

Welcome to  
**ENEE2301**  
**Network Analysis 1**

**Instructor**  
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**(Office Masri216)**

**Text Book: *Electric Circuits, 10<sup>th</sup> Edition* by Nilsson/Riedel**

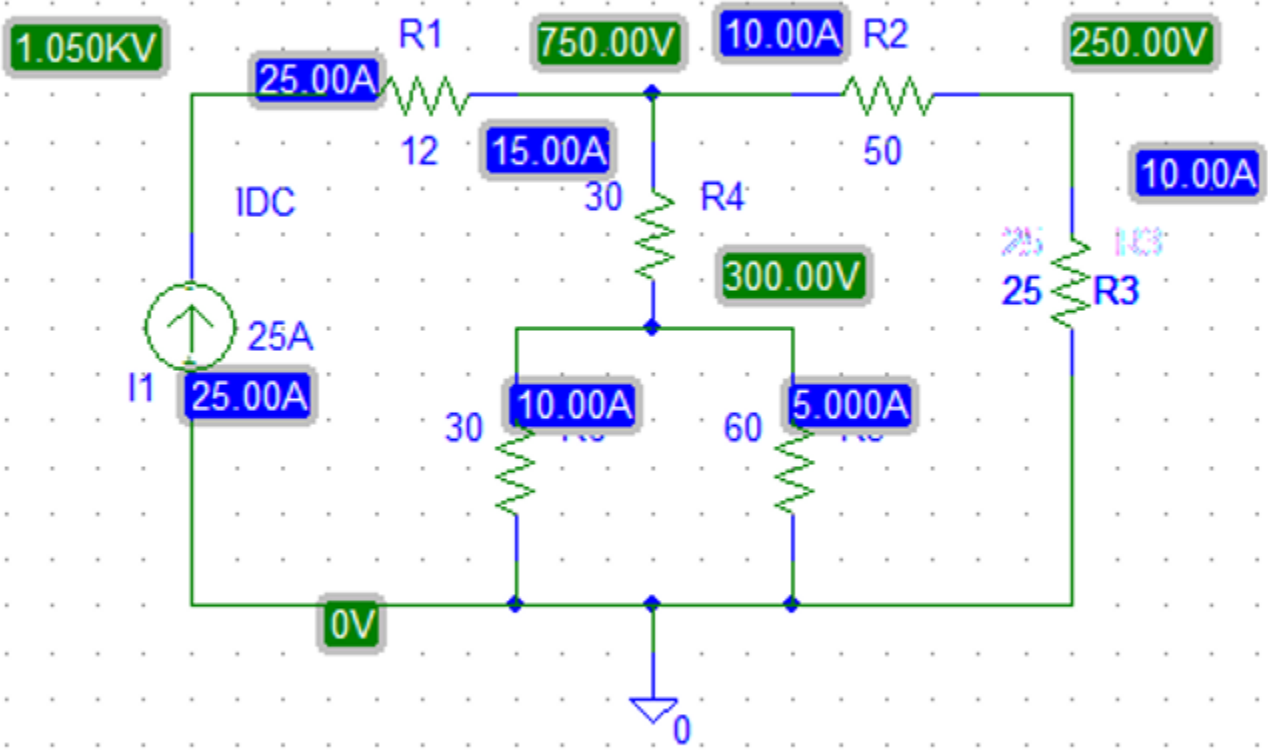
## Course Objectives

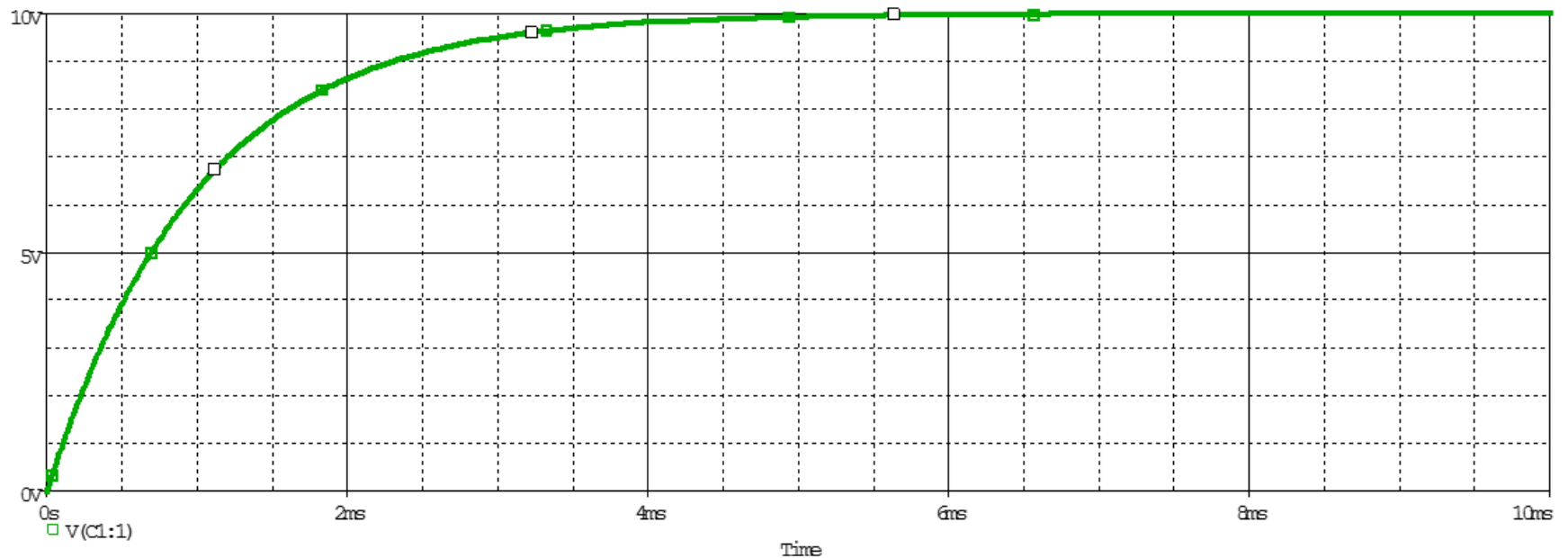
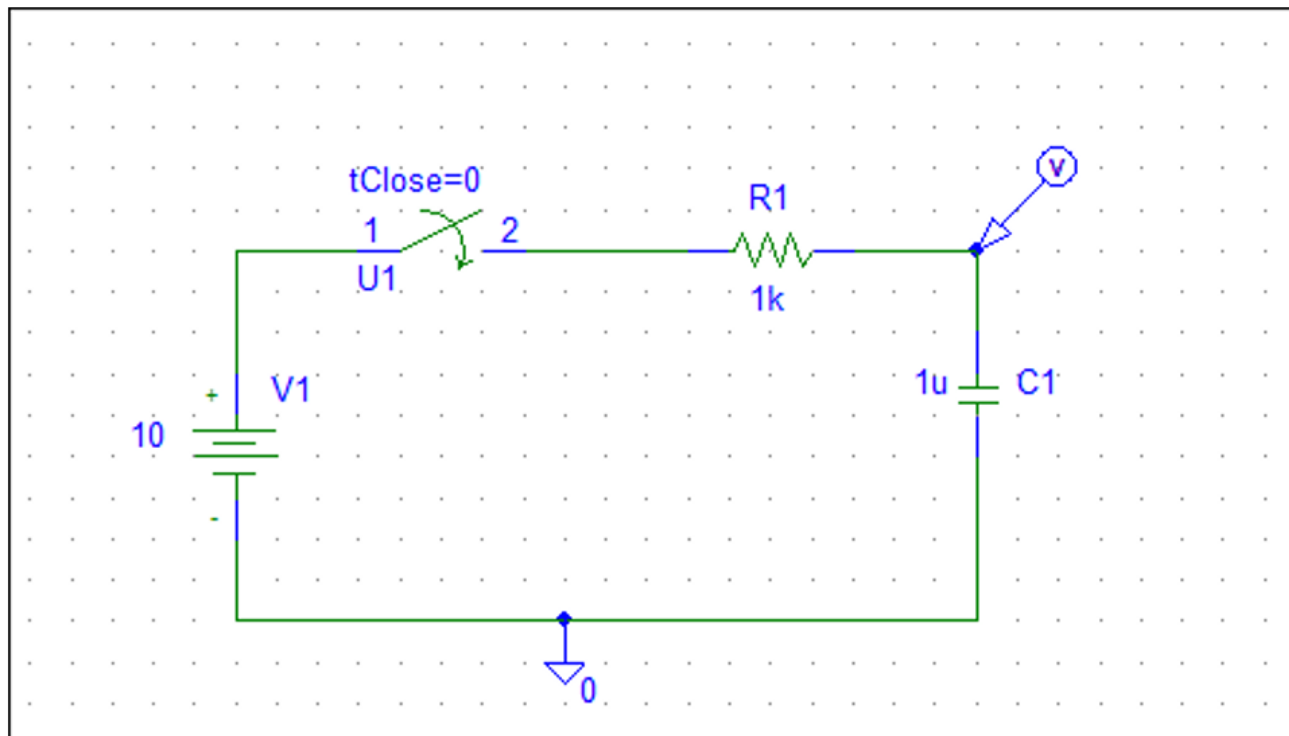
- Analysis of DC circuits with different techniques.
- Analysis of transient circuits using:  
1st, 2nd order DE.
- Analysis of AC circuits using phasors.
- Sinusoidal Steady state Power analysis.
- Analysis of three phase circuits.
- Analysis of linear and ideal transformer circuits
- Using software tools (Pspice) to analyze various types of circuits.

