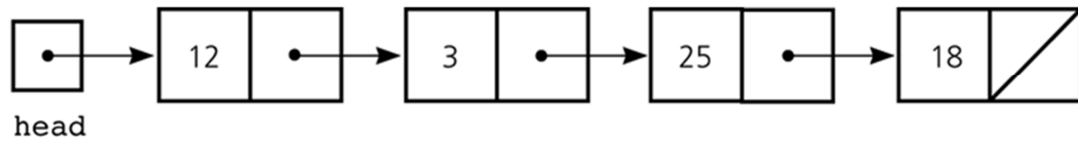




## Linked List

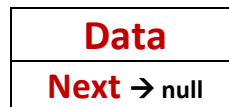
**Algorithm** - abstract way to perform computation tasks

**Data Structure** - abstract way to organize information



**Linked List:**

**Node:**



**Node code:**

```

public class Node<T> {
    private T data;
    private Node<T> next;

    public Node(T data) { this.data = data; }

    public void setData(T data) { this.data = data; }
    public T getData() { return data; }

    public Node<T> getNext() { return next; }
    public void setNext(Node<T> next) { this.next = next; }
}
  
```

**Linked List Code:**

```

public class LinkedList<T> {
    private Node<T> head;
}
  
```

**Inserting a new node:**

Inserting a Node into a Specified Position of a Linked List:

Three steps to insert a new node into a linked list

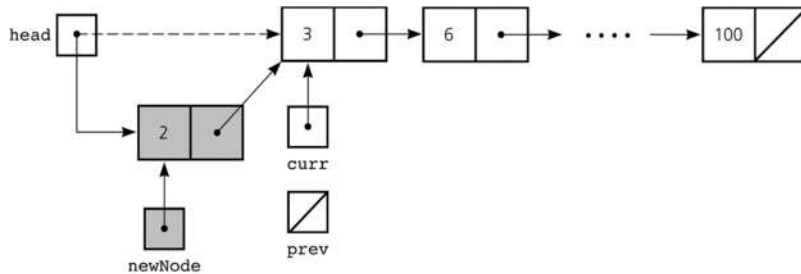
- Determine the point of insertion
- Create a new node and store the new data in it
- Connect the new node to the linked list by changing references





Case 1: To insert a node at the beginning of a linked list: (`curr == head`)

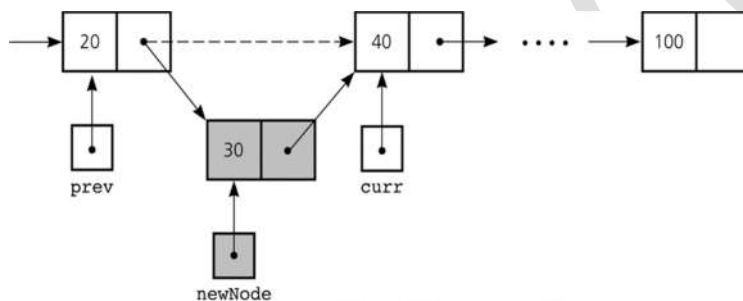
```
newNode.next = head;
head = newNode;
```



What's the time complexity of inserting an item to the head?? → **O(1)**

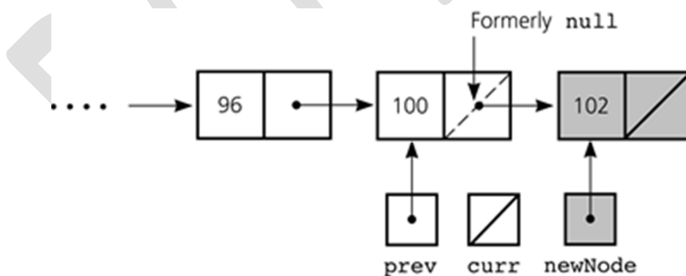
Case 2: To insert a node between two nodes:

```
newNode.next = curr;
prev.next = newNode;
```



Case 3: Inserting at the end of a linked list is a special case if `curr` is `null`:

```
newNode.next = curr;
prev.next = newNode;
```



Time Complexity → **O(n)**

H.W. → implement insert into a sorted linked list

Determining `curr` and `prev`

Determining the point of insertion or deletion for a sorted linked list of objects

```
for ( prev = null , curr = head;
      (curr != null) && (newValue.compareTo(curr.item) > 0);
```





```
prev = curr , curr = curr.next ); // end for
```

Create a driver class to test linked list classes.

