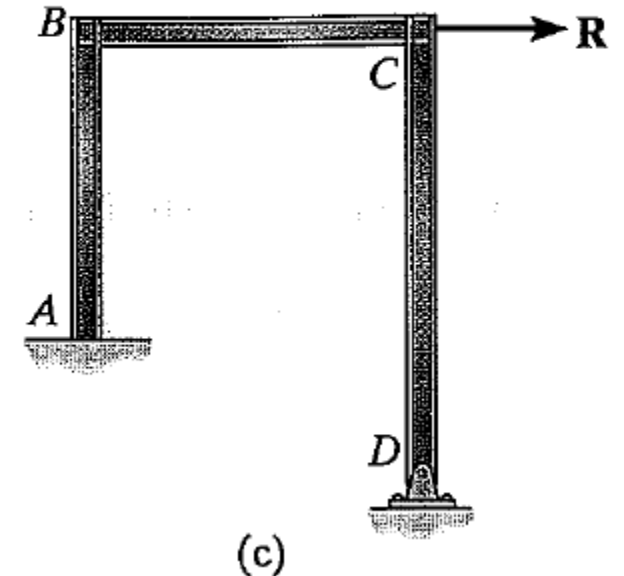
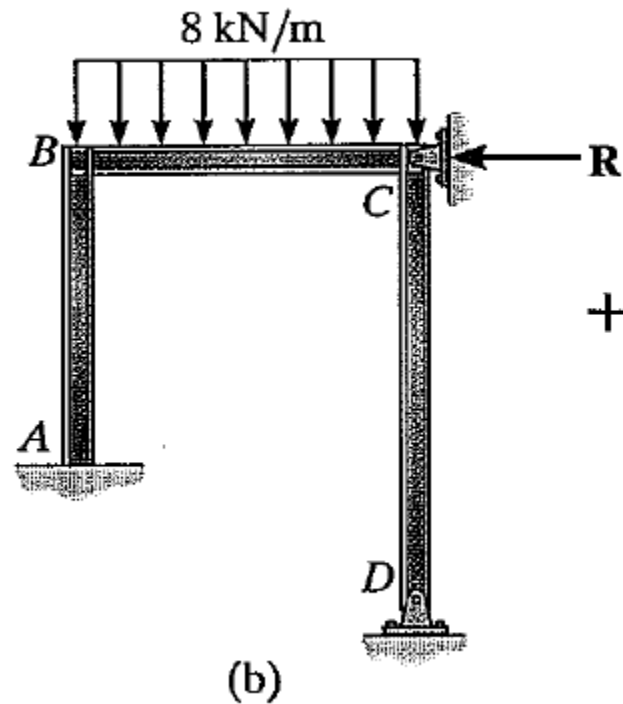
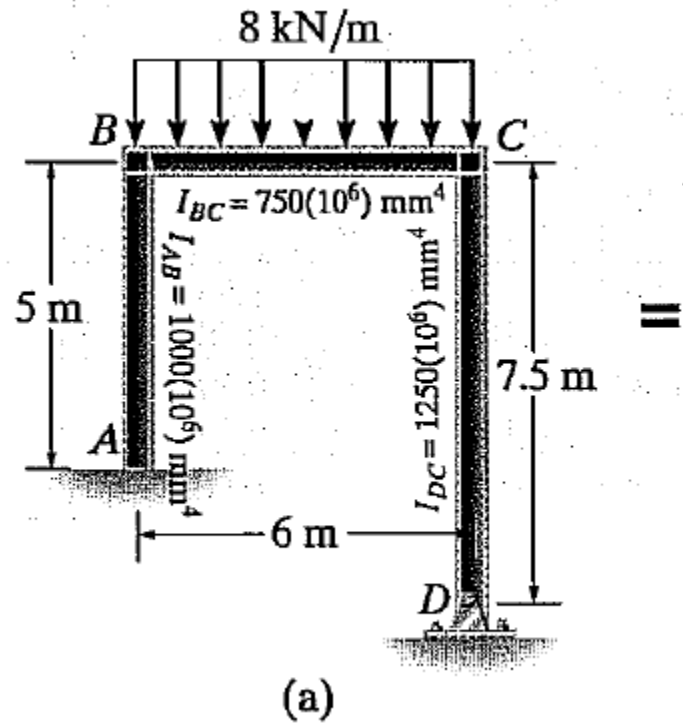


