

## تجميع قوانين فايننس 2 (FINN2300)

### Chapter 8: RISK & RETURN

Total rate of return:

$$r_t = \frac{C_t + P_t - P_{t-1}}{P_{t-1}} \quad (8.1)$$

where

- $r_t$  = actual, expected, or required rate of return during period  $t$
- $C_t$  = cash (flow) received from the asset investment in the time period  $t - 1$  to  $t$
- $P_t$  = price (value) of asset at time  $t$
- $P_{t-1}$  = price (value) of asset at time  $t - 1$

Expected return:

$$\bar{r} = \sum_{j=1}^n r_j \times Pr_j$$

where

- $r_j$  = return for the  $j$ th outcome
- $Pr_j$  = probability of occurrence of the  $j$ th outcome
- $n$  = number of outcomes considered

3. The formula for finding the expected value of return,  $\bar{r}$ , when all of the outcomes,  $r_j$ , are known and their related probabilities are equal, is a simple arithmetic average:

$$\bar{r} = \frac{\sum_{j=1}^n r_j}{n} \quad (8.2a)$$

where  $n$  is the number of observations.

Standard deviation of returns:

The expression for the *standard deviation of returns*,  $\sigma_r$ , is<sup>4</sup>

$$\sigma_r = \sqrt{\sum_{j=1}^n (r_j - \bar{r})^2 \times Pr_j} \quad (8.3)$$

Coefficient of variation:

$$CV = \frac{\sigma_r}{\bar{r}} \quad (8.4)$$

## تجميع قوانين فايننس 2 (FINN2300)

### Portfolio return:

$$r_p = (w_1 \times r_1) + (w_2 \times r_2) + \dots + (w_n \times r_n) = \sum_{j=1}^n w_j \times r_j \quad (8.5)$$

where

$w_j$  = proportion of the portfolio's total dollar value represented by asset  $j$

$r_j$  = return on asset  $j$

Of course,  $\sum_{j=1}^n w_j = 1$ , which means that 100 percent of the portfolio's assets must be included in this computation.

### Total Security Risk:

$$\text{Total security risk} = \text{Nondiversifiable risk} + \text{Diversifiable risk} \quad (8.6)$$

### Portfolio beta:

$$\beta_p = (w_1 \times \beta_1) + (w_2 \times \beta_2) + \dots + (w_n \times \beta_n) = \sum_{j=1}^n w_j \times \beta_j \quad (8.7)$$

Of course,  $\sum_{j=1}^n w_j = 1$ , which means that 100 percent of the portfolio's assets must be included in this computation.

### The capital asset pricing model (CAPM):

$$r_j = R_F + [\beta_j \times (r_m - R_F)] \quad (8.8)$$

where

$r_j$  = required return on asset  $j$

$R_F$  = risk-free rate of return, commonly measured by the return on a U.S. Treasury bill

$\beta_j$  = beta coefficient or index of nondiversifiable risk for asset  $j$

$r_m$  = market return; return on the market portfolio of assets

### Risk-free rate of return:

$$R_F = r^* + IP \quad (8.9)$$

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### Chapter 6: INTEREST RATES AND BOND VALUATION

**Nominal rate of interest:**

**Risk premium:**

**Risk-free rate:**

$$r_1 = \underbrace{r^* + IP}_{\text{risk-free rate, } R_F} + \underbrace{RP_1}_{\text{risk premium}} \quad (6.1)$$

As the horizontal braces below the equation indicate, the nominal rate,  $r_1$ , can be viewed as having two basic components: a risk-free rate of return,  $R_F$ , and a risk premium,  $RP_1$ :

$$r_1 = R_F + RP_1 \quad (6.2)$$

For the moment, ignore the risk premium,  $RP_1$ , and focus exclusively on the risk-free rate. Equation 6.1 says that the risk-free rate can be represented as

$$R_F = r^* + IP \quad (6.3)$$

**Risky non-Treasury issues:**

$$r_1 = \underbrace{r^* + IP}_{\text{risk-free rate, } R_F} + \underbrace{RP_1}_{\text{risk premium}}$$

In words, the nominal rate of interest for security 1 ( $r_1$ ) is equal to the risk-free rate, consisting of the real rate of interest ( $r^*$ ) plus the inflation expectation premium ( $IP$ ), plus the risk premium ( $RP_1$ ). The *risk premium* varies with specific issuer and issue characteristics.