Override the **toString** methods first

**Node toString:**

**@Override**

```
public String toString() { return data.toString(); }
```

**LinkedList toString:**

**@Override**

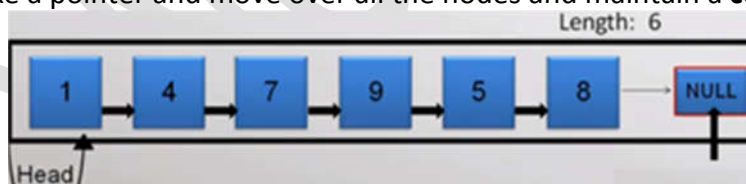
```
public String toString() {
    String res = "→";
    Node<T> curr = head;
    while (curr != null) {
        res += curr + "→ ";
        curr = curr.next;
    }
    return res + "NULL";
}
```

**Length of Linked List?**



**Case 1:** If it's empty:

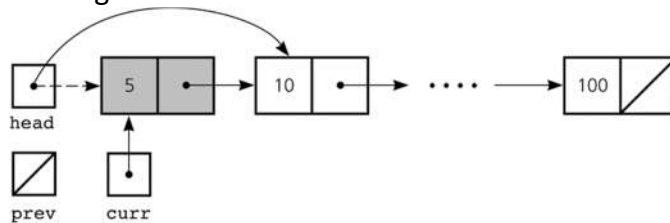
**Case 2:** If not: Make a pointer and move over all the nodes and maintain a **counter**



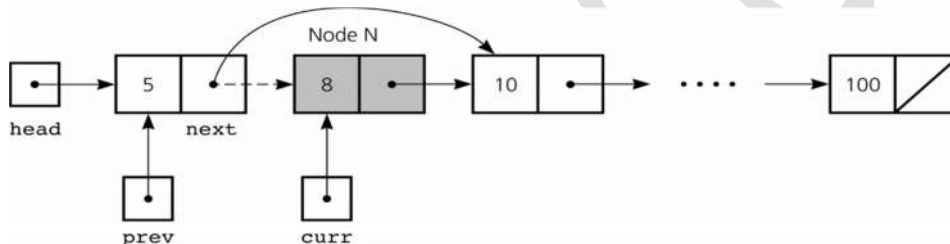
**Length code: Time Complexity →  $O(n)$**

```
public int length() {
    int length = 0;
    Node<T> curr = head;
    while (curr != null) {
        length++;
        curr = curr.next;
    }
    return length;
}
```



**Deleting Nodes:****Case 1: Deleting the head node:**Simply move the **head** to the **head.next**: `head = head.next;`Now first Node has no reference to it → **Garbage**Time Complexity → **O(1)****Delete at head code:** // make sure linked list is not empty

```
public Node<T> deleteAtStart() {
    Node<T> toDel = head;
    head = head.next;
    return toDel;
}
```

**Case 2: Delete node N which curr references:**Set **next** in the node that precedes **N** to reference the node that follows **N**`prev.next = curr.next; // prev.next = prev.next.next;`**Searching for an Item in a Linked List:**Time Complexity: linear growth → **O(n)**

Find code:

```
public Node<T> find(T data) {
    Node<T> curr = head;
    while (curr != null) {
        if (curr.getData() == data) // if (curr.getData().equals(data))
            return curr;
        curr = curr.next;
    }
    return null;
}
```

