

94
106

051 →
01

Name: Ali Samar
COMP 439

Number: 1090604
20-11-2012

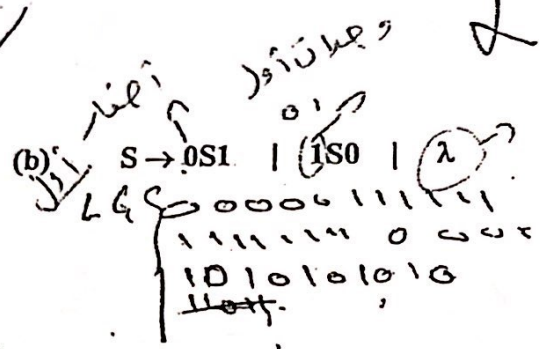
Midterm Exam

[1] Describe the language generated or accepted by the following CFG and FSAs:

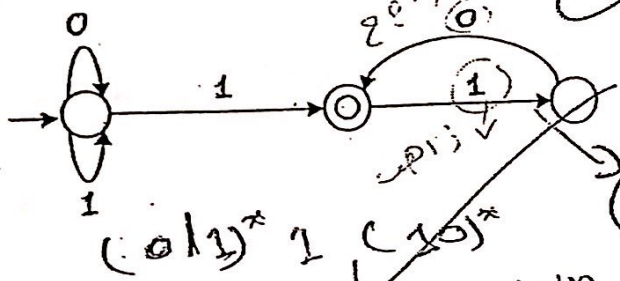
(a) $S \rightarrow OS1 \mid \lambda$

$L(S) = \{0^n 1^n \mid n \geq 0\}$

any string of a's and b's start and end with a or b

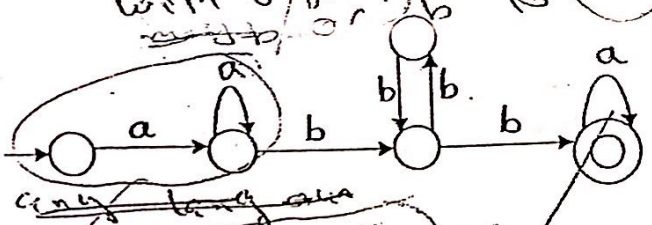


any string contains 0's or 1's in the same number and if it start with 0 it must end with 0 or if it start with 1 it must end with 1



(ii)
Concatenate
المركب

(d)



at $(b(bb)^* b a^*$

any string start with a and it contains b's or a's and must end with b or a

at $(a(a)^* b(bb)^* b a^*$

[2] Given the grammar,

$$E \rightarrow E+T \mid T$$

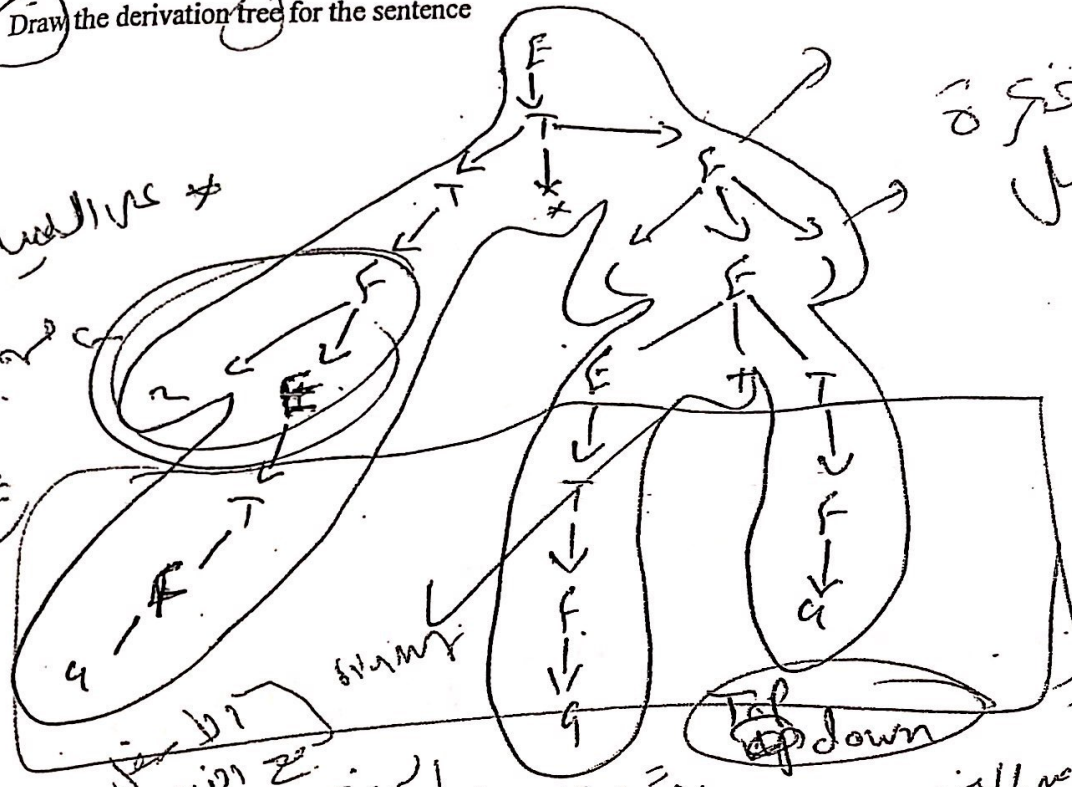
$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid a \mid \sim E$$