# Moment distribution method – sway frames

# Sway frames: principle of superposition



- Actual system

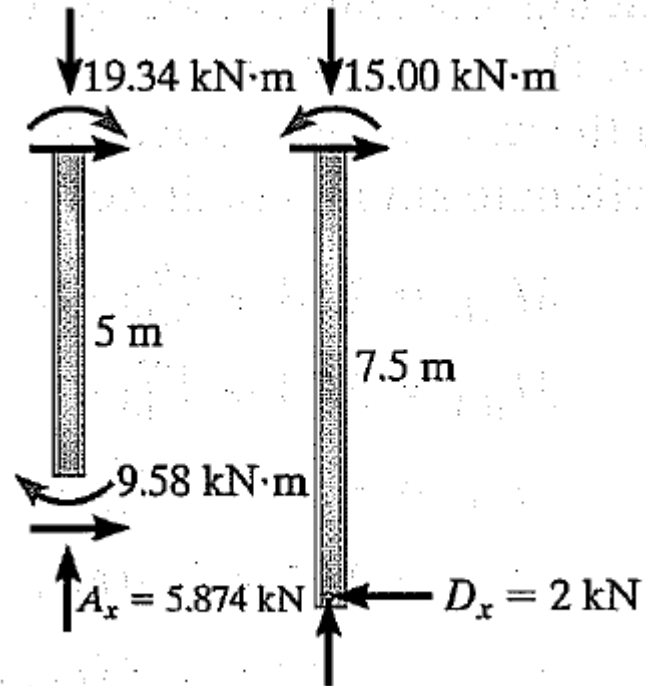
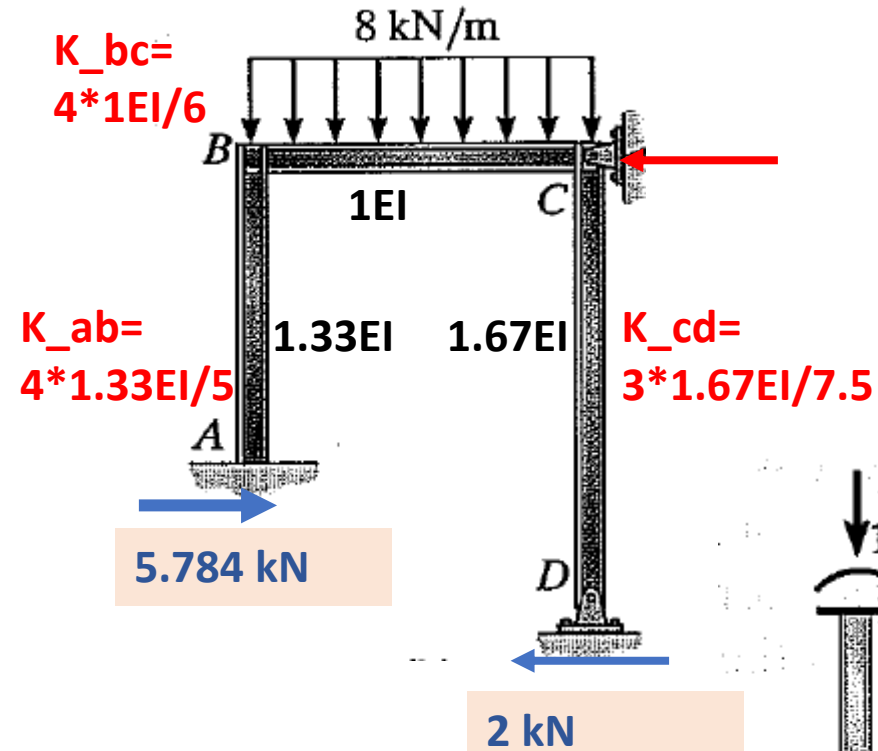
- Non-Sway system (applied loading)

- Sway system (only swaying forc)

$$\text{Moment} = M_I + (R/R') M_{II}$$

# Non-sway

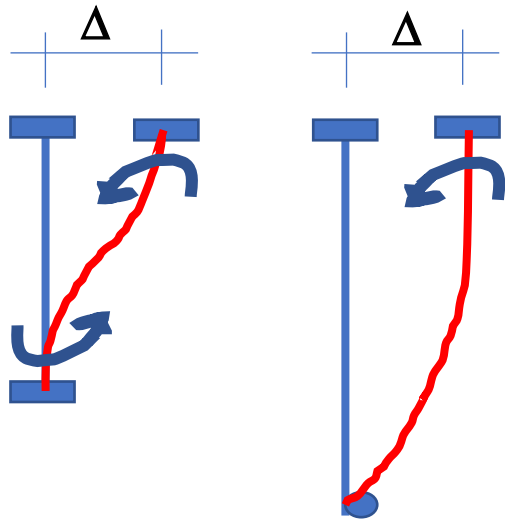
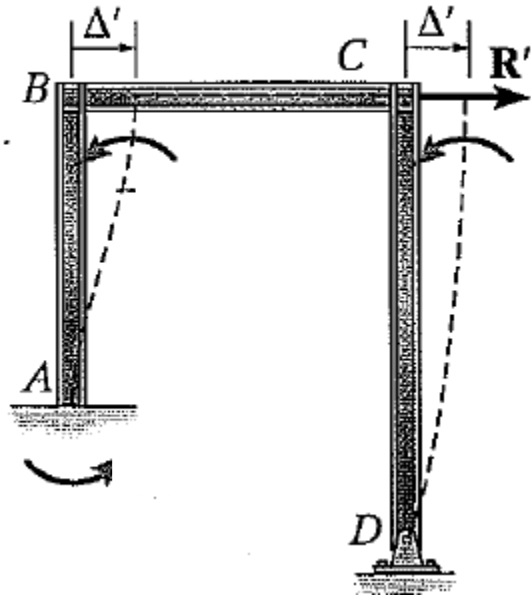
Joint	A	B		C		D
Member	AB	BA	BC	CB	CD	DC
DF	0	0.615	0.385	0.5	0.5	1
FEM Dist.		14.76	-24 9.24	24 -12	-12	
CO Dist.	7.38	3.69	-6 2.31	4.62 -2.31	-2.31	
CO Dist.	1.84	0.713	-1.16 0.447	1.16 -0.58	-0.58	
CO Dist.	0.357	0.18	-0.29 0.11	0.224 -0.11	-0.11	
$\Sigma M$	9.58	19.34	-19.34	15.00	-15.00	0



