

Alternative	Favorable Market	un-Favorable Market
Construct Large Plant	200 000	-180 000
Construct Small Plant	100 000	-20 000
Do nothing	0	0

0,4

0,6

القيمة

Max	Min	Avg	
200 000	-180 000	10 000	$\frac{200\,000 + (-180\,000)}{2}$
100 000	-20 000	40 000	$\frac{100\,000 + (-20\,000)}{2}$

$$\sum \left[\frac{(|E_t|)}{A_t} \cdot 100 \right] = 81.3\%$$

الكل

$$\textcircled{1} \text{ CFE} = \sum E_t = -15$$

$$\textcircled{2} \text{ MSE} = \frac{\sum E^2}{n} = \frac{5275}{8} = 659.4$$

$$\textcircled{3} \text{ MAP} = \frac{\sum |E_t|}{n} = \frac{195}{8} = 24.4$$

$$\textcircled{4} \text{ MAPE} = \left[\frac{\sum |E_t| \cdot 100\%}{n} \right] = \frac{81.3\%}{8} = 10.2\%$$

$$* \frac{|Et|}{At} \times 100\%$$

EX :- calculate : CFC, MSE, MAD, MAPE.

Month	At demand	Forecast Ft	Et error	Et ² error square	Et	* absolute error
1	200	225	-25	625	25	12.5%
2	240	220	+20	400	20	8.3%
3	300	285	+15	225	15	5%
4	270	290	-20	400	20	7.4%
5	230	250	-20	400	20	8.7%
6	260	240	20	400	20	7.7%
7	210	250	-40	1600	40	19%
8	275	240	35	1225	35	12.7%

$$\sum Et = -15$$

$$\sum Et^2 = 5,275$$

$$\sum |Et| = 195$$

الخطأ

$$\textcircled{1} \text{ MSE} = \frac{\sum E_t^2}{n}$$

$$\textcircled{2} \sigma = \sqrt{\frac{\sum (E_t - \bar{E})^2}{n-1}}$$

$$\textcircled{3} \text{ MAD} = \frac{\sum |E_t|}{n}$$

$\textcircled{4}$ MAPE :- a measurement that relates the forecast error to the level of demand and is useful for putting forecast performance in the error perspective.

$$\text{MAPE} = \frac{\left[\frac{\sum |E_t|}{n} \right] \times 100}{A_t}$$

$$\text{Tracking signal} = \frac{\text{CFE}}{\text{MAD}}$$

↳ a measure that indicate whether a method of forecasting is accurately predicting actual changes in demand

④ Forecast Error

① cumulative sum of forecast error

$$(cFc) = \sum E_t$$

↳ a measurement of total forecast error that assesses the bias in a forecast.

$$\bar{E} = \text{mean bias } \frac{cFc}{n} = \frac{\sum E_t}{n}$$

② MSE - the mean squared error =

σ^2 standard deviation, and

MAD (mean absolute deviation) measure the dispersion of forecast error.

⑤ Regression (Time series)

$$y = B_0 + B_1 X$$

$$y = 5 + 2x$$

$$y(5) = 5 + 2(5) = 15$$

$$SSX = \sum X^2 - \left[\frac{(\sum X)^2}{n} \right]$$

$$SSxy = \sum Xy - \left[\frac{(\sum X)(\sum y)}{n} \right]$$

$$\bar{X} = \frac{\sum X}{n}, \quad \bar{y} = \frac{\sum y}{n}$$

$$B_1 = \frac{SSxy}{SSX}, \quad B_0 = \bar{y} - B_1(\bar{X})$$

days	W1	W2	Avg	SE	W3
Sun	5	8	$\frac{5+8}{2} = 6,5$	$\frac{6.5}{31} = 0,209$	$0,209 \times 3228$ $= 6867,1$
Mon	20	15	$\frac{20+15}{2} = 17,5$	$\frac{17,5}{31} = 0,564$	18432,8
Tue	30	32	$\frac{30+32}{2} = 31$	$\frac{31}{31} = 1$	23857,14
Wed	35	30	$\frac{35+30}{2} = 32,5$	$\frac{32,5}{31} = 1,04$	34171
Thur	49	45	$\frac{49+45}{2} = 47$	$\frac{47}{31} = 1,516$	49811
Fri	70	70	$\frac{7+70}{2} = 70$	$\frac{70}{31} = 2,25$	73928
Sat	15	10	$\frac{15+10}{2} = 12,5$	$\frac{12,5}{31} = 0,403$	13241

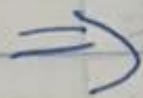
→ Avg W3

Ex : $F(w_3) = 230\,000$, and w_3 (Per day)

$$\textcircled{1} \text{ Avg}(w_3) = \frac{230\,000}{7} = 32857,14$$

$$\textcircled{2} \text{ Avg for all weeks} = \frac{5+8+20+15+\dots+10}{14} = 31$$

داعاً أولاً نشي يطلع الأ فريق الصغيرة التي برقم ① بعدين
الأ فريق الكبار التي برقم ② تخسان اعرض اصل السؤال.



$$SE = \frac{\text{Avg } Q \cdot 5}{\text{Avg} \cdot \text{All } Q} \leftarrow$$

Quanten

yr. 1

yr. 2

yr. 3

yr. 4

Avg(Qs)

