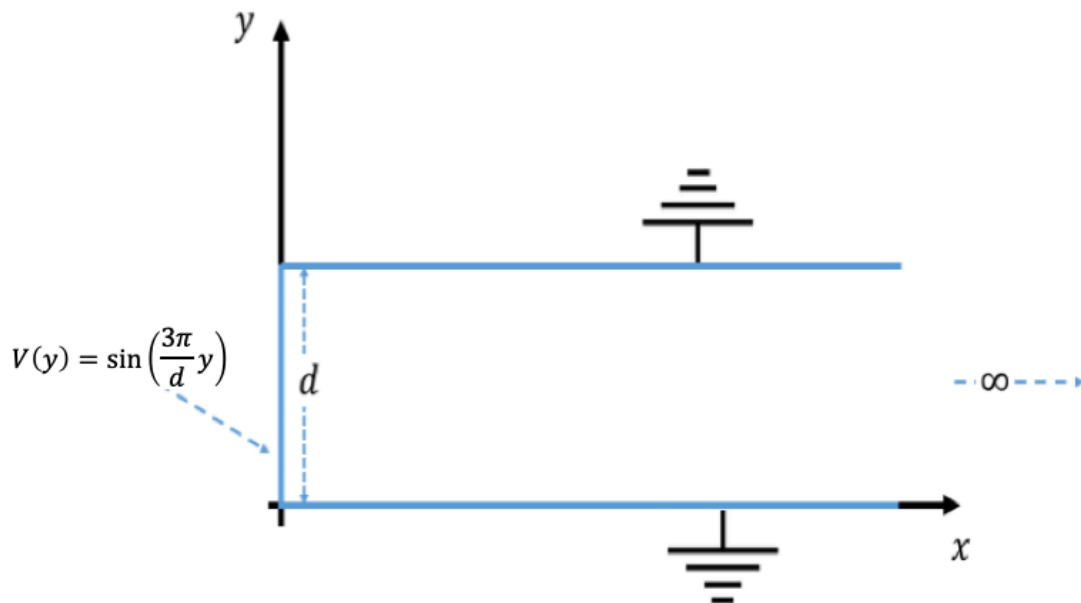


Phys331/Midterm Exam Spring 2020/2021

- 1) (10%) If Ω is a sphere of radius R that is centered around the origin. Use appropriate functions and theorems you learned to evaluate

$$\int_{\Omega} \left(\frac{\vec{r}}{r^3} \right) \vec{\nabla} \left(\frac{r^4 - R^4}{r^5 + 7r^3 + 2} \right) d\tau$$

- 2) An infinitely long 2-D slot has a width d . The walls are conductors that held at fixed potentials as shown in the figure.



- a. (20%) Determine the electric potential inside the slot.
- b. (5%) If a positive charge q is placed at the coordinates $(d, \frac{d}{2}, 0)$, find the force (\vec{F}) on q .

- 3) If the linear charge density of a circular ring of radius R that is placed in the xy –plane and centered around the origin is given by

$$\lambda(\phi) = \lambda_0 \cos^3 \phi$$

- a. (3%) Write the linear charge density as a volume charge density in cylindrical coordinates.
 - b. (3) Calculate the total charge (Q) on the ring.
 - c. (9%) Calculate the electric dipole moment (\vec{p}) of the ring.
- 4) (10%) If \vec{c} is a constant vector, find the charge density that give rise to the electric field $\vec{E} = (\vec{c} \cdot \vec{r})\vec{c}$.
- 5) A conducting spherical shell of radius R and zero thickness is held at a potential $V(\theta) = V_0 \sin^4(\theta)$.
- a. (20%) Determine the potential produced by the sphere everywhere.
 - b. (10%) Determine the electric field produced by the sphere everywhere.
 - c. (10%) Determine the surface charge density on the sphere.