

Question 1: (60 points, 3 points each). Select the correct answer

1	2	3	4	5	6	7	8	9	10
<del>A</del>	<del>D</del>	<del>C</del>	<del>D</del>	<del>C</del>	<del>E</del>	<del>D</del>	<del>B</del>	<del>C</del>	<del>C</del>

11	12	13	14	15	16	17	18	19	20
<del>E</del>	<del>B</del>	<del>D</del>	<del>A</del>	<del>A</del>	<del>A</del>	<del>B</del>	<del>C</del>	<del>A</del>	<del>D</del>

1. Convert the following BCD number to decimal  $(10000000011)_{BCD}$

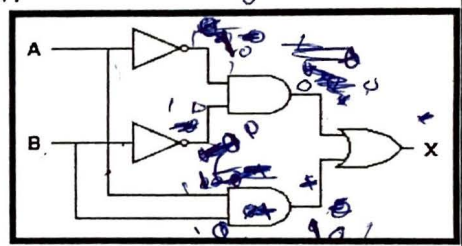
- A. 803
- B. 103
- C. 8003
- D. 1003
- E. None of the above

8 0 3

2. What type of logic circuit is represented by the figure shown below?

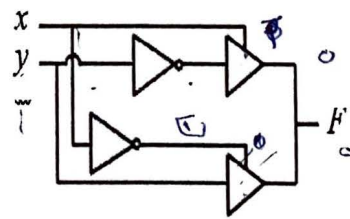
- A. NAND
- B. XOR
- C. NOR
- D. XNOR
- E. None of the above

A B  
C 0 1  
0 1  
1 0  
1 1



3. For the shown circuit the function F is

- A.  $F = X \text{ AND } Y$
- B.  $F = X \text{ OR } Y$
- C.  $F = X \text{ XOR } Y$
- D.  $F = X \text{ XNOR } Y$
- E. None



X Y  
0 0  
0 1  
1 0  
1 1

4. Consider the number  $(A95.2D3C)_{16}$ . How many digits would you need to represent this number in signed octal?

- A. 2 octal digits
- B. 4 octal digits
- C. 8 octal digits
- D. 10 octal digits
- E. None of the above

8 4 2 1  
1 0 1 0 1 0 1 0 1 0 0 0 1 0 1 0 0 0 1 1 1 0 0

A 10  
B 11  
C 12  
D 13  
E 14  
F 15

5. Simplify the Boolean function  $F = X'Y'Z + X'YZ + XY'Z + XYZ$

A.  $X'Z + XZ$   
 B.  $YZ' + XZ$   
 C.  $Z$   
 D.  $1$   
 E. None of the above

$yz(x' + x) + yz(x' + x)$   
 $yz + yz$   
 $2/0$

6. The logic realized by the circuit shown in figure is

A.  $F = B \oplus C$   
 B.  $F = (B \oplus C)'$   
 C.  $F = A \oplus C$   
 D.  $F = (B \oplus C)'$   
 E. None of the above

Handwritten truth table for the MUX circuit:

A	B	C	F
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	0

7. For the output F to be 1 in the logic circuit shown, the input combination should be

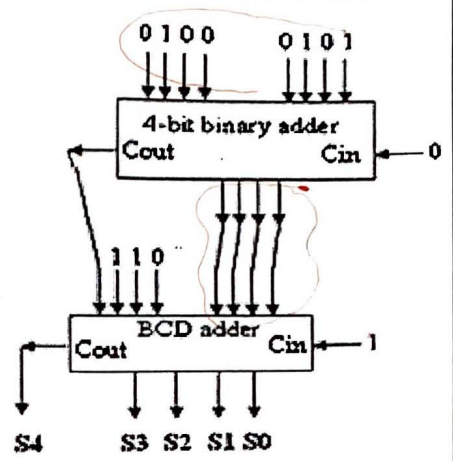
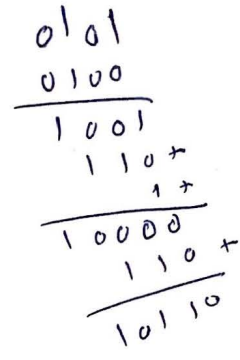
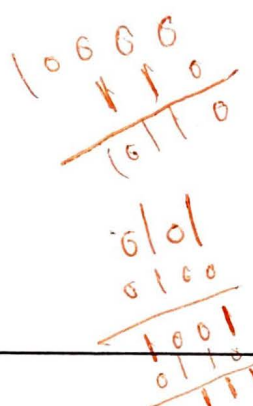
A.  $A=1, B=1, C=1$   
 B.  $A=1, B=0, C=0$   
 C.  $A=0, B=1, C=0$   
 D.  $A=0, B=0, C=1$   
 E. None

Handwritten truth table for the logic circuit:

A	B	C	F
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	0

8. The binary value of S4 S3 S2 S1 S0 in the circuit beside is:

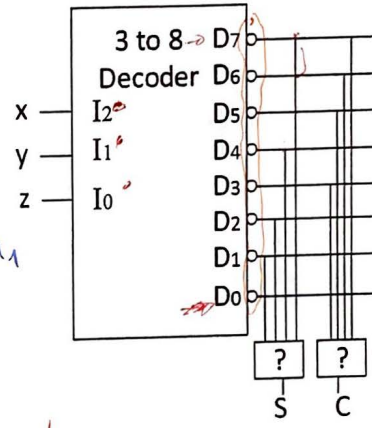
- A. 10001
- B. 10110**
- C. 10000
- D. 01001



9. Implementation of a full adder with an active low decoder and two

- A. OR gates
- B. AND gates
- C. NOR gates**
- D. NAND gates
- E. None

$M7, M4, M2, M1$   
 $M7$



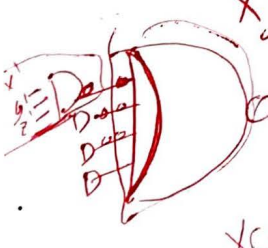
	yz		
x	00	01	11
	10	11	00

x	y	z	
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0

$$x\bar{y}\bar{z} + x\bar{y}z + xy\bar{z} + xyz$$

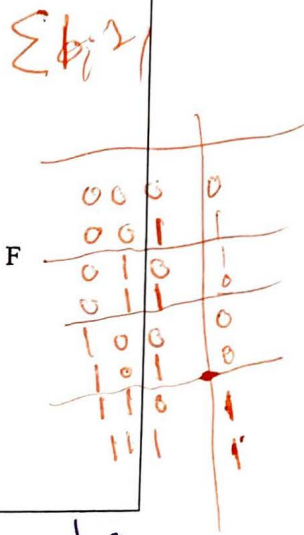
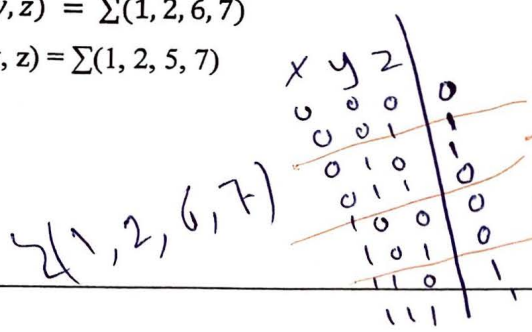
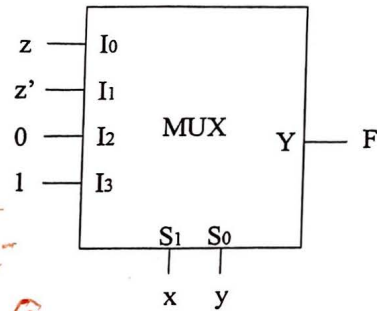
$$x(\bar{y}\bar{z} + \bar{y}z + y\bar{z} + yz)$$

$$x(y \oplus z)$$



10. Which function F is implemented by using this 4X1 Multiplexer

- A.  $F(x, y, z) = \sum(0, 3, 4, 5)$
- B.  $F(x, y, z) = \sum(1, 3, 6, 7)$
- C.  $F(x, y, z) = \sum(1, 2, 6, 7)$
- D.  $F(x, y, z) = \sum(1, 2, 5, 7)$
- E. None

