Chapter 0 Algebraic Concepts 2

Sections 1-2

Use ∈ or ∉ in blank place to indicate whether the given object is an element of the given set.

 $6 _ \{1, 2, 3, 4, 5, 6\}$ A) $6 \in \{1, 2, 3, 4, 5, 6\}$ B) $6 \notin \{1, 2, 3, 4, 5, 6\}$ Ans: A

- 2. Use \in or \notin in blank place to indicate whether the given object is an element of the given set.
 - 4 ____{x: x is a natural greater than 4 } A) 4 \in {x: x is a natural number greater than 4 }
 - B) $4 \notin \{x : x \text{ is a natural number greater than } 4 \}$

Ans: B

3. Use \in or \notin in blank place to indicate whether the given object is an element of the given set.

7 ____ {*x* : *x* is a natural number less than 7}

- A) $7 \in \{x : x \text{ is a natural number less than } 7\}$
- B) $7 \notin \{x : x \text{ is a natural number less than } 7\}$

- 4. Use \in or \notin in blank place to indicate whether the given object is an element of the given set.
 - $5 _ \emptyset$ A) $5 \in \emptyset$ B) $5 \notin \emptyset$ Ans: B
- 5. Write the following set a second way.

 $\{x: x \text{ is a natural number greater than } 11 \text{ and less than } 15\}$

- A) {11,12,13,14}
- B) {11,12,13}
- C) {12,13,14}
- D) {12,13,14,15}
- E) $\{10, 11, 12, 13\}$

Ans: C

Ans: B

6. Write the following set a second way. {5,6,7,8,...}
A) {x: x is a natural number greater than 4 and less than 9}
B) {x: x is a natural number greater than 5 and less than 8}

- C) $\{x: x \text{ is a natural number greater than 6}\}$
- D) $\{x: x \text{ is a natural number greater than 5}\}$
- E) $\{x : x \text{ is a natural number greater than 4}\}$

Ans: E

7. If $A = \{a, b, c, d\}$ and $B = \{c, a, b, d\}$, is A a subset of B?

- A) yes
- B) no
- Ans: A

8. Is $A \subseteq B$ if $A = \{1, 4, 5, 12\}$ and $B = \{1, 4, 5, 13, 18, 22\}$?

- A) yesB) noAns: B
- 9. Use \subseteq notation to indicate which of the sets *E* and *F* is a subset of the other. $E = \{y, x, a, d\}, F = \{a, 6, x, d, 2, y\}$
 - A) $F \subseteq E$ B) $E \subseteq F$ C) $E \subseteq U$ D) $F \subseteq E$ and $E \subseteq F$ E) $F \supseteq E$ and $F \subseteq E$ Ans:B
- 10. Use \subseteq notation to indicate all containment relations between the following two sets.
 - $D = \{a, e, 1, 3, c\}, F = \{1, a, c, e, 3\}$ A) $F \supseteq D$ B) $D \subseteq U$ C) $D \supseteq F$ D) $D \subseteq F \text{ and } F \subseteq D$ E) $D \subseteq F \text{ and } F \supseteq D$ Ans: D
- 11. Indicate whether the following sets are equal.
 - $A = \{x, h, a, n\}, D = \{x, a, b, y\}$ A) $A \neq D$ B) A = DAns: A

- 12. Indicate whether the following sets are equal.
 - $F = \{x : x \text{ is a natural number greater than 7}\}, G = \{8,9,10,...\}$ A) F = G
 - B) $F \neq G$ Ans: A

13. If the sets A and B are nonempty and disjoint, what does $A \cap B$ equal?

- A) \varnothing B) $A \cap A'$ C) AD) BE) $A \cup B'$ Ans: A
- 14. Find $A \cap B$, the intersection of sets *A* and *B*. $A = \{2, 3, 4, 5, 6\}$ and $B = \{4, 6, 8, 10, 12\}$
 - A) $A \cap B = \{4, 5, 7, 9, 11\}$
 - B) $A \cap B = \{3, 5\}$
 - C) $A \cap B = \{4, 6, 8, 10, 12\}$
 - D) $A \cap B = \{2, 3, 4, 5, 6\}$
 - E) $A \cap B = \{4, 6\}$