# Finding R values and direction



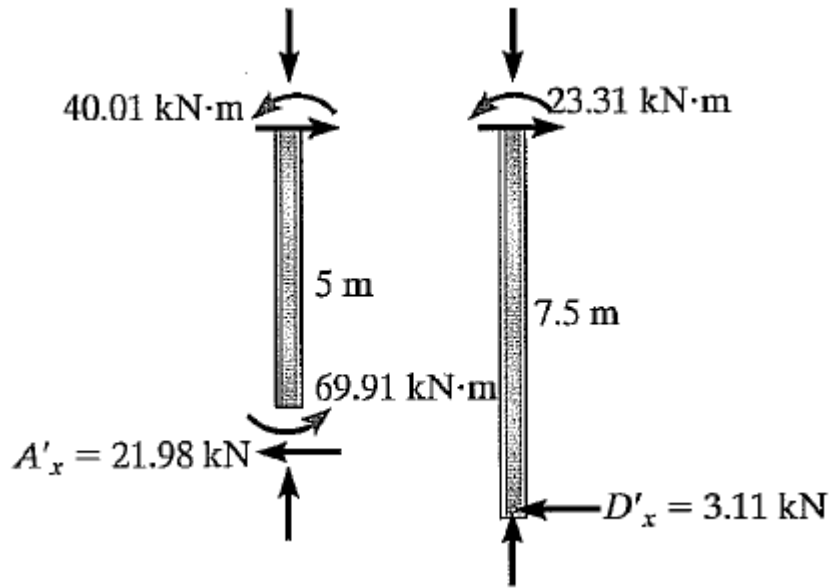
Sway Frame: Set of FEM due of drift following the compatibility conditions for the frame



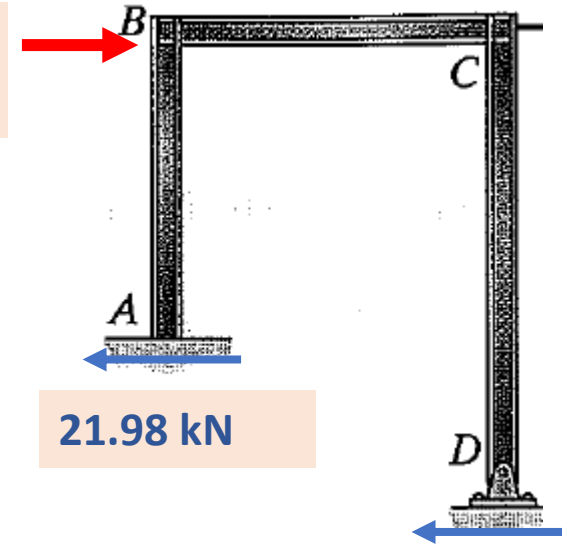
FEM <sub>ab</sub>	:	FEM <sub>ba</sub>	:	FEM <sub>cd</sub>
$6EI * \Delta / (Lab)^2$	:	$6EI * \Delta / (Lab)^2$	:	$3EI * \Delta / (Lcd)^2$
0.3192	:	0.3192	:	0.0891
1	:	1	:	0.2778
100	:	100	:	27.78
C.C.W.	:	C.C.W.	:	C.C.W.