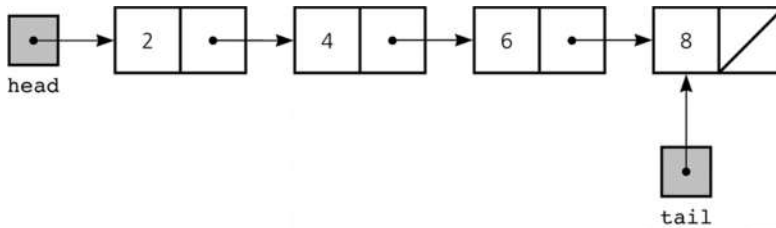


## Variations of the Linked List:

### 1- Tail References (Doubly Ended Linked List)

- Remembers where the end of the linked list is.
- Therefore, we can add and delete at both ends.
- To add a node to the end of a linked list

`tail.next = new Node(request, null);`



```
public class DoubleEndedList<T> extends LinkedList<T> {
    private Node<T> tail;
    public Node<T> getTail() { return tail; }

    public void addAtEnd(T data) {
        Node<T> newNode = new Node<T>(data);
        if (head == null) { // empty
            head = newNode;
            tail = newNode;
        }
        else {
            tail.setNext(newNode);
            tail = newNode;
        }
    }
}
```

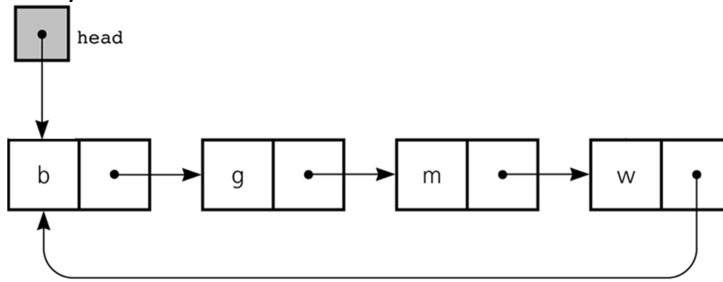
**Make sure to override addAtStart to set the tail pointer correctly:**

```
@Override
public void addAtStart(T data) {
    Node<T> newNode = new Node<T>(data);
    if (head == null) { // empty
        head = newNode;
        tail = newNode;
    }
    else{
        newNode.setNext(head);
        head = newNode;
    }
}
```



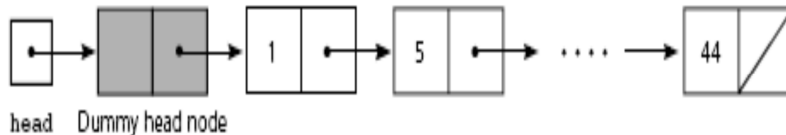
## 2- Circular Linked List

- Last node references the first node
- Every node has a successor



## 3- Dummy Head Nodes

- Always present, even when the linked list is empty
- Insertion and deletion algorithms initialize **prev** to reference the dummy head node, rather than **null**



## Processing Linked Lists Recursively:

### • Traversal

- Recursive strategy to display a list
  - Write the first node of the list
  - Write the list minus its first node

```
public static void traversList(Node curr) {
    if(curr == null)
        System.out.println("NULL");
    else {
        System.out.print "[" + curr + "-->";
        traversList(curr.next);
    }
}
```

- Recursive strategies to display a list backward
  - writeListBackward strategy
    - Write the last node of the list
    - Write the list minus its last node backward

```
public static void traversListBackward(Node curr) {
    if(curr == null)
        System.out.print("NULL");
    else {
        traversListBackward(curr.next);
        System.out.print("<--[ " + curr + "]");
    }
}
```



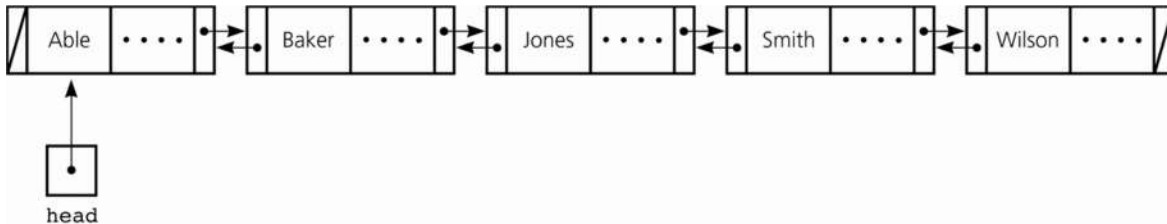


## Doubly Linked List

Node:

<b>Date</b>
<b>Next</b> → null
null ← <b>Prev</b>

**Doubly Linked List:** Each node references both its predecessor and its successor:



**Doubly Node Code:**

```
public class DNode <T extends Comparable<T>>{
    T data;
    DNode next;
    DNode prev;

    public DNode(T data) { this.data = data; }
    public T getData() { return data; }
    public DNode getNext () { return next; }
    public DNode getPrev () { return prev; }

    public void setNext(DNode next) { this.next = next; }
    public void setPrev(DNode prev) { this.prev = prev; }
    public String toString() { return this.data.toString(); }
}
```

**Doubly Linked List code:**

```
public class DLinkedList <T extends Comparable<T>>{
    DNode head;
}
```

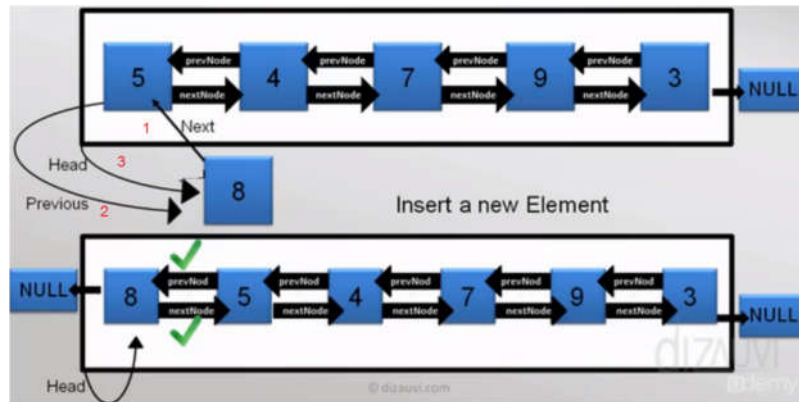
**Override toString method code:**

```
public String toString() {
    String res = "Head-->";
    DNode<T> curr = this.head;
    while (curr != null) {
        res += "["+curr + "]";
        curr = curr.getNext();
        if(curr!=null)
            res += "<=>";
    }
    return res + "-->NULL";
}
```



**Insert a new node (not sorted)**

Case 1: Insert at head:



```

public void insertAtHead(T data) {
    DNode<T> newNode = new DNode(data);
    if(head==null) // empty linkedlist
        head = newNode;
    else {
        newNode.setNext(this.head);
        head.setPrev(newNode);
        head = newNode;
    }
}

```

Case 2: Insert at end:

**Student Activity: insert at last**

```

public void insertAtEnd(T data) {
    DNode<T> newNode = new DNode(data);
    if (head == null) // empty linkedlist
        head = newNode;
    else { // find last node
        DNode<T> last = head;
        while(last.getNext() != null)
            last = last.getNext();
        last.setNext(newNode);
        newNode.setPrev(last);
    }
}

```

Length of a doubly linked list code:

```

public int length() {
    int length = 0;
    DNode<T> curr = this.head;
    while (curr != null) {
        length++;
        curr = curr.getNext();
    }
    return length;
}

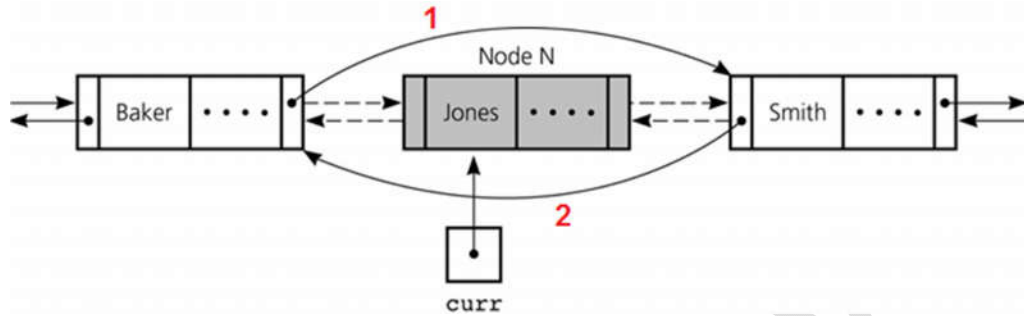
```





