



Numbering Systems

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Outline

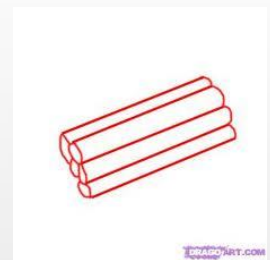
- History.
- Decimal System.
- Binary System.
- Octal System.
- Hexadecimal System.
- Converting from one System to another system & back.
- Binary Addition
- Signed Numbers
- Summary

History

- ❖ Long ago, humans used sticks to count.



- ❖ Later learned how to draw pictures of sticks in the ground and eventually on paper.



- ❖ Using symbols to represent the numbers instead of sticks.

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Decimal System

- ❖ Most People Use decimal representation to count.
- ❖ In decimal there are **10** digits
0,1,2,3,4,5,6,7,8,9
- ❖ The base is **10**
- ❖ We can Represent any value for these digits
Ex: 754 , 123 , 889 , 345

Decimal System

Ex: 754

$$7 \cdot 10^2 + 5 \cdot 10^1 + 4 \cdot 10^0 = 700 + 50 + 4 = 754$$

base

Digit
position

123 ???

Binary System

- ❖ Computer is not smart as a human .
- ❖ Easy to make an electronic machine with two states: on and off , or 1 and 0.
- ❖ In Binary there are **2** digits
0,1

The base is **2**

Binary System

- ❖ Each digit in binary number called **BIT**.

1 0 1 0 , 4 digits , **How many bits ?**

answer : 4 bits

- ❖ 4 bits form a **NIBBLE**.

- ❖ 8 bits form a byte.

- ❖ 1 0 1 0 0 0 1 1 , **How many Bits, Nibbles and Bytes?**

Answer :8 bits ,2 Nibbles and 1 byte

Binary System

❖ Two bytes form a **WORD** and two words form a **DOUBLE WORD (rarely used)** .

EX:

0000 1111 1010 1010 : 16 bits , WORD

Octal System

❖ Uses 8 digits

0,1,2,3,4,5,6,7

❖ The base is **8**

❖ **EX** $(123)_8$, $(156)_8$

Hexadecimal System

❖ Uses 16 digits

0,1,2,3,4,5,6,7,8,9,A,B,C,D,E,F

❖ The base is **16**

❖ **EX: 123h , 456h 0E120h**

❖ **Suppose we need to develop new system with base 5,7 or 3?**

Base 5 : 0,1,2,3,4

Base 7 : 0,1,2,3,4,5,6

Base 3: 0,1,2



Binary to Decimal

❖ 10110b

$$1*2^4+0*2^3+1*2^2+1*2^1+0*2^0=$$

$$16+0+4+2= (22)_{10}$$

1010b =?? , 0010b = ?? , 101b=??

Answer: 1010b=(10)₁₀

0010b=(2)₁₀

101b=(5)₁₀

Decimal to Binary

$$(22)_{10} = ()_2$$

Input	Result	Remainder
22/2	11	0
11/2	5	1
5/2	2	1
2/2	1	0
1/2	0	1



$$(22)_{10} = (10110)_2$$

Decimal to Binary

$$(13)_{10} = (1101)_2$$

$$(220)_{10} = (11011100)_2$$

$$(21)_{10} = (\quad)_2 \text{ H.W}$$

$$(15)_{10} = (\quad)_2 \text{ H.W}$$

Binary to Octal

$$100101010b = ()_8$$

$$100 \ 101 \ 010 = (452)_8$$

$$111000111b = ()_8$$

$$111 \ 000 \ 111 = (707)_8$$

Binary to Octal

$$\ast 100101011b = (453)_8$$

$$\ast 101101011b = (\quad)_8 \quad \text{H.W}$$

$$\ast 100101001b = (\quad)_8 \quad \text{H.W}$$

Binary to Hexadecimal

$$10010101b = (\quad)_h$$

$$1001 \ 0101 \ = (95h)$$

$$11100011b = (E3h) \ H.W$$

Decimal to Hexadecimal

Let's convert the value $(39)_{10}$ to
Hexadecimal

Input	Result	Remainder
39/16	2	7
2/16	0	2



$$(39)_{10} = (27h)$$

H.W

Covert the following numbers to **decimal**

a. $(72)_8 = (58)_{10}$

b. $(72)_{16} = (114)_{10}$

c. $(DE1)_{16} = (3553)_{10}$

Extra Exercises

Using pen and paper , solve the following questions :

a. $(AB)_{16} = (\quad)_2$

b. $(23)_4 = (\quad)_8$

c. $(35)_7 = (\quad)_8$

d. $(72E)_{16} = (\quad)_8$

Binary Addition

$$\begin{array}{r} 0 \\ + 0 \\ \hline \end{array}$$

0

$$\begin{array}{r} 0 \\ + 1 \\ \hline \end{array}$$

1

$$\begin{array}{r} 1 \\ + 0 \\ \hline \end{array}$$

1

$$\begin{array}{r} 1 \\ + 1 \\ \hline \end{array}$$

10

$$\begin{array}{r} 1 \\ + 1 \\ + 1 \\ \hline \end{array}$$

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Binary Addition

$$01111 + 00110 =$$

$$\begin{array}{r} 0 1 1 1 \\ + 0 0 1 0 \\ \hline 1 0 0 \end{array}$$

Binary Addition

H.W

Solve Question 7 ,lab 1 ,page 9

Signed Numbers

Our study of binary arithmetic, we have only considered positive numbers .

What about negative numbers?

Signed Numbers

➤ Signed Magnitude

add an extra digit to the front of our binary number to indicate whether the number is positive or negative.

this digit called sign bit.

0 for positive

1 for negative

Signed Numbers

Example:

$$(5)_{10} = (101)_2$$

Positive 5 is 0 1 0 1

Negative 5 is 1 1 0 1

The Problem : We need to specify how many bits in our numbers so we can be certain which bit is representing the sign !!!



Signed Numbers

1 1 0 1 is 13 or -5

➤ One's Complement

Representing a signed number with 1's

Complement is done by changing all the bits that are 1 to 0 and all bits that are 0 to 1.

Signed Numbers

- ❑ Represent -5 in 1's complement by using 4-bit arithmetic?

0101 → 1010

- ❑ Represent -1 in 1's complement ?

0001 → 1110

Signed Numbers

➤ Two's Complement

2's comp = 1's comp + 1

□ Represent -5 in 2's complement by using 4-bit arithmetic?

(101)_{1's} → 1010

2's + 1

1 0 1 1 = (-5)

H.W

Lab 1 . P8,9

Q.1,2,3,4,8,10

Summary

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Converting from one System to another system & back.

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Signed Numbers