| <b>Chapters</b> | <b>Topic</b>   | <b>Sections</b>             |
|-----------------|--|-----------------------------|
| <b>1</b>        | <b>Circuit Variables (self reading)</b>                                  | <b>1.1 – 1.6</b>            |
| <b>2</b>        | <b>Circuit Elements</b>  | <b>2.1 – 2.5</b>            |
| <b>3</b>        | <b>Simple resistive circuits</b>   | <b>3.1 – 3.7</b>            |
| <b>4</b>        | <b>Techniques of circuit analysis.</b>                                   | <b>4.1 – 4.13</b>           |
| <b>6</b>        | <b>Inductance , Capacitance (self reading)<br/>and Mutual inductance</b> | <b>6.1 – 6.3</b>            |
| <b>7</b>        | <b>Response of first order RL and RC circuits</b>                        | <b>7.1 – 7.6</b>            |
| <b>8</b>        | <b>Natural and step responses of RLC circuits</b>                        | <b>8.1 – 8.4</b>            |
| <b>9</b>        | <b>Sinusoidal steady-state analysis</b>                                  | <b>9.1 – 9.12</b>           |
| <b>10</b>       | <b>Sinusoidal steady state power calculations</b>                        | <b>10.1 – 10.6</b>          |
| <b>11</b>       | <b>Balance three-phase circuits</b>                                      | <b>11.1 – 11.6</b>          |
| <b>Ch A</b>     | <b>Magnetically coupled networks</b>                                     | <b>6.4, 6.5, 9.10, 9.11</b> |

## Grading Policy

|   |     |
|---|-----|
| Quizzes , PSPICE Simulation, and Participation: | 25% |
| Midterm Exam:                                   | 30% |
| Final Exam:                                     | 45% |