**Delete a node:**

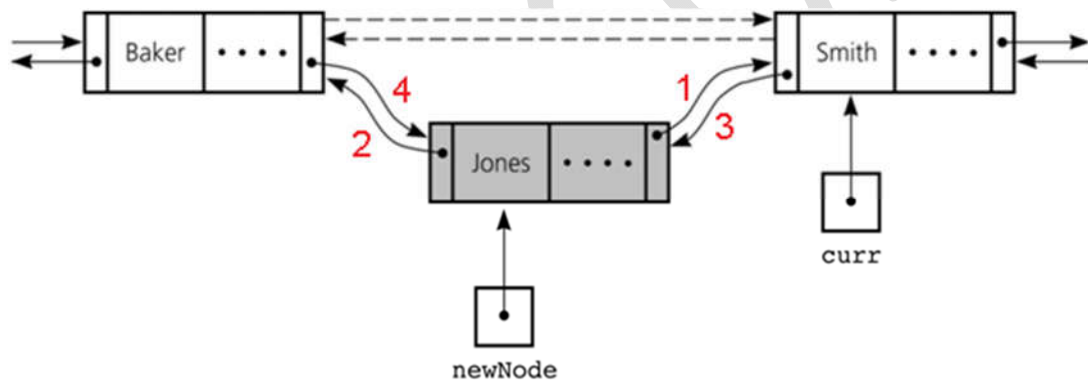
- To delete the node that **curr** pointer references



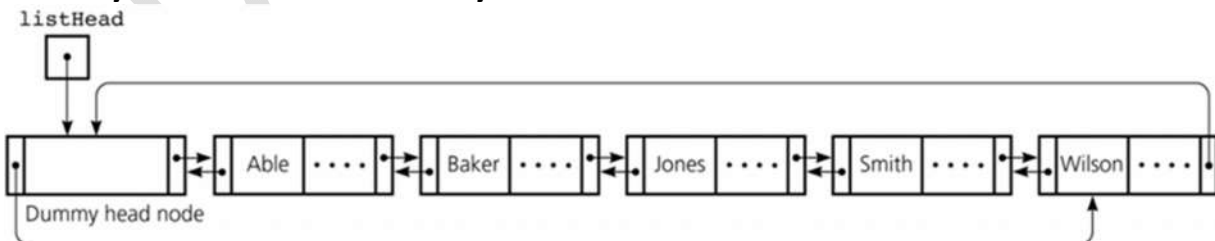
```
curr.prev.next = curr.next;
curr.next.prev = curr.prev;
```

**Insert a new Node (Sorted):**

- To insert a new node that **newNode** references before the node referenced by **curr**



```
newNode.next = curr; // 1
newNode.prev = curr.prev; // 2
curr.prev = newNode; // 3
newNode.prev.next = newNode; // 4
```

**Circular doubly linked list with dummy head:**

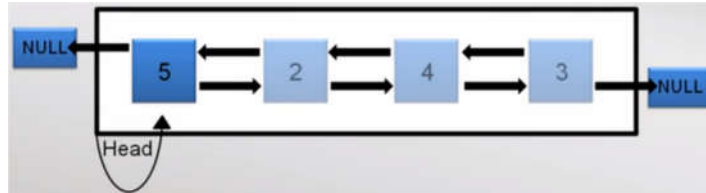
- Preceding reference of the dummy head node references the last node.
- next reference of the last node references the dummy head node.
- **Eliminates special cases for insertions and deletions.**