**Value of any asset at time zero:**

$$V_0 = \frac{CF_1}{(1+r)^1} + \frac{CF_2}{(1+r)^2} + \dots + \frac{CF_n}{(1+r)^n} \quad (6.4)$$

where

- $V_0$  = value of the asset at time zero
- $CF_t$  = cash flow *expected* at the end of year  $t$
- $r$  = appropriate required return (discount rate)
- $n$  = relevant time period

We can use Equation 6.4 to determine the value of any asset.

## تجميع قوانين فايننس 2 (FINN2300)

### Basic model for the value:

$$B_0 = I \times \left[ \sum_{t=1}^n \frac{1}{(1 + r_d)^t} \right] + M \times \left[ \frac{1}{(1 + r_d)^n} \right] \quad (6.5)$$

where

$B_0$  = value of the bond at time zero

$I$  = *annual* interest paid in dollars

$n$  = number of years to maturity

$M$  = par value in dollars

$r_d$  = required return on the bond

### Present value instead of future value:

1. Converting annual interest,  $I$ , to semiannual interest by dividing  $I$  by 2.
2. Converting the number of years to maturity,  $n$ , to the number of 6-month periods to maturity by multiplying  $n$  by 2.
3. Converting the required stated (rather than effective)<sup>6</sup> annual return for similar-risk bonds that also pay semiannual interest from an annual rate,  $r_d$ , to a semiannual rate by dividing  $r_d$  by 2.

$$B_0 = \frac{I}{2} \times \left[ \sum_{t=1}^{2n} \frac{1}{\left(1 + \frac{r_d}{2}\right)^t} \right] + M \times \left[ \frac{1}{\left(1 + \frac{r_d}{2}\right)^{2n}} \right] \quad (6.6)$$

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### CHAPTER 7: STOCK VALUATION

#### Basic valuation model for common stock:

$$P_0 = \frac{D_1}{(1+r_s)^1} + \frac{D_2}{(1+r_s)^2} + \dots + \frac{D_\infty}{(1+r_s)^\infty} \quad (7.1)$$

where

$P_0$  = value today of common stock

$D_t$  = per-share dividend *expected* at the end of year  $t$

$r_s$  = required return on common stock

#### Zero-Growth Model:

$$P_0 = D_1 \times \sum_{t=1}^{\infty} \frac{1}{(1+r_s)^t} = D_1 \times \frac{1}{r_s} = \frac{D_1}{r_s} \quad (7.2)$$

$D_1$  represent the amount of the annual dividend

#### Constant-Growth Model:

#### Gordon growth model:

By letting  $D_0$  represent the most recent dividend, we can rewrite Equation 7.1 as

$$P_0 = \frac{D_0 \times (1+g)^1}{(1+r_s)^1} + \frac{D_0 \times (1+g)^2}{(1+r_s)^2} + \dots + \frac{D_0 \times (1+g)^\infty}{(1+r_s)^\infty} \quad (7.3)$$

If we simplify Equation 7.3, it can be rewritten as

$$P_0 = \frac{D_1}{r_s - g} \quad (7.4)$$

#### Value of the stock:

$$P_0 = \underbrace{\sum_{t=1}^N \frac{D_0 \times (1+g_1)^t}{(1+r_s)^t}}_{\text{Present value of dividends during initial growth period}} + \underbrace{\left[ \frac{1}{(1+r_s)^N} \times \frac{D_{N+1}}{r_s - g_2} \right]}_{\text{Present value of price of stock at end of initial growth period}} \quad (7.5)$$

