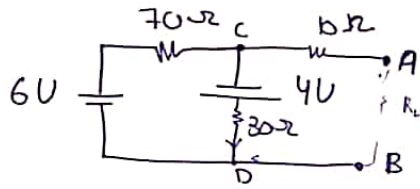
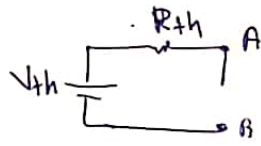


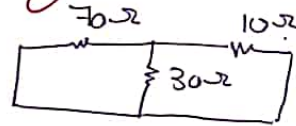
3



(a)



(c) to find  $R_{th} \Rightarrow$



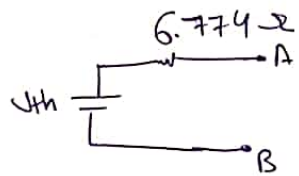
~~$(70 \parallel 30) + 10$~~

~~$\frac{(70 \cdot 30)}{(70 + 30)} + 10 = 21 + 10 = 31 \Omega$~~

$\frac{1}{R} = \frac{1}{70} + \frac{1}{30} + \frac{1}{10}$

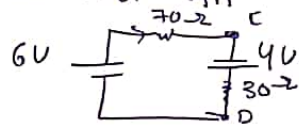
$\frac{1}{R} = 0.1476$

$R_{th} = 6.774 \Omega$



(b) to find  $V_{th}$

$V_{th} = V_{AB} = V_{CD} - V_{10\Omega}$



$I_{short} = \frac{6 + 4}{70 + 30}$

$I_{short} = \frac{10}{100} = 0.1 \text{ Ampere}$

~~$V_{th} = 4V - (30\Omega) I_{short}$   
 $= 4 - 30(0.1)$   
 $= 4 - 3$   
 $V_{th} = 1V$~~

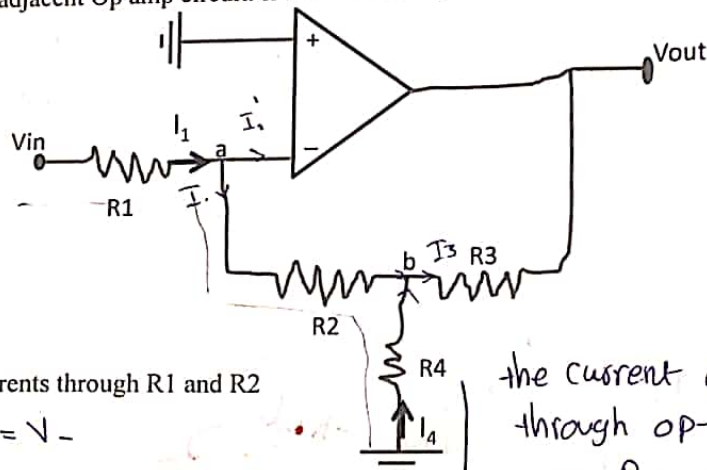
(d)



$I_{AR} = \frac{V_{th}}{R_{th} + R_L} = \frac{1}{6.774 + 20} = \frac{1}{26.774} = (0.037 \text{ A})$

$V_{RL} = I_{RL} \times R_L = 0.037 \times 20 = 0.74 \text{ V}$

2) In the adjacent Op amp circuit. If  $R_1=R_2=R_3=R$ , Find:



a) The currents through  $R_1$  and  $R_2$

$$V_+ = 0 = V_-$$

$$V_{in} - V_{R_1} = V_- = 0$$

$$V_{in} = I_1 R_1 = I_1 R \Rightarrow I_1 = \frac{V_{in}}{R}$$

the current doesn't pass through op-amp so  $I_1' = 0$  as  $R_{op-amp} = \infty$

