$\text{Tension} =$~~

$$\alpha = \frac{a}{R} \dots (1)$$

$$F - mg = ma \Rightarrow \tau_{\text{net}} = I\alpha$$

$$F = m(a + g) \quad \tau_1 = FR \sin 90^\circ = I\alpha$$

$$\tau_1 = m(a + g)R = I\left(\frac{a}{R}\right)$$

$$a = \frac{(\tau_1 - mRg)}{\left(mR + \frac{I}{R}\right)} = \frac{9 - 10(8 \times 10^{-2})(9.8)}{10(8 \times 10^{-2}) + \frac{0.12}{(8 \times 10^{-2})}} = 0.5 \text{ m/s}^2$$

ans: A



71

The Ans is B. 9.8 N

~~71~~

The suspension holding the cylinder pulls up on the cylinder with a force of $T = m_{\text{disk}}g + M_{\text{block}}(g - a_{\text{block}})$ where a_{block} - the acceleration of 2-kg mass. At the same time that is the tangential acceleration of the disk. Let's find it.

$$\tau = I\alpha = F \times R = M_{\text{block}}(g - a_{\text{block}})R$$

$$\left(\frac{a}{R}\right) \frac{MR^2}{2} = M_{\text{block}}(g - a_{\text{block}})R$$

$$\frac{Ma_{\text{disk}}}{2} = M_{\text{block}}(g - a) \Rightarrow 2M_{\text{block}}(g - a) = m_{\text{disk}}a$$

~~$a = \frac{2 \times 2 \times 9.8}{2 + 2} = 2(9.8) / (2 + 2)$~~

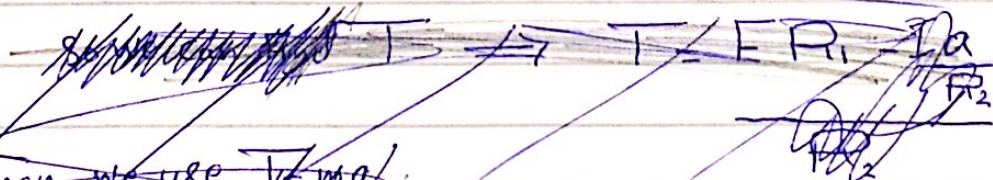
$$2M_{\text{block}}g - 2M_{\text{block}}a = m_{\text{disk}}a \Rightarrow 2M_{\text{block}}g = a(m_{\text{disk}} + 2M_{\text{block}})$$

$$a = \frac{2M_{\text{block}}g}{m_{\text{disk}} + 2M_{\text{block}}} = 8.34 \text{ m/s}^2$$

$$\begin{aligned} T &= m_{\text{disk}}g + M_{\text{block}}(g - a) \\ &= (0.7)(9.8) + 2(9.8 - 8.34) \\ &= 9.8 \text{ N} \end{aligned}$$

ans: B

~~$\tau = FR = FR_2 = I\alpha$~~



~~then we use $\tau = ma$~~

~~To find $a = \dots$~~

Continued

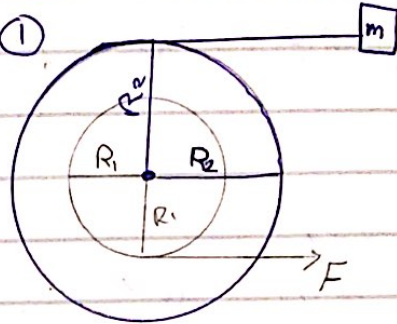
Q.72

72

$$\tau_{net} = \tau_{by F} - \tau_{by T} = I\alpha \dots \textcircled{1}$$

$$\tau_{net} = R_1 F_1 - T R_2 = I\alpha$$

The point here is that $\alpha = \frac{a}{R_2}$



So we can now find T from ①

$$T = -\frac{I a}{R_2^2} + \frac{F R_1 R_2}{R_2^2} = \frac{F R_1 R_2 - I a}{R_2^2}$$