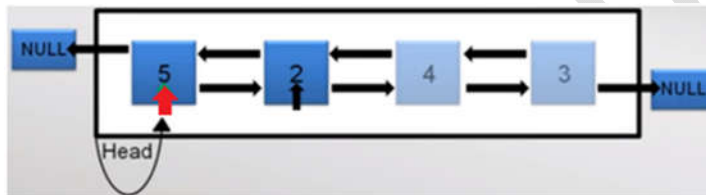
### Case Study: Insertion Sort using doubly linked list (Using NO extra space):

**Review insertion sort logic and point to problem of insertion and time needed to shift the items  
Worst case if the array is reverse sorted**

**Example:** assume we need to sort the following doubly linked list:



**Assumption:** 1<sup>st</sup> node is sorted. We start from the 2<sup>nd</sup> element:



**Here:**

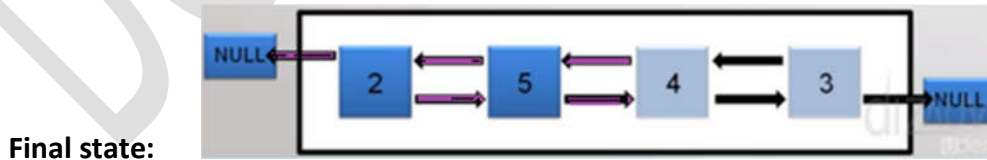
- The **black** pointer points to the **current** node to be sorted.
- The **red** pointer points to previous node of **current** node to be sorted.
- The **green** pointer points to next node of **current** node to be sorted.

**Step 1:** The **red** pointer keeps move backward until it reaches a node which has a value **smaller** than the **current** node **OR** reach **NULL**.

**Step 2:** the **current** item will be inserted after **red** pointer as follow:

**Make sure you maintain references correctly.**

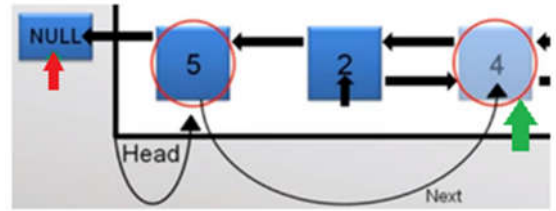
**To do so draw the expected outcome and follow the steps to change the pointers:**



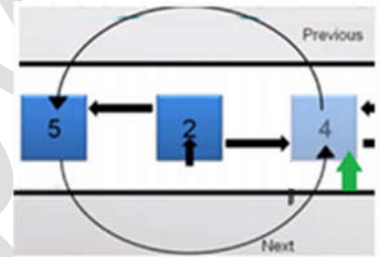
#### Case 1: insert to head

Step 2.0: make new **green** pointer = **black.next**

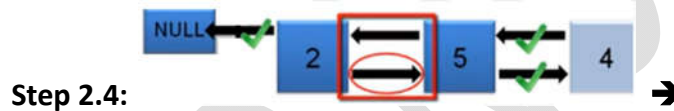
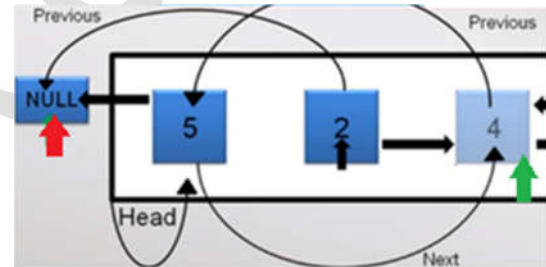




