

is right:

for check if the inverse function That you found is right:

for (f(x)) = X X X C D(P)

If it's Not merce function That you found

· How to find $f^{-1}(x)$?

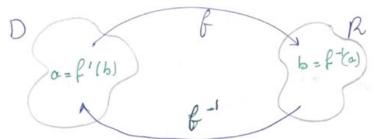
a-solve for x:

b-inter change x by y and y by xc-Replace y by $f^{-1}(x)$

· Theorem: Given a 1-1 function:

 $f: D \rightarrow R$ with f' exists and never zero on D(F)Then $f^{-1}: R \rightarrow D$ is diff s.+ on R

where: $-(f^{-1})^{\circ}(b) = \frac{1}{f^{\circ}(f^{-1}(b))}$ $\frac{df^{-1}}{dx} = \frac{1}{\frac{df}{dx} = f^{-1}(b)}$



f:D-R

P-1.R→D (P-1)=P→D

7.21 Natural logarithms et: defined by: In X = Sit dt , X>0

D: 10.00)

R: (-a. a)

Notice that: - lim lnx=0

lim Inx = -00

Differentiation of Mained legarithm

1- If girpin diff and never zero and y = lng(x)

Then $y = \frac{dx}{dx} = \frac{g'(x)}{g(x)}$

2- and $\int g(x) = \ln |g(x)| + C$ (so the number we use Absolute value That's why we use Absolute value

. Proprietes of Natural Logarithm for a > 0 & b > 0 :-

1- ln (a)(b) = ln a + ln b

 $2 - \ln \frac{(a)}{(b)} = \ln a - \ln b$

 $3-\ln a^{r} = r\ln a$ $4-\ln \frac{1}{a} = \ln 1-\ln a = 0-\ln a = -\ln a$

UPLOADED BY AHMAD JUNDI * Natural logarethm and trigonometric functions :-1- Stanxdx = In |Secx|+C=In |Cosx+C 2- Scot x dx = -ln | Cscx + C = ln | sin x | + C 3. Secx dx = ln /secx + tanx/ +c 4- JCSCX dx=-h | CSCX + Cotx 1+C Why? (good question:P) · to prove it :-1- $\int tan x dx = \int \frac{\sin x}{\cos x} dx = \int \frac{(\cos x)}{(\cos x)} dx$ (COSX) = Sinx VI Remark: - In logarithms - lnx = lnx (it is proved In the first page 2- Scot x dx = Sonx dx = Sinx dx (Sin X) z COSX) = ln |sinx1 + C =- ln Csal + C * Don't forget the Abs. valu . 3- Sec x dx = Sec x (secx + banx) dx = Sec x + banxsecx dx + Sec x = S(tanx) + (Secx) dx (tan X) = Sec 2 X (Sec X) = tan x sec x = In tanx + Secx +C

$$4-\int CSC \times dx = \int \underbrace{CSC \times \left(CSC \times + CO + X\right)}_{CSC \times + CO + X} dx$$

$$(\cot x)^2 - \csc^2 x$$

$$= \int -(\cot x)^2 + (\csc x)$$

$$(\csc x)^2 - \csc x \cot x$$

$$= \int -(\cot x)^2 + (\csc x)$$

$$(\csc x)^2 - \csc x \cot x$$

7.3: Exponensial function

$$f(x) = e^{x} = \ln^{-1} x$$

$$N: (-\infty, \infty)$$

$$D: (-\infty, \infty)$$
 $R: (0, \infty)$

· Remembrer:

. Proprieties of ex

Propheties of E:

$$1 - e^{-1} = X + X > 0$$
 $3 - e^{-1} = e^{(X_1 + X_2)} = e^{(X_1 + X_2)} = e^{-1} =$

. Differentiation and integration of ex 1- If y(x) = a u(x) where are and unisolite

$$\frac{1-17}{1 \text{ hen }} y(x) = a u(x) \ln a u(x)$$

I hen
$$g(x)$$
 = $\alpha^{u(x)} + C$
 $2 - \int a^{u(x)} \ln a \ u'(x) \ dx$ = $\alpha^{u(x)} + C$

· Natural logarithm is a special case of General Ingrithmic function (G. L.f.) Georvial: y(x) = log u(x) = ln u(x)a>0 a = 1 Natural: α (the base) = . e so ln $e = 1 \rightarrow \log u(x) = \ln u(x)$ · Diff + integration of (G.L.f.) • If $y(x) = \log u(x) \implies y'(x) = \frac{1}{\ln a} \left(\frac{u'(x)}{u(x)} \right)$ and $\int \frac{u'(x)}{u(x)} \frac{1}{\ln a} dx = \log u(x) + C$ · Droprieties :-1- loga x = X +x = why?: - loga x = lna x x hazx 2-a log x = X + X>0 3-logxy = logx +logy 4-log & = log x - log y 5-log y = log 1 - log y = 0-log y = -log y 6-logx - ylogx = y(lnx)