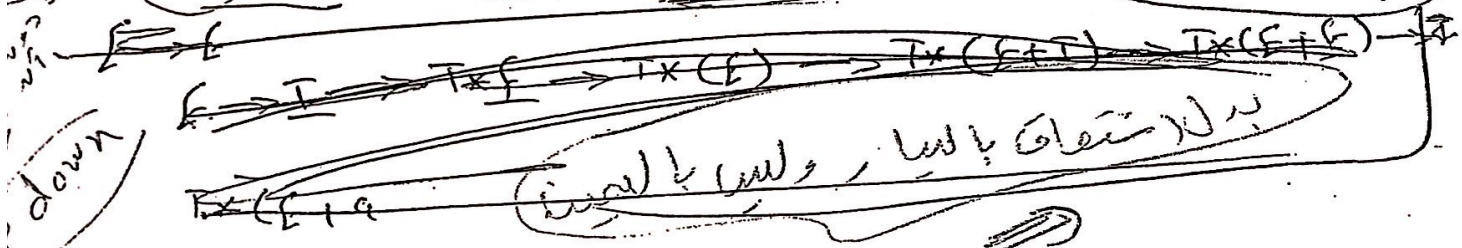
Given the sentence $\sim a^*(a+a)$

ترجم الى العربي

(a) Draw the derivation tree for the sentence

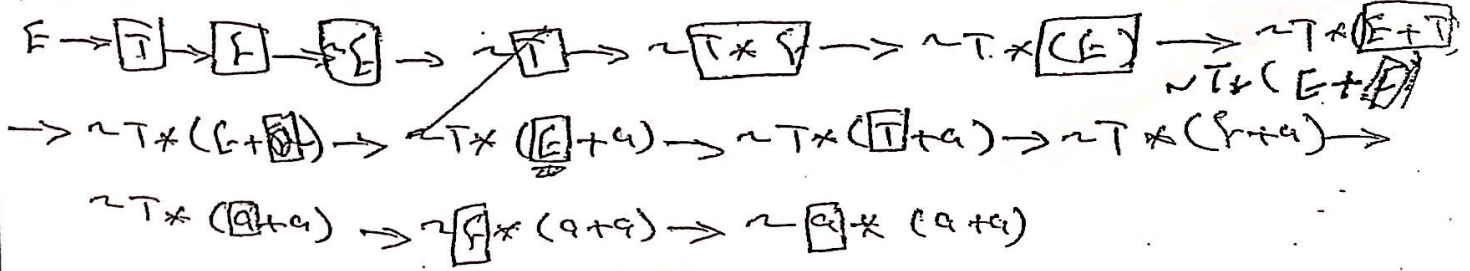


(b) In bottom-up parsing, show the handle in each reduction step.



$E \rightarrow T \rightarrow F \rightarrow \sim E \rightarrow \sim T \rightarrow \sim T * F \rightarrow T * (E) \rightarrow$
 $\sim T * (E + T) \rightarrow \sim T * (E + F) \rightarrow \sim T * (E + a) \rightarrow T * (T + a) \rightarrow$
 $\sim T * (F + a) \rightarrow \sim T * (a + a) \rightarrow a * (a + a)$

The handle



5] (a) Given a sample program (sentence) in some programming language $L(G)$ where:
 $V_T = \{var, int, exit, exp, ;, =, [,]\}$

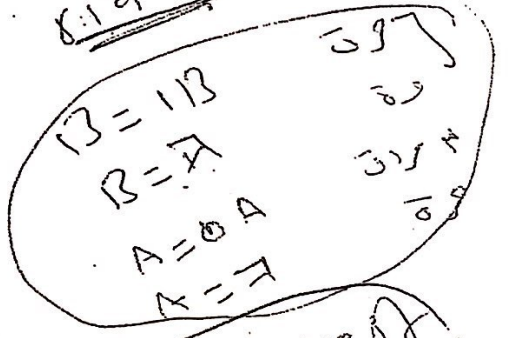
```

var
  int name;
  int name;
  ...
  [ name = exp;
    name = exp;
    {
      name = exp;
    }
  ] exit
  
```

block

Dec it me

right most



Write down the production rules P, that generates this language.

$prog \rightarrow decl \text{ Main } exit$

$decl \rightarrow Var \text{ decl-list}$

$decl-list \rightarrow decl-item \text{ more-decl}$

$decl-item \rightarrow type \text{ var-name}$

$main \rightarrow [stmt-list]$

$stmt-list \rightarrow stmt ; stmt-list \mid \lambda$

$stmt \rightarrow var-name = exp$

$var-name \rightarrow name$

$type \rightarrow int$

(b) Given the CFG:

$S \rightarrow AIB$

$A \rightarrow 0A \mid \lambda$

$B \rightarrow 1B \mid \lambda$

(i) Define $L(G)$?

$L(G) = \{ 0^m 1^n \mid m \geq 0, n \geq 1 \}$

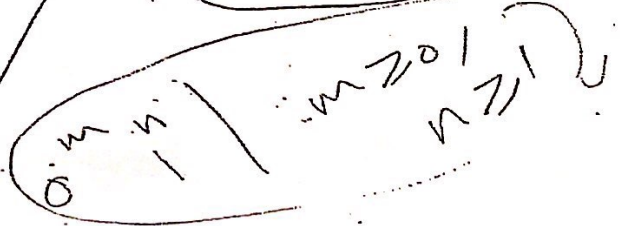
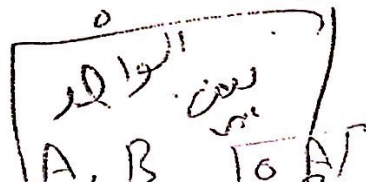
(ii) Show a leftmost and a rightmost derivation for the sentence 00011

Leftmost derivation: $S \xrightarrow{Lm} AIB \xrightarrow{Lm} 0AIB \xrightarrow{Lm} 00AIB \xrightarrow{Lm} 000AIB \xrightarrow{Lm} 000\lambda B \xrightarrow{Lm} 0001B \xrightarrow{Lm} 00011$

Rightmost derivation: $S \xrightarrow{rm} AIB \xrightarrow{rm} A1B \xrightarrow{rm} A11 \xrightarrow{rm} 0A11 \xrightarrow{rm} 00A11 \xrightarrow{rm} 000A11 \xrightarrow{rm} 000\lambda 11 \xrightarrow{rm} 00011$

B=7

right most



4) Given the following DFSA.

Reduce it to FSA with minimum states using tabular methods.

- Draw the final FSA.
- The underline states are final states.

