

Birzeit University  
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EDM

# Introduction

1- current EDMs use infrared, light, laser light or microwaves.

2- microwaves systems use a receiver/transmitter at both ends of the measured line whereas infrared and laser systems utilize a transmitter at one end of the measured line and a reflecting prism at the other end.

# Basic principle of electronic distance measurements (EDMs)

1- Light wave is travelling along x-axis with a velocity of  $299792.5 \pm 0.4$  km/s

2- The frequency wave is the time taken for one complete length

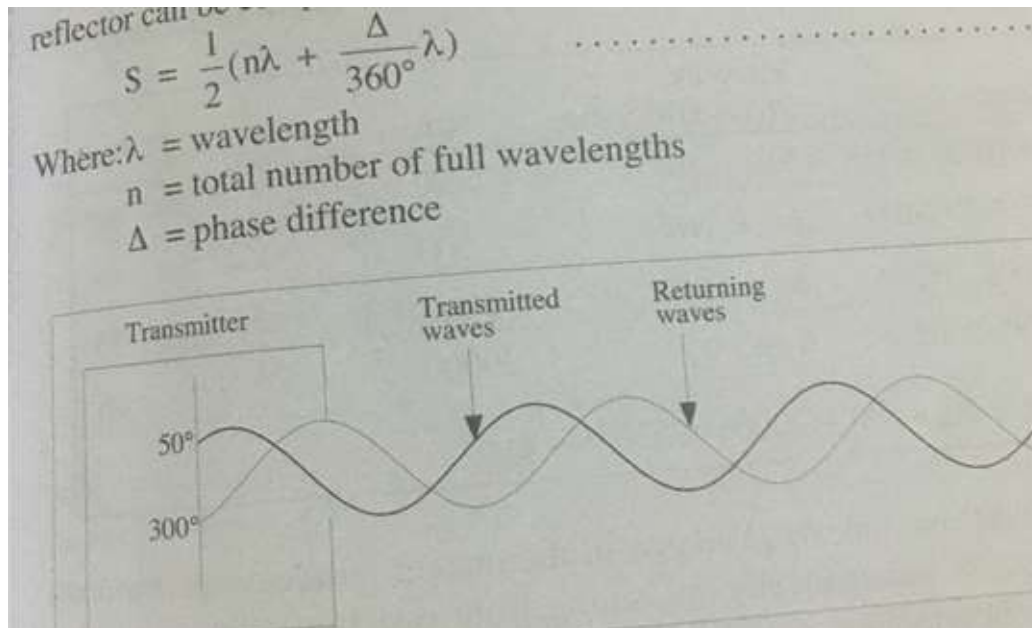
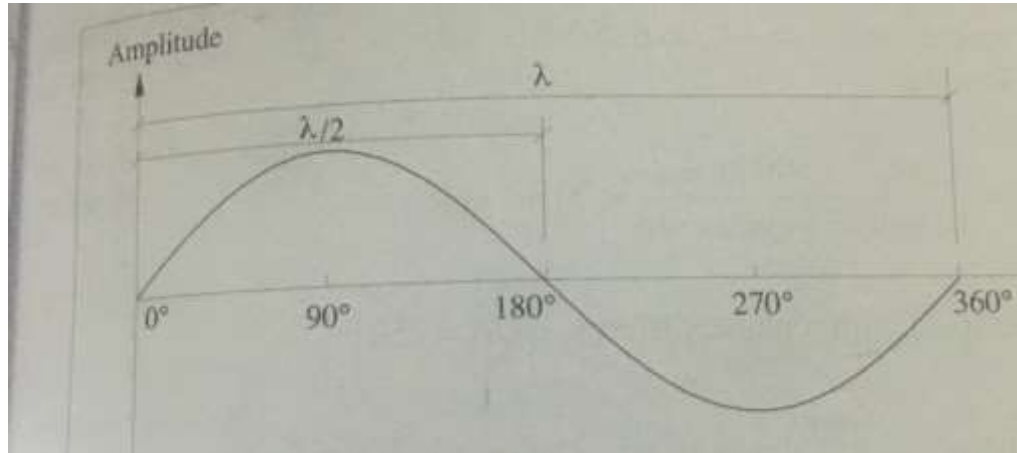
$$\lambda = \frac{c}{f}$$

*where  $\lambda$  = wave-length(meters)*

*c = velocity(km/ sec)*

*f = frequency(hertz = onecycle / sec)*

# Sloping distance



- 3- The instrument can count number of full waves length or instead the instrument can send out a series (3 or 4) of modulated waves at different frequencies
- 4- The frequency is typically reduced each time by a factor of 10 so the wave length is increased each time by a factor of 10
- 5- substituting the resulting values of wave lengths and phase difference into  $S$ , the value of  $n$  can be found
- 6- the instruments are designed to carry out this procedure in a matter of seconds and then to display the value of  $L$  in digital form