Joint	A	B		C		D
Member	AB	BA	BC	CB	CD	DC
DF	0	0.615	0.385	0.5	0.5	1
FEM	-100	-100			-27.78	
Dist.		61.5	38.5	13.89	13.89	
CO	30.75		6.94	19.25		
Dist.		-4.27	-2.67	-9.625	-9.625	
CO	-2.14		-4.81	-1.34		
Dist.		2.96	1.85	0.67	0.67	
CO	1.48		0.33	0.92		
Dist.		-0.20	-0.13	-0.46	-0.46	
$\Sigma M$	-69.91	-40.01	40.01	23.31	-23.31	0

# Calculation of $R'$ and finding end moments



$$R' = 21.98 + 3.1 = 25.1$$



21.98 kN

3.1 kN

Actual end-moments of the system

$$M_{AB} = 9.58 + \left(\frac{3.78}{25.1}\right)(-69.91) = -0.948 \text{ kN} \cdot \text{m}$$

$$M_{BA} = 19.34 + \left(\frac{3.78}{25.1}\right)(-40.01) = 13.3 \text{ kN} \cdot \text{m}$$

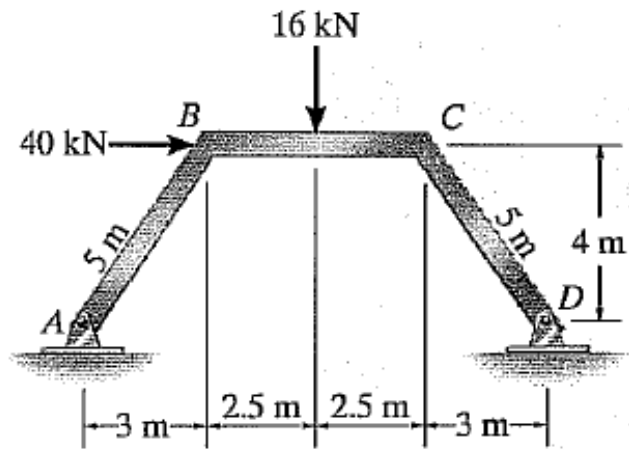
$$M_{BC} = -19.34 + \left(\frac{3.78}{25.1}\right)(40.01) = -13.3 \text{ kN} \cdot \text{m}$$

$$M_{CB} = 15.00 + \left(\frac{3.78}{25.1}\right)(23.31) = 18.5 \text{ kN} \cdot \text{m}$$

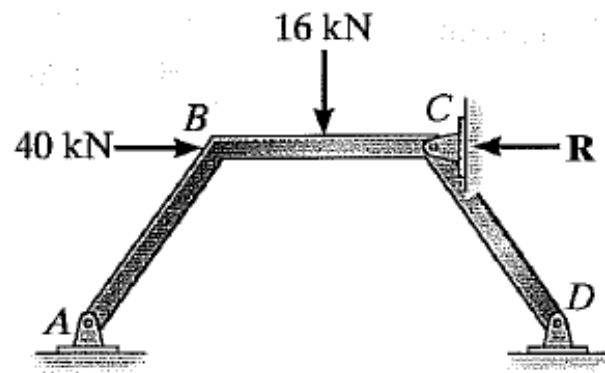
$$M_{CD} = -15.00 + \left(\frac{3.78}{25.1}\right)(-23.31) = -18.5 \text{ kN} \cdot \text{m}$$

**Assignment:** find the reaction forces of the frame system and draw shear and bending moment diagrams indicating key values and sketch deformed shape

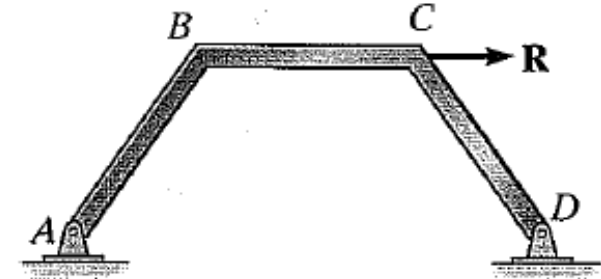
# Analysis of swaying Frame with inclined columns