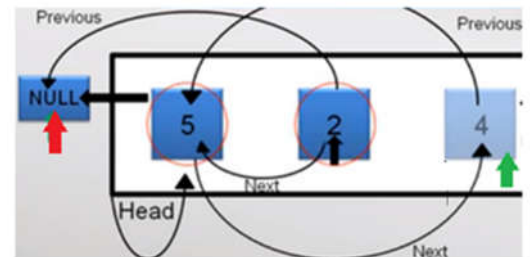
if (**green** != null) **green**.prev = black.prev



black.prev = **red**

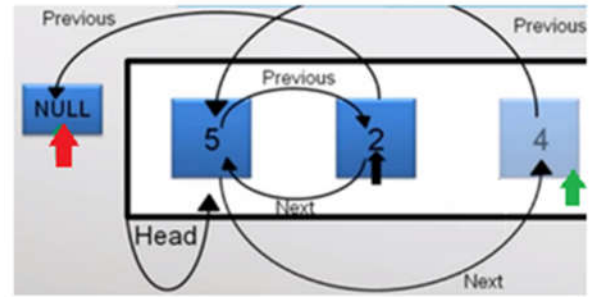


if (**red** == null) black.next = black.next.prev  
else  
black.next = **red**.next



If (**red** == null) black.next.prev = black  
else  
**red**.next.prev = black



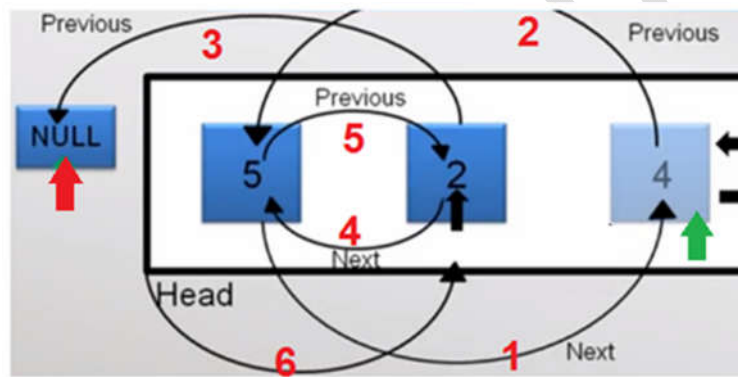


Step 2.6:

```

if (red == NULL) head = black;
else red.next = black;

```

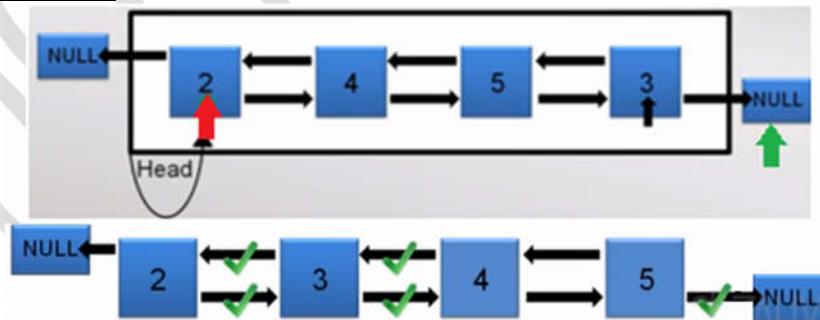


Step 2.7: black = green

Case 2: insert 4 in the middle

Practice yourself

Case 3: insert last element





## Insertion Sort Code:

```
// Insertion Sort of a Doubly Linked List
public void sort() {
    DNode black = head.next;
    while (black != null) {
        DNode red = black.prev;
        while (red != null && (red.data.compareTo(black.data) > 0)) // step 1.0
            red = red.prev;

        DNode green = black.next; // step 2.0
        if (red != null || (head != black)) {
            black.prev.next = green; // step 2.1
            if (green != null) {
                green.prev = black.prev; // step 2.2
            }
            black.prev = red; // step 2.3
        }
        if (red == null) { // set the black as head
            if (head != black) {
                black.next = head; // step 2.4
                black.next.prev = black; // step 2.5
                head = black; // step 2.6
            }
        } else { // red is not null
            black.next = red.next; // step 2.4
            red.next.prev = black; // step 2.5
            red.next = black; // step 2.6
        }
        black = green; // step 2.7
    }
}
```