1 way \rightarrow 2

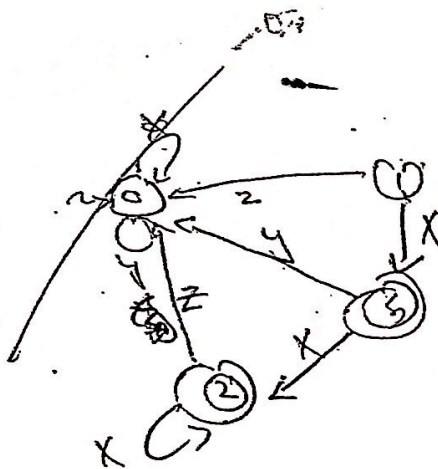
δ	x	y	z
0	3	3	
1	5		4
2	6		4
3	3	4	
4	0	4	
5	6	3	
6	2		

	x	y	z
(2,6)	(2,6)		(4,4)
(0,3)	(3,3)	(3,4)	
(0,4)	(3,0)	(3,4)	
(3,4)	(3,0)	(3,4)	

so $2 \equiv 6$ $0 \equiv 3 \equiv 4$

- new state

	x	y	z
0	0	0	
1	5		0
2	2		0
5	2	0	

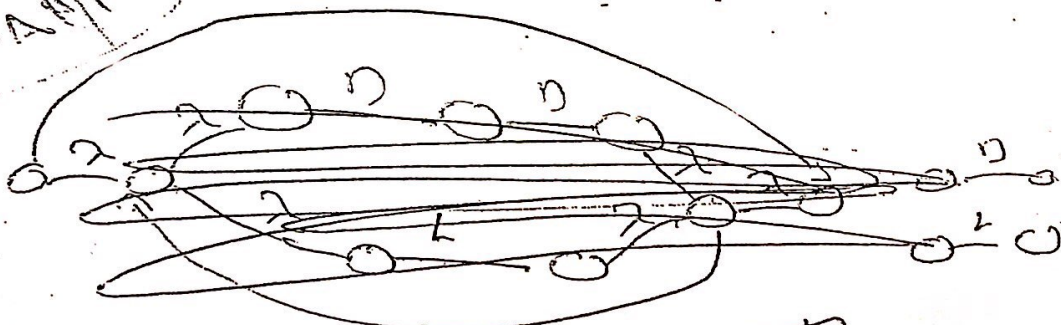


but this state unaccessible

(b) Draw a FSA that accepts regular expression

$L (DD | L)^* (D | L)^* \epsilon$

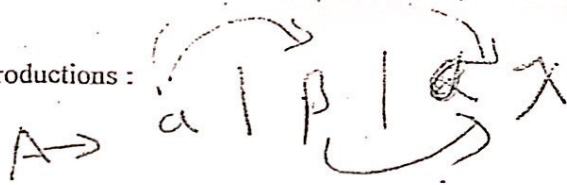
FSA (1)



0 for L's \rightarrow initial state

[5] (a) Given the grammar G with productions:

- $A \rightarrow \alpha$
- $A \rightarrow \beta$
- $A \rightarrow \lambda$

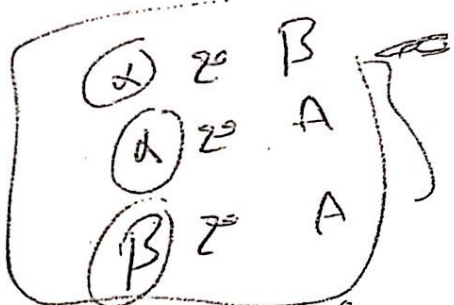


State explicitly the conditions so that the above grammar is LL(1).

to be LL(1) according to formal definition is

LL(1) conditions

- (1) $FIRST(\alpha) \cap FIRST(\beta) = \emptyset$
- (2) $FIRST(\alpha) \cap FOLLOW(A) = \emptyset$
- (3) $FIRST(\beta) \cap FOLLOW(A) = \emptyset$



$FIRST(A) = \{ \alpha, \beta, \lambda \}$

(b) Given the grammar G,
 $S' \rightarrow SS$
 $S \rightarrow (L) | a$
 $L \rightarrow SA$
 $A \rightarrow (SA) | \lambda$

Using the formal definition only, Examine if G is LL(1)?
 Do you think it is LL(2)? Use the formal definition only.

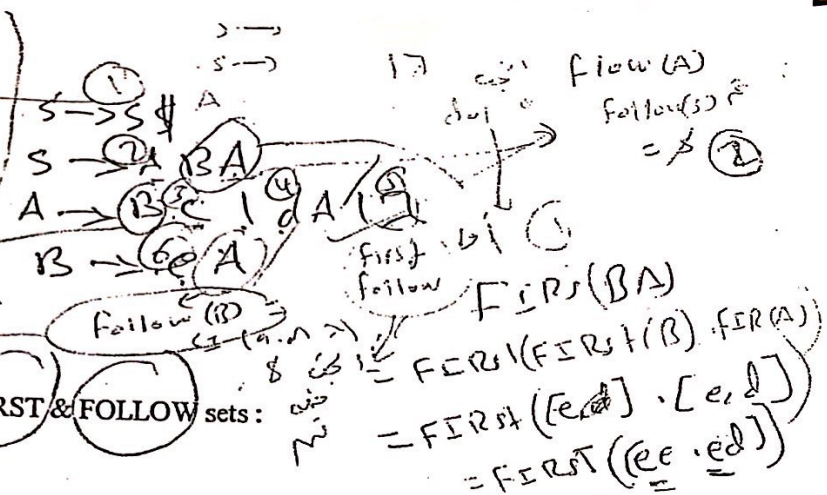
for LL(1):
 $FIRST((L)) \cap FIRST(a) = \{ (\} \cap \{ a \} = \emptyset$
 $FIRST((SA)) \cap FOLLOW(A) = \{ (\} \cap \{ ',) \} = \emptyset$

because it is LL(1) so it is LL(2) let see it LL(2)

for LL(2):
 $FIRST_2((L)) \cap FIRST_2(a) = \{ (\} \cap \{ a \} = \emptyset$
 $FIRST_2((SA)) \cap FOLLOW_2(A) = \{ (, a \} \cap \{ ',) \} = \emptyset$

Consider the grammar:

- (1) $S' \rightarrow SS$
- (2) $S \rightarrow ABA$
- (3) $A \rightarrow Bc$
- (4) $A \rightarrow dA$
- (5) $A \rightarrow \lambda$
- (6) $B \rightarrow eA$



(a) Fill in the table below with FIRST & FOLLOW sets:

	FIRST	FOLLOW
S'	c, d	-
S	e, d, λ	λ
A	e, d, λ	c, e, d, λ
B	e	c, e, d, λ

(b) Fill in the LL(1) parsing table

	c	d	e	λ
S'		1	1	1
S		2	2	
A	3	4	3	5
B			6	

$FIRST(A) = \{FIRST(B), d, \lambda\}$
 $FOLLOW(A) = \{c, e, d, \lambda\}$

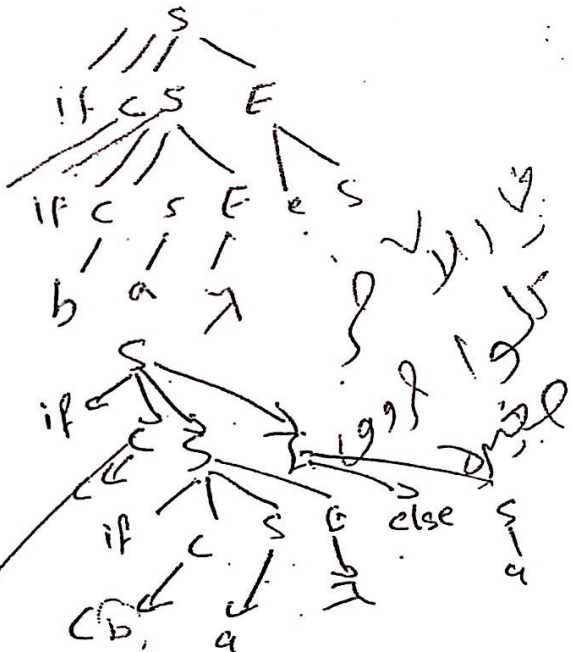
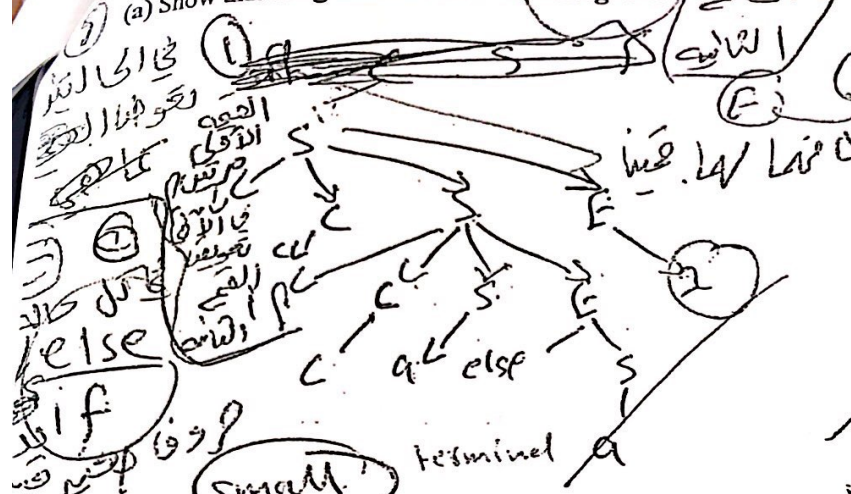
$FIRST(S) = \{c, e, d, \lambda\}$
 $FOLLOW(S) = \{\lambda\}$

$S \rightarrow ABA$

$FOLLOW(A)$
 $FOLLOW(S)$

The grammar for the if...else... structure can be given as:
 $S \rightarrow \text{if } C S E \mid \dots$
 $E \rightarrow \dots$
 $C \rightarrow b \mid a$

(a) Show that the grammar above is ambiguous.



ambiguous because we can build two derivation tree for the same ~~string~~ entrance

1) $\text{follow}(E) = \text{follow}(S)$
 $\text{follow}(E) = \text{FIRST}(E) \cup \text{follow}(E)$

(b) Build the LL(1) parsing table. Is the grammar LL(1)? why? How can you fix the problem without changing the grammar structure? Explain.

	if	b	a	else
S	1		1	
E				3, 4
C		5		

$C \rightarrow b$
 $C \rightarrow a$

2) The grammar is not LL(1) because there is conflict

we can avoid this problem by ~~the~~ constant ~~the~~ else for nearest if ~~the~~ multiple production
 Grammar multiple production

Name: Jamal Abed Alnaser

Number: 11020410

COMP 439 / AL Gharaybiel Midterm Exam

11-04-2013

[1] Reduce the following NDFSA to DFSA with fewest states using tabular methods:

	a	b	λ
1	2,4	3	2,3
2	4		2
3	2	3	
④	2,4	3,4	1,2,3
⑤	2,4	3,4	
⑥	2,4	3,4	

δ	a	b	λ
1	2		2,3
2	4		2
3	2	3	
④		4	1

final

final

$(2,4) \equiv 5$
 $(3,4) \equiv 6$

Node

	a	b
1	4,5	3
2	4	
3	2	3
④	4,5	6,4
⑤	5	6
⑥	5	6

$(1,2,3)$ ✓
 $(1,2)$ ✗ $(1,3)$
 $(2,3)$ ✗
 $(4,5,6)$ ✓
 $(4,5)$ ✗ $(4,6)$
 $(5,6)$ ✓

reduce

	a	b
(1,3)	(5,2)	(3,3)
(4,5)	(5,5)	(6,6)
(4,6)	(5,5)	(6,6)
(5,6)	(5,5)	(6,6)

$4 \equiv 5 \equiv 6$

$5,6$
 $(4 \leftarrow 5,6)$

3, 4, 5, 6
 1, 2, 3, 4, 5, 6

(a) In some programming language, the structure of the CASE statement as follows:

case variable-name of
 int-value : statement ;
 int-value : statement ;

int-value : statement ;
 else: statement ;

end

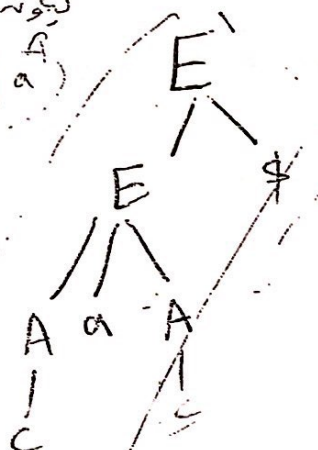
Write down the production rules that generate the CASE statement above. (words in bold are reserved words)

Programme \rightarrow ~~declaration~~ "case of" "else" "end"
 declaration \rightarrow decl item ; declarations
 decl item \rightarrow type name-list
 type \rightarrow "int" | "float"
 name-list \rightarrow ~~more-names~~ | "UDN" more names
 more names \rightarrow name-list
 case of \rightarrow ~~statement~~ ; statement ; statement list
 statement \rightarrow "type" - value : statement
 else
 "end"

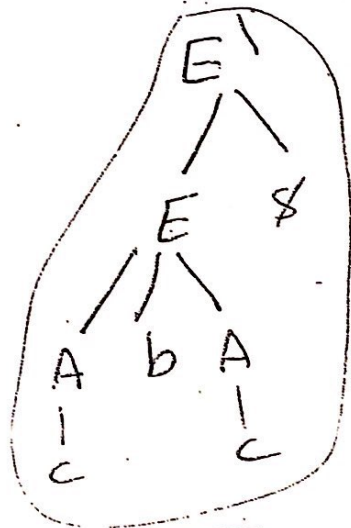
(b) Do you think the following grammar is ambiguous?

