

27] Suppose that the total ~~cost~~ revenue is $R(x) = 50x$, and the total cost is $C(x) = 1900 + 30x + 0.01x^2$

a) Find the profit from the production and sale of 500 units

$$\begin{aligned} P(x) &= R(x) - C(x) \\ &= 50x - 1900 - 30x - 0.01x^2 \\ &= 20x - 0.01x^2 - 1900 \end{aligned}$$

at $x = 500$

$$\begin{aligned} P(500) &= 20(500) - 0.01(500)^2 - 1900 \\ &= 5600 \text{ \$} \end{aligned}$$

b) Find the marginal profit.

$$\begin{aligned} MP &= P'(x) = 20 - 0.01(2)x \\ &= 20 - 0.02x \end{aligned}$$

c) Find ~~the~~ MP at $x = 500$ and explain what it predicts.

$$MP(500) = P'(500) = 20 - 0.02(500)$$

$$= 20 - 10$$

~~the~~ the profit will increase by about \$10 if a 501st unit is sold