

15/15

Student name: _____

Student ID: _____

1. Write the number of the significant figures in the following numbers:

- a. 0.098050 5
- b. 24300 ± 20 4
- c. 12.02021 7
- d. 0.00021015 5
- e. 3.10278 × 10⁶ 6
- f. 4109.0051 ± 0.0006 8

2. A student measured the radius of a sphere (r) 8 times as follows : 3.31 , 3.41 , 3.26 , 3.20 , 3.44 , 3.35 , 3.25 and 3.43 in cm. Find:

a. The best estimate value of the radius of the sphere. = 3.3325

b. The sample standard deviation in the radius of sphere. s = 0.09

c. The radius of sphere in correct form (r ± Δr).

$$s_m = \frac{s}{\sqrt{n}} = \frac{0.090622}{\sqrt{8}} = 0.03$$

~~r = 3.33 ± 0.09~~ ⇒ r = 3.33 ± 0.03

3. The radius of circle is measured to be (5.337 ± 0.005) cm. Find the area of circle.

$$A = \pi r^2 \Rightarrow \Delta A = 2\pi r \Delta r$$

$$A = \pi r^2 = \pi \times (5.337)^2 = 89.4384 \text{ cm}^2$$

A = 89.44 ± 0.17 cm²

$$\Delta A = 2\pi \times 5.337 \times 0.005 = 0.167 \Rightarrow 0.17$$

4. Find the uncertainty (ΔR) expression for the following calculated values :

a. R(x, y, z) = sin(x³ - yz)

$$\Delta R = \frac{\partial R}{\partial x} \Delta x + \frac{\partial R}{\partial y} \Delta y + \frac{\partial R}{\partial z} \Delta z = \cos(x^3 - yz) \cdot 3x^2 \Delta x + \cos(x^3 - yz) \cdot (-z) \Delta y + \cos(x^3 - yz) \cdot (-y) \Delta z$$

b. R(x, y, z) = $\frac{z^4 y^{\frac{1}{2}}}{x^5}$

~~ΔR = 3x² cos(x³ - yz) Δx + z cos(x³ - yz) Δy + y cos(x³ - yz) Δz~~

ΔR = 3x² cos(x³ - yz) Δx + z cos(x³ - yz) Δy + y cos(x³ - yz) Δz

General Rule
 (b) ΔR = $\frac{\partial R}{\partial x} \Delta x + \frac{\partial R}{\partial y} \Delta y + \frac{\partial R}{\partial z} \Delta z \Rightarrow \left(\frac{\Delta R}{R} = \left(4 \frac{\Delta z}{z} + \frac{1}{2} \frac{\Delta y}{y} + 5 \frac{\Delta x}{x} \right) \times R \right)$

$$\Delta R = \frac{4 \Delta z}{z} \cdot \frac{z^4 y^{\frac{1}{2}}}{x^5} + \frac{1}{2} \frac{\Delta y}{y} \cdot \frac{z^4 y^{\frac{1}{2}}}{x^5} + 5 \frac{\Delta x}{x} \cdot \frac{z^4 y^{\frac{1}{2}}}{x^5} \Rightarrow \Delta R = \frac{4z^3 y^{\frac{1}{2}}}{x^5} \Delta z + \frac{z^4 y^{-\frac{1}{2}}}{2y^{\frac{1}{2}} x^5} \Delta y + \frac{5z^4 y^{\frac{1}{2}}}{x^6} \Delta x$$

12/5/15

Student name: _____

Student ID: _____

1. Write the number of the significant figures in the following numbers:

- a. 0.09050 4 ✓
- b. 243000 ± 200 4 ✓
- c. 12.020210 8 ✓
- d. 0.0002115 4 ✓
- e. 3.102780 × 10⁻⁵ 7 ✓
- f. 4109.051 ± 0.006 7 ✓

~~243000~~
2430 × 10² ± 2 × 10²

2. The radius (r) of right cylinder (الاسطوانة قائمة) is measured to be (3.27 ± 0.05) cm, and its height (L) is founded (8.41 ± 0.03) cm Find the surface area of the cylinder (A ± ΔA).