The term  $(\Delta/360^\circ)\lambda$  represents the fractional wavelength preceding example, with  $f = 14.989625$  MHz, and taking the speed as 299,792.5 km/sec:

$$\lambda = \frac{V}{f} = \frac{299,792,500 \text{ m/sec}}{14,989,625 \text{ cycles/sec}} = 20 \text{ m/cycle}$$

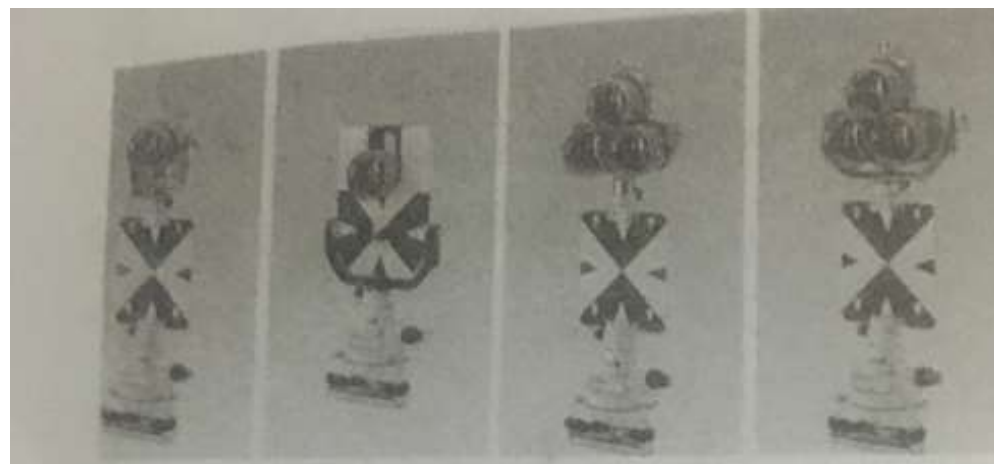
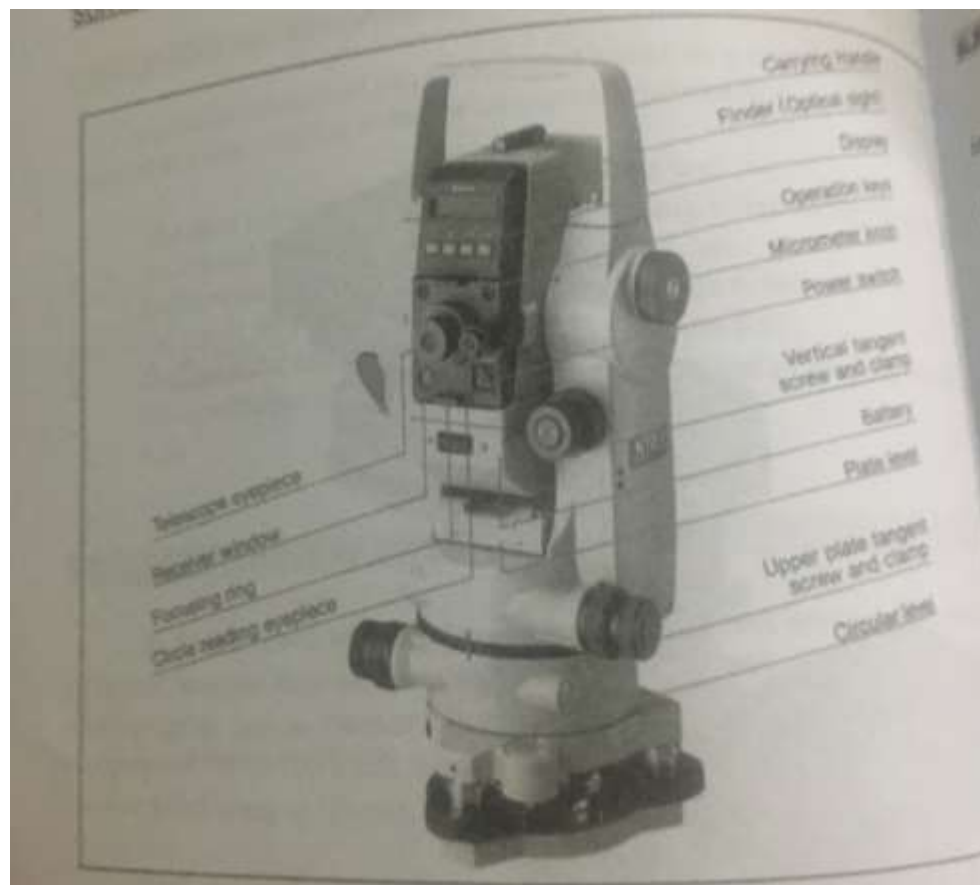
Using Equation (6.3) with a phase difference  $(\Delta) = 250^\circ$ :

$$S = \frac{1}{2} \left[ 20n + \frac{250^\circ}{360^\circ} \cdot 20 \right] \text{ meters} = [10n + 6.944] \text{ meters}$$