Ans: E

- 15. Find $A \cap B$, the intersection of sets A and B.
 - $A = \{a, b, c, d, e\}$ and $B = \{c, h, d, g, e, r\}$
 - A) $A \cap B = \{h, g, r\}$ B) $A \cap B = \{c, d, e\}$ C) $A \cap B = \{c, h, d\}$
 - D) $A \cap B = \{g, e, r\}$
 - $E) \qquad A \cap B = \{c, e, r\}$

Ans: B

- 16. Find $A \cap B$, the intersection of sets A and B.
 - $A = \{x : x \text{ is a natural number less than } 4\}$ $B = \{2, 3, 4, 5, 6\}$ A) $A \cap B = \emptyset$ B) $A \cap B = \{2, 3\}$ C) $A \cap B = \{4, 5, 6\}$ D) $A \cap B = \{2, 3, 4, 5, 6\}$ E) $A \cap B = \{-2, -1, 0, 2, 3\}$ Ans: B
- 17. Find $A \cup B$, the union of sets *A* and *B*. $A = \{a, f, h, o, u\}$ and $B = \{a, b, c, d\}$ A) $A \cup B = \{f, h, o, u\}$ B) $A \cup B = \{a, b, c, d\}$ C) $A \cup B = \{a, b, c, d, f, h, o, u\}$ D) $A \cup B = \{a, c, d, f, h, o, u\}$ E) $A \cup B = \{a, c, d, f, u\}$ Ans: C
- 18. Find $A \cup B$, the union of sets A and B.

 $A = \{x : x \text{ is a natural number greater than 5}\}$

 $B = \{x : x \text{ is a natural number less than 5}\}$

- A) $A \cup B = \{x : x \text{ is a natural number greater than or equal to 5}\}$
- B) $A \cup B = \{5\}$
- C) $A \cup B = \{x : x \text{ is a natural number not equal to 5}\}$
- D) $A \cup B$ is the set of natural numbers.
- E) $A \cup B = \{x : x \text{ is a natural number less than 5}\}$
- Ans: C

19. Assume that $A = \{1, 2, 5, 7, 8\}$ and that U is the universal set of natural numbers less than

- 11. Find A'
- A) $A' = \{1, 2, 5, 7, 8\}$
- B) $A' = \{3, 4, 6, 9, 10\}$
- C) $A' = \{2, 3, 5, 6\}$
- D) $A' = \{4, 6, 9, 10\}$
- E) $A' = \{1, 3, 5, 7\}$

Ans: B

20. Assume that

$$A = \{1, 2, 3, 5, 8, 7\}$$

 $B = \{1, 2, 5, 7, 8\}$
and that *U* is the universal set of natural numbers less than 11. Find $A \cap B'$.
A) $A \cap B' = \{1, 2, 3, 5, 8, 7\}$
B) $A \cap B' = \{3, 4, 6, 9, 10\}$
C) $A \cap B' = \{3\}$
D) $A \cap B' = \{1, 2, 6, 7, 8, 9, 10\}$
E) $A \cap B' = \{1, 2, 5, 7, 8, 9\}$

E)
$$A \cap B' = \{1, 2, 5, 7, 8, 9\}$$

Ans: C

21. Assume that

 $A = \{1, 2, 3, 5, 8, 7\}$ $B = \{1, 2, 5, 7, 8\}$

and that U is the universal set of natural numbers less than 11. Find $A' \cap B'$.

