

Birzeit University
Faculty of Engineering & Technology
Civil Engineering Department
Statics - CE 232
Summer Semester 2018/2019

Midterm Exam – Saturday, July 20, 2019

Time total allowed = 75minutes

Student Name	Mohamad Moayed Shannaf . محمد مؤيد شناق
Student No.	1181401

Instructor and section:

Abdallah Hamdan – Section 1	
Abdallah Hamdan – Section 2	
Abdallah Hamdan – Section 3	✓
Dr. Omar Zamo – Section 4	
Farhat Majadbeh – section 5	

Grading

Problem 1	25
Problem 2	25
Problem 3	25
Problem 4	08
SUM/100	

83

ملاحظات مهمة

- اكتب اسمك ورقمك في المكان المخصص على كل ورقة من أوراق الامتحان
- اختر شعبتك من الشعب اعلاة. ان عدم اختيار الشعبه او كتابتها بصورة خاطئة قد يؤدي لخصم من علامتك المحصله بهذا الامتحان
- اجب في المكان المخصص فقط ويمكنك استعمال الوجه الاخر للورقة ان لزم
- الإجابات الغير مدعاه بحسابات صحيحة او تفسير منطقي لن تؤخذ بعين الاعتبار
- اكتب بخط واضح ومقروء ونظم حلك بتسلسل منطقي وترابط بحيث يسهل مراجعة خطواتك. سيتم اعتبار وضوح الحل وتسلسله عند تقييم الإجابات ولن يتم تقييم اي معلومات تقدمها غير مرتبطة بالحل الصحيح او لا تؤدي اليه.
- لتجنب الأخطاء الحسابية ينصح بفحص الإجابات للتأكد منها بكل طريقة ممكنه.
- عدد أسئلة الامتحان أربعة وعدد الصفحات ست

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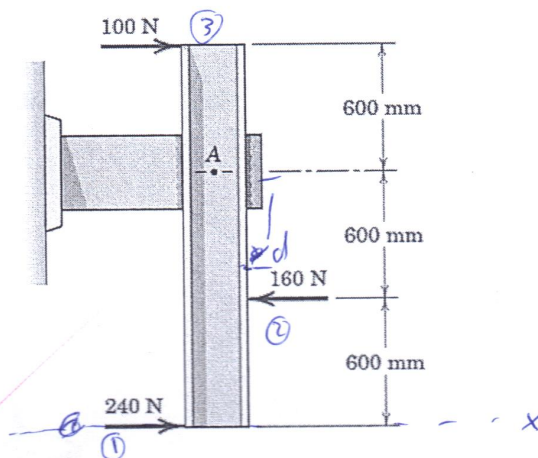
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Problem I (Weight 25)

- A. Replace the three forces shown by an equivalent force-couple system at point A.
- B. If the forces are replaced by a single resultant force, determine the distance d below/ above point A to its line of action.



A.

$$\vec{F}_1 = 240 \text{ N } \hat{i}$$

$$\vec{F}_2 = -160 \text{ N } \hat{i}$$

$$\vec{F}_3 = 100 \text{ N } \hat{i}$$

$$\text{at } A \quad \vec{R} = (240 - 160 + 100) \text{ N } \hat{i} = 180 \text{ N } \hat{i}$$

~~$$\vec{M}_A = d \times \vec{F}_1 + d \times \vec{F}_2 + d \times \vec{F}_3$$~~

$$\vec{M}_R = \vec{d}_1 \times \vec{F}_1 + \vec{d}_2 \times \vec{F}_2 + \vec{d}_3 \times \vec{F}_3 = (1.2)(240) - (0.6)160 + 100(0.6)$$

$$= 288 - 96 - 60 = 132 \hat{k} \text{ N}\cdot\text{m}$$

$$\vec{R} = 180 \text{ N } \hat{i} \quad \text{and} \quad \vec{M}_A = 132 \hat{k} \text{ (N}\cdot\text{m)}$$

B. $M_A^R = d (\vec{R}) \Rightarrow d = \frac{132}{180} = 0.733 \text{ m below } A$

محمد مازن

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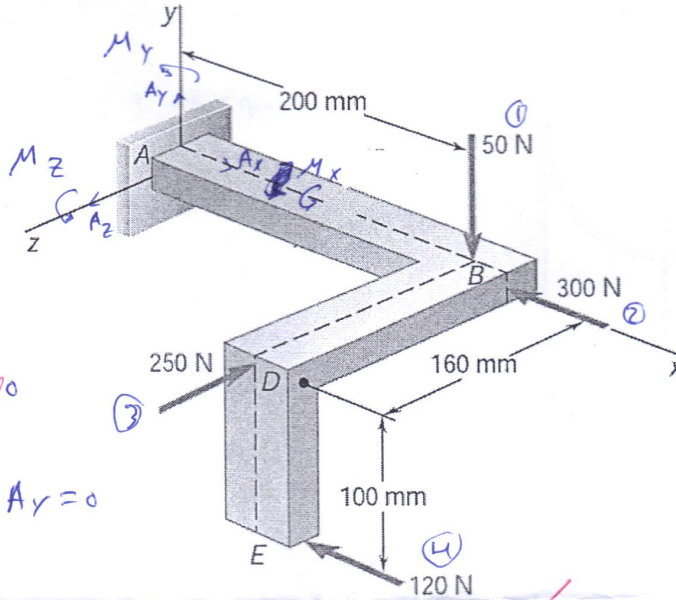
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Problem 2 (Weight 25)