SE

yr. 5

Q₁

45

70

100

100

$$\frac{45 + 70 + 100 + 100}{4} = 78.75$$

$$\frac{78.75}{387.5} = 0.203$$

$$0.203 \times 650 = 132$$

Q₂

335

370

585

725

$$\frac{335 + 370 + 585 + 725}{4} = 503.75$$

$$\frac{503.75}{387.75} = 1.3$$

$$1.3 \times 650 = 845$$

Q₃

520

590

830

1160

775

$$\frac{775}{387.5} = 2$$

$$2 \times 650 = 1300$$

Q₄

100

170

285

215

1925

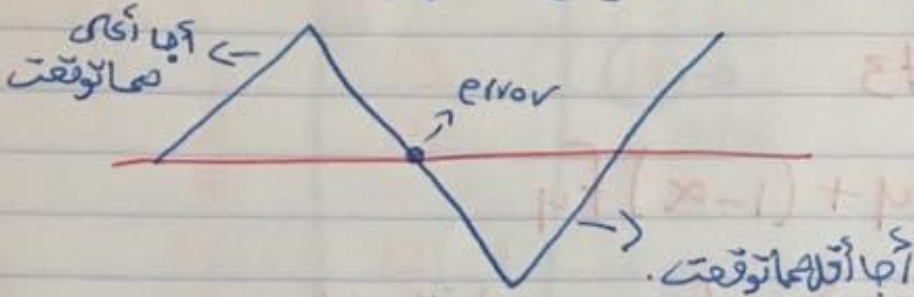
$$0.996$$

$$0.996 \times 650 = 323$$

2600
ASE

$$3) E_3 = 9 - 12,9 = \boxed{-3,9}$$

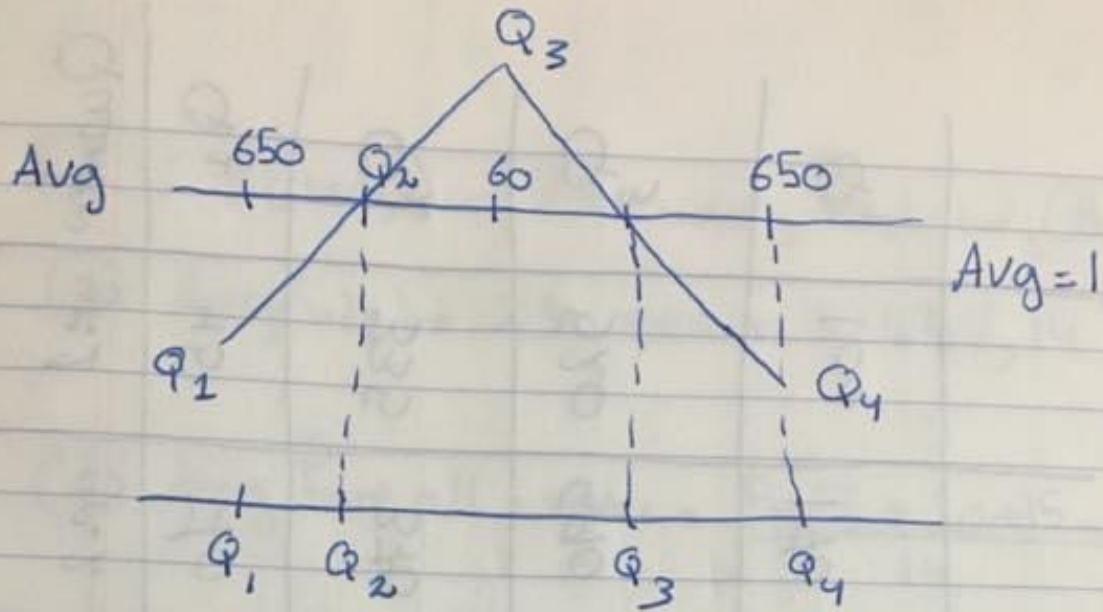
التوقع أكبر من القيمة الفعلية



④ Seasonal Patterns: [Multiplicative seasonal method]

are regularly repeating upward or downward measurement in demand measures in periods of less than one year (hrs, day, weeks, months or quarterly).

* In the next, the time periods are called seasons.



Ex: A manager wants to forecast customer demand for each next Quarter of yrs 5. Based on the estimated of total yr. 5 demand of 2600 customers.

دالة التوزيع
المتوسط

1) Avg. Q yrs = $\frac{2600}{4} = 650$ → numbers of quarters.

2) Avg. for all Q = $45 + 70 + 100 + 100$
 $+ 335 + 370 + \dots +$
 $\dots + 215$

16

= 387.5

$$\begin{aligned}F_4 &= \alpha A_3 + (1-\alpha)F_3 \\ &= (0,3)(9) + (1-0,3)12,9 \\ &= 11,73\end{aligned}$$

$$\begin{aligned}F_5 &= \alpha A_4 + (1-\alpha)F_4 \\ &= 0,3(12) + (1-0,3)11,7 \\ &= 11,8\end{aligned}$$

$$\begin{aligned}F_6 &= \alpha A_5 + (1-\alpha)F_5 \\ &= (0,3)(13) + (0,7)11,8 \\ &= 12,16\end{aligned}$$

$$E_t = A_t - F_t$$

$$1) E_1 = 12 - 12 = 0 \Rightarrow A_1 - F_1$$

$$2) E_2 = 15 - 12 = 3 \Rightarrow A_2 - F_2$$

EX on using Exponential Smoothing.

Period	Actual	F _t (Forecast)
1	12	(12) →
2	15	
3	9	
4	12	
5	13	

$$F_1 = A_1$$

$$\alpha = 0.3$$

Find $F_2, F_3, F_4, F_5, F_6 \Rightarrow$ Exponential Smoothing.

$$F_{t+1} = \alpha A_t + (1 - \alpha) F_t$$

$$F_2 = \alpha A_1 + (1 - \alpha) F_1$$

$$= (0.3)12 + (1 - 0.3)12 = 12$$

$$F_3 = \alpha (A_2) + (1 - \alpha) F_2$$

$$= (0.3)(15) + (1 - 0.3)12$$

$$\textcircled{1} F_4 = \alpha(A_3) + (1-\alpha)F_3 \rightarrow$$

أرهدنا كما ار
لأنوعتي أآرهن
فترة لوفترة وهدر
لستأزم

$$F_3 = \frac{A_2 + A_1}{2} = \frac{480 + 380}{2} = 390,1$$

$$\textcircled{2} F_4 = 0,1(411) + 0,9(390) = 392,1$$

$$\textcircled{2} E_4 = A_4 - F_4 = 415 - 392,1$$

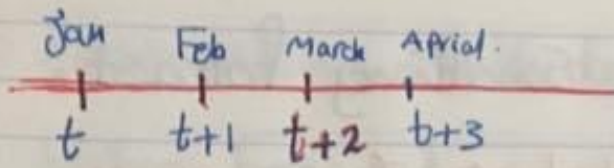
given ↪

$$22,1 \approx 23$$

$$\textcircled{3} F_5 = \alpha(A_4) + (1-\alpha)F_4$$

$$= (415)0,1 + (0,9)392,1$$

$$= 394,4$$



EX^o_v

week	A _t	F _t
1	400	
2	380	
3	411	

EX^o_v using exponential smoothing if $\alpha = 0.91$

- 1) calculate F₄
- 2) what is E₄ if A₄ = 415
- 3) what is F₅??