The surface area = 2 × area of circle + circumference × height

$$= 2 \times \pi r^2 + 2\pi r h = 2 \times \pi (3.27)^2 + 2 \times \pi (3.27)(8.41) = 239.8558$$

$$\frac{\Delta A}{A} = \frac{\Delta r}{r} + \frac{\Delta L}{L}$$

$$\frac{\Delta A}{A} = \frac{\Delta r}{r} + \frac{\Delta L}{L} \Rightarrow \frac{\Delta A}{239.8558} = \frac{0.05}{3.27} + \frac{0.03}{8.41} \Rightarrow \Delta A = 4.52$$

A ± ΔA
240 ± 5 cm²

3. Find the uncertainty (ΔR) expression for the following calculated values:

a. $R(x, y, z) = y^2 + 5 \ln(2x - z^3)$

$$\frac{\Delta R}{R} = \frac{\partial R}{\partial x} \Delta x + \frac{\partial R}{\partial y} \Delta y + \frac{\partial R}{\partial z} \Delta z = 5 \ln(2x - z^3) \times 2 \Delta x + 2y \Delta y + 5 \ln(2x - z^3) \times 3z^2 \Delta z$$

$$\frac{\Delta R}{R} = 10 \ln(2x - z^3) \Delta x + 2y \Delta y + 15 \ln(2x - z^3) z^2 \Delta z \Rightarrow \Delta R = (y^2 + 5 \ln(2x - z^3)) [10 \ln(2x - z^3) \Delta x + 2y \Delta y - 15 \ln(2x - z^3) z^2 \Delta z]$$

~~A = 2πr² + 2πrh~~
~~ΔA = 2πr(Δr + h)~~
~~ΔA/A = Δr/r + h/L~~

b. $R(x, y, z) = \frac{z^6 y^3}{x^3}$

$$\frac{\Delta R}{R} = 6 \frac{\Delta z}{z} + \frac{1}{3} \frac{\Delta y}{y} + 3 \frac{\Delta x}{x}$$

4. Answer the two following question about today's experiment:

- a) What is meaning of "conservation of linear momentum", write the law and explain all symbols in it? it means that the linear momentum is conserved before and after
- b) What are the physical quantity you will measure it today? $P_i = P_f$

mass, velocity/speed

$$m_i v_i = m_f v_f$$

mass initial speed final speed

PHY 111

Quiz 2 sec # 3

10.5

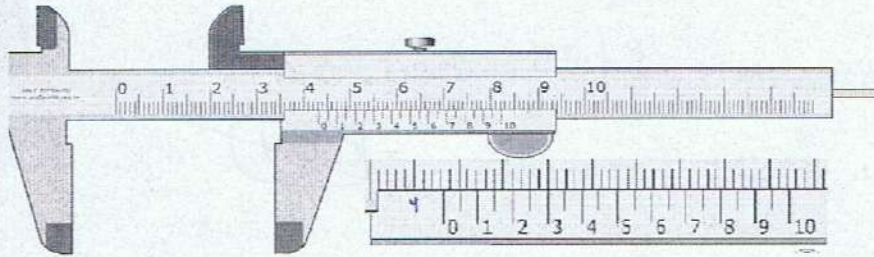
Student name: _____

Student ID: _____

1. Write the reading of the Vernier caliper and Micrometer in mm unit

a.

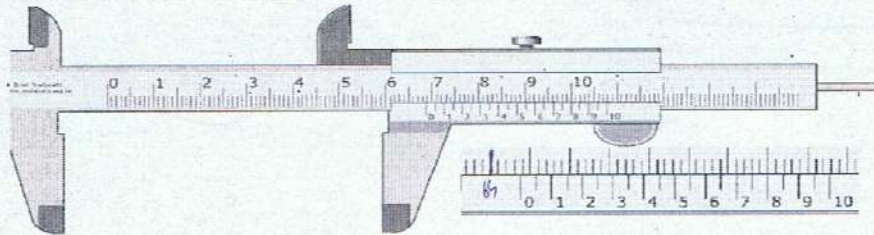
43.30



43.30 mm

b.

68.65

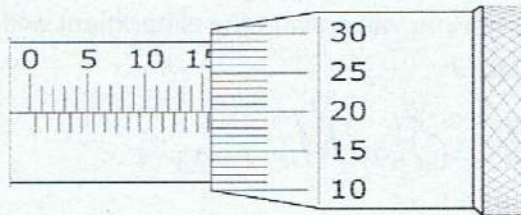


68.65 mm

c.

~~15.50 mm~~ = 15.70 mm
+ 0.20

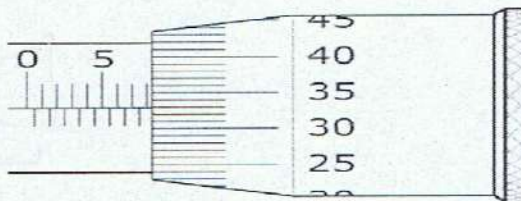
d.