The frame ABDE is supported by a fixed support at A and subjected to four forces as shown in the diagram. Find the reaction of the support at A.

$$\begin{aligned} \vec{F}_1 &= -50 \hat{j} \text{ N} \\ \vec{F}_2 &= -300 \hat{i} \text{ N} \\ \vec{F}_3 &= -250 \hat{i} \text{ N} \\ \vec{F}_4 &= -120 \hat{j} \text{ N} \\ \sum F_x &= 0 \end{aligned}$$



$$-300 - 120 + A_x = 0$$

$$A_x = 420 \text{ N}$$

$$\sum F_y = 0 \Rightarrow -50 + A_y = 0$$

$$A_y = 50 \text{ N}$$

$$\sum F_z = 0 \Rightarrow -250 + A_z = 0 \Rightarrow A_z = 250 \text{ N}$$

$$\sum M_A = 0 \Rightarrow \sum \vec{r} \times \vec{F} = 0 \Rightarrow 0 = (0.2 \hat{i}) \times (-50 \hat{j})$$

$$\Rightarrow -10 \hat{k} + 50 \hat{j} + M_x \hat{i} = 0$$

$$-12 \hat{i} - 19.2 \hat{j}$$

$$+ M_z \hat{i} + M_y \hat{j}$$

$$+ (0.2 \hat{i}) \times (-300 \hat{i})$$

$$+ (0.2 \hat{i} + 0.16 \hat{i}) \times (-250 \hat{i})$$

$$+ (0.2 \hat{i} - 0.1 \hat{j} + 0.16 \hat{i}) \times (-120 \hat{j})$$

$$+ M_x \hat{i} + M_y \hat{j} + M_z \hat{i}$$

$$(M_z - 22) \hat{i} + (30.8 + M_y) \hat{j} + M_x \hat{i} = 0$$

$$M_x = 0$$

$$M_y = -30.8 \text{ N.m}$$

$$M_z = 22 \text{ N.m}$$

$$A = (420 \hat{i} + 50 \hat{j} + 250 \hat{k}) \text{ N}$$

$$M_A = (-30.8 \hat{j} + 22 \hat{i}) \text{ N.m}$$

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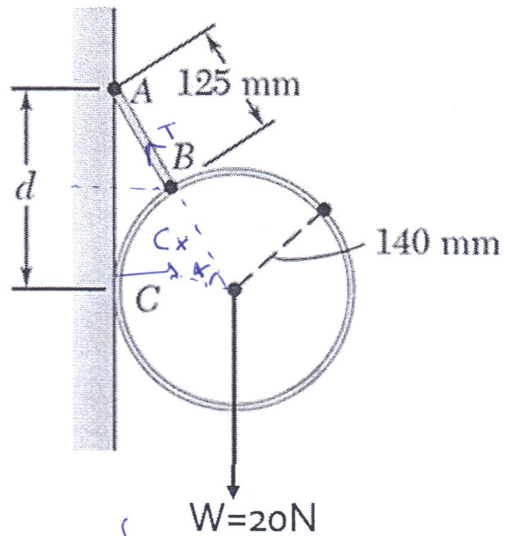
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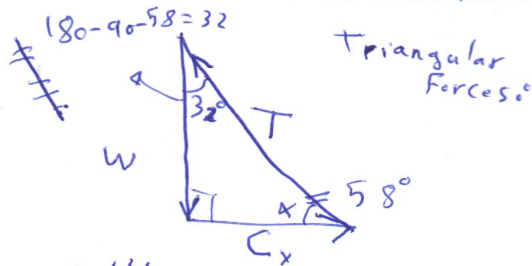
Problem 3 (Weight 25)

A 20 N thin ring of radius $r = 140$ mm is held against a frictionless wall by a 125-mm string AB. Determine

- (a) The distance d .
- (b) The tension in the string.
- (c) The reaction at C.



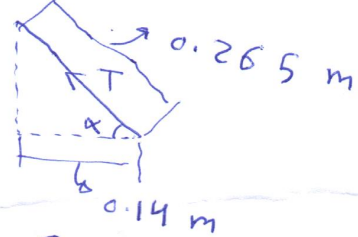
Concurrent forces \Rightarrow equilibrium.