③ Exponential Smoothing Forecast.

↳ A weighted moving average method that calculate the average of a time series by giving recent demands more weighted than earlier.

$$\text{New Forecast} = \alpha \left(\begin{array}{c} \text{last Period} \\ \text{Actual demand} \end{array} \right) + (1-\alpha) \times$$

↓
[last Period Forecast]

$$F_{t+1} = \alpha A_t + (1-\alpha) F_t \text{ . where :-}$$

F_{t+1} = New forecast

F_t = Previous Period forecast

A_t = Previous Period Actual demand

α = Smoothing (or weighed) constant. ثابت

مراجعة قبل الامتحان

* Forecasting methods :-

① Naive Forecast اذا كان عشري نقطة وحدة

$$F_{t+1} = A_t \text{ و } E = A_i - F_i$$

② moving Average (M.A)

a) simple moving Average

$$F_{t+1} = \sum_{i=1}^n \frac{A_i}{n}$$

b) weighted moving Average

$$WMA_{t+1} = \sum_{i=1}^n w_i * A_i$$

③



Periods	A_t	weight
1	12	
2	15	0,1
3	9	0,5
4	12	0
5	13	0,4

Ex: use (0,4, 0, 0,5, 0,1) as weights for most recent data. Find F_6

← الأحدث

$$F_6 = A_5(w_5) + A_4(w_4) + A_3(w_3) + A_2(w_2)$$

$$= 13(0,4) + 12(0) + 9(0,5) + 15(0,1)$$

$$F_6 = 11,2$$

③ Weighted Moving Average

→ used when some trend might be present.

→ weights based on experienced intuition.

$$WMA_{t+1} = \sum_{i=1}^n w_i * A_i$$

w_i : the weight for period i ,

$$\sum_{i=1}^n w_i = 1$$

$$\text{e.g. } WMA_{t+1} = w_1(A_1) + w_2(A_2) + w_3(A_3) \dots$$

$$w_1 + w_2 + w_3 = 1$$

$$F_4 = \frac{\sum_{i=1}^3 A_i}{n}$$

$$= \frac{A_1 + A_2 + A_3}{3} = \frac{400 + 380 + 411}{3}$$

$$F_4 = 397$$

$$\textcircled{2} A_4 = 415, F_4 = 397$$

$$E_t = A_t - F_t = 415 - 397 = 18$$

$$\textcircled{3} F_5 = \frac{A_4 + A_3 + A_2}{3} = \frac{415 + 411 + 380}{3}$$

$$F_5 = 402$$

Ex 90

- ① compute a 3-week moving Average Forecast in week 4.
- ② if the actual number of Patient arrivals in week 4 is 415, what is the forecast error for week 4??
- ③ what is the forecast for week 5?

Week	Patient Arrivals
1	400
2	380
3	411
4	415

→
observed

Present	A_t	F_t
1	10	33
2	20	10
3	34	20
4	50	34

② Moving Average (MA)

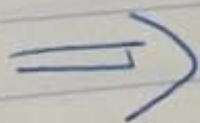
A) simple moving Average Forecast. (No trend)

$$F_{t+1} = \sum_{i=1}^n \frac{A_i}{n}, \quad E_t = A_t - F_t$$

A_t = demand in Period t .

E_t = Forecast error for Period t .

Example is

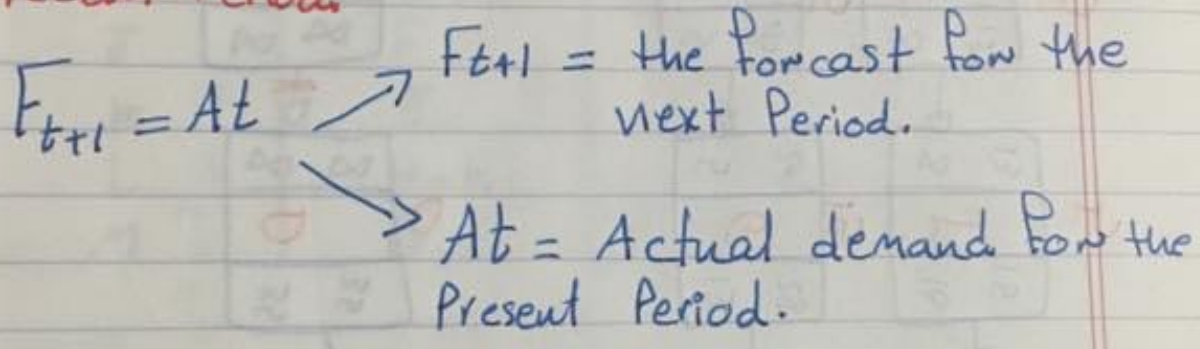


$$E = \frac{a + 4M + b}{6} \Rightarrow \text{Duration}$$



* Time Series Techniques

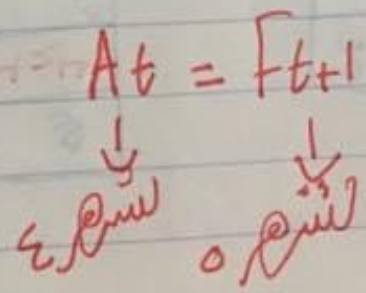
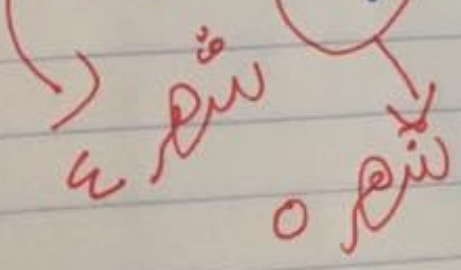
① Naive Forecast: Assume demand in next period is the same as demand in most recent period.