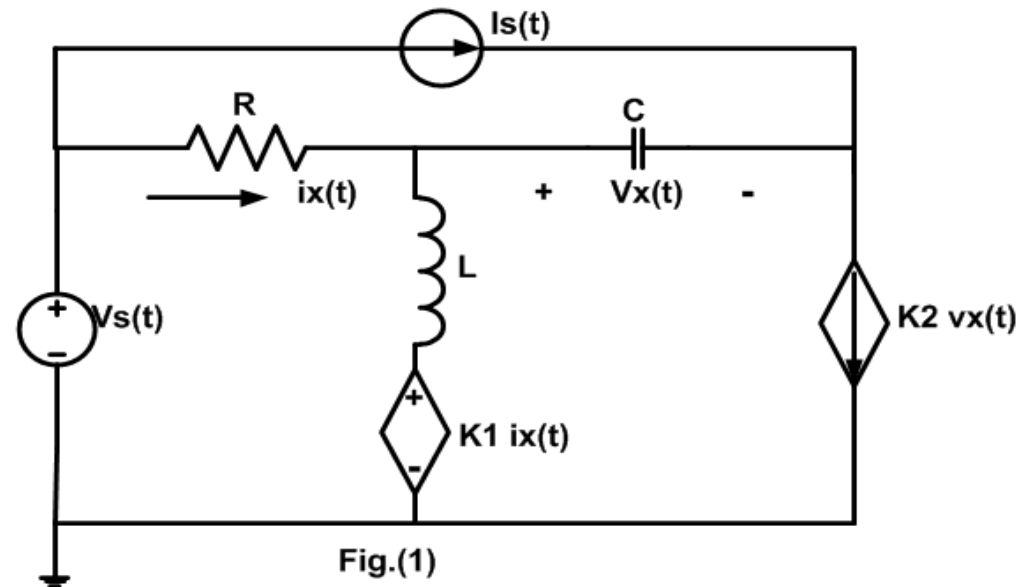


**Reading Assignment: Chapter 2 in *Electric Circuits, 10<sup>th</sup> Edition* by Nilsson**

## **Chapter 2: Circuit Elements**

Several types of electrical devices are introduced in this chapter, including independent sources, dependent sources, and resistors.

**Reading Assignment: Chapter 2 in *Electric Circuits, 9<sup>th</sup> Edition* by Nilsson**  
**Chapter 2: Circuit Elements**



- Network : the interconnection of two or more simple circuit element is called electrical network.
- Circuit : if the network contains at least one closed path ,it is called electric circuit .
- Circuit analysis : given a circuit in which all the components are specified , **analysis involves finding such things as the voltage across some elements or the current through another. The solution is unique.**
- Circuit design involves determining the circuit configuration that will meet certain specifications . **The solution is not unique.**



## Circuit Elements

- 1) Active element : capable of delivering power to some external elements (sources).
- 2) Passive element : capable only of receiving power (R,L,C,...).

Circuit element can be classified according to the relationship of the current through the element to the voltage across the element .

## Chapter 2: Circuit Elements

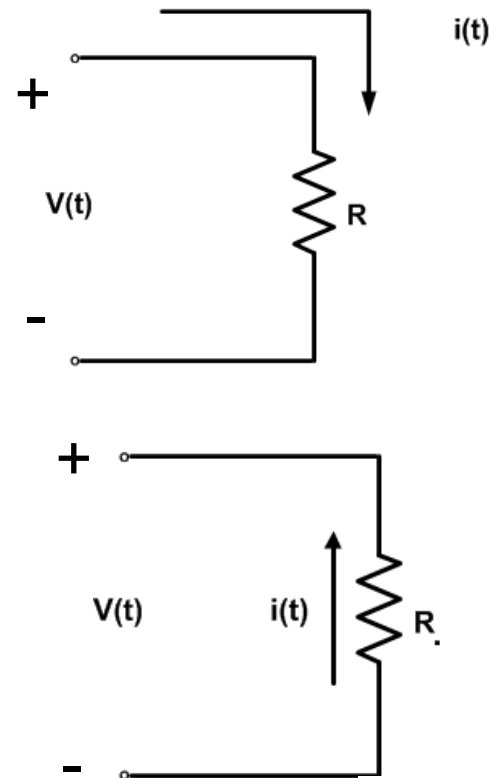
### 1) Resistor

$$V(t) = R \cdot i(t)$$

$$i(t) = \frac{1}{R} \cdot V(t)$$

$$= G \cdot V(t)$$

$$V(t) = - R \cdot i(t)$$



- R is called the resistance of the the component and is measured in units of ohm ( $\Omega$ )
- G is called the conductance of the component and is measured in units of Siemens ( $\upsilon$ )

