

Birzeit University  
Department of Physics  
Mathematical Physics, Phys330  
Fall 2020  
Homework 5: Due date Dec. 15th 2020

1. Solve the following Problem in spherical coordinates, by separation of variables and choose the appropriate values of the constants to obtain a physical solution. Show that the equation for  $\theta$  can reproduce the Legendre equation and the associated Legendre equation.

$$\nabla^2 \phi(r, \theta, \phi) = 0$$

2. Using the generating function of the Legendre polynomial obtain a general expression for  $P_n(0)$
3. Prove all parts of equation 5.8 page 570 of the book
4. Find a general expression for the following integrals:

$$\int_{-1}^1 x P_l(x) P_n(x) dx$$
$$\int_{-1}^1 x^2 P_l(x) P_n(x) dx$$

5. Dirac delta function is defined as:

$$\delta(x - a) = \begin{cases} 0 & \text{if } x \neq a \\ \infty & \text{if } x = a \end{cases}$$
$$\int_{x_1}^{x_2} f(x) \delta(x - a) dx = f(a) \quad \text{if } a \in (x_1, x_2)$$

write  $\delta(x - a)$  as a Fourier series.