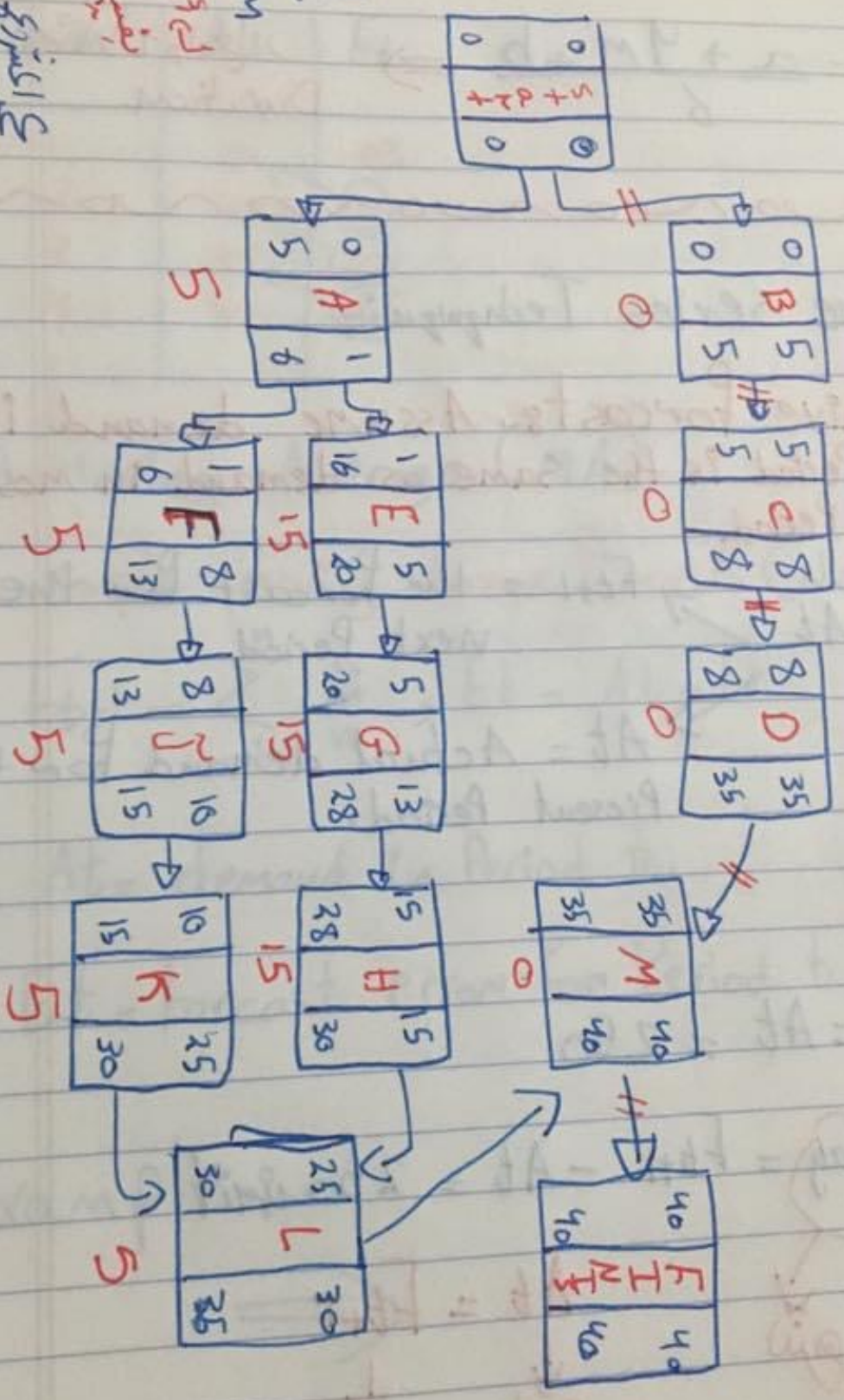
Ex^o

$A_{\text{April}} = A_t = 250$

Final $F_{\text{May}} = F_{t+1} = A_t = 250$ unit

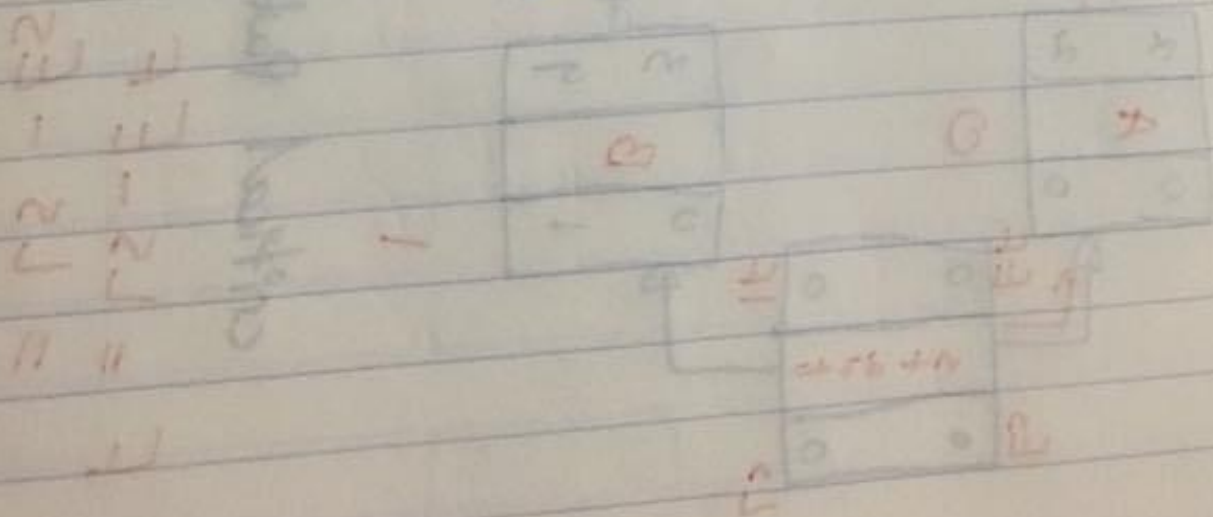


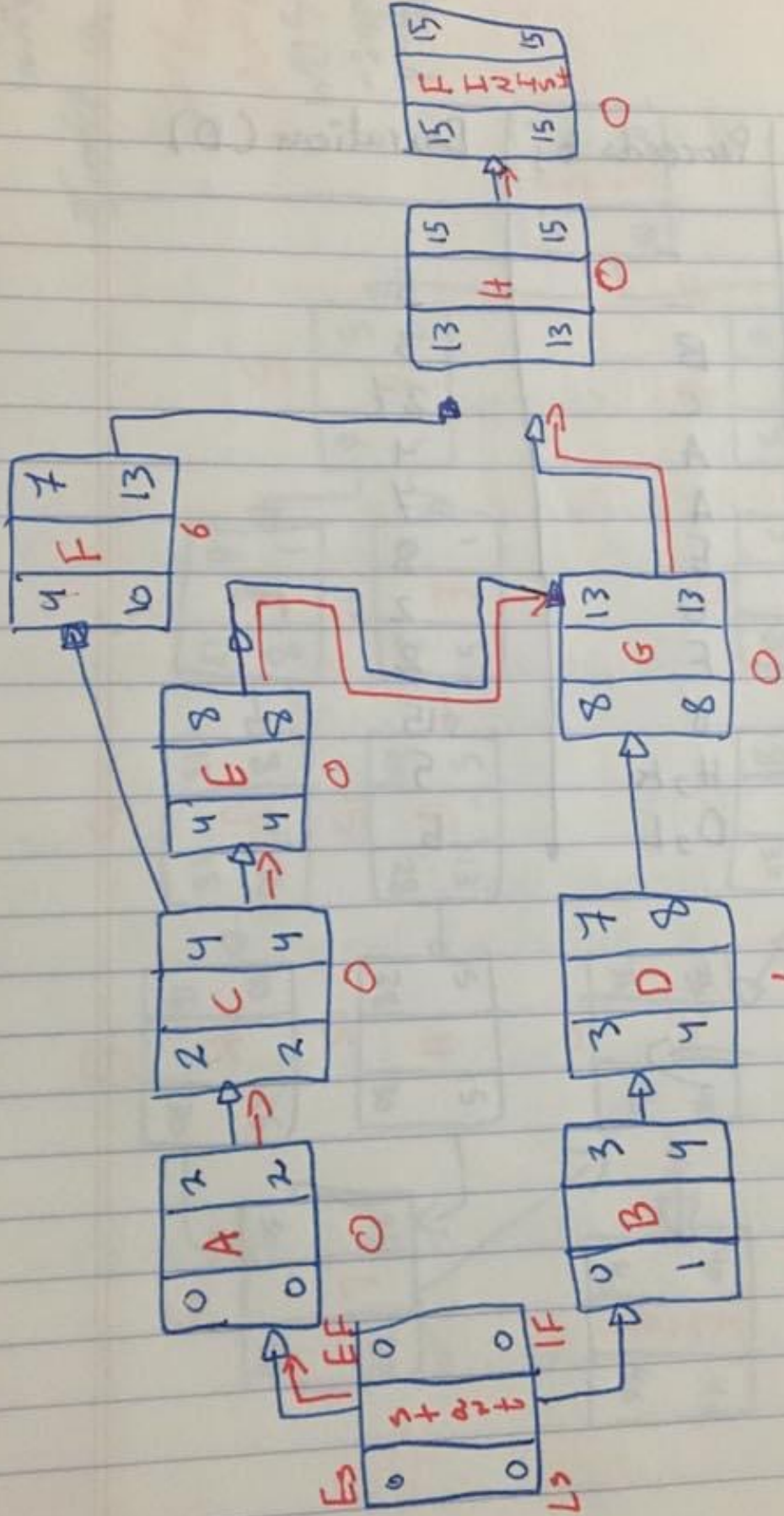
1) Critical Path :-
 B, S, D, M
 لی کی ترتیب سے
 ہفتے کے انتظامیہ
 2) 40 کے انتظامیہ کے
 سے



Activity | Proceeds by | Duration (D)

Activity	Proceeds by	Duration (D)
A	-	1
B	-	5
C	B	3
D	C	27
E	A	4
F	A	7
G	E	8
H	G	2
J	F	2
K	J	15
L	H, K	5
M	D, L	5





