



**BIRZEIT UNIVERSITY**  
 Faculty of Engineering and Technology  
 Electric and Computer Engineering Department  
 Digital Signal Processing ENCS4310

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Quiz # 1 (A)

19/20

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Duration: 25 minutes

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Question 1: Examine the system  $y[n]=x[n]\cos(\omega_0 n)$  with respect to the following properties:

- a) Linear or nonlinear.
- b) Time variant or time invariant.
- c) Stable or unstable.
- d) causal or noncausal.
- e) Memory or memoryless.

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a)  $\alpha_1 y_1 = \alpha_1 x[n] \cos(\omega_0 n)$  ✓  
 $\alpha_2 y_2 = \alpha_2 x[n] \cos(\omega_0 n)$  ✓  
 $\alpha_1 y_1 + \alpha_2 y_2 = \alpha_1 x[n] \cos(\omega_0 n) + \alpha_2 x[n] \cos(\omega_0 n)$  ✓  
 $\alpha_3 y_3 = \alpha_1 y_1 + \alpha_2 y_2$        $\alpha_3 x_3 = \alpha_1 x_1 + \alpha_2 x_2$   
 $\alpha_3 y_3 = \alpha_3 x[n] \cos(\omega_0 n)$

$\alpha_1 y_1 + \alpha_2 y_2 = (\alpha_1 x_1 + \alpha_2 x_2) \cos(\omega_0 n)$  ✓      linear ✓

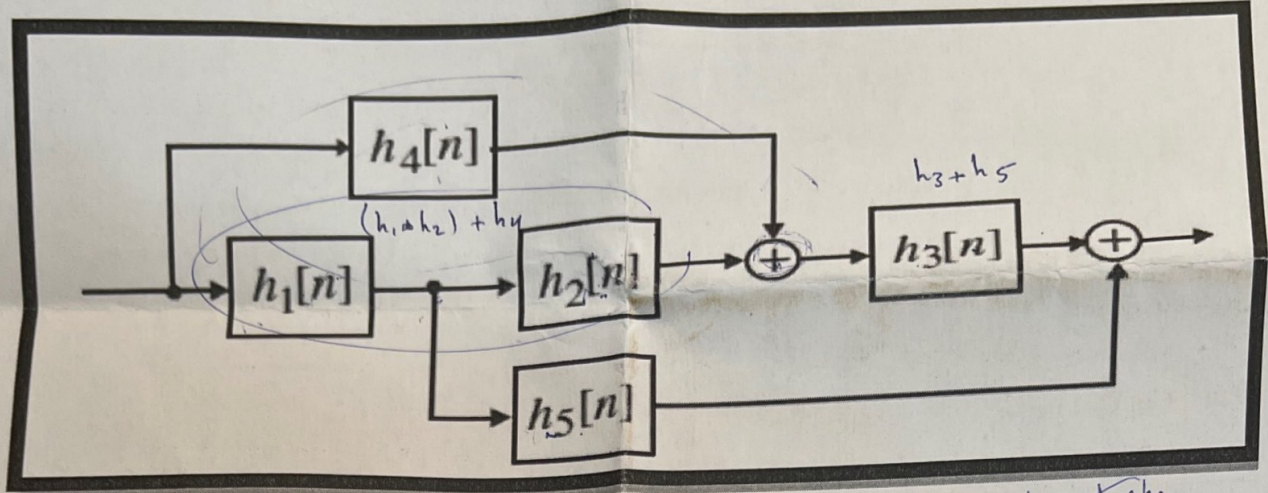
b)  $y(n-n_0) = x(n-n_0) \cos(\omega_0(n-n_0))$   
 $T(x[n-n_0]) = x(n-n_0) \cos(\omega_0(n-n_0)) \neq x(n-n_0) \cos(\omega_0 n)$  ✓ time variant

c)  $|y[n]| = |x[n] \cos(\omega_0 n)| < \infty$   
 $\text{constant } B_x \cos(\omega_0 n) < \infty$   
 $x[n] \rightarrow BI \rightarrow \text{stable}$   
 $y[n] \text{ stable if } \cos(\omega_0 n) < \infty$

d) ~~causal~~ ✓ because output depend on ~~present~~ or now value  
 Past

e) ~~memory less~~ ✓ because system doesn't have ~~present~~ value  
 Past

Question 2: Determine the expression of the overall impulse response of the following system?



$$h_6 = h_1 * h_2$$

$$h_7 = h_6 + h_4$$

$$h_8 = h_7 * h_3$$

$$h_9 = h_5 + h_8$$

$$h = h_9$$

$$h[n] = h_5 + ((h_1 * h_2) + h_4) * h_3$$

$$h_5 + h_7 * h_3$$

$$h_5 + (h_6 + h_4) * h_3$$

$$h_5 + (h_1 * h_2 + h_4) * h_3$$

b) Given that  $h[n] = \{1, 5, 2, 1, 4\}$ , what is the output  $y[n]$  of the following input  $x[n] = \{1, 3, 2, 1, 2\}$ ?

$x[n]$	1	3	2	1	2
1	1	3	2	1	2
5	5	15	10	5	10
2	2	6	4	2	4
1	1	3	2	1	2
4	4	12	8	4	8

$$y[n] = \{1, 8, 19, 18, 18, 26, 13, 6, 8\}$$