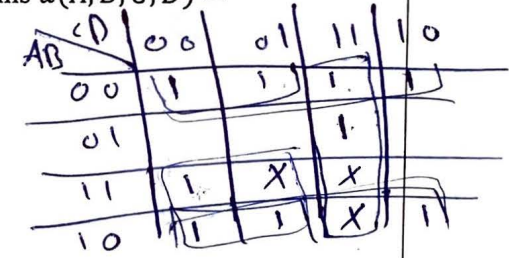
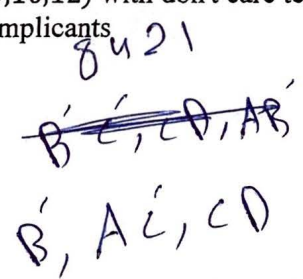


11. The Boolean function  $F = A \oplus B \oplus C \oplus D = 1$  means:

- A. all inputs are zeros ( $A = 0, B = 0, C = 0, D = 0$ ).
- B. all inputs are ones ( $A = 1, B = 1, C = 1, D = 1$ ).
- C. half of the inputs are zeros (for example:  $A = 0, B = 0, C = 1, D = 1$ ).
- D. one or two or three of the inputs are ones.
- E. one or three of the inputs are ones.

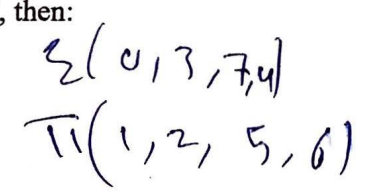
12. Consider the  $F(A, B, C, D) = \sum(0, 1, 2, 3, 7, 8, 9, 10, 12)$  with don't care terms  $d(A, B, C, D) = \sum(11, 13, 15)$ . List all of the essential prime implicants

- A.  $B', AD, AC', CD$
- B.  $B', AC', CD$
- C.  $AD, AC', CD$
- D.  $B', AD, CD$
- E. None



13. Given  $F(x, y, z) = \prod(0, 3, 4, 7)$ , and G is the complement of F, then:

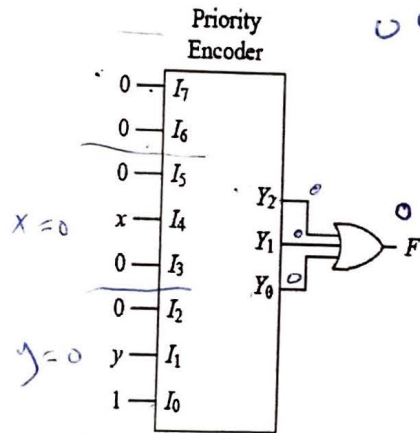
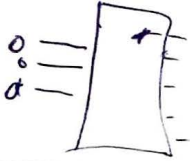
- A.  $G(x, y, z) = \sum(0, 1, 2, 3, 5, 7)$
- B.  $G(x, y, z) = \prod(0, 3, 4, 7)$
- C.  $G(x, y, z) = \sum(1, 2, 5, 6)$
- D.  $G(x, y, z) = \sum(0, 3, 4, 7)$
- E. None of the above





14. The shown priority encoder gives highest priority to  $I_7$ . The output  $F$ :

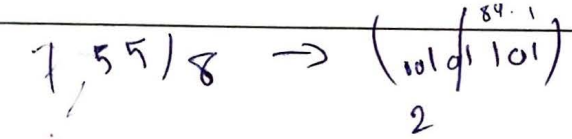
- A. is = 0 when  $x = 0$  and  $y = 0$ .
- B. is = 0 when  $x < y$ , i.e.  $x = 0$  and  $y = 1$ .
- C. is = 0 when  $x = y = 1$ , i.e.  $x = 1$  and  $y = 1$ .
- D. is = 0 when  $x > y$ , i.e.  $x = 1$  and  $y = 0$ .
- E. is always = 1.