Then we use T to find a : since $T = ma$

$$a = \frac{T}{m} = \frac{F R_1 R_2 - I a}{m R_2^2} \Rightarrow a m R_2^2 = F R_1 R_2 - I a$$

$$a(m R_2^2 + I) = F R_1 R_2$$

$$a = \frac{F R_1 R_2}{m R_2^2 + I}$$

ans: C

Q.73

73

From problem 72

$$T = am = \frac{m F R_1 R_2}{m R_2^2 + I}$$

The ~~answer~~ answer is C

Q.74

74

ans: A

Q.75

75

By $v = \omega r \Rightarrow \omega = \frac{v}{r} \Rightarrow \omega = \frac{2}{3 \times 10^{-2}} = 66.7 \text{ rad/s}$

Thus by KE (rotational) = $\frac{1}{2} I \omega^2$
 $= \frac{1}{2} (45 \times 10^{-3}) (66.7)^2 = 10 \text{ J}$

ans: D

Q.76

76

ans: C

Q.77

77

work done = $F \times \text{distance}$ distance = $\pi R = 3.14 (0.25) = 0.7854 \text{ m}$

work done = $(2)(0.7854) = 1.6 \text{ J}$

Ans: A

$W = \tau \theta$
 ~~$W = F R \theta$~~
 $= F R \pi$
 $= 1.6 \text{ J}$

constant $\omega \Rightarrow \alpha = 0$

78) $Work = \tau \cdot \theta$ ~~$\tau = 0.80$~~ $\theta = \omega t = 20 \times 60 = 1200 \text{ rad}$
 $= (0.80)(1200)$
 $= 960 \text{ J}$ ans: C



79

$$\omega_f = \omega_i + \alpha t = 0 + 2(5) = 10 \text{ rad/s}$$

$$Work \text{ done by } \tau_{net} = \Delta k = \frac{1}{2} I (\omega_f^2 - \omega_i^2)$$
$$= \frac{1}{2} (6) (10)^2 = 300 \text{ J}$$

ans: D

80

$$\tau_{net} = I \alpha \rightarrow \text{constant}$$

\downarrow constant \downarrow constant

$$\omega_f = \omega_i + \alpha t$$

$$\omega(5) = \alpha 5$$

$$\omega(10) = 10\alpha$$

$$Work \text{ done by } \tau_{net} = \Delta k = \frac{1}{2} I (\omega_f^2 - \omega_i^2)$$

$$Work \text{ in first } 5s = \frac{1}{2} I 25\alpha \dots (1)$$

$$Work \text{ in second } 5s = \frac{1}{2} I 100\alpha \dots (2)$$

$$\frac{(2)}{(1)} = 4$$

ans: D

81

ans: A



"أحسبها"

لا تنسوا من صالح دعواتي بظهر الغيب

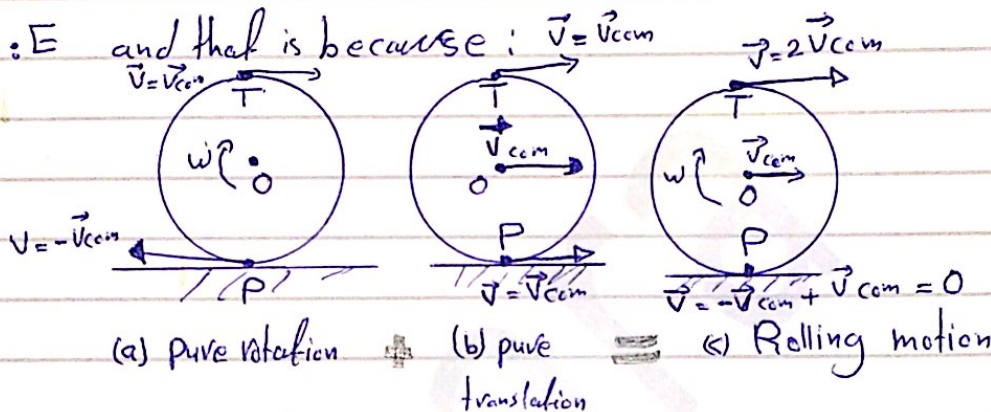
Chapter 11:

Rolling, Torque, and Angular Momentum

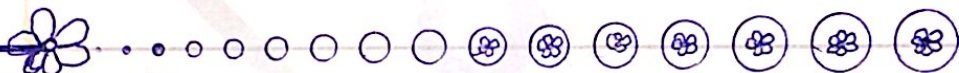
Test bank answers

1

ans: E and that is because: $\vec{v} = \vec{v}_{cm}$



راجعوا صفحة
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الكتاب



2

$$\Delta\theta = \omega t + \frac{1}{2} \alpha t^2$$

$$= 0 + \frac{1}{2} (6) (3)^2 = 27 \text{ rad}$$

but $s = \theta R = 27 (0.5)$

$$= 13.5 \text{ m}$$

ans: C

3 $v = \omega R$ and if v is the same in the two cases and $R_2 = 2R_1$

then $\omega_1 = \frac{v}{R_1}$ $\omega_2 = \frac{v}{R_2} = \frac{v}{2R_1} = \frac{1}{2} \omega_1$ ans: C

A-7 دوائر الاستكمال غير مطلوبة سبب حاجوا
سا وردة بالفاينل

8

$$k_{rot} = \frac{1}{2} I_{cm} \omega^2$$

$$k_{translation} = \frac{1}{2} M v_{cm}^2$$

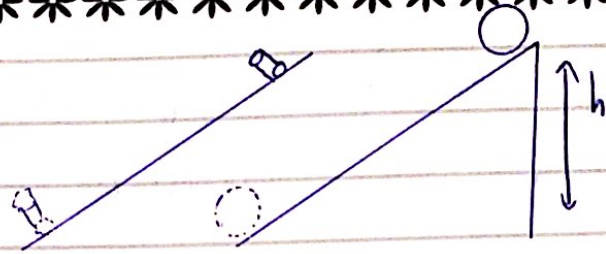
$$= \frac{1}{2} M R^2 \omega^2$$

$$= \frac{1}{2} M R^2 \left(\frac{v^2}{R^2} \right) = \frac{1}{2} M v_{cm}^2$$

$$\text{so } \frac{k_{rot}}{k_{trans}} = 1$$

ans: A

9) ans: E



Lava P

$$I_{\text{sphere}} = \frac{2}{5} MR^2$$

$$I_{\text{cylinder}} = \frac{1}{2} MR^2$$

* so the first option A is wrong because $I_{\text{cylinder}} > I_{\text{sphere}}$

$$K_{\text{rotational sphere}} = \frac{1}{2} I_{\text{sphere}} \omega^2 = \frac{1}{2} \left(\frac{2}{5} MR^2 \right) \left(\frac{V}{R} \right)^2 = \frac{1}{5} MV^2 \quad \text{--- (1)}$$

$$K_{\text{rotational cylinder}} = \frac{1}{2} I_{\text{cylinder}} \omega^2 = \frac{1}{2} \left(\frac{1}{2} MR^2 \right) \frac{V^2}{R^2} = \frac{1}{4} MV^2 \quad \text{--- (2)}$$

here we will use the conservation of Energy

First for the sphere: $(K+U)_i = (K+U)_f$

$$Mgh = K_{\text{rot}} + K_{\text{trans}}$$

$$Mgh = \frac{1}{2} I \omega^2 + \frac{1}{2} MV^2$$

$$Mgh = \frac{1}{5} MV^2 + \frac{1}{2} MV^2 \Rightarrow Mgh = \frac{7}{10} MV^2_{\text{sphere}}$$

$$V_{\text{sphere}} = \sqrt{\frac{10}{7} gh} \Rightarrow \text{(it reaches first)}$$

Second for the cylinder $Mgh = \frac{1}{4} MV^2 + \frac{1}{2} MV^2 = \frac{3}{4} MV^2_{\text{cylinder}}$

$$V_{\text{cylinder}} = \sqrt{\frac{4}{3} gh} \Rightarrow V_{\text{sphere}} > V_{\text{cylinder}} \text{ --- (sphere reach first)}$$