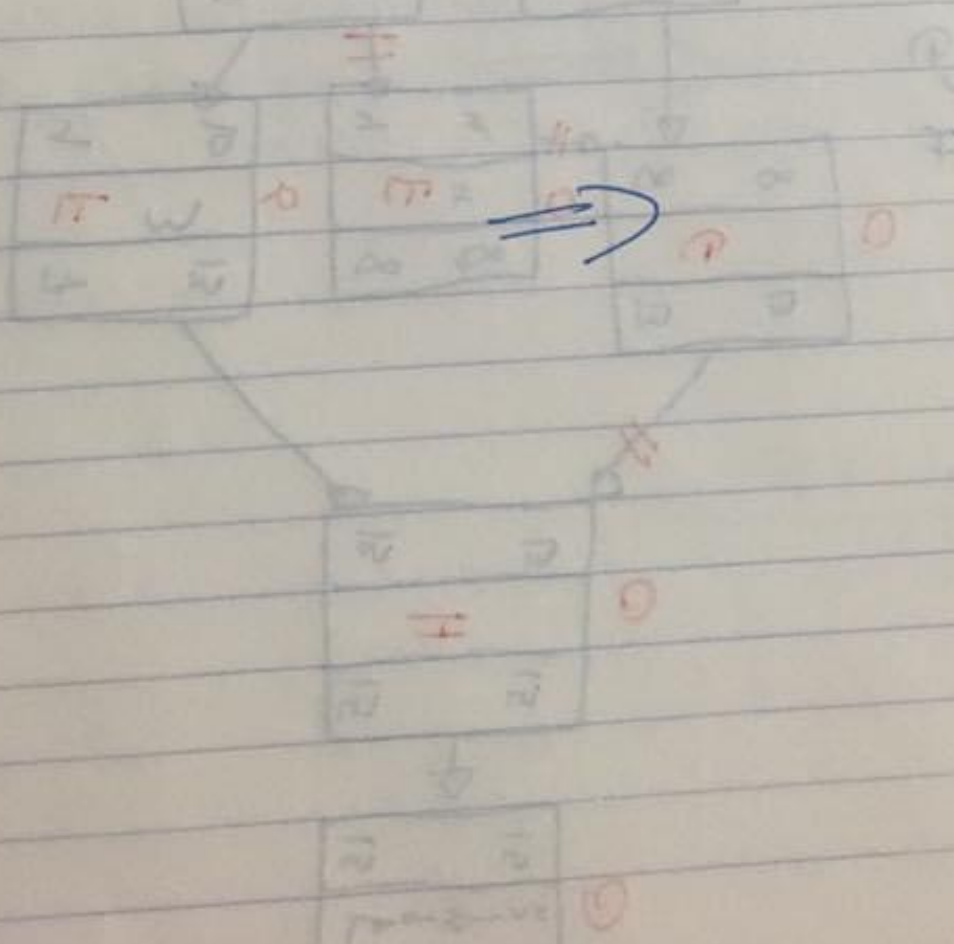
$\xrightarrow{\text{max}}$
 $\xleftarrow{\text{min}}$

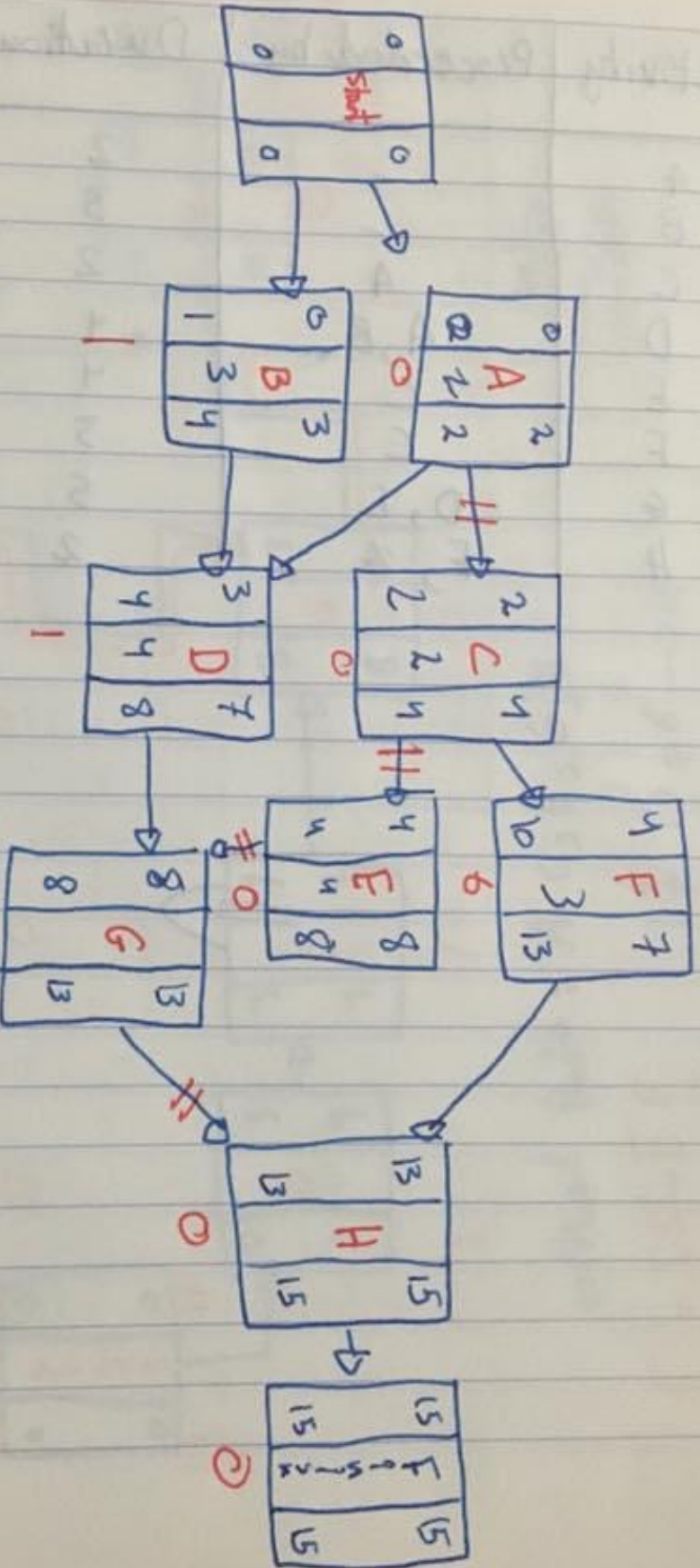
critical path: A, C, E, G, H
 if $D_1 = 6 \rightarrow 16$?