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### Free cash flow valuation model:

$$V_C = \frac{FCF_1}{(1 + r_d)^1} + \frac{FCF_2}{(1 + r_d)^2} + \dots + \frac{FCF_\infty}{(1 + r_d)^\infty} \quad (7.6)$$

where

- $V_C$  = value of the entire company
- $FCF_t$  = free cash flow *expected* at the end of year  $t$
- $r_d$  = the firm's weighted average cost of capital

### Find common stock value:

$$V_S = V_C - V_D - V_P \quad (7.7)$$

To find common stock value:  $V_S$ , we must subtract the market value of all the firm's debt:  $V_D$ , and the market value of preferred stock:  $V_P$  from  $V_C$ :

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### CHAPTER 9: COST OF CAPITAL

#### Before-tax cost of debt:

$$r_d = \frac{I + \frac{\$1,000 - N_d}{n}}{\frac{N_d + \$1,000}{2}} \quad (9.1)$$

where

$I$  = annual interest in dollars  
 $N_d$  = net proceeds from the sale of debt (bond)  
 $n$  = number of years to the bond's maturity

#### After-tax cost of debt:

$$r_i = r_d \times (1 - T) \quad (9.2)$$

where

Tax rate:  $T$

#### Cost of preferred stock:

$$r_p = \frac{D_p}{N_p} \quad (9.3)$$

where

annual dollar dividend =  $D_p$

net proceeds from the sale of the stock =  $N_p$

#### Gordon growth model:

$$P_0 = \frac{D_1}{r_s - g} \quad (9.4)$$

where

$P_0$  = value of common stock  
 $D_1$  = per-share dividend *expected* at the end of year 1  
 $r_s$  = required return on common stock  
 $g$  = constant rate of growth in dividends

## تجميع قوانين فايننس 2 (FINN2300)

### Cost of common stock equity:

$$r_s = \frac{D_1}{P_0} + g \quad (9.5)$$

### Required return:

$$r_s = R_F + [\beta \times (r_m - R_F)] \quad (9.6)$$

where

$R_F$  = risk-free rate of return

$r_m$  = market return; return on the market portfolio of assets

### Cost of retained earnings:

$$r_r = r_s \quad (9.7)$$

### Cost of a new issue of common stock:

$$r_n = \frac{D_1}{N_n} + g \quad (9.8)$$

If we let  $N_n$  represent the net proceeds from the sale of new common stock after subtracting underpricing and flotation costs, the cost of the new issue,  $R_n$ .

### Weighted average cost of capital (WACC):

$$r_a = (w_i \times r_i) + (w_p \times r_p) + (w_s \times r_{r \text{ or } n}) \quad (9.9)$$

where

$w_i$  = proportion of long-term debt in capital structure

$w_p$  = proportion of preferred stock in capital structure

$w_s$  = proportion of common stock equity in capital structure

$w_i + w_p + w_s = 1.0$

$R_a$  = weighted average cost of capital



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### Chapter 10 :CAPITAL BUDGETING TECHNIQUES

#### Net present value (NVP):

The net present value (NPV) is found by subtracting a project's initial investment ( $CF_0$ ) from the present value of its cash inflows ( $CF_t$ ) discounted at a rate equal to the firm's cost of capital ( $r$ ):

NPV = Present value of cash inflows – Initial investment

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+r)^t} - CF_0 \quad (10.1)$$

#### Profitability index (PI):

$$PI = \frac{\sum_{t=1}^n \frac{CF_t}{(1+r)^t}}{CF_0} \quad (10.2)$$

#### Internal Rate of Return (IRR):

$$\$0 = \sum_{t=1}^n \frac{CF_t}{(1+IRR)^t} - CF_0 \quad (10.3)$$

$$\sum_{t=1}^n \frac{CF_t}{(1+IRR)^t} = CF_0 \quad (10.3a)$$