15.70 mm

80 + 0.33

8.33 mm

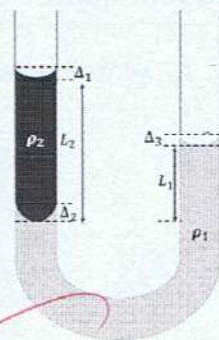


~~8.33 mm~~

$$\Delta L_1 = \Delta_2 + \Delta_3 = 0.4 \text{ cm}$$

$$\Delta L_2 = \Delta_2 + \Delta_1 = 0.5 \text{ cm}$$

2. In the density of liquid experiment, one of students measured $L_1 = 15.8 \text{ cm}$, $L_2 = 18.9 \text{ cm}$, also he estimated the quantities $\Delta_1 = 0.2 \text{ cm}$, $\Delta_2 = 0.3 \text{ cm}$, and $\Delta_3 = 0.1 \text{ cm}$, assuming the density of water $\rho_1 = 1.04 \text{ gm/cm}^3$, Find the density of liquid ρ_2 (with uncertainty)



$$\frac{\rho_1 L_1}{L_2} = \frac{\rho_2 L_2}{L_2} \Rightarrow \rho_2 = \rho_1 \frac{L_1}{L_2} = 1.04 \frac{\text{gm}}{\text{cm}^3} \times \frac{15.8 \text{ cm}}{18.9 \text{ cm}}$$

$$\rho_2 = 0.8694 \text{ gm/cm}^3$$

$$\frac{\Delta \rho_2}{\rho_2} = \frac{\Delta L_1}{L_1} + \frac{\Delta L_2}{L_2} \Rightarrow \Delta \rho_2 = \rho_2 \left(\frac{0.4}{15.8} + \frac{0.5}{18.9} \right) = 0.045$$

$$= 0.04$$

$$\rho_2 \pm \Delta \rho_2$$

$$= 0.87 \pm 0.04 \text{ gm/cm}^3$$

1.5

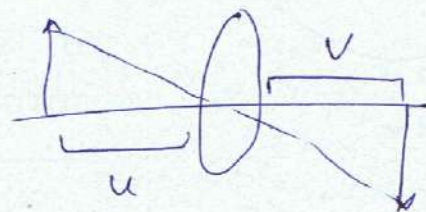
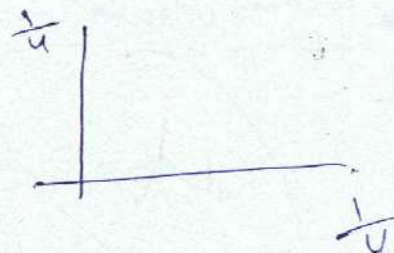
3. In the today's experiment:

- a) What is the aim of the experiment? calculate the focal length and convex length of a lens
- b) What is the graph you will draw in the experiment and what are the quantity will you calculate?