$F = LS - EF$
 $= LS - ES$

۷ مرتبہ ما، کو معطیہ ایا لزم نو ہرہا بالاول

Activity	Preceded by	Duration
A	-	2
B	-	3
C	A	2
D	A, B	4
E	C	4
F	C	3
G	D, E	5
H	F, G	2

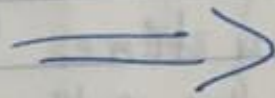




critical Path: A, C, E, G, H

کے لیے صیغہ بتاؤ

Activity	Predecessors	Time
A	- ماہنامہ کی اشیا	2
B	-	3
C	A	2
D	A, B	4
E	C	4
F	C	3
G	D, E	5
H	F, G	2



- Earliest start (ES) : the earliest possible beginning time for the activity.

لأول مرة بقدر البلى فيها.

- latest start (LS) : the latest possible beginning time from activities that will allow the project to be finished on schedule.

- Earliest finish time : (EF) : the earliest start time plus the time needed for the activity.

- latest finish time : (LF) : the latest possible completion time for an activity that will not delay the entire project

$$\text{current M.P} = \frac{0}{\Sigma I} = \frac{0}{\text{Labour} + \text{Material} + \text{Capital} + \text{energy}}$$

$$= \frac{240}{3000 + 1000 + 350 + 150}$$

$$= 0,0533 \text{ crates}/\$$$

$$\text{New} = \frac{260}{3080 + 1000 + 350 + 150}$$

$$= 0,0568 \text{ crates}/\$$$

$$\text{the increase in } P = \Delta P = \frac{P_{\text{new}} - P_{\text{current}}}{P_{\text{current}}}$$

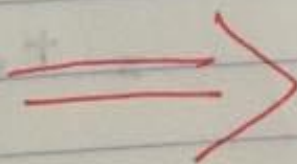
$$= \frac{0,0568 - 0,0533}{0,0533}$$

$$= +6.6\%$$

Problem 1.2

Avg cost per labour is 10\$

	Current	New
output	240 crates	260 crates
Labour hour	300	308 (300+8)
Material	1000/day	1000 (same)
Capital	350/day	350 (same)
energy	150/day	150/day
Labour cost	$10\$ * 300$ $= 3000/day$	$10\$ * 308$ $= 3080/day$



$$\textcircled{1} \text{ Current Labour Productivity} = \frac{\text{output}}{\text{Input}} = \frac{240}{3 \text{ Labour} \times 100}$$

$$= 0,8 \text{ crates/Loh}$$

$$\textcircled{2} \text{ Suggest} = \frac{0}{I} = \frac{260}{3 \times 100 + 48} = \frac{260}{308} =$$

$$= 0,844 \text{ crates/Loh}$$

$$\Delta P \frac{0,844 - 0,8}{0,8} = 5,5\%$$

Solved Problem 1.11 P. 57

* Current situation

- output = 240 crates per 100 loges
- He currently purchase 100 loges/day
- each bgs requires 3 Labour.hrs to produced

* Suggest situation

- output = 260 crates per 100 bgs
- Hrs Labour-hrs will increase by 8 hrs per day.

* What will be the input on Productivity (crates / labour.hrs) if buyer hired?

الطريقة الثانية

②

Multi Factor
Productivity =
 $\frac{\text{output}}{\text{Input}}$

	current	Suggest
	$\frac{8}{640+400}$	$\frac{14}{640+800}$
	= 0,0076 0,0076/\$	= 0,0097 title/\$

$$\Delta P_1 = \frac{\overset{\text{القيمة الجديدة}}{0,437} - \underset{\text{القيمة القديمة}}{0,25}}{0,25} \% = +75\% \uparrow$$

لأنها موجبة

$$\Delta P_2 = \frac{0,0097 - 0,0077}{0,0077} = +26\% \uparrow$$

بفضل أنها موجبة

③ $\frac{P_{\text{new}} - P_{\text{current}}}{P_{\text{current}}}$

* Both the labour (single factor) & Multiple factor Productivity measure show an increase in Productivity

لازم تشرح الحل بالأمثلة

EX 2 & P 50

	Current system	Suggested
Staff	4 labour	same (4)
W.H → working hours	8 hrs / day	same (8)
Payroll cost	640 / day	same (640)
overhead cost	400 / day	800
out Put	8 titles/day	14 title / day

الطريقة الأتوك
 ① Single Factor Productivity

$$= \frac{\text{unit Produced}}{\text{Labour.hrs}}$$

 داي ا ب ضرب
 عدد ال Labour
 في عدد الساعات

Current	Suggest
8 title / day	14 titles / day
4 Labour * 8 hrs / day	4 * 8
= 2.5 title / Labour	= 0.4375 title / \$

① * Labor Productivity = $\frac{\text{units Produced}}{\text{Labor-hours used (Input used)}}$