=



+



Moment

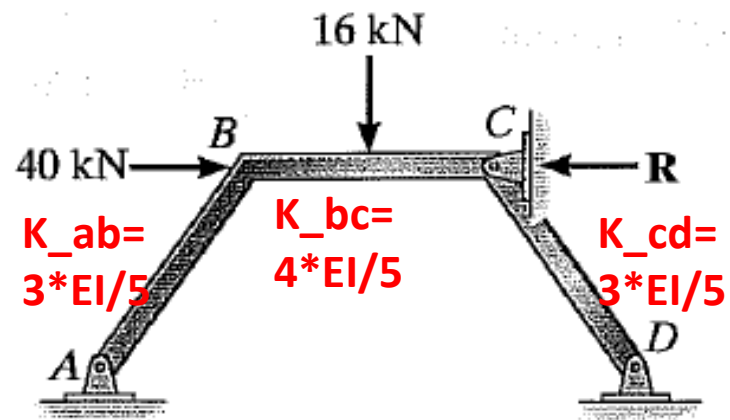
=

$M_I$

+

$(R/R') M_{II}$

# Non-sway

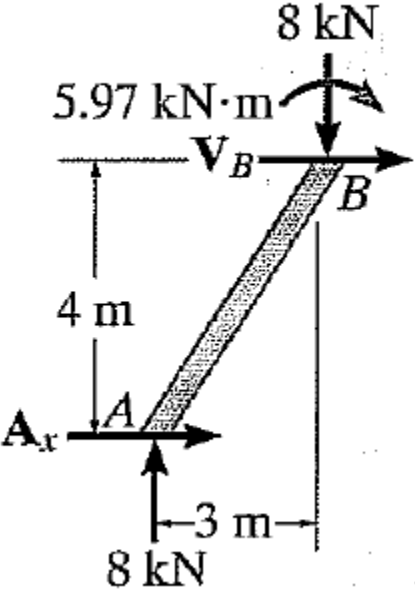


Joint	A	B		C		D
Member	AB	BA	BC	CB	CD	DC
DF	1	0.429	0.571	0.571	0.429	1
FEM			-10	10		
Dist.		4.29	5.71	-5.71	-4.29	
CO			-2.86	2.86		
Dist.		1.23	1.63	-1.63	-1.23	
CO			-0.82	0.82		
Dist.		0.35	0.47	-0.47	-0.35	
CO			-0.24	0.24		
Dist.		0.10	0.13	-0.13	-0.10	
$\Sigma M$	0	5.97	-5.97	5.97	-5.97	0

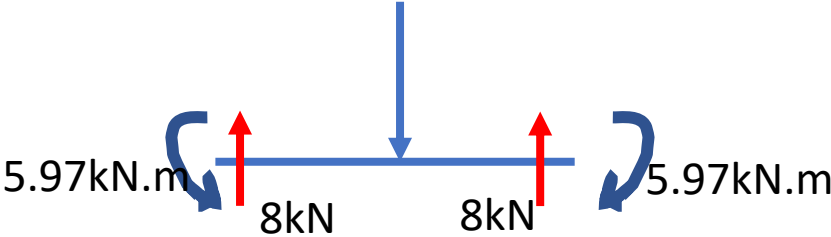


# Finding R

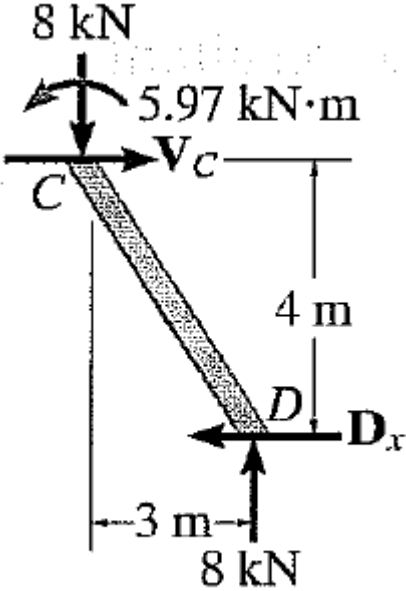
Step Two: shear in the beam is vertical loading on column



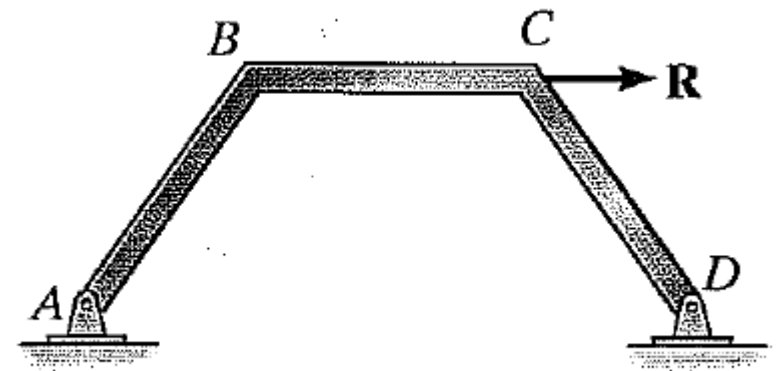
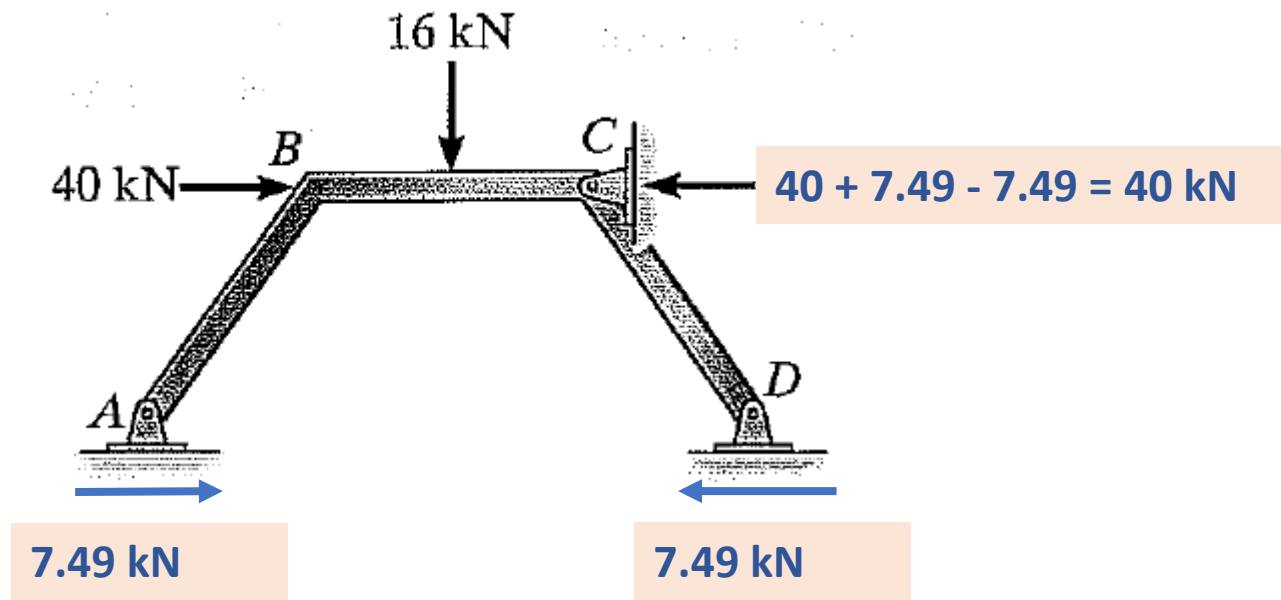
Step One: shear in the beam