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15. The number  $(55)_8$  is equivalent to:

- A.  $(2D)_{16}$
- B.  $(D2)_{16}$
- C.  $(B1)_{16}$
- D.  $(1B)_{16}$
- E.  $(55)_{16}$



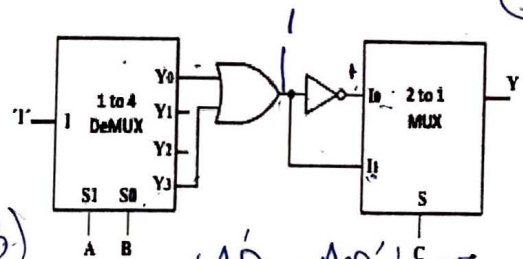
$AB + A'B'$

~~$AB$~~

16. The output  $Y$  of the circuit is

- A.  $Y(A,B,C) = \sum(1,2,4,7)$
- B.  $Y(A,B,C) = \sum(0,3,5,6,7)$
- C.  $Y(A,B,C) = \prod(1,2,4,7)$
- D.  $Y(A,B,C) = \prod(0,3,5,6,7)$
- E. None

$A'B' + AB$



$(A'B' + AB)$   
 $A'B'C + AB'C$

$(A'B + AB')$   
 $A'B'C' + AB'C'$

$\sum(1, 2, 4, 7)$

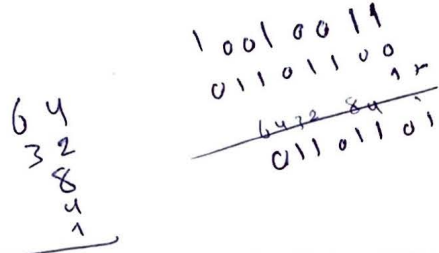
17. A full adder can be made out of

- A. Two half adders
- B. Two half adders and OR gate
- C. Two half adders and NOT gate
- D. Two half adders and AND gate

$A'B'C$   
 $AB'C$

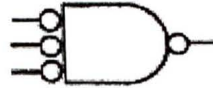
18. What is the number represented of the binary words 10010011, assuming the representation is in Two's complement

- A. -19
- B. 109
- C. -109
- D. -108
- E. None

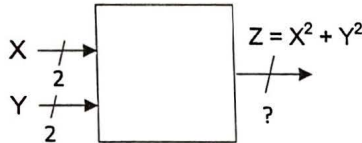


19. The shown symbol is an equivalent representation of the

- A. NOT gate
- B. AND gate
- C. OR gate
- D. NOR gate
- E. None

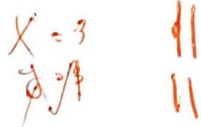
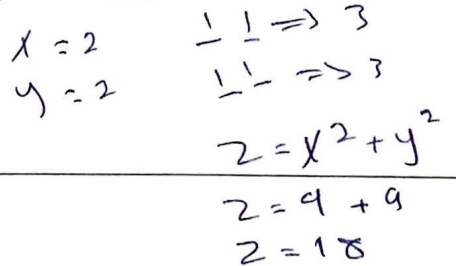