(a)

$$\cos \alpha = \frac{0.14}{0.265} = 0.53 \Rightarrow \alpha = 58^\circ$$

$$\sin \alpha = \frac{d}{0.265} = \sin 58^\circ \Rightarrow d = (\sin 58^\circ) 0.265 = 0.225 \text{ m} = 225 \text{ mm}$$



$$\alpha = \cos^{-1}\left(\frac{0.14}{0.265}\right) = 58^\circ$$

(b) Sines law
(Triangular Forces):

$$\frac{T}{\sin 90} = \frac{C_x}{\sin 32} = \frac{W}{\sin 58} = 23.6$$

$$\Rightarrow T = (23.6) \sin 90 = 23.6 \text{ N} = T_{BA}$$

$$C_x = (23.6) \sin 32 \Rightarrow C_x = 12.5 \text{ N} \uparrow$$

(c) $d = 0.225$ m

$$\vec{T}_{BA} = T_{BA} (\cos 58^\circ \hat{i} + \sin 58^\circ \hat{j}) = (-12.5 \hat{i} + 20 \hat{j}) \text{ N}$$

$$\vec{C} = (12.5 \hat{i}) \text{ N}$$

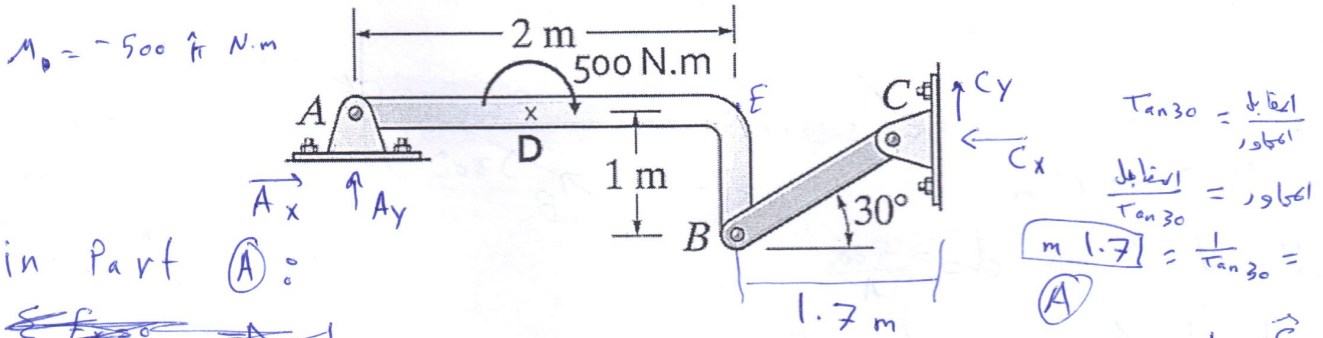
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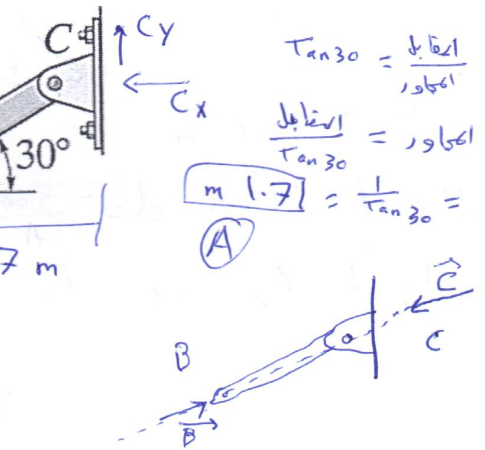
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Problem 4 (Weight 25)

The frame shown consists two members ADB and BC that are joint together by a pin at B. A and C are pin (hinge) supports. A moment of 500 N.m is applied at D. Determine reactions at the pins A and C.



Special Case: \vec{B} and \vec{C} Same magnitude " direction opposite sense.



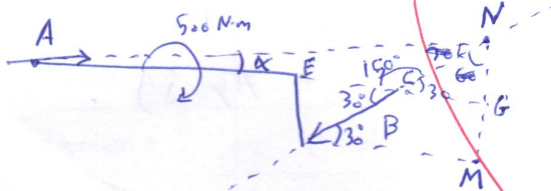
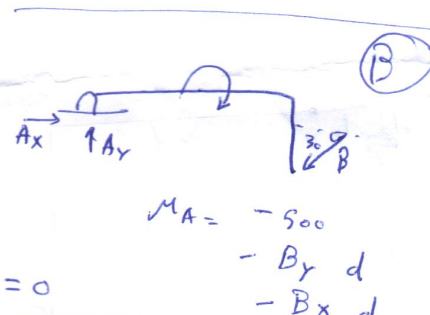
in Part (B):

$\sum F_x = 0 \Rightarrow A_x - B_x = 0$

$A_x = B_x$

$\sum F_y = 0 \Rightarrow A_y - B_y = 0 \Rightarrow A_y = B_y$

$\sum M_A = 0 \Rightarrow (-500) - A_y(2) - B_x(1) = 0$



$EC = 1.7 \text{ m}$

$AE = 2 \text{ m}$

$AC = 3.7 \text{ m}$

$NG = NM$

$\frac{A}{\sin 120} = \frac{B}{\sin(90+x)} = \frac{500}{\sin 30}$