- A) $A' \cap B' = \{1, 5, 7, 8\}$
- B) $A' \cap B' = \{2, 4, 9, 10\}$

C)
$$A' \cap B' = \{3, 6, 7\}$$

D)
$$A' \cap B' = \{4, 6, 9, 10\}$$

E)
$$A' \cap B' = \{1, 3, 5, 7\}$$

Ans: D

22. Assume that

$$A = \{1, 2, 3, 5, 8, 7\}$$
$$B = \{1, 2, 5, 7, 8\}$$

and that U is the universal set of natural numbers less than 11. Find $(A \cap B)'$.

A)
$$(A \cap B)' = \{3, 4, 6, 9, 10\}$$

B)
$$(A \cap B)' = \{1, 4, 7, 9, 10\}$$

C)
$$(A \cap B)' = \{2, 5, 6, 7, 9\}$$

D)
$$(A \cap B)' = \{1, 4, 5, 7, 9\}$$

E)
$$(A \cap B)' = \{3, 5, 7, 9\}$$

Ans: A

23. Assume that

 $A = \{1, 2, 3, 5, 8, 7\}$

 $B = \{1, 2, 5, 7, 8\}$

and that U is the universal set of natural numbers less than 11. Find $(A \cup B)'$.

- $A) \qquad (A' \cup B)' = \{3\}$
- B) $(A'\cup B)' = \{6,9,10\}$

C)
$$(A' \cup B)' = \{5\}$$

D)
$$(A' \cup B)' = \{7\}$$

E) $(A' \cup B)' = \{3, 7\}$

Ans: A

24. Assume that

 $A = \{1, 2, 3, 5, 8, 7\}$ $B = \{1, 2, 5, 7, 8\}$ $C = \{2, 3, 5, 6\}$

and that U is the universal set of natural numbers less than 11. Find $A \cap (B \cup C)$.

A)
$$A \cap (B' \cup C') = \{1, 2, 3, 8, 9\}$$

B)
$$A \cap (B' \cup C') = \{1, 4, 7, 8\}$$

C)
$$A \cap (B' \cup C') = \{1, 3, 7, 8\}$$

D)
$$A \cap (B' \cup C') = \{3, 5, 7\}$$

E)
$$A \cap (B' \cup C') = \{1, 7, 8\}$$

Ans: C

25. Assume that

$$A = \{1, 2, 3, 5, 8, 7\}$$
$$B = \{1, 2, 5, 7, 8\}$$
$$C = \{2, 3, 5, 6\}$$

and that U is the universal set of natural numbers less than 11. Find $A \cap (B \cup C)$.

A)
$$A \cap (B \cup C) = \{2, 5, 6\}$$

B)
$$A \cap (B \cup C) = \{1, 2, 3, 5, 7, 8\}$$

$$\mathbf{C}) \qquad A \cap (B \cup C) = \{3, 7\}$$

D)
$$A \cap (B \cup C) = \{1, 2, 4, 7, 9\}$$

E)
$$A \cap (B \cup C) = \{3, 5, 7, 9\}$$

Ans: B

- 26. Find A-B if the universal set $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$. $A = \{1, 2, 3, 6, 9\}$ $B = \{1, 2, 5, 6, 7\}$ A) $A-B = \emptyset$ B) $A-B = \{8, 9\}$ C) $A-B = \{2, 3, 7\}$ D) $A-B = \{5, 7, 8\}$ E) $A-B = \{3, 9\}$
- Ans: E 27. Find A - B if the universal set $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$. $A = \{6, 5, 4, 1, 3, 2\}$ $B = \{1, 2, 3, 4, 5, 6\}$ A) $A - B = \emptyset$ B) $A - B = \{1, 2, 3, 4, 5, 6\}$ C) $A - B = \{2, 4, 6, 8\}$ D) $A - B = \{3, 6, 8\}$ E) $A - B = \{2, 5, 7\}$

E)
$$A-B = \{3,5,7\}$$

Ans: A

28. Find A - B if the universal set $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$.

$$A = \{1, 2, 3, 4, 5\}$$

$$B = \{2, 3, 5, 7, 9\}$$

A) $A - B = \emptyset$
B) $A - B = \{1, 4\}$
C) $A - B = \{2, 3, 5\}$
D) $A - B = \{7, 9\}$
E) $A - B = \{3, 5\}$
Ans: B

- 29. Suppose that a survey of 100 advertisers in U.S. News, These Times, and World found the following.
 - 15 advertised in all three
 - 18 advertised in These Times and U.S. News
 - 39 advertised in World and U.S. News
 - 33 advertised in World and These Times
 - 49 advertised in These Times
 - 53 advertised in U.S. News
 - 68 advertised in World

How many advertised in none of these publications?