20. A logic circuit has two inputs X & Y each is a 2-bit unsigned number. It has an output number Z such that

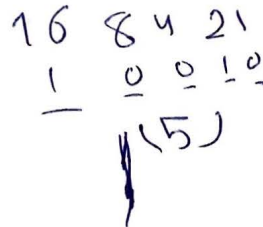


the minimum number of bits required for the output number Z is

- A. 2
- B. 3
- C. 4
- D. 5
- E. 6



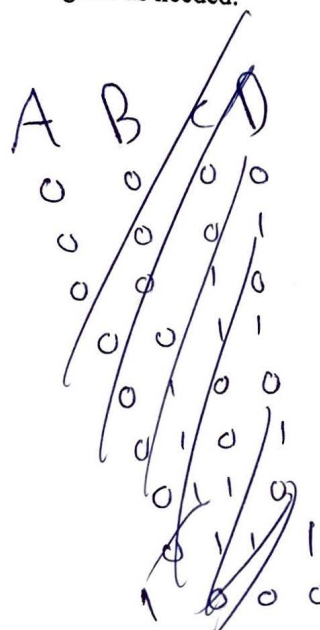
$Z = 18$



**Question#2: 10 points**

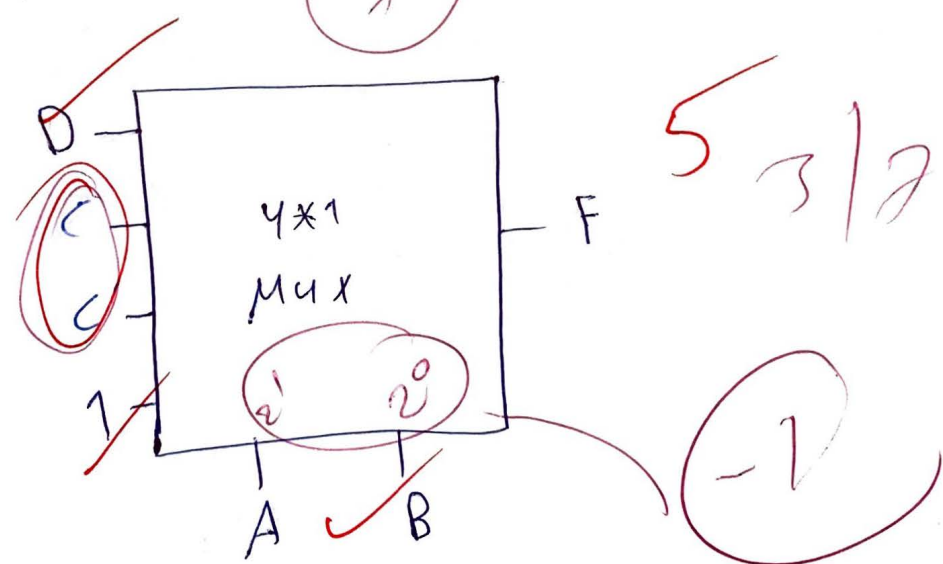
The following function is given in sum of minterms form  $F(A,B,C,D) = \sum(1,3,4,11,12,13,14,15)$ . Implement this function using one mux 4\*1 with minimum number of external gates as needed.

A	B	C	D	F
0	0	0	0	0
0	0	0	1	1
0	0	1	0	0
0	0	1	1	1
0	1	0	0	1
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1



2

2



Question#3: 10 points

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Implement the following function using NOR-NOR two level implementations

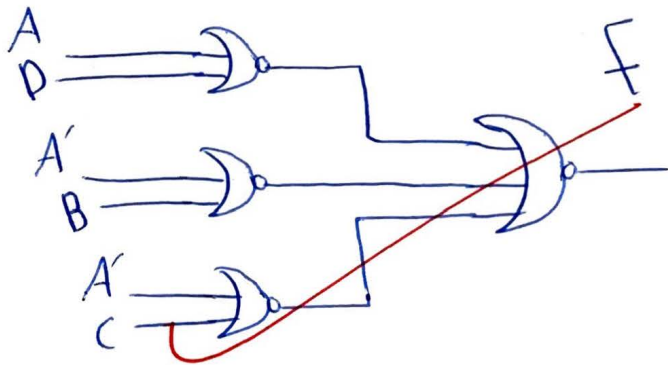
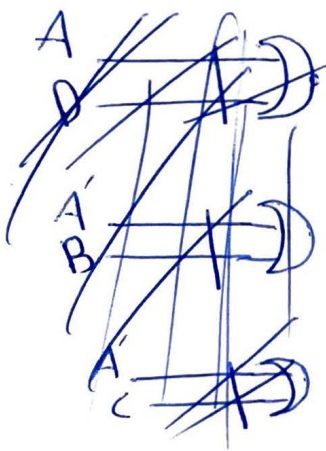
$$F(A,B,C,D) = \Sigma (1,3,5,7,14,15)$$

