

**(Q1)** (a) 5

- (b) Not possible.
- (c) Not possible.
- (d) 5

**(Q2)** (a) Take  $t_0 = x_0 - h$ ,  $t_1 = x_0$ ,  $t_2 = x_0 + 3h$  $f(t) = P_2(t) + E_2(t)$ , where  $P_2(t)$  is Newton's polynomial $f''(x_0) = f''(t_1) = P_2''(t_1) + E_2''(t_1)$ . Continue, you'd get the formula.(b) Take  $t_0 = x_0 - h$ ,  $t_1 = x_0$ ,  $t_2 = x_0 + 3h$  $f(t) = P_2(t) + E_2(t)$ , where  $P_2(t)$  is Lagrange's polynomial $f''(x_0) = f''(t_1) = P_2''(t_1) + E_2''(t_1)$ . Continue, you'd get the formula.(c)  $f_{-1} = \dots$  $3f_{-1} = \dots$  $f_3 = \dots$  $3f_{-1} + f_3 = \dots$  Continue, you'd get the formula.**(Q3)** (a) Take  $t_0 = x_0 - 4h$ ,  $t_1 = x_0 + h$  $f(t) = P_1(t) + E_1(t)$ , where  $P_1(t)$  is Newton's polynomial $f'(x_0) = P_1'(x_0) + E_1'(x_0)$ . Continue, you'd get the formula:  $f'(x_0) = \frac{f_1 - f_{-4}}{5h} + \frac{3hf''(c)}{2}$ (b) Take  $t_0 = x_0 - 4h$ ,  $t_1 = x_0 + h$  $f(t) = P_1(t) + E_1(t)$ , where  $P_1(t)$  is Lagrange's polynomial $f'(x_0) = P_1'(x_0) + E_1'(x_0)$ . Continue, you'd get the formula:  $f'(x_0) = \frac{f_1 - f_{-4}}{5h} + \frac{3hf''(c)}{2}$ (c)  $f_1 = \dots$  $f_{-4} = \dots$  $f_1 - f_{-4} = \dots$  Continue, you'd get the formula:  $f'(x_0) = \frac{f_1 - f_{-4}}{5h} + \frac{3hf''(c)}{2}$ **(Q4)**  $A = 6$ ,  $B = 15$ **(Q5)** Optimal  $h = 0.121951859$ **(Q6)** (a) + (b) + (c) Try!

(d) 
$$h = \left(\frac{\epsilon}{4M}\right)^{1/3}$$

(e)  $f'(4.4) \approx 3.325$