$E' \rightarrow ES$
 $E \rightarrow AaA \mid a$
 $E \rightarrow AbA$
 $A \rightarrow c$

[ac\$]



not ambiguous grammar



[cbcs\$]

Given the grammar G below:

$$A' \rightarrow AS$$

$$A \rightarrow xA \mid yA \mid y$$

$$FIRST(A) = [x, y]$$

$$FIRST(A') = (x, y)$$

$$follow(A) = [\$]$$

(a) Using the formal definition only, Examine if G is LL(1)

$$FIRST(xA) \cap FIRST(yA)$$

$$= [x] \cap [y] = \emptyset$$

$$FIRST(xA) \cap FIRST(y)$$

$$[x] \cap [y] = \emptyset$$

$$FIRST(yA) \cap FIRST(y)$$

$$= [y] \neq \emptyset$$

is not LL(1) grammar.

(b) Using the formal definition only, Examine if G is LL(2)

$$FIRST_2(xA) \cap FIRST_2(yA)$$

$$= [xx, xy] \cap [yx, yy] = \emptyset$$

$$FIRST_2(xA) \cap FIRST_2(y)$$

$$= [xx, xy] \cap [y] = \emptyset$$

$$FIRST_2(yA) \cap FIRST_2(y)$$

$$= [yx, yy] \cap [y\$]$$

$$= \emptyset$$

G is LL(2) grammar

(c) If we replace the production $A \rightarrow y$ by $A \rightarrow \lambda$, How this will affect (a) and (b)?

$$A' \rightarrow AS$$

$$A \rightarrow xA \mid yA \mid \lambda$$

$$follow(A) = [\$]$$

$$follow_2(A) = [\$ \$]$$

$$FIRST(A) = [x, y, \lambda]$$

$$FIRST(A') = [x, y, \$]$$

LL(1) \Rightarrow LL(2)

$$FIRST(xA) \cap FIRST(yA)$$

$$[x] \cap [y] = \emptyset$$

$$FIRST(xA) \cap follow(A)$$

$$[x] \cap [\$] = \emptyset$$

$$FIRST(yA) \cap follow(A)$$

$$[y] \cap [\$] = \emptyset$$

G is LL(1) grammar

$$FIRST_2(xA) \cap FIRST_2(yA)$$

$$= [xx, xy] \cap [yx, yy] = \emptyset$$

$$FIRST_2(xA) \cap follow_2(A)$$

$$[xx, xy] \cap [\$ \$] = \emptyset$$

$$FIRST_2(yA) \cap follow_2(A)$$

$$= [yx, yy] \cap [\$ \$] = \emptyset$$

G is LL(2) grammar

Consider the grammar:

- (1) $S' \rightarrow SS$
 (2) $S \rightarrow [SX]$ (3) $S \rightarrow a$
 (4) $X \rightarrow +SY$ (5) $X \rightarrow Yb$ (6) $X \rightarrow \lambda$
 (7) $Y \rightarrow -SXc$ (8) $Y \rightarrow \lambda$

(a) Fill in the table below with FIRST & FOLLOW sets :

	FIRST	FOLLOW
S'	[, a	=
S	[, a	, +, -, b,] c
X	+ , - , b ,]	,] c
Y	- ,]	b,] c

(b) Fill in the LL(1) parsing table

	a	b	c	+	-	[]	S
S'	1					1		
S	3					2		
X		4	5			6	5	
Y		8	7			8		

(c) Is the above grammar LL(1) ? why ? If so, Show how to parse the sentence [a+a]

1) $FIRST([SX]) \cap FIRST(a)$
 $= [] \cap [a] = \emptyset$

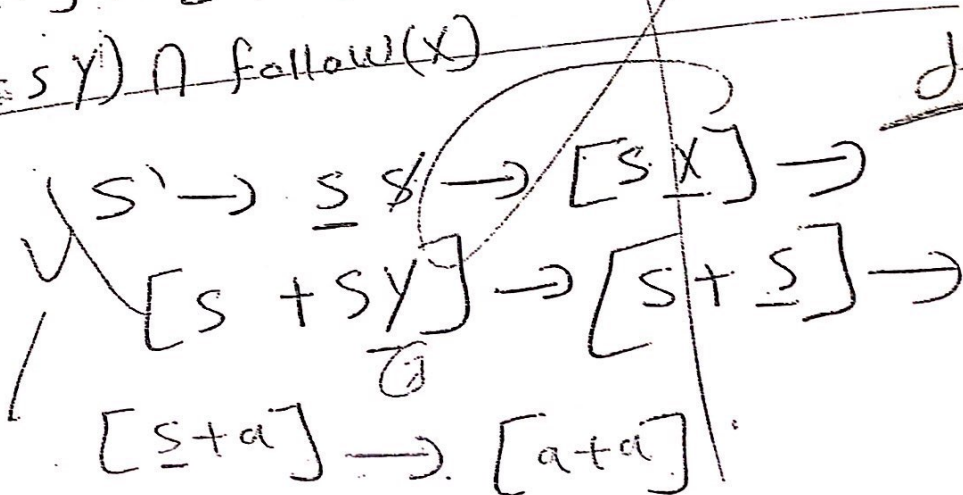
2) $FIRST(+SY) \cap FIRST(Yb)$
 $= [+] \cap [- ,]] = \emptyset$

3) $FIRST(+SY) \cap FOLLOW(X)$

not is LL(1) grammar

because exist multiple entries.