\Rightarrow The option B is wrong because the sphere reaches first

The option C is wrong because $K_{\text{rot sphere}} < K_{\text{rot cylinder}}$

The option D is wrong because They didn't reach the bottom together

So option E is correct

10) $I_{\text{cylinder}} = \frac{1}{2} MR^2$

$$I_{\text{sphere}} = \frac{2}{5} MR^2$$

$$I_{\text{ring}} = MR^2$$

for hoop:

$$\frac{1}{2} MV^2 + \frac{1}{2} MV^2 = Mgh$$

$$MV^2 = Mgh$$

$$h = \frac{V^2}{g}$$

disk for cylinder:

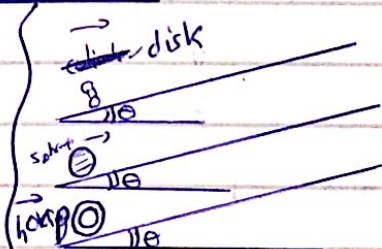
$$\frac{3}{4} MV^2 = Mgh$$

$$h = \frac{3}{4} \frac{V^2}{g}$$

for sphere:

$$\frac{7}{10} MV^2 = Mgh$$

$$h = \frac{7}{10} \frac{V^2}{g}$$



So answer is

$h_{\text{hoop}} > h_{\text{disk}} > h_{\text{sphere}}$

ans: A

11) Ans: B $k_{rot} = \frac{1}{2} I \omega^2 = \frac{1}{2} M R^2 \left(\frac{V^2}{R^2} \right) = \frac{1}{2} M V^2 = k_{trans}$

12) غير مطلوب؟ 13) 0? 14) Ans: D

15) Ans: E السرعة له قيمة عمالته وانما تكون $v = \sqrt{\frac{4}{3} gh}$ بالنسبة ليهو ابعدها

16) Ans: A

As the bodies roll from rest down the inclined plane, the initially gravitational potential energy is converted to translational and rotational kinetic energies. Since the ball is bigger than the ball bearings, its moment of inertia is larger, so that the amount of gravitational potential energy converted to rotational kinetic energy $\frac{1}{2} I \omega^2$ is also larger, leaving a smaller amount for the translational kinetic energy $\frac{1}{2} m v^2$, so that its translational speed at the bottom is smaller.

For the block mounted on roller bearings, the ball bearings are smaller than the ball, so they also have smaller moments of inertia, converting less amount of the initial gravitational potential energy to rotational kinetic energy of the ball bearings, leaving behind a larger amount for the translational kinetic energy of the block, making its translational speed at the bottom higher.

17) غير مطلوب 18) ans: E 19) Ans: D $kg \cdot m^2/s$ 20) Ans: A

21) Ans: D 22) $L = I\omega = mR^2\omega = 2(0.5)^2(12) = 6 \text{ kg} \cdot m^2/s$ نفسه السؤال المرفوع مختلفه Ans: A

23) Ans: C 24) $L = r \times p = (12)(6)(4) \sin 30 = 144$ ans: C

25) $L_{ball 1} = (1)(6)(2) \sin 90 = 12$ $L_{ball 2} = (2)(3)(3) \sin 90 = 18$
 $L_{total} = 12 + 18 = 30 \text{ kg} \cdot m^2/s$ ans: D

26) $v(2) = at = 4(2)i - 3(2)j = 8i - 6j \text{ m/s}$
 $r(2) = v_0t + \frac{1}{2}at^2 + r_0 = 0 + \frac{1}{2}(4i - 3j)(2)^2 + 3i$
 $= 8i - 6j + 3i = 11i - 6j$
 $L = r \times p = (11i - 6j) \times (16i - 12j)$
 $= -(36 \text{ kg} \cdot m^2/s)k$ Ans: B

Lava

27 ~~$L = I\omega = \frac{1}{2} m R^2 \omega = \frac{1}{2} (15) (3.3)^2$~~

$L = I\omega = mR^2\omega = \left(\frac{15}{1000}\right) (0.3)^2 (3.3) = 4.7 \times 10^{-5}$

Ans: B

~~$L = I\omega = mR^2\omega = 2(0.5)^2(12) = 6 \text{ kg}\cdot\text{m}^2/\text{s}$~~

28 + 29 + 30 :

يوجد خطأ في إرقام السؤاله يجب ان يتحول 0.75 إلى 0.61

المهم فقرة اللغه بالتاليه لهما وليست:

- 1) The z component
- 2) the xy plane component

بداية " دائرة 29" نقليه الـ z component

$L_1 = I\omega = mR^2\omega = 2(0.5)^2(12) = 6 \text{ kg}\cdot\text{m}^2/\text{s}$ Ans: A

The component in the xy plane و دائرة 30

$L_2 = I\omega = mR^2\omega = 2(0.61)^2(12) = 9 \text{ ans: C}$

$L_{net} = \sqrt{L_1^2 + L_2^2} \iff$ لحد الـ 28 دائرة
 $= \sqrt{(6)^2 + (9)^2} \approx 11 \text{ kg}\cdot\text{m}^2/\text{s}$

منه عارفة الارقام ما يتربط الا هيليه مستحيل ترتب مع وجود 0.75
 عموماً الفكرة

31 using parallel axis theorem

$I = I_{com} + Mh^2$ so $L = (I_{com} + Mh^2)\omega$ Ans: B

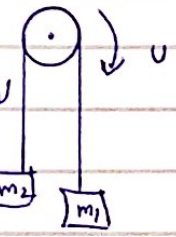
32 ~~$L = m_1 v R + I\omega$~~ $L_1 = m_1 v R$

$L_2 = m_2 v R \Rightarrow L_{net} = (m_1 + m_2) v R + I\omega$

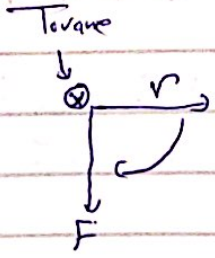
$L_{for the pulley} = I\omega = (m_1 + m_2) v R + I \frac{v}{R}$

Ans: B

$L_{net} = (m_1 + m_2) v R + I v / R$



33 ans: B



34 Ans: C

35 Ans: A

36 $F_{\text{centrifugal}} = m \omega^2 R = (2)(12)^2(0.5) = 144$

The distance from the origin = 0.75

$\tau = r F = 0.75(144) = 108$

Ans: E

37 $\tau = F \times F$

Force perpendicular component: since the 2kg mass is located 3m from the origin on the positive x-axis, only the y-component of the force cause torque. To determine the y-component of the force, we use the y-component of the acceleration $a = 4\hat{i} - 3\hat{j}$

$(-3\hat{j}) \text{ m/s}^2$ is the y-component

Force = (mass)(acceleration) = $-6\text{N}\hat{j}$

$\tau = \vec{r} \times \vec{F} = rF \sin 90 = (3)(-6) = -18 \text{ N}\cdot\text{m}$

Ans: B

38 ans: A

39 Ans: C

40 ans: A

41 $I_{\text{cm}} = I_P \frac{4}{6}$

$I_P = \frac{I_{\text{cm}}}{4}$

ans: D

42 Ans: E

43 ans: B

44 ans: C

Internal forces are unable to change angular Momentum

The Answer is L

45 Ans: B

45 السؤال

الاجابة (ans: B)

46 Ans: C

47 $L_{\text{Before}} = L_{\text{After}}$

$$I\omega + 4I\omega = 3I\omega_f$$

$$\omega_f = \frac{5I\omega}{3I} = \frac{5}{3}\omega$$

Ans: A

Lara @

48 $L_{\text{Before}} = L_{\text{After}} \Rightarrow I\omega_0 = \omega_f(2I+I)$

$$\omega_f = \frac{\omega_0 I}{3I} = \omega_0/3$$

Ans: C

49 Ans: D

50 From the conservation law.

The total angular Momentum of the child before = $L_{\text{child + merry-go-round}}$
After

$$MRV = MRV' + I\omega$$

$$MRV = MR(\omega R) + I\omega \Rightarrow MRV = \omega(MR^2 + I)$$

$$\text{So } \omega = \frac{MRV}{I + MR^2}$$

Ans: E

* 51 $L_{\text{Before}} = L_{\text{After}}$

$$600(0.8) = 600\omega_f + 20(3)^2\omega_f$$

$$600(0.8) = (600 + 180)\omega_f$$

$$\omega_f \approx 0.62 \text{ Ans: A}$$

52 Ans: A

53 Ans: C

54 Ans: A

The End 