TABLE 6.1: Calculations

Frequency	Measured Phase Difference	$\lambda$ (m)	$\frac{1}{2} \frac{\Delta}{360^\circ} \lambda$
$F_1 = 14.989625$ MHz	$\Delta_1 = 250^\circ$	20	6.944 m
$F_2 = 1.4989625$ MHz	$\Delta_2 = 98^\circ$	200	27 m
$F_3 = 149.89625$ KHz	$\Delta_3 = 190^\circ$	2000	527 m
$F_4 = 14.989625$ KHz	$\Delta_4 = 91^\circ$	20000	2527 m
$S = 6.944 + 20 + 500 + 2000 = 2526.944 \text{ m}$			

Most EDM instruments available in the market nowadays perform the



# Factors affecting the velocity of EDM

- The velocity of light through the atmosphere can be affected by 1- temperature 2- atmospheric pressure 3- water vapour content
- It can be corrected by consulting nomographs or by performing automatically on some EDMs by the on-board processor/ calculator after entering the values for temperature and pressure
- for short distances these factors have relatively small significance but for large ones atmospheric corrections can become quite important



# EDM characteristics

- 1- Distance range 800m-10 km (single prism with average atmospheric conditions)
- 2- short range EDMs can be extended to 1300 m using 3 prisms
- 3- long range

# EDM accuracies

1- accuracies are stated in terms of a constant instrumental error plus a measuring error proportional to the distance being measured

2- Accuracy is claimed to be ( $\pm(5\text{mm} + 5\text{ppm})$ ) where  $\pm 5\text{mm}$  is the instrument error that is independent of length of measurements whereas 5ppm denotes the distance related error

## 6.9 SOURCES OF MEASUREMENT ERRORS

When using electro-optical instruments for distance measurement, the following sources of errors may occur:

- (1) Eccentric error due to inexact centering of the instrument and reflector over the survey stations.
- (2) Inexactness of the instrument in performing phase measurements.
- (3) The zero point of the light ray used in phase measurement does not coincide exactly with the theoretical center of the instrument.
- (4) The actual center of the reflector does not coincide with the theoretical center.
- (5) The actual modulating frequencies differ from the theoretical values of these frequencies.
- (6) The refraction index ( $N_s$ ) is not constant through the line to be measured.

# Index of refraction

The ratio between the velocity of propagation of electromagnetic wave in a vacuum ( $V_o$ ) and the velocity in the atmosphere ( $V$ ) is called the index of refraction ( $N_a$ ); that is:

$$N_a = \frac{V_o}{V} \dots \dots \dots (6.4)$$

$N_a$  depends on the wavelength, atmospheric pressure, temperature and relative humidity. For dry atmosphere at 0°C and at sea level (pressure = 760 mm Hg), the refractive index for light waves is given by:

$$N_g = 1 + (287.604 + 4.886 \lambda^{-2} + 0.068 \lambda^{-4}) 10^{-6} \dots \dots \dots (6.5)$$

Where:  $\lambda$  = wavelength of light in  $\mu\text{m}$   
 = 0.9 - 0.93  $\mu\text{m}$  for near infrared light from Gallium Arsenide diode  
 = 0.6328  $\mu\text{m}$  for light generated by helium-neon laser

At other atmospheric conditions:

$$N_a = 1 + \frac{0.359474 (N_g - 1) P}{273.2 + t} \dots \dots \dots (6.6)$$

Where:  $P$  = atmospheric pressure in mm Hg  
 $t$  = air temperature in °C

Thus for  $\lambda = 0.9 \mu\text{m}$ ,  $N_a = 1.000294$  at sea level (760 mm Hg) and air temperature of 20°C. In EDM applications,  $N_a$  is often expressed as follows:

$$N_a = 1 + 10^{-6} N \dots \dots \dots (6.7)$$

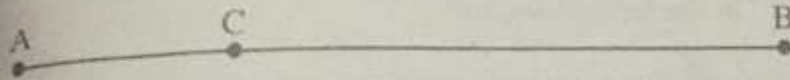


FIGURE 6.8: Layout for determination of correction for zero centering errors.