- A) 35
- B) 15
- C) 5
- D) 11
- E) 55
- Ans: C
- 30. Suppose that a survey of 100 advertisers in U.S. News, These Times, and World found the following.
 - 15 advertised in all three
 - 18 advertised in These Times and U.S. News
 - 39 advertised in World and U.S. News
 - 33 advertised in World and These Times
 - 49 advertised in These Times
 - 53 advertised in U.S. News
 - 68 advertised in World

How many advertised only in These Times?

- A) 13
- B) 21
- C) 3
- D) 6
- E) 49
- Ans: A

31. Suppose that a survey of 100 advertisers in U.S. News, These Times, and World found the following.

15 advertised in all three

- 18 advertised in These Times and U.S. News
- 39 advertised in World and U.S. News
- 33 advertised in World and These Times
- 49 advertised in *These Times*
- 53 advertised in U.S. News
- 68 advertised in World

How many advertised in U.S. News or These Times?

- A) 84
- B) 27
- C) 3
- D) 39
- E) 53
- Ans: A
- 32. In a survey of the dining preferences of 110 dormitory students at the end of the spring semester, the following facts were discovered about Adam's Lunch *AL*, Pizza Tower *PT*, and the Dining Hall *DH*.
 - 15 liked AL but not PT10 liked AL only23 liked AL42 liked PT48 liked DH
 - 4 liked PT and AL but not DH
 - 25 liked PT and DH

How many liked PT or DH?

- A) 52
 B) 25
 C) 39
 D) 27
 E) 65
- Ans: E

- 33. In a survey of the dining preferences of 110 dormitory students at the end of the spring semester, the following facts were discovered about Adam's Lunch *AL*, Pizza Tower *PT*, and the Dining Hall *DH*.
 - liked AL but not PT
 liked AL only
 liked AL
 liked PT
 liked DH
 liked PT and AL but not DH
 liked PT and DH

How many liked all three?

A) 37
B) 34
C) 18
D) 0
E) 38

- Ans: D
- 34. In a survey of the dining preferences of 110 dormitory students at the end of the spring semester, the following facts were discovered about *AL*, Pizza Tower *PT*, and the Dining Hall *DH*.
 - 19 liked AL but not PT
 - 10 liked AL only
 - 23 liked AL
 - 42 liked PT
 - 48 liked DH
 - 4 liked PT and AL but not DH
 - 25 liked PT and DH

How many liked only DH?

- A) 23B) 14
- C) 9
- D) 25
- E) 34
- Ans: B

35. Indicate whether the given expression is one or more of the following types of numbers: rational, irrational, integer, natural.

15

- 3
- A) integer
- B) rational
- rational, integer C)
- D) rational, integer, natural
- E) irrational

Ans: D

36. Indicate whether the given expression is one or more of the following types of numbers: rational, irrational, integer, natural.

-1.2290

- A) integer
- B) rational
- C) rational, integer
- D) rational, integer, natural
- E) irrational

Ans: B

37. Indicate whether the given expression is one or more of the following types of numbers: rational, irrational, integer, natural.

3.23

- A) integer
- B) rational
- rational, integer C)
- rational, integer, natural D)
- E) irrational
- Ans: B
- 38. Indicate whether the given expression is one or more of the following types of numbers: rational, irrational, integer, natural.