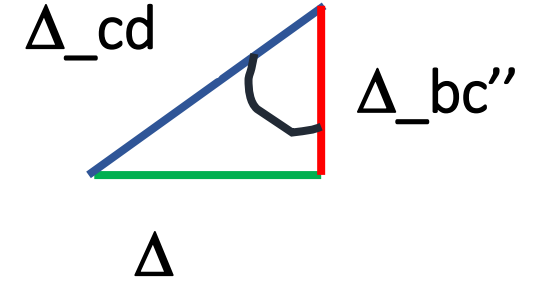
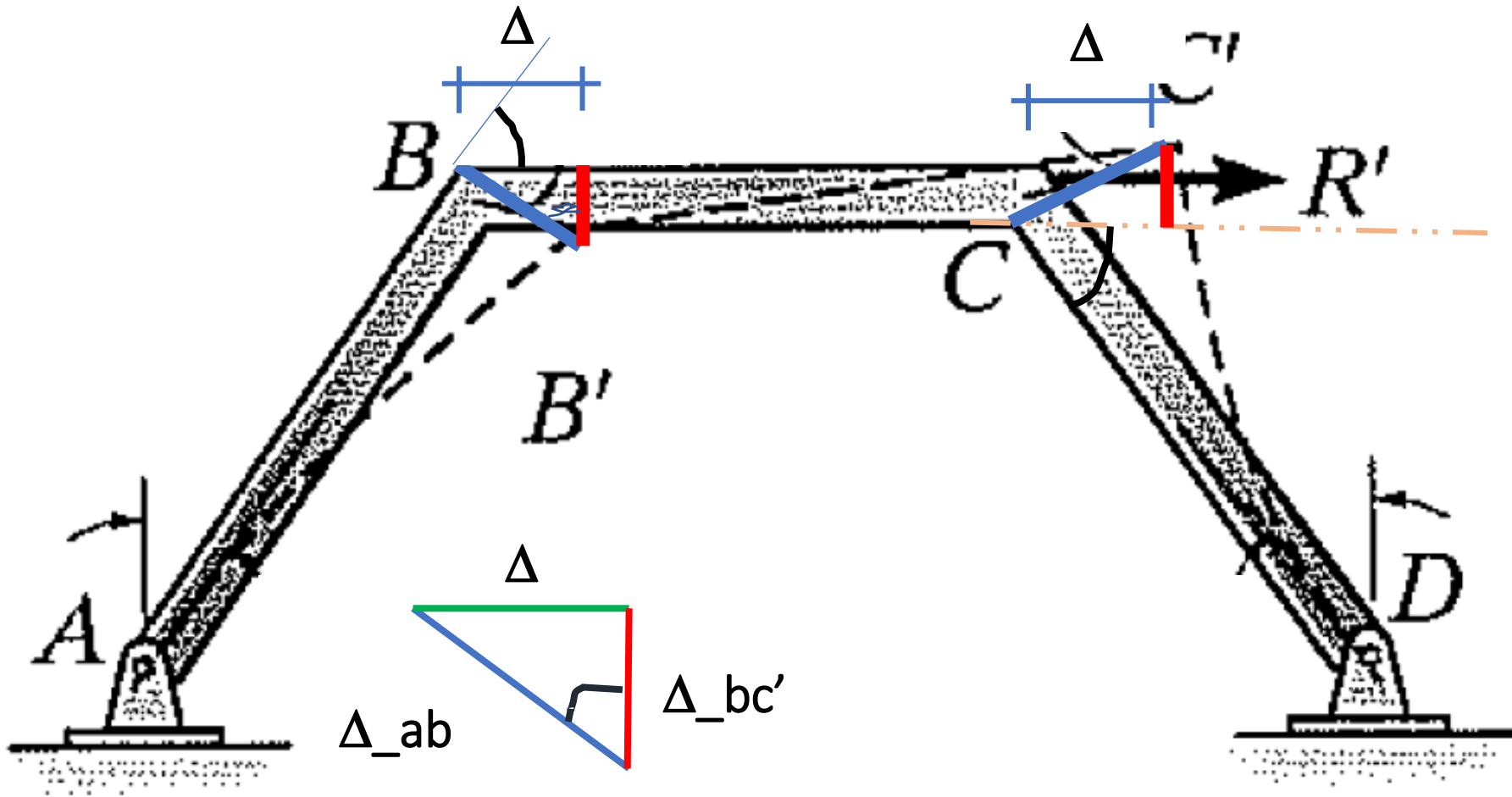