Let the actual calibrated lengths be  $\overline{AB}$ ,  $\overline{AC}$  &  $\overline{CB}$ , and the measured lengths by the EDM instrument be  $\overline{AB}$ ,  $\overline{AC}$  &  $\overline{CB}$ .

Let the unknown correction be  $(c)$ .

$$\text{Then: } \overline{AB} = \overline{AB} + c$$

$$\overline{AC} = \overline{AC} + c$$

$$\overline{CB} = \overline{CB} + c$$

$$\text{But: } \overline{AB} = \overline{AC} + \overline{CB} \Rightarrow \overline{AB} + c = \overline{AC} + \overline{CB} + 2c$$

$$\Rightarrow c = \overline{AB} - \overline{AC} - \overline{CB} \dots\dots\dots(6.8)$$

### EXAMPLE 6.1:

To determine the zero centering correction for an EDM, the following values for  $\overline{AB}$ ,  $\overline{AC}$  and  $\overline{CB}$  were measured by the EDM:

$$\overline{AB} = 313.647 \text{ m, } \overline{AC} = 112.556 \text{ m, and } \overline{CB} = 201.088 \text{ m.}$$

- Find the correction for zero centering  $(c)$ .
- A distance was recorded to be 718.128 m when using the same instrument. Compute the correct distance.

### SOLUTION:

$$(a) c = \overline{AB} - \overline{AC} - \overline{CB} = 313.647 - 112.556 - 201.088 = +0.003 \text{ m}$$

$$(b) \text{ Corrected distance} = 718.128 + 0.003 = 718.131 \text{ m}$$

1. Measure  $f'$  in the laboratory, or
2. If this is not possible, measure two known distances such as in Figure 6.8. Then:
 
$$\overline{AB} = g \cdot \overline{AB} + c$$

$$\overline{AC} = g \cdot \overline{AC} + c$$

Where:  $\overline{AB}$  and  $\overline{AC}$  are the known distances,  
 $\overline{AB}$  and  $\overline{AC}$  are the measured distances,  
 $g = f'/f = \text{scale factor}$ ,  
 $c = \text{correction for zero centering}$

### EXAMPLE 6.2:

The following data belongs to Figure 6.8:

$$\overline{AB} = 1499.8635 \text{ m,}$$

$$\overline{AB} = 1499.9000 \text{ m,}$$

Determine  $g$  and  $c$ .

$$\overline{AC} = 149.9921 \text{ m}$$

$$\overline{AC} = 149.9935 \text{ m.}$$

### SOLUTION:

$$1499.8635 = 1499.9000 g + c$$

$$149.9921 = 149.9935 g + c$$

Solving these two equations for  $g$  and  $c$ :  $\Rightarrow$

# Distance and elevation

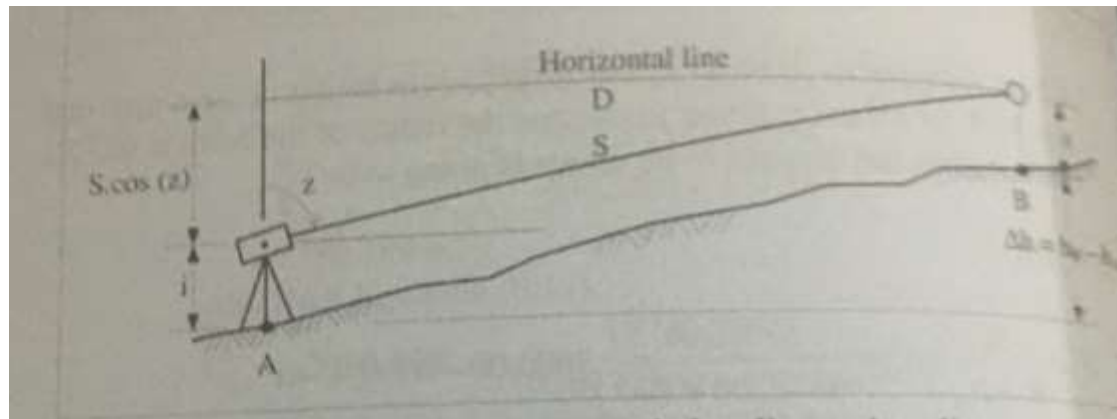


FIGURE 6.11: Trigonometric leveling – short line.

The following relation exists:

$$\Delta h = h_B - h_A = s \cos z + i - t \quad \dots\dots\dots$$

Also, the horizontal distance (D):

$$D = s \sin z \quad \dots\dots\dots$$

Where:

$h_A$  and  $h_B$  are the elevations of points A and B

$S$  = the slope distance along the line of sight

$z$  = zenith angle

$i$  = the height of the instrument (total station)

$t$  = the height of the sight target (reflector)