$$F(A,B,C,D) = \Pi (0,2,4,6,8,9,10,11,12,13)$$

~~$F(A,B,C,D) =$~~   
=  
=

AB \ CD	00	01	11	10
00	0			0
01	0			
11	0	0		
10	0	0	0	0

$$F(A,B,C,D) = (A+D) \cdot (A'+B) \cdot (A'+C)$$



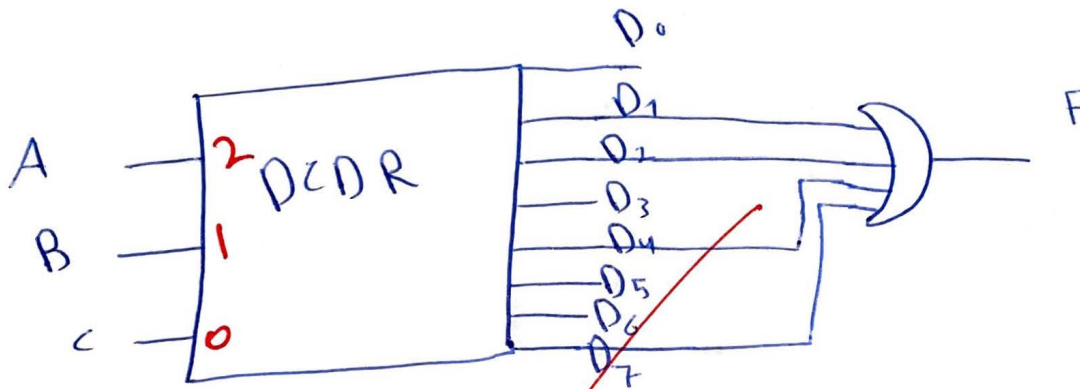


Question#4: 10 points

Use a suitable size of decoder and an external logic gate to implement the even parity generator for a circuit with three inputs A, B, C

$$(A, B, C) = \Sigma(1, 2, 4, 7)$$

A	B	C	P
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1



9

**Question#5: 10 points**

Derive the truth table only for a four bit combinational circuit 2's complementer (The output generates the 2's complement of the input binary number)

A	B	C	D	<del><math>y_0</math></del>	$y_1$	$y_2$	$y_3$	$y_4$
0	0	0	0	1	0	0	0	0
0	0	0	1	0	1	1	1	1
0	0	1	0	0	1	1	0	0
0	0	1	1	0	1	0	1	1
0	1	0	0	0	1	1	0	0
0	1	0	1	0	1	0	1	1
0	1	1	0	0	1	0	1	0
0	1	1	1	0	1	0	0	1
1	0	0	0	0	1	0	0	0
1	0	0	1	0	0	1	1	1
1	0	1	0	0	0	1	1	0
1	0	1	1	0	0	1	0	1
1	1	0	0	0	0	1	0	0
1	1	0	1	0	0	0	1	1
1	1	1	0	0	0	0	1	0
1	1	1	1	0	0	0	0	1

9

Handwritten notes and calculations on the left side of the page, including binary addition and subtraction examples:

- $0000$
- $0001$
- $0010$
- $0011$
- $0100$
- $0101$
- $0110$
- $0111$
- $1000$
- $1001$
- $1010$
- $1011$
- $1100$
- $1101$
- $1110$
- $1111$

Handwritten notes and calculations on the right side of the page, including binary addition and subtraction examples:

- $1000$
- $0100$
- $0011$
- $0110$