Step Two: shear in the beam is vertical loading on column



$\Sigma F_y = 0 \text{ ----- } A_y = 8 \text{ kN}$   
 $\Sigma M \text{ at } B = 0 \text{ ----- } 8 \cdot 3 + 5.97 = A_x(4) \text{ ----- } A_x = 7.49 \text{ kN}$   
 In the same way  
 $\Sigma M \text{ at } C = 0 \text{ ----- } C_y \cdot 3 + M_{cd} = D_x(4) \text{ ----- } D_x = 7.49 \text{ kN}$





$$\Delta_{cd} = \Delta / \sin(\beta) = 5/4 \Delta$$

$$\Delta_{bc''} = \Delta / \tan(\beta) = 3/4 \Delta$$

$$\Delta_{ab} = \Delta / \sin(\alpha) = 5/4 \Delta$$

$$\Delta_{bc'} = \Delta / \tan(\alpha) = 3/4 \Delta$$

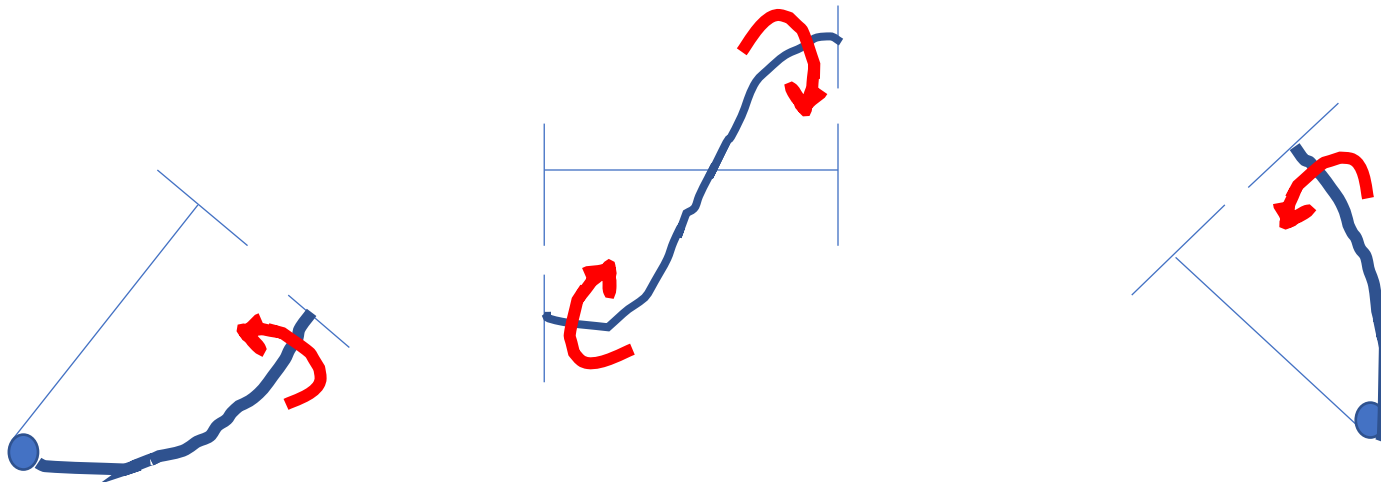
$$\Delta_{ab} = 1.25 \Delta$$

$$\Delta_{bc} = \Delta_{bc'} + \Delta_{bc''} = 1.5 \Delta$$

$$\Delta_{cd} = 1.25 \Delta$$

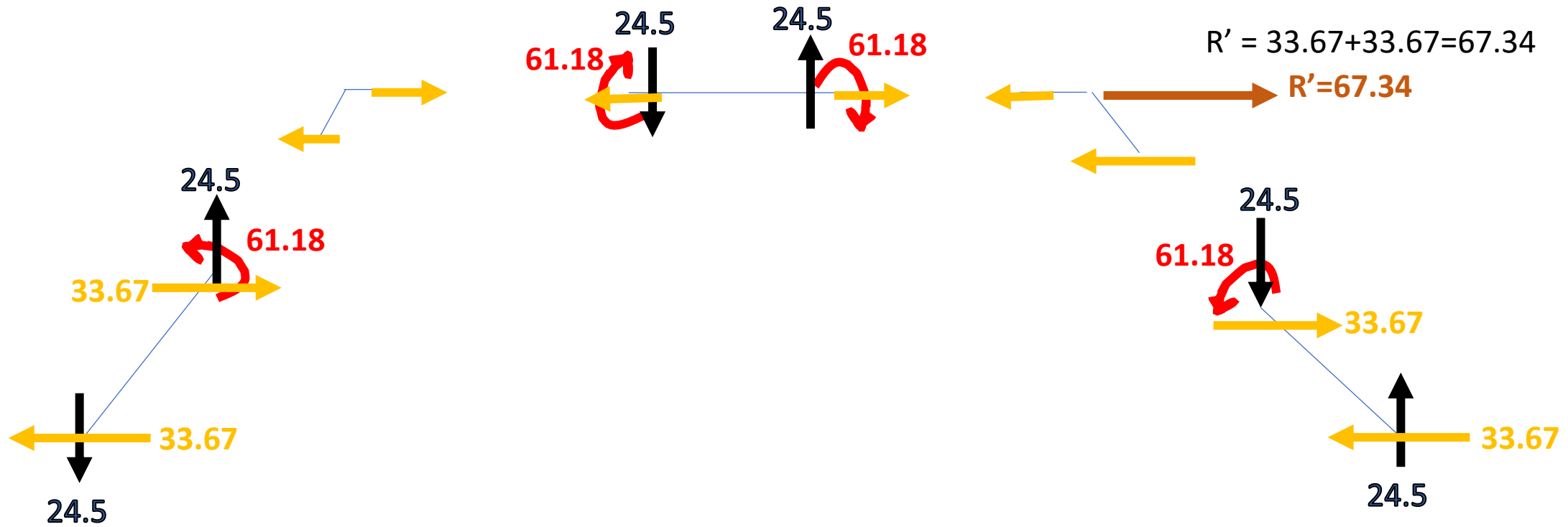
# Sway: Set of FEM

<b>FEM<sub>ba</sub></b>	<b>:</b>	<b>FEM<sub>bc</sub></b>	<b>:</b>	<b>FEM<sub>cb</sub></b>	<b>:</b>	<b>FEM<sub>cd</sub></b>
$3EI * \Delta_{ab} / (L_{ab})^2$	<b>:</b>	$6EI * \Delta_{bc} / (L_{cb})^2$	<b>:</b>	$6EI * \Delta_{bc} / (L_{cb})^2$	<b>:</b>	$3EI * \Delta_{cd} / (L_{cd})^2$