 $\frac{1}{4}$

- A) integer
- B) rational
- rational, integer C)
- rational, integer, natural D)
- E) irrational

Ans: B

39. Which property of the real numbers is illustrated in this equality?

 $7(3\cdot 2) = (7\cdot 3)2$

- A) additive identity
- B) multiplicative inverse
- C) associative
- D) multiplicative identity
- E) commutative

Ans: C

40. Which property of the real numbers is illustrated in this equality?

9 + 0 = 9

- A) additive identity
- B) multiplicative inverse
- C) associative
- D) multiplicative identity
- E) commutative

Ans: A

41. Which property of the real numbers is illustrated in this equality?

$$\left(\frac{2}{4}\right)\left(\frac{4}{2}\right) =$$

A) additive identity

1

- B) multiplicative inverse
- C) additive inverse
- D) multiplicative identity
- E) associative

Ans: B

42. Choose the proper symbol <, =, or > to replace \Box .

 $\pi \Box 3.14$ A) $\pi < 3.14$ B) $\pi = 3.14$ C) $\pi > 3.14$ Ans: C

43. Choose the proper symbol $\langle , = , \text{ or } \rangle$ to replace \Box .

0.1111
$$\Box \frac{1}{9}$$

A) 0.1111 < $\frac{1}{9}$
B) 0.1111 = $\frac{1}{9}$
C) 0.1111 > $\frac{1}{9}$
Ans: A

44. Choose the proper symbol $\langle , = , \text{ or } \rangle$ to replace \Box .

 $\frac{\frac{1}{3} + \frac{1}{5} \Box \frac{8}{15}}{\frac{1}{3} + \frac{1}{5} < \frac{8}{15}}$ A) $\frac{1}{3} + \frac{1}{5} < \frac{8}{15}$ B) $\frac{1}{3} + \frac{1}{5} = \frac{8}{15}$ C) $\frac{1}{3} + \frac{1}{5} > \frac{8}{15}$ Ans: B

45. Choose the proper symbol $<, =, \text{ or } > \text{ to replace } \square$.

$$|-3-7| \Box |-3|+|7|$$
A) $|-3-7| < |-3|+|7|$
B) $|-3-7| < |-3|+|7|$
C) $|-3-7| = |-3|+|7|$
Ans: B

46. Evaluate the following expression.

$$(-2)^2 + 10.5$$

A) 46
B) 70
C) 54
D) 30
E) -46
Ans: C

47. Evaluate the following expression.

$6 + 4^2$	
2	
A)	5
B)	7
C)	14
D)	10
E)	11
Ans:	Е

48. Evaluate the following expression.

$(8+2)^2$	
2	
A)	50
B)	34
C)	33
D)	6
E)	42
Ans:	А

49. Evaluate the following expression.

(-6)	(-2)-(-2)(3)
	-2+5
A)	-6
B)	9
C)	6
D)	2
E)	-2
Ans:	С

50. Evaluate the following expression.

<u> </u>	5-16
1	-3^{2}
A)	$\frac{17}{16}$
B)	$\frac{3}{16}$
C)	$16 \\ -15$
D)	$\frac{16}{3}$
E)	16 _ <u>17</u>
Ans:	16 D

51. Evaluate the following expression.

5^2-3	3(-3)(-2)
2	$-2^2 \div 4$
A)	86
B)	7
C)	-14
D)	43
E)	-86
Ans:	В

52. Evaluate the following expression.

 $\frac{4-6(3-5)}{(-2)^2-2^2+2}$ A) -4 B) 8 C) -2 D) 2 E) 7 Ans: B

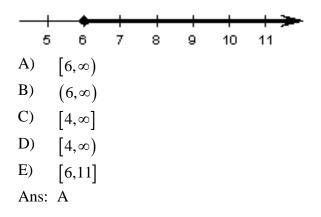
- 53. Choose the interval which corresponds to $x \ge 9$.
 - A) $(9,\infty)$ B) $(-\infty,9)$ C) $(-\infty,\infty)$ D) $(-\infty,9]$ E) $[9,\infty)$ Ans: E
- 54. Express the inequality using interval notation.
 - $\begin{array}{l} -6 \le x \le 2 \\ A) & (-6,2] \\ B) & (-\infty,2) \\ C) & [-6,\infty) \\ D) & [-6,2] \\ E) & [-6,2] \\ Ans: D \end{array}$
- 55. Name the type of interval expressed in the inequality.