$\Rightarrow$  current pass through  $R$  equals to current through  $R_1 = \frac{V_{in}}{R}$

b) The voltages at points a and b

$$V_a = V_{in} - V_{R_1} = V_- = 0$$

$$V_b = V_{R_4} - 0 = V_{R_4} + I_4 R_4$$

$$V_a - I_2 R_2 - V_b + V_{R_4} = 0 \quad V_b = -V_{R_4} = -I_4 R_4$$

c) The current through  $R_4$

$$V_a - I_1 R_2 + I_4 R_4 = 0$$

$$V_a = 0 \Rightarrow I_4 R_4 + I_1 R_2$$

$$I_4 = \frac{I_1 R_2}{R_4} = \frac{V_{in}}{R} \frac{R}{R_4} = \frac{V_{in}}{R_4}$$

d) From a, b, and c, find the gain in the circuit in terms of  $R$  and  $R_4$

$$I_1 = I_2 + I_3 \quad I_3 = I_1 + I_4 = \frac{V_{in}}{R} + \frac{V_{in}}{R_4} = V_{in} \left( \frac{1}{R} + \frac{1}{R_4} \right)$$

$$V_{out} + I_3 R_3 + I_4 R_4 = 0$$

$$V_{out} = -(I_3 R + I_4 R)$$

$$= - \left( V_{in} R \left( \frac{1}{R} + \frac{1}{R_4} \right) + \frac{V_{in}}{R_4} R_4 \right)$$

$$= -V_{in} \left( 1 + \frac{R}{R_4} + \frac{R}{R_4} \right) = -V_{in} \left( 2 + \frac{R}{R_4} \right)$$

$$G = \frac{V_{out}}{V_{in}} = - \left( 2 + \frac{R}{R_4} \right)$$

4. If  $V_0 = 10V$ ,  $R_1 = R_2 = 10\text{ k}\Omega$ . Find the current in  $R_2$  when  $R_L$  a) goes to infinity

$$R_L \rightarrow \infty$$

$$I' = 0$$

$$\Rightarrow V_0 - I R_1 - I R_2 = 0$$

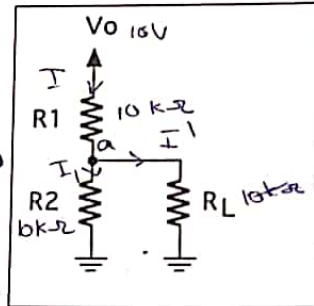
$$I = \frac{V_0}{R_1 + R_2}$$

$$= \frac{10}{10 + 10}$$

$$\times 10^3$$

$$= \frac{10 \times 10^3}{20} = 0.5 \times 10^{-3} \text{ A}$$

$$= 0.5 \text{ mA}$$



- b) goes to zero

$$R_L \rightarrow 0 \Rightarrow I' = I$$

No current will pass through  $R_2$

$$I_{R_2} = 0$$

- c)  $R_L = 5\text{ k}\Omega$

$$V_{R_L} = V_{R_2} = V_0 - I R_1$$

$$I' R_L = I R_2$$

$$I' (5 \times 10^3) = I (10 \times 10^3)$$

$$I' = 2 I_1$$

$$I' + I_1 = I$$

$$2 I_1 + I_1 = I \quad I = 3 I_1$$

$$V_0 - I R_1 = V_{R_2}$$

$$V_0 - 3 I_1 (10 \times 10^3) = I_1 (10 \times 10^3)$$

$$V_0 = 4 I_1 (10 \times 10^3)$$

$$I_1 = \frac{1}{4} \times 10^{-3} \text{ A}$$

$$I_1 = 0.25 \text{ mA}$$

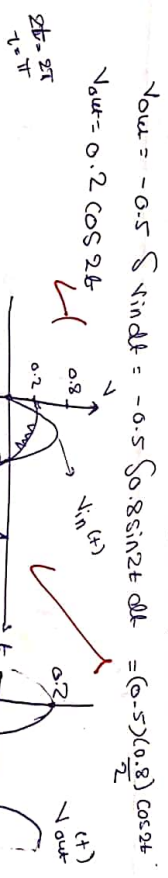
1) The drawing shows an amplifier whose input voltage is connected to the inverting side through a capacitor with capacitance C and a feedback resistance R. If  $R=10k\Omega$  and  $C=50\mu F$ . Find:

a) The relation between the output and input voltages

$V_{in} - V_c = V_- = 0 \Rightarrow V_{in} - V_c = 0$   
 $V_{out} + I_f R = V_- = 0$   
 $I_f = \frac{V_{in} - V_c}{C} = \frac{V_{in}}{C}$   
 $V_{out} = -I_f R = -R \frac{V_{in}}{C} = -R C S V_{in} \sin \omega t$   
 $V_{out} = -0.5 \sin \omega t$   
 $R = 10k\Omega, C = 50\mu F$   
 $R C = 0.5$



b) If the amplifier is powered by + and -10V source and the input voltage is  $V_{in} = 0.8 \sin 2t$ . Draw the input and output voltages as functions of time and show the actual values. Show at least two periods in the drawing. Use back, if needed.



c) Find the input impedance of the circuit

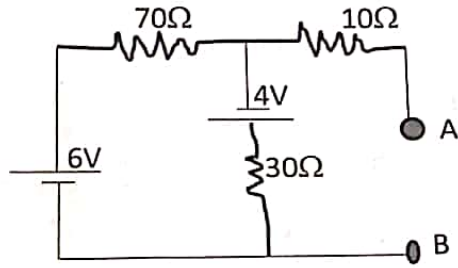
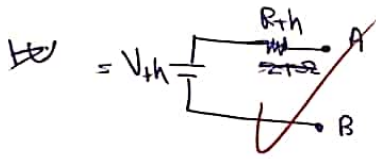
$Z_c = \frac{1}{i\omega C}$   
 $Z_R = R$   
 Input impedance =  $Z_c + Z_R$   
 $= \frac{1}{i\omega C} + R$   
 $| \text{input impedance} | = \sqrt{\frac{1}{\omega^2 C^2} + R^2}$



the op-amp have  $\infty$  input impedance.

3) In the adjacent circuit.

A) Draw the Thevenin's equivalent circuit between points A and B



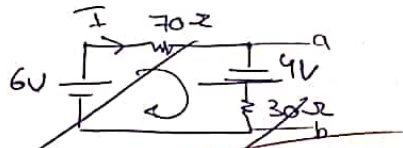
B) Find the Thevenin's equivalent voltage

$$6V - I(70) + 4 - I(30) = 0$$

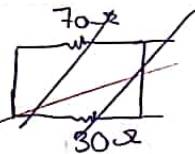
$$I = \frac{10}{70+30} = \frac{10}{100} = 0.1 \text{ A}$$

$$V_{th} = V_{ab} = 4 - I(30) = 4 - (0.1)(30)$$

$$V_{th} = 4 - 3 = 1 \text{ V}$$



C) The Thevenin's equivalent resistance



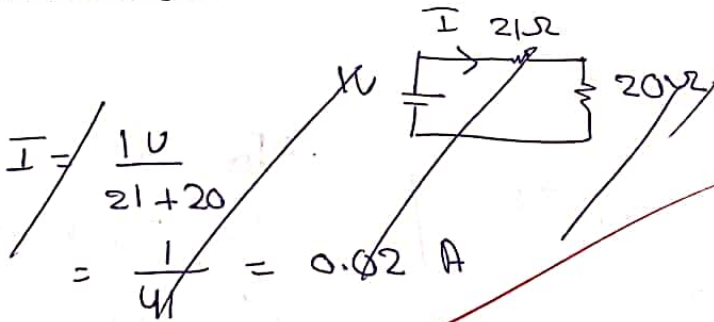
$$\frac{1}{R_{th}} = \frac{1}{70} + \frac{1}{30}$$

$$= \frac{70+30}{70 \times 30}$$

$$= \frac{100}{2100}$$

$$R_{th} = 21 \Omega$$

D) If a load resistor of 20Ω is connected between A and B. Find the voltage across the resistor and the current through it.