<b>0.15</b>	<b>:</b>	<b>0.36</b>	<b>:</b>	<b>0.36</b>	<b>:</b>	<b>0.15</b>
<b>0.417</b>	<b>:</b>	<b>1</b>	<b>:</b>	<b>1</b>	<b>:</b>	<b>0.417</b>
<b>41.7</b>	<b>:</b>	<b>100</b>	<b>:</b>	<b>100</b>	<b>:</b>	<b>41.7</b>
<b>C.C.W.</b>	<b>:</b>	<b>C.W.</b>	<b>:</b>	<b>C.W.</b>	<b>:</b>	<b>C.C.W</b>



joint	A	B		C		D
end-moment	AB	BA	BC	CB	CD	DC
DF	1	0.429	0.571	0.571	0.429	1
FEM	0	-41.7	100	100	-41.7	0
Dist	0	-25	-33.31	-33.31	-25	0
CO	0		-16.65	-16.65		0
Dist	0	7.143	9.507	9.507	7.143	0
CO	0		4.753	4.753		0
Dist	0	-2.04	-2.71	-2.71	-2.04	0
CO	0		-1.36	-1.36		0
Dist	0	0.582	0.776	0.776	0.582	0
CO	0		0.388	0.388		0
Dist	0	-0.17	-0.22	-0.22	-0.17	0
	0	-61.18	61.18	61.18	-61.18	0

# Finding R' and final values of end moments



Actual end-moments of the system

End moment	AB	BA	BC	CB	CD	DC
MI	0	5.97	-5.97	5.97	-5.97	0
MII * (R/R')	0	-36.34	36.34	36.34	-36.34	0
MI+ (R/R')MII	0	-30.4	30.4	42.3	-42.3	0

Assignment:

Analyze the following frame system, draw shear and bending moment diagrams indicating key values and draw the deformed shape