 $-4 \le x \le 5$ A) closed interval

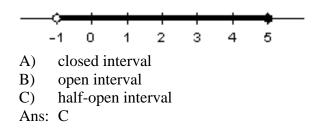
- B) open interval
- C) half-open interval

Ans: A

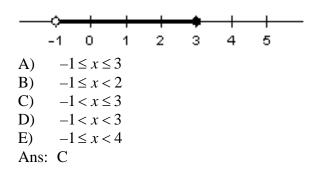
Harshbarger/Reynolds, Mathematical Applications for the Management, Life, and Social Sciences, 10e 56. Express the graph below using interval notation.

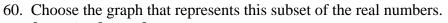


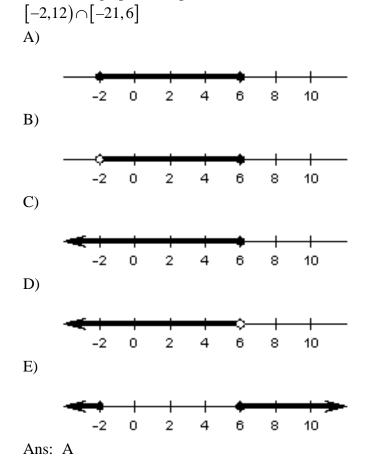
57. Name the type of interval shown in the graph below.



- 58. Choose the inequality that describes the interval below. $(3,\infty)$
 - A) x < 3B) $x \le 3$ C) -3 < x < 3D) x > 3E) $x \ge 3$ Ans: D
- 59. Choose the inequality that describes the graph below.

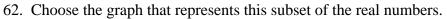


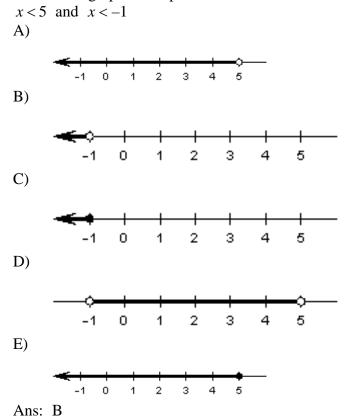




61. Choose the correct interval notation for this subset of the real numbers.

$$\begin{array}{l} [-4,16) \cap [-14,9] \\ A) & [-14,9] \\ B) & [-4,9] \\ C) & [-4,16] \\ D) & [-14,16] \\ E) & \varnothing \\ Ans: & B \end{array}$$



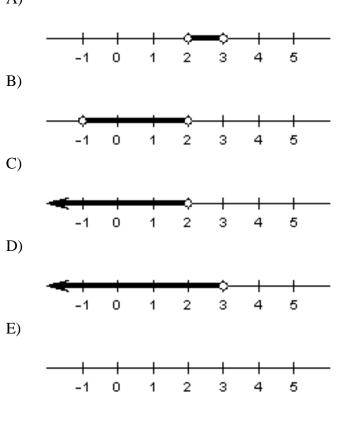


- 63. Choose the correct interval notation for this subset of the real numbers. x < 7 and x < -4
 - A) $(-\infty, 7]$ B) $(-\infty, -4]$ C) $(-\infty, 7)$ D) $(-\infty, -4)$ E) \varnothing Ans: D

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64. Choose the graph that represents this subset of the real numbers.