4) FIRST



(a) Given the languages $L = \{aa, \lambda\}$, $M = \{b, cc\}$ defined over $V_T = \{a, b, c\}$

(i) Compute $L^2 M$

$$L^2 M = \{aaaa, aa, aa, \lambda\} \cdot \{b, cc\}$$

$$(aa, \lambda) (aa, \lambda)$$

$$L^2 = \{aaaa, aa, aa, \lambda\}$$

$$= \{aaaab, aab, aab, b, aaaaacc, aaacc, aaacc, cc\}$$

(ii) Compute $L^2 \phi$

$$L^2 \phi = \phi$$

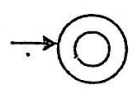
(iii) Compute $L^2 \{\lambda\}$

$$= \{aaaa, aa, aa, \lambda\} \cdot \{\lambda\}$$

$$= \{aaaa, aa, aa, \lambda\} = L^2$$

(b) What is the language recognized by the following FSA:

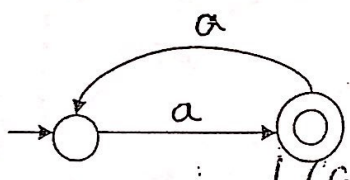
(i)



$$L(G) = \{a\}$$

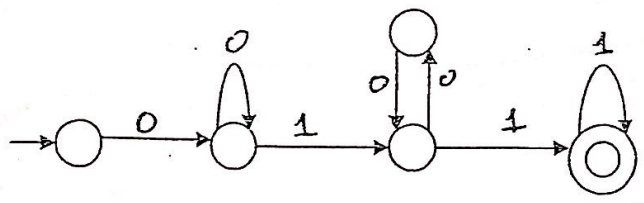
$$L(G) = \{\lambda\}$$

(ii)



$$L(G) = (aa)^*$$

(iii)

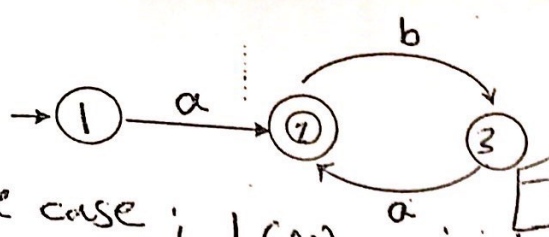


$$L(G) = (0)^+ \mid (00)^* \mid (1)^+$$

(a) Using Mathematical Induction, prove that the lang. accepted by the machines:

$$L(M) = \{ a(ba)^n, n \geq 0 \}$$

	a	b
1	2	
2		3
3	2	



1) base case; $L(M) = \{ a \}$ is true when $n=0$ [The property is true]

$$L(M) = a(ba)^0 = a(ba)$$

2) inductive step: I assume $L(M) = a(ba)^n$

then prove that $L(M+1) = a(ba)^{n+1}$

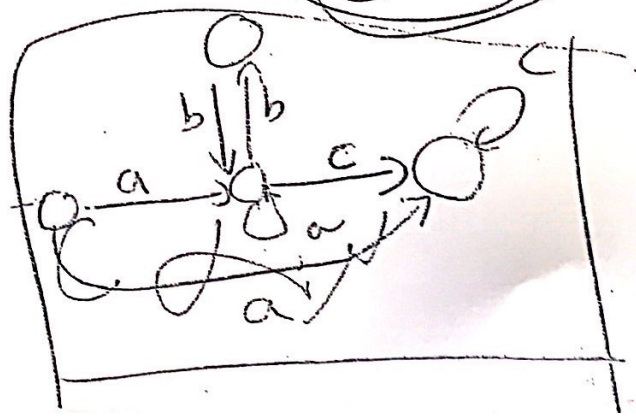
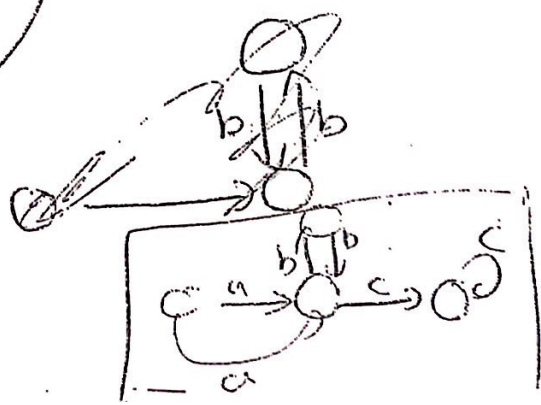
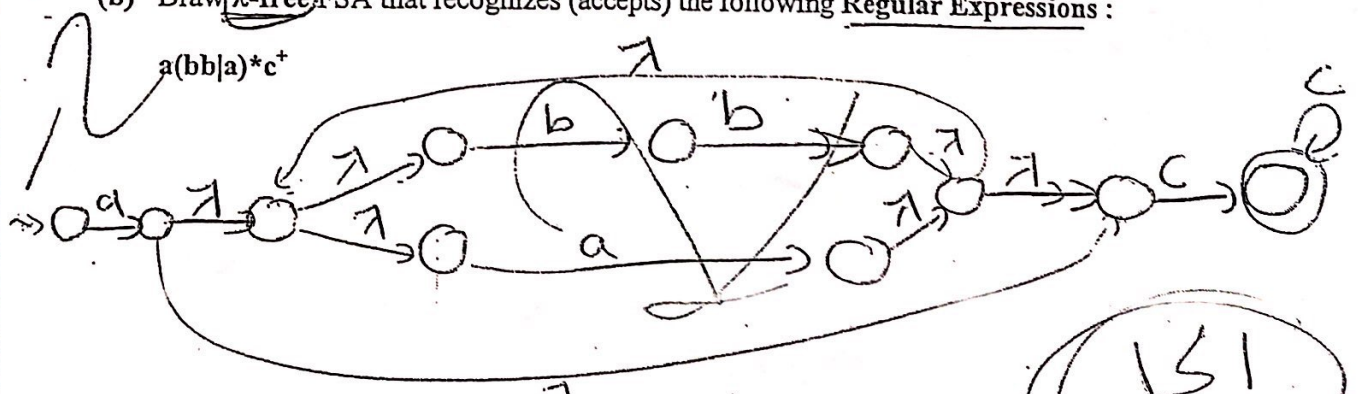
$$L(M+1) = a(ba)^{n+1} = a(ba)^n \cdot a(ba)$$

$$a(ab)^*$$

$$L(M+1) = L(M)$$

(b) Draw λ -free FSA that recognizes (accepts) the following Regular Expressions:

$a(bb|a)^*c^+$



(1) (a) Explain briefly the meaning of Machine Readability of a PL

The ability to develop and write an Algorithm to translate the PL in an unambiguous and finite way.

(b) Explain Briefly the meaning and give examples of multiplicity in a PL.

The ability to use PL in many platforms
↳ Like Java

(c) What is the major one difference between compiler and interpreter.

