



Computer Science Department

Worksheet - COMP233

- 1- Let  $C = \{n \in \mathbf{Z} \mid n = 6r - 5 \text{ for some integer } r\}$  and  $D = \{m \in \mathbf{Z} \mid m = 3s + 1 \text{ for some integer } s\}$ .  
Prove or disprove  $C=D$ .
- 2- Let  $A = \{1, 3, 5, 7, 9\}$ ,  $B = \{3, 6, 9\}$ , and  $C = \{2, 4, 6, 8\}$ .  
Find each of the following:  

a. $A \cup B$	b. $A \cap B$	c. $A \cup C$	d. $A \cap C$
e. $A - B$	f. $B - A$	g. $B \cup C$	h. $B \cap C$
- 3- Let  $C_i = \{i, -i\}$  for all nonnegative integers  $i$ .  
Find
  - a.  $\bigcup_{i=0}^4 C_i$
  - b.  $\bigcap_{i=0}^4 C_i$
  - c. Are  $C_0, C_1, C_2, \dots$  mutually disjoint?
  - d.  $\bigcup_{i=0}^{\infty} C_i$
  - e.  $\bigcap_{i=0}^{\infty} C_i$
- 4- Use an element argument to prove the following statement  
For all sets  $A$  and  $B$ ,  $(A \cap B) \cup (A \cap B^c) = A$
- 5- Prove for all sets  $A$  and  $B$ ,  $(A \cap B) \cap (A \cap B^c) = \emptyset$ .
- 6- Prove or disprove for all sets  $A$ ,  $B$ , and  $C$ ,  $(A \cap B) \cup C = A \cap (B \cup C)$ .
- 7- Construct an algebraic proof for the given statement. Cite a property from Theorem 6.2.2 for every step. For all sets  $A$ ,  $B$ , and  $C$ ,  
 $(A \cap B) \cup C = (A \cup C) \cap (B \cup C)$ .