



Faculty of Engineering and Technology  
Electrical and Computer Engineering Departmen  
Advanced Digital Design ENCS533  
Homework#5

**Prepared By:**

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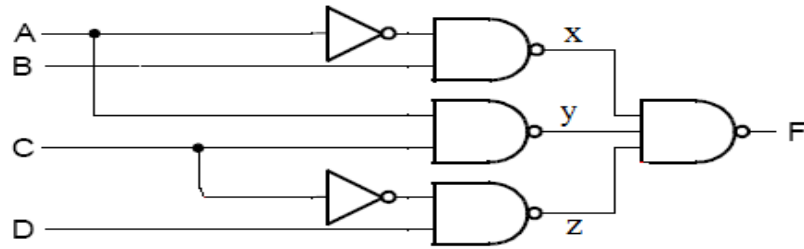
**Section: 1**

**Date: 21/2/2020**

Q1) For the following circuit

i) Determine the values of inputs at which hazard may occur.

ii) Draw the hazard-free circuit (NAND-NAND implementation).



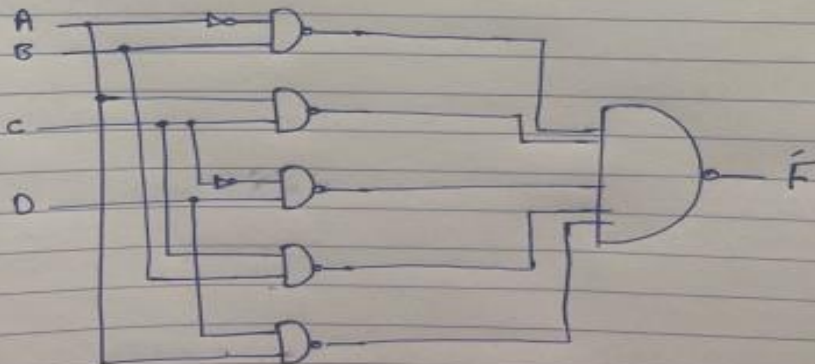
a)  $F = \bar{A}.B + A.C + \bar{C}.D$

| AB \ CD | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00      | 0  | 1  | 0  | 0  |
| 01      | 1  | 1  | 1  | 1  |
| 11      | 0  | 1  | 1  | 1  |
| 10      | 0  | 1  | 1  | 1  |

∴ value of inputs at hazard may occur:

A B C D  
 0 1 1 1  
 1 0 0 1  
 0 1 1 0  
 0 1 1 1

b) new  $F = \bar{F} = \bar{A}.B + A.C + \bar{C}.D + A.D + B.C$



**Q2)** Use asynchronous design procedure to design a positive edge TFF that has 2 inputs T and CLK, and one output Q. Use SR Latches in your design.

\*

|   | T | CLK | Q | Stable | Note       |
|---|---|-----|---|--------|------------|
| A | 0 | 0   | 0 | ✓      | after C, E |
| B | 0 | 0   | 1 | ✓      | after D, F |
| C | 0 | 1   | 0 | ✓      | after G, A |
| D | 0 | 1   | 1 | ✓      | after B, H |
| E | 1 | 0   | 0 | ✓      | after A, G |
| F | 1 | 0   | 1 | ✓      | after B, H |
| G | 1 | 1   | 0 | ✓      | after C, F |
| H | 1 | 1   | 1 | ✓      | after D, E |

\* Primitive flow table :

|   | 00     | 01     | 11     | 10     |
|---|--------|--------|--------|--------|
| A | (A, 0) | C, -   | -, -   | E, -   |
| B | (B, 1) | D, -   | -, -   | F, -   |
| C | A, -   | (C, 0) | G, -   | -, -   |
| D | B, -   | (D, 1) | H, -   | -, -   |
| E | A, -   | -, -   | H, -   | (E, 0) |
| F | B, -   | -, -   | G, -   | (F, 1) |
| G | -, -   | C, -   | (G, 0) | E, -   |
| H | -, -   | D, -   | (H, 1) | F, -   |

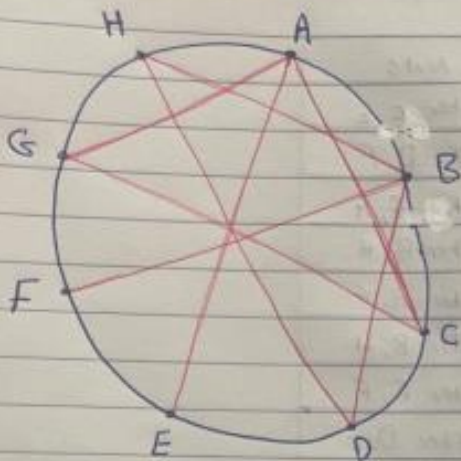
\* Implication chart:

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| B | × |   |   |   |   |   |   |
| C | ✓ | × |   |   |   |   |   |
| D | × | ✓ | × |   |   |   |   |
| E | ✓ | × | × | × |   |   |   |
| F | × | ✓ | × | × | × |   |   |
| G | ✓ | × | ✓ | × | × | × |   |
| H | × | ✓ | × | ✓ | × | × | × |
|   | A | B | C | D | E | F | G |

So comparable pairs is

(A, C), (A, E)  
 (A, G), (B, D)  
 (B, F), (B, H)  
 (C, E), (D, H)

\* Menger Diagram



\* Max compatible pairs:

$(A, C, G) \rightarrow (A, C, G)$

$(B, D, H) \rightarrow (B, D, H)$

$(A, E) \rightarrow (E)$

$(B, F) \rightarrow (F)$

|         | 00   | 01   | 11   | 10   |
|---------|------|------|------|------|
| A, C, G | A, 0 | C, 0 | G, 0 | E, - |
| B, D, H | B, 1 | D, 1 | H, 1 | F, - |
| E       | A, - | -, - | H, - | E, 0 |
| F       | B, - | -, - | G, - | F, 1 |

notes:

$A, C, G \rightarrow A$

$B, D, H \rightarrow B$

$E \rightarrow C$

$F \rightarrow D$

|   | 00   | 01   | 11   | 10   |
|---|------|------|------|------|
| A | A, 0 | A, 0 | A, 0 | C, - |
| B | B, 1 | B, 1 | B, 1 | D, - |
| C | A, - | -, - | B, - | C, 0 |
| D | B, - | -, - | A, - | D, 1 |

| $y_1, y_2$ | 00 | 01 | 11 | 10 |
|------------|----|----|----|----|
| 00         | 00 | 00 | 00 | 11 |
| 01         | 01 | 01 | 01 | 10 |
| 11         | 00 | XX | 01 | 11 |
| 10         | 01 | XX | 00 | 10 |

| $y_1, y_2$ | 00 | 01 | 11 | 10 |
|------------|----|----|----|----|
| 00         | 0  | 0  | 0  | X  |
| 01         | 1  | 1  | 1  | X  |
| 11         | X  | X  | X  | 0  |
| 10         | X  | X  | X  | 1  |

$$Q = y_1 y_2 + y_2 y_1$$

$$= y_1 \oplus y_2$$



\* SR Latch Table

$y_1$ :

| $T/C$<br>$y_1/y_2$ | 00 | 01 | 11 | 10 |
|--------------------|----|----|----|----|
| 00                 | 0  | 0  | 0  | 1  |
| 01                 | 0  | 0  | 0  | 1  |
| 11                 | 0  | X  | 0  | 1  |
| 10                 | 0  | X  | 0  | 1  |

| $T/C$<br>$y_1/y_2$ | 00 | 01 | 11 | 10 |
|--------------------|----|----|----|----|
| 00                 | 0  | 0  | 0  | 1  |
| 01                 | 0  | 0  | 0  | 1  |
| 11                 | 0  | X  | 0  | X  |
| 10                 | 0  | X  | 0  | X  |

| $T/C$<br>$y_1/y_2$ | 00 | 01 | 11 | 10 |
|--------------------|----|----|----|----|
| 00                 | X  | X  | X  | 0  |
| 01                 | X  | X  | X  | 0  |
| 11                 | 1  | X  | 1  | 0  |
| 10                 | 1  | X  | 1  | 0  |

$$S = T \cdot \bar{c}$$

$$R = \bar{T} + c$$

$y_2$ :

| $T/C$<br>$y_1/y_2$ | 00 | 01 | 11 | 10 |
|--------------------|----|----|----|----|
| 00                 | 0  | 0  | 0  | 1  |
| 01                 | 1  | 1  | 1  | 0  |
| 11                 | 0  | X  | 1  | 1  |
| 10                 | 1  | X  | 0  | 0  |

| $T/C$<br>$y_1/y_2$ | 00 | 01 | 11 | 10 |
|--------------------|----|----|----|----|
| 00                 | 0  | 0  | 0  | 1  |
| 01                 | X  | X  | X  | 0  |
| 11                 | 0  | X  | X  | X  |
| 10                 | 1  | X  | 0  | 0  |

| $T/C$<br>$y_1/y_2$ | 00 | 01 | 11 | 10 |
|--------------------|----|----|----|----|
| 00                 | X  | X  | X  | 0  |
| 01                 | 0  | 0  | 0  | 1  |
| 11                 | 1  | X  | 0  | 0  |
| 10                 | 0  | X  | X  | X  |

$$S = y_1 \cdot \bar{y}_2 \cdot \bar{T} + \bar{y}_1 \cdot \bar{y}_2 \cdot T \cdot \bar{c}$$

$$R = y_1 \cdot y_2 \cdot \bar{T} + \bar{y}_1 \cdot y_2 \cdot T \cdot \bar{c}$$

