

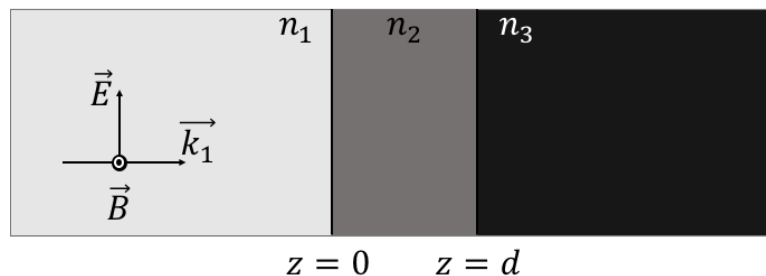
Phys332/midterm exam

Due on Saturday 28/11/2020 at 10:00 am

1. (20%) Find self-inductance per unit length of two straight parallel wires of the radii R_1 and R_2 with the distance $d > (R_1 + R_2)$ between their axes. The current I passing through the wires is oppositely directed.

2. If the electric field component of two electromagnetic waves is given by (i) $\vec{E} = E_0 e^{i(kz - \omega t)} \hat{x} + E_1 e^{i(kz - \omega t + \phi)} \hat{x}$ and (ii) $\vec{E} = E_0 e^{i(kz - \omega t)} \hat{x} + E_1 e^{i(kz - \omega t + \phi)} \hat{y}$.
 - a. (8%) Find the magnetic field component of each wave.
 - b. (8%) Calculate the Poynting vector for each electromagnetic wave.
 - c. (8%) Calculate the Maxwell stress tensor for each electromagnetic wave.
 - d. (8%) Calculate the average momentum density for each electromagnetic wave.

3. An electromagnetic plane wave is incident perpendicular to a layered interface as shown in the figure below. The indices of refraction of the three media is $n_1 = i_2, n_2 = 0.1(10i_1 + i_2)$ and $n_3 = 0.1(20i_1 + i_7)$, while the permeability of all three regions is μ_0 . The thickness of the intermediate layer is d . Each of the other media is semi-infinite. i_1, i_2 and i_7 are obtained from your student id number: e.g. If ID #: 1101534, then $i_1 = 1, i_2 = 1, i_3 = 0, i_4 = 1, i_5 = 5, i_6 = 3$ and $i_7 = 4$.



- a. (20%) Compute $\left(\frac{E_{0T}}{E_{0I}}\right)^2$, the ratio between the incident electric field in medium 1 and the transmitted electric field in medium 3.
- b. (8%) For which value of d , $\left(\frac{E_{0T}}{E_{0I}}\right)^2$ is the smallest.

4. A constant current I is maintained within a circular wire of radius a that fixed in the xy -plane and centered at the origin. Another circular wire of radius b and resistance R is centered on and is normal to the z axis is moved by an applied force along the z -axis at constant velocity v such that its center is located at $z = vt$. Assuming $b \ll a$,
- (10%) estimate the current in the moving wire as function of time.
 - (10%) estimate the force required to keep the ring moving at constant velocity as function of time.

