## COMP2321—DATA STRUCTURES

### **Heaps (Priority Queue)**

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### Heaps (Priority Queue)

- Queues are implemented under the FIFO principle.
- The first element to come in, the first element to be served.
- However, there has to be a scheme for cases in which there are some priorities.

## Heaps (Priority Queue)

- Take an example a queue system for printers.
- The first print job to come in is the first to be printed.
- Imagine you are printing a 2-paper report but unfortunately there are a few jobs that have been enqueued before. Each of these jobs of thousands of pages!
- This means you have to wait until all jobs have been finished.

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## Heaps (Priority Queue)

- There has to be a method so that short jobs to finish as fast as possible. These jobs have higher precedence over jobs that have already been running.
- However, some (not short) jobs are still important and they should have higher precedence in some cases! The Heaps data structures is a special kind of queue (called Priority Queue).
- Heaps use Binary Search Tree (BST) implementation. This gives O(log n) average running time for both operations.

### MinHeap / MaxHeap

- MinHeap: a Binary Search Tree such that the data in each node is less than or equal to the data in the nodes' children.
- In MinHeap, the root is the minimum value in the tree.
- In the MaxHeap, the root is the maximum value in the tree.

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### Heaps (Priority Queue)

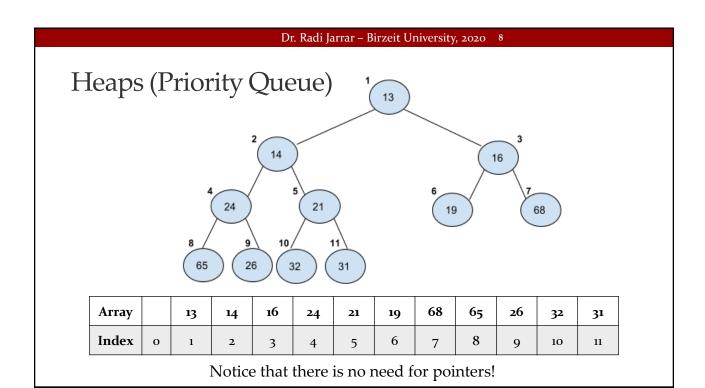
- There are two basic operations in Heaps:
  - 1. Insert (enqueue)
  - 2. DeleteMin (or max) (dequeue): finds, return, and delete the minimum element in the priority queue

### Heaps (Priority Queue)

- Heap Data Structure: it is an array that can be viewed as Binary Search Tree. It may also be called Binary Heaps.
- For any element at position i:

$$Parent(i) = i/2$$

= 2i + 1 right



## Heap Order Property

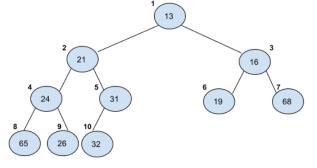
- Goal: find the min value quickly.
- It makes sense to have the minimum value at the root as we always delete min.
- Any node should be smaller than any of its descendants.
- For every node X, the key in the parent of X is smaller than (or equal to the key in X.

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### Heaps - Example

• Insert(14) to the following MinHeap.

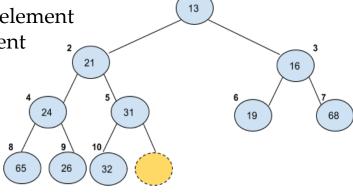
1. Find the next available spot in the tree to insert a new node

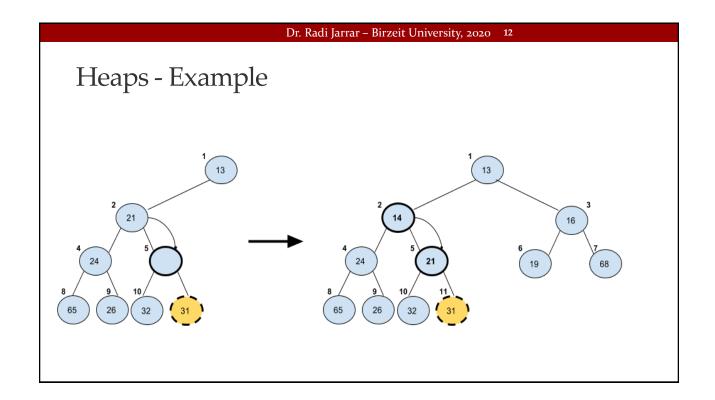


## Heaps - Example

2. If X can be placed without violating the rule of heaps, then done.

3. Otherwise, slide the element that is in the hole's parent node into the hole.

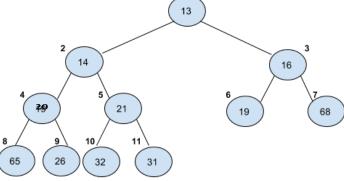




## Heaps - Example

• Delete: We can delete either the min or max values. In our case, it is the min as we are operating on MinHeap.

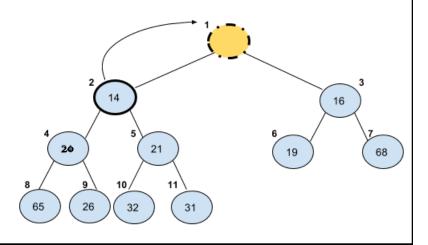
 Example: Delete() from the MinHeap in the following heap



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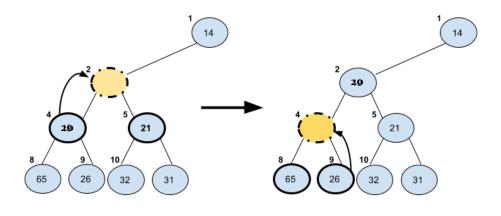
## Heaps - Example

1. Find min and remove it. Keep a hole in its place (root).



## Heaps - Example

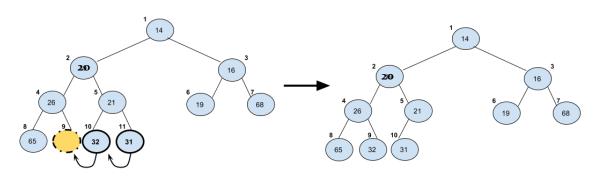
2. Push the smaller of the children up.



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## Heaps - Example

2. Slide the elements on the right to the left to fill the empty spot.



## **Applications**

- Priority queue.
- Heap sort: sorting data using heaps.
- Selection of min/max from a set of data in O(1) time.
- Graph algorithms: heaps are used in graph algorithms like implementing Dijkstra's algorithm.

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# Running time

	Insert	DeleteMin	FindMin
Binary Heap	O(log n)	O(log n)	O(1)