Compiler generate object code while interpreter generate Intermediate code

(d) Two advantages of a compiler are :

1- Generate object code ✓

2- Faster ✓

while two advantages of an interpreter are :

1- Generate portable Intermediate code. ✓

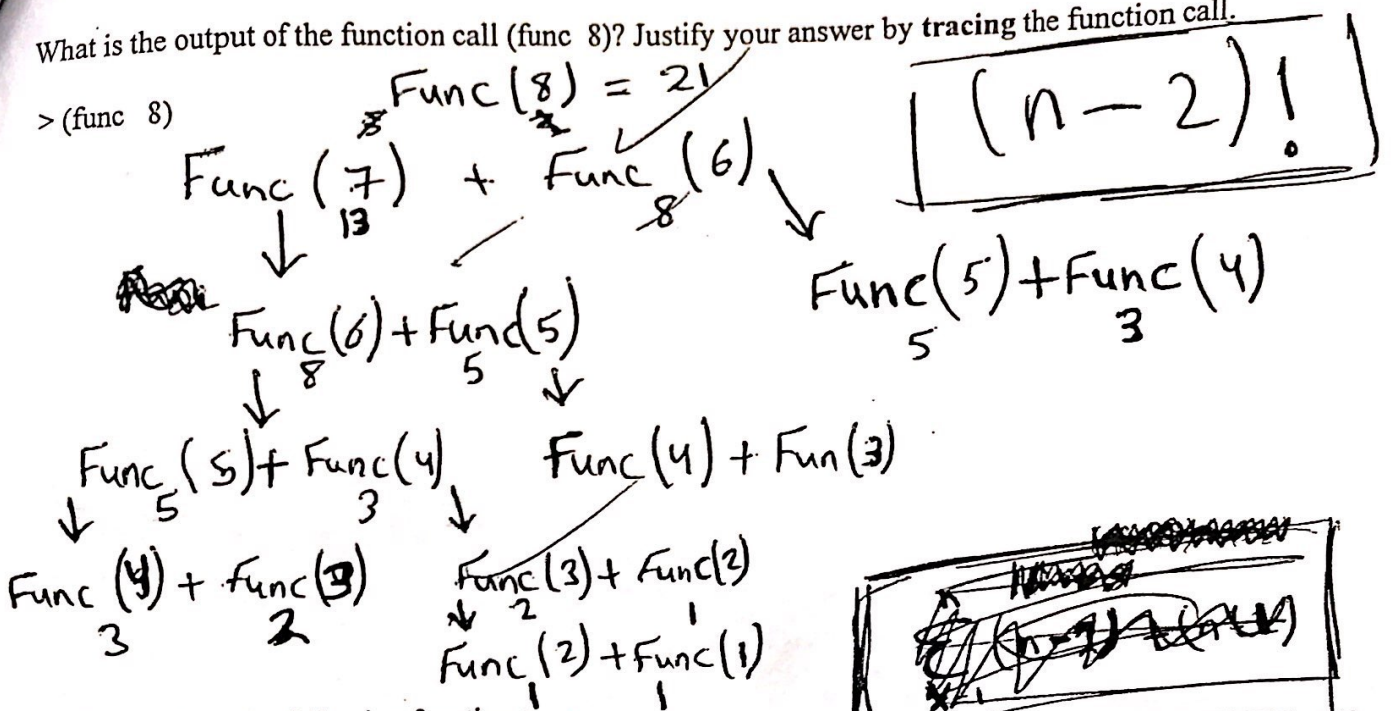
2- easy to implement. ✓

chapter #3

(a) Given the following function in CLISP

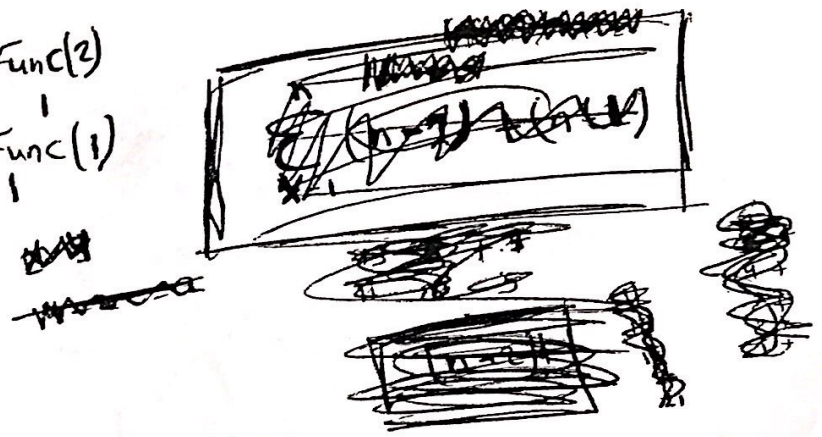
```
(defun func (n)
  (if (= n 1) 1
      (if (= n 2) 1
          (+ (func (- n 1)) (func (- n 2))))))
```

What is the output of the function call (func 8)? Justify your answer by tracing the function call.



(b) In C, given the following function:

```
int F(int m, int n) // m, n > 0
{ while (m != n)
  if (m > n) m = m - n;
  else n = n - m;
  return m; }
```



Rewrite this function in CLISP. What do you think the function do? Gcd

```
(defun Gcd (m n)
  (if (= m n) m
      (if (< m n)
          (+ Gcd (m - n) n)
          (+ Gcd m (n - m))))))
```

Greatest Common Divisor

Given the following simple grammar in BNF:

$$\text{exp} \rightarrow (\text{list}) \mid a$$

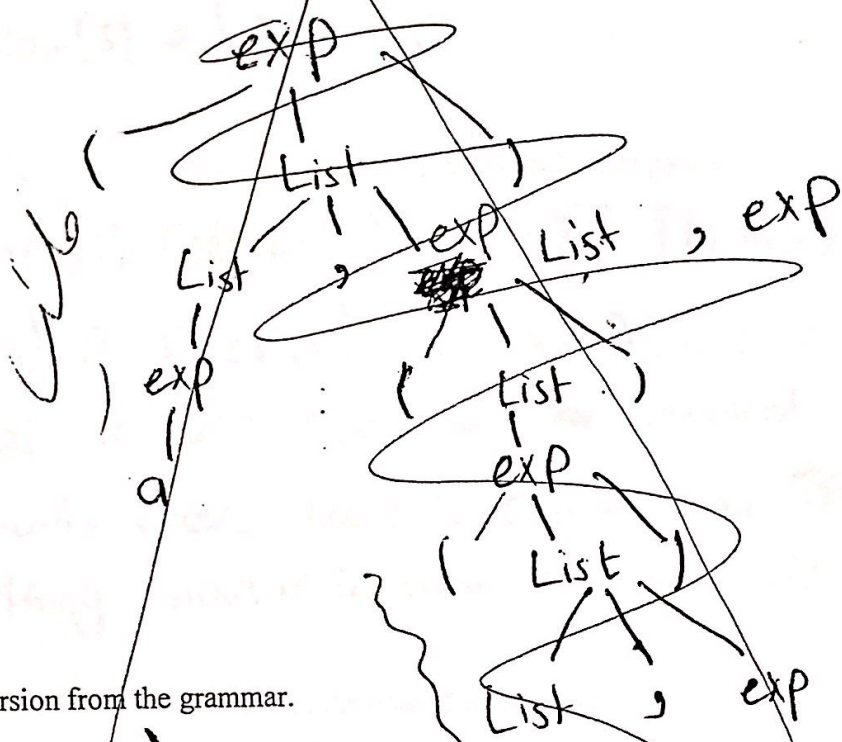
$$\text{list} \rightarrow \text{list}, \text{exp} \mid \text{exp}$$