 $(-\infty, 3) \cup (-1, 2)$ A)



This graph represents the empty set. Ans: D

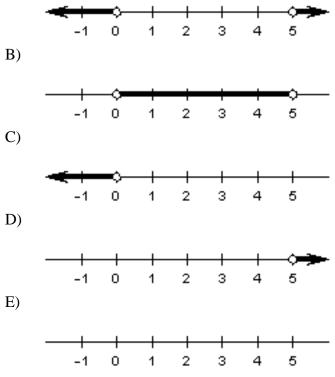
65. Choose the correct interval notation for this subset of the real numbers.

$$(-\infty, 6) \cup (-1, 4)$$

- A) $(-\infty, 6)$
- B) $(-\infty, 4)$
- C) (-1, 6)
- D) (-1,4)
- E) Ø
- Ans: A

66. Choose the graph that represents this subset of the real numbers.

x > 5 and x < 0A)



This graph represents the empty set. Ans: A

67. Use your calculator to approximate the following expression.

 $\begin{array}{c} \underline{54.858}\\ 155.73\\ A) & 2.83878377\\ B) & 0.35226353\\ C) & 3.52263533\\ D) & 0.03522635\\ E) & 28.3878377\\ \end{array}$

Ans: B

68. Use your calculator to approximate the following expression. $(2.84)^7$

- A) 524.69876294
- B) 4232.01034237
- C) 251.23401195
- D) 1490.14448675
- E) 184.75308554

Ans: D

Harshbarger/Reynolds, Mathematical Applications for the Management, Life, and Social Sciences, 10e 69. Use your calculator to approximate the following expression.

$$65\left(\frac{(1.09)^9 - 4}{0.07}\right)$$
A) -1697.52766909
B) -3573.11265112
C) 1756.75804520
D) 1959.61518805
E) 84.03020602
Ans: A

- 70. The approximate percent *P* of average income used to pay federal, state, and local taxes is given by P = 0.24627t + 25.96473, where *t* is the number of years after 1950. Which *t*-value represents the year 1985?
 - A) 20
 - B) 35
 - C) 25
 - D) 30
 - E) 40
 - Ans: B
- 71. The approximate percent *P* of average income used to pay federal, state, and local taxes is given by P = 0.24627t + 25.96473, where *t* is the number of years after 1950. The actual tax load for 1980 was 33.8%. What does the formula give as an approximation? Round your answer to one decimal place.
 - A) 18.6%
 - B) 42.1%
 - C) 33.4%
 - D) 13.8%
 - E) 42.9%
 - Ans: C
- 72. The approximate percent *P* of average income used to pay federal, state, and local taxes is given by P = 0.24627t + 25.96473, where *t* is the number of years after 1950. Approximate the tax load for year 2012. Round your answer to one decimal place.
 - A) 50.1%
 - B) 41.3%
 - C) 41.2%
 - D) 52.1%
 - E) 21.7%
 - Ans: C

- 73. From data adapted from the National Center for Health Statistics, the height *H* in inches and age *A* in years for boys between 4 and 16 years of age are related according to H = 2.65A + 34.50. To account for normal variability among boys, normal height for a given age is $\pm 5\%$ of the height obtained from the equation. Find the inequality which represents the normal height range for a boy who is 13.75 years old. Round your answer to two decimal places.
 - A) $70.94 \le H \le 74.48$ B) $67.39 \le H \le 70.94$ C) $67.39 \le H \le 74.48$ D) $67.39 \le H \le 78.21$
 - E) $64.02 \le H \le 74.48$
 - Ans: C
- 74. Based on data adapted from the National Center for Health Statistics, the height *H* in inches and age *A* in years for boys between 4 and 16 years of age are related according to: H = 2.56A + 29.95. To account for normal variability among boys, normal height for a given age is $\pm 5\%$ of the height obtained from the equation. Find the inequality which represents the normal height range for a boy who is 8.25 years old. Round your answer to two decimal places.
 - A) $48.52 \le H \le 53.62$
 - B) $48.52 \le H \le 51.07$
 - C) $51.07 \le H \le 53.62$
 - D) $48.52 \le H \le 56.30$
 - E) $46.09 \le H \le 53.62$

Ans: A