$$I = \frac{1 \text{ V}}{21 + 20}$$

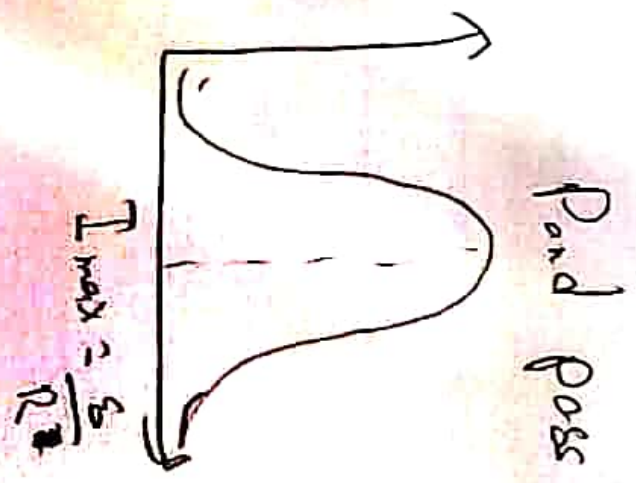
$$= \frac{1}{41} = 0.02 \text{ A}$$



$$V = \frac{1}{\sqrt{1 + (\omega C)^2}}$$

① at high  $\omega \Rightarrow V \approx 0$

at low  $\omega \Rightarrow V \approx 1$



$$\varepsilon = \varepsilon_0 \cos(\omega t) = \varepsilon_0 e^{i\omega t}$$

$$I = \frac{\varepsilon}{Z} = \frac{\varepsilon_0 e^{i\omega t}}{Z}$$

$$I_0 = \frac{\varepsilon_0}{|Z|} = \frac{\varepsilon_0}{\sqrt{Z Z^*}}$$

$$\text{For } Z = R + i\left(\omega L - \frac{1}{\omega C}\right)$$

$$Z^* = R - i\left(\omega L - \frac{1}{\omega C}\right)$$

$$I_0 = \frac{\varepsilon_0}{\sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}}$$

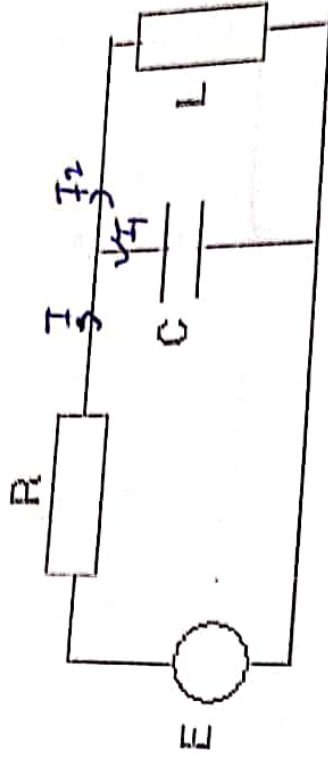
$$Z_R = R$$

$$Z_C = \frac{-j}{\omega C}$$

$$Z_L = j\omega L$$

$$Z_{total} = R + j\omega L + \frac{-j}{\omega C}$$

- Derive an expression for the current passing through R.
- Derive an expression for the phase shift between the input voltage and the current passing through R.
- At what value of  $\omega$  would the current be zero.



$$I = \frac{E \cos(\omega t)}{Z_{eq}} = \frac{E_0 \cos(\omega t)}{Z_{eq}}$$

$$Z_{eq} = \sqrt{R^2 + (\omega L - \frac{1}{\omega C})^2}$$

$$Z_{eq} = \sqrt{R^2 + (\omega L - \frac{1}{\omega C})^2} \quad \phi = \theta$$