$$\frac{1}{u} \text{ vs } \frac{1}{v}$$

the quantities are

u, v

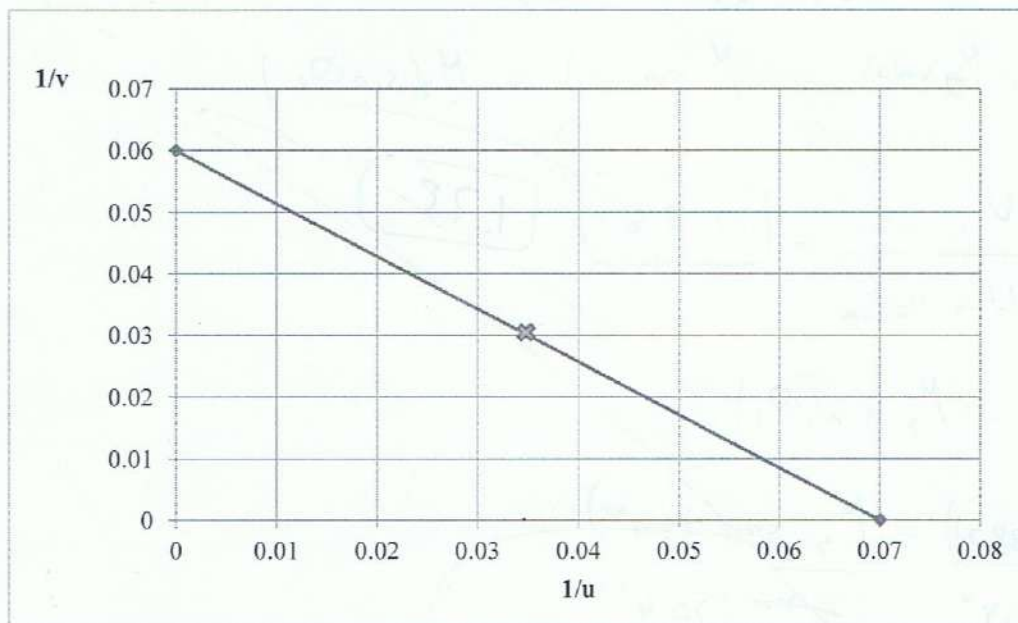


7/10 + 1

Student name: _____

Student ID: _____

1. Consider the following graph of $\frac{1}{v}$ vs $\frac{1}{u}$ from the focal length of convex lens experiment, and let $\Delta v = \Delta u = 0.16 \text{ cm}$, what is the focal length of the lens ($f \pm \Delta f$)?



$\Delta u = \Delta v = 0.16 \text{ cm}$

take the x-intercept $\Rightarrow \frac{1}{f} = \frac{1}{u} + \frac{1}{v} \Rightarrow \frac{1}{f} = 0.07 \text{ cm} \Rightarrow f = 14.286 \text{ cm}$

take the y-intercept $\Rightarrow \frac{1}{f} = \frac{1}{u} + \frac{1}{v} \Rightarrow \frac{1}{f} = 0.06 \text{ cm} = 16.666 \text{ cm}$

$\bar{f} = \frac{f_1 + f_2}{2} = 15.476 \text{ cm}$

$\frac{\Delta f}{f^2} = \frac{\Delta u}{u^2} + \frac{\Delta v}{v^2} \Rightarrow \frac{\Delta f}{(\bar{f})^2} = \frac{0.16}{u^2} + \frac{0.16}{v^2}$

$\Rightarrow \Delta f = 0.0814 \approx 0.08 \text{ cm}$

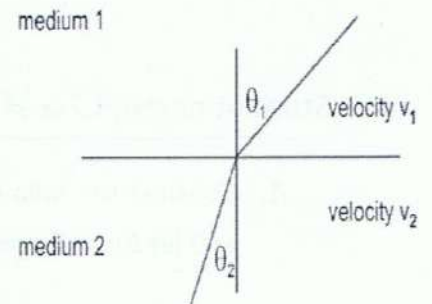
$f \pm \Delta f \Rightarrow 15.48 \pm 0.08 \text{ cm}$

$(\frac{1}{u}, \frac{1}{v}) = (0.035, 0.03) \text{ cm}$
 $(u, v) = (28.57, 33.33) \text{ cm}$

2. The speed of light in medium 1 (v_1) is 225000 km/sec, let $\theta_1 = 38.7^\circ$, $\theta_2 = 20.4^\circ$ and using the speed of light in vacuum $c = 300000$ km/sec,

Find

- The refraction indices of medium 1 and medium 2?
- The speed of light in medium 2 (v_2) in km/sec unit?



$$U_{\text{in medium}} = 225000 \text{ km/sec} \quad \theta_1 = 38.7^\circ$$

$$U_{\text{in vacuum}} = 300000 \text{ km/sec} \quad \theta_2 = 20.4^\circ$$

$$M_1 \sin(\theta_1) = M_2 \sin(\theta_2) \Rightarrow M_1 \sin(38.7^\circ) = M_2 \sin(20.4^\circ)$$

$$M_{\text{medium 1}} = \frac{U_{\text{in vacuum}}}{U_{\text{in medium}}} = \boxed{0.75} \quad \boxed{1.33}$$

$$M_1 \sin(\theta_1) = M_2 \sin(\theta_2)$$

$$0.75 \frac{\sin(38.7^\circ)}{\sin(20.4^\circ)} = M_2 \frac{\sin(20.4^\circ)}{\sin(20.4^\circ)}$$

$$\boxed{M_2 = 1.345} = 2.385$$

$$M_{\text{medium 2}} = \frac{U_{\text{in medium 2}}}{U_{\text{in vacuum}}} \Rightarrow U = M U_{\text{vacuum}}$$

$$\boxed{403588.2 \text{ km/sec}}$$

$$125751.615$$