↳ one resource
input

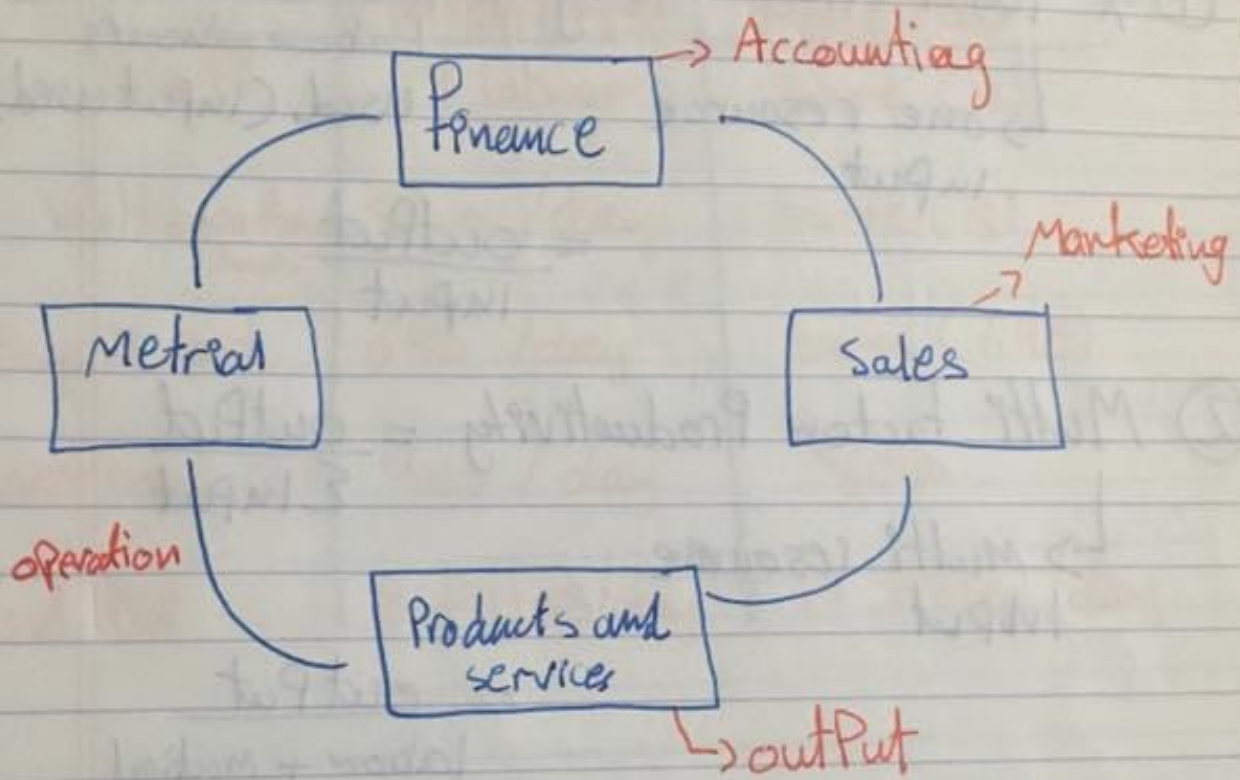
= $\frac{\text{output}}{\text{input}}$

② Multi Factor Productivity = $\frac{\text{output}}{\Sigma \text{Input}}$

↳ Multi resource
input

= $\frac{\text{output}}{\text{labor + material
+ energy + etc.}}$

* Essential functions:



* quality assurance → معايرة الجودة

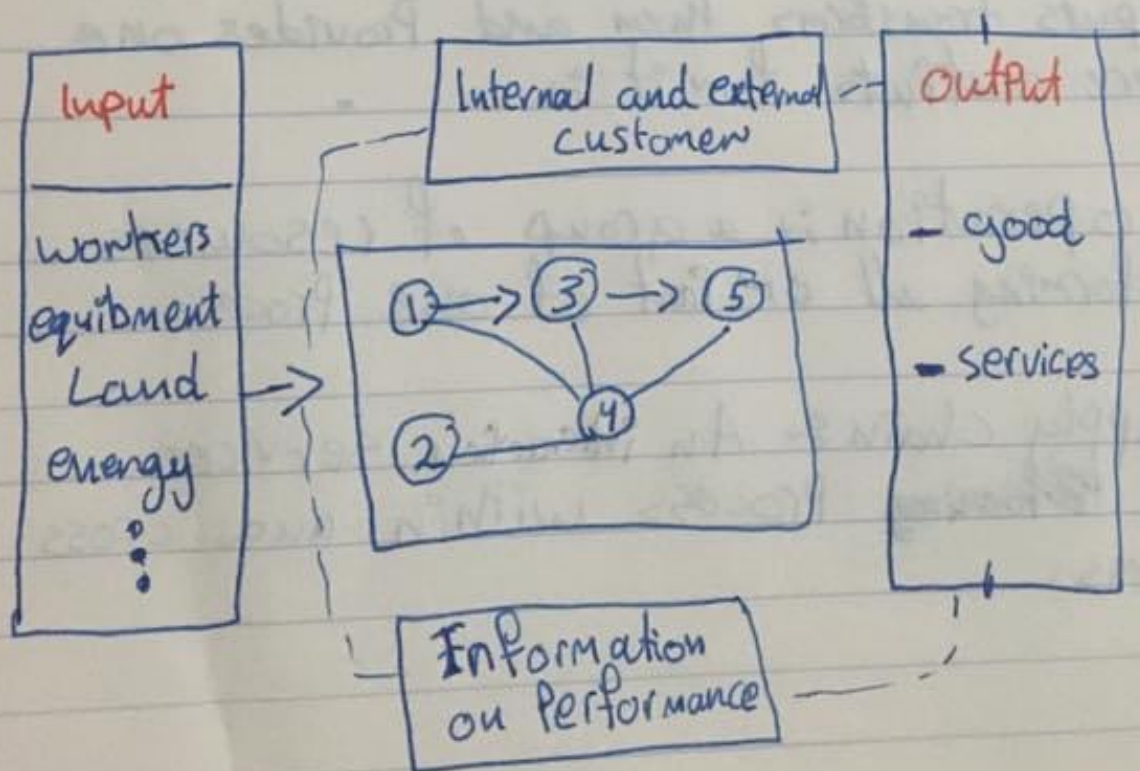
$$\text{Productivity} = \frac{\text{units Produced}}{\text{Inputs}}$$

* operation management → transforming input into output.

* that Produces services or Product of the satisfaction of outcome

* supply chain Management (SCM) is the system of firms Process with those of it is suppliers and customers to the flow of material services and information with customer demands.

* How Process works



Ch 1 ~ Introduction to OM

- * Production \Rightarrow the creation of goods and servicing.
- * Operation Management \Rightarrow the systemic design, direction and control of Process that transform employee input into Services and Products for internal as well as external customers.
- * Process \Rightarrow is an activity of group of activities that takes on or more input transform them and Provides one or more outputs transforms them and Provides one more outputs for it is .
- * Operation is a group of resources performing all or part of one Process.
- * supply chain ~ An interaction services of ~~performing~~ Process within and cross terms.