Where: $V_N = \{\text{exp}, \text{list}\}$, $V_T = \{(\text{,}, \text{,}, \text{a})\}$

a) Rewrite these productions in EBNF.

$$\text{list} \rightarrow \text{exp}(\text{exp})^*$$

(b) Draw the derivation tree for the sentence (a, ((a, a), a))



(c) Eliminate left recursion from the grammar.

$$\begin{aligned} \text{exp} &\rightarrow a \text{exp}' \\ \text{exp}' &\rightarrow (\text{List}) \text{exp}' \\ \text{List} &\rightarrow \text{exp} \text{List}' \\ \text{List}' &\rightarrow \text{List}, \text{exp} \text{List}' \end{aligned}$$

Given the grammar :

$G \rightarrow \underline{S}S$
 $S \rightarrow a\underline{S}A \mid \lambda$
 $A \rightarrow b\underline{S} \mid c$

$V_N = \{G, S, A\}$, $V_T = \{a, b, c, \$\}$

(a) Compute:

FIRST(A) = $\{b, c\}$ ✓
FIRST(S) = ~~$\{a, \lambda\}$~~ $\{a, \lambda\}$ ✓
FIRST(G) = ~~$\{a, \lambda\}$~~ $\{a, \lambda\}$ ✓
FOLLOW(S) = $\{\$, b, c\}$
FOLLOW(A) = Follow(s) = $\{\$, b, c\}$

(b) Do you think this grammar is suitable (ملائم) for a recursive descent parsing? Explain your answer.

$$\text{First}(aS) \cap \text{Follow}(s) = \{a\} \cap \{\$, b, c\} = \emptyset$$

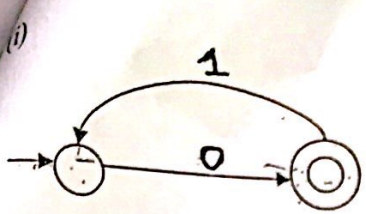
$$\text{First}(bS) \cap \text{First}(c) = \{b\} \cap \{c\} = \emptyset$$

As we see we checked the statements where there is choices and there is nothing similar in them so it's suitable.

(c) If so, write a recursive descent parser for the non-terminal S only.

```
Func S () {  
    if (token == "a")  
        get token();  
    Call S();  
    Call S();  
    Call A();  
    else if (token != "$" || token != "b"  
             || token != "c")  
        Error();  
}
```

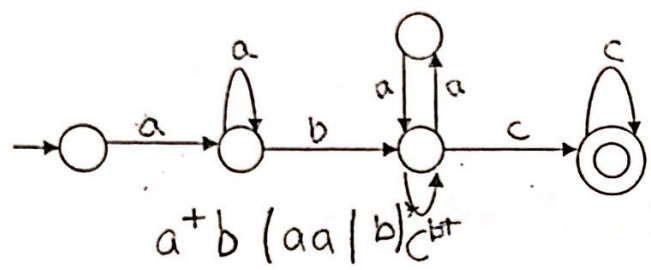
(a) What is the language recognized by the following FSA:



$(0(1)^*)$

$0(10)^*$

(ii) $0(10)^*$



$a^*b(aa|b)^*c^*$

$a^+b(aa|b)^+c^{++}$

(b) The grammar for the if...else... structure can be given as:

$S' \rightarrow SS$ ①

$S \rightarrow iCSE$ ② | a ③

$E \rightarrow eS$ ④ | λ ⑤

$C \rightarrow c$ ⑥

$V_N = \{S', S, C, E\}$

$V_T = \{i, a, c, e, \$\}$

Build the LL(1) parsing table. Is the grammar LL(1)? why? Fix it without changing the grammar.

$V_N \setminus V_T$	i	a	c	e	$\$$
S'	1	1			
S	2	3			
E				4,5	5
C			6		

~~we will add a delimiter (d) at the end of the statement S. there will be no conflict if we build the table again.~~

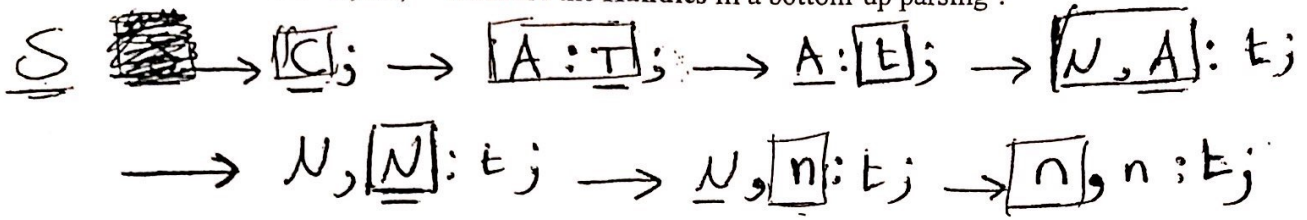
There are a conflict in the table so it's not LL(1).

we will add a delimiter (d) at the end of the statement (S) there will be no conflict if we build the table again.

(a) Given the grammar:

- $S \rightarrow C;$
- $C \rightarrow A:T$
- $A \rightarrow N | N, A$
- $N \rightarrow n$
- $T \rightarrow t$

Given the sentence $n,n;t$; What are the Handles in a bottom-up parsing?



$[]$ Are the handles



(b) What is the problem with the following right associative grammar? Explain in full.

- $E \rightarrow T + E | T$
- $T \rightarrow F * T | F$
- $F \rightarrow (E) | a$

~~There is a problem with the grammar~~

The problem here is in the precedence in ~~the~~ the real world we make the mathematic operation ~~and~~ from left to the write whit ~~focus of~~ Focus of precedence. but this differ from our imagination.

4

how