## **\*\* two special resistor values**

First : short circuit

$$R=0 \Omega$$

$$V(t)=0 \text{ V} \quad i(t)= ???$$

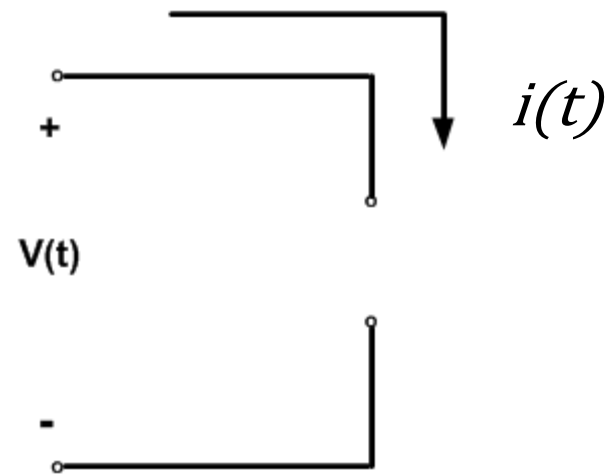
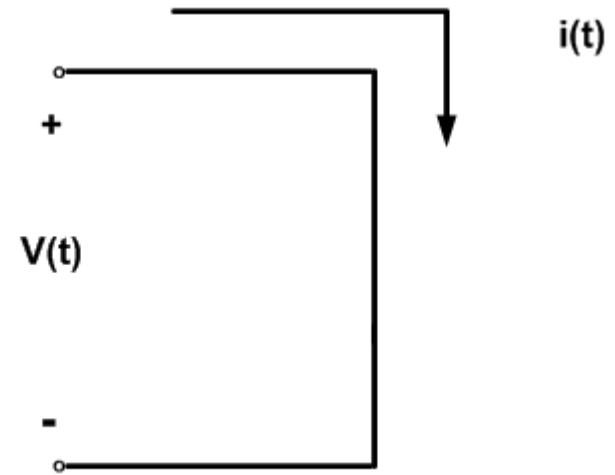
$$G=\infty \text{ U}$$

Second: Open Circuit

$$R=\infty \Omega$$

$$i(t)= 0 \text{ A} \quad V(t)= ???$$

$$G= 0 \text{ U}$$



## Resistors and electric Power

**Resistors are passive elements that can only absorb energy**

$$P(t) = V(t) \cdot i(t)$$

$$V(t) = R \cdot i(t)$$

$$P(t) = \frac{V^2(t)}{R}$$

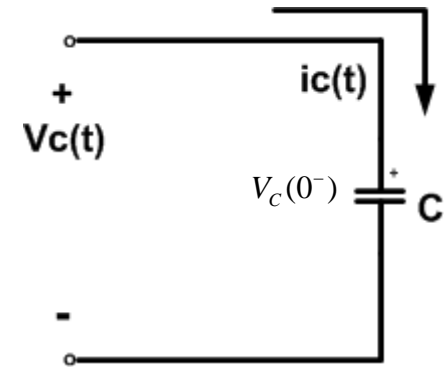
$$P(t) = R \cdot i^2(t)$$

## 2. Capacitors

$$V_C(t) = \frac{1}{C} \int_{-\infty}^t i_C(t) dt$$

$$V_C(t) = V_C(0^-) + \frac{1}{C} \int_{0^-}^t i_C(t) dt \quad \text{for } t \geq 0$$

$$i_C(t) = C \frac{dv_C(t)}{dt}$$



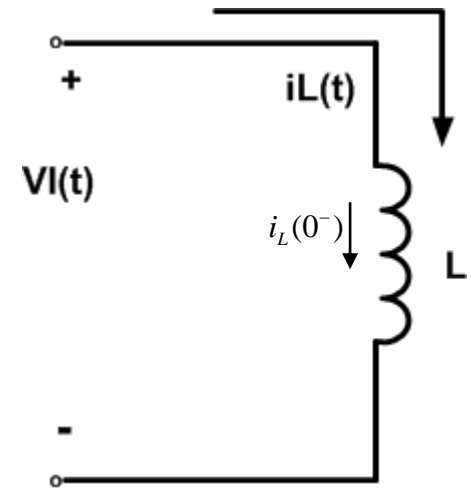
C is called the capacitance of the capacitor and is measured in units of farad (F)

### 3. Inductors

$$V_L(t) = L \frac{di_L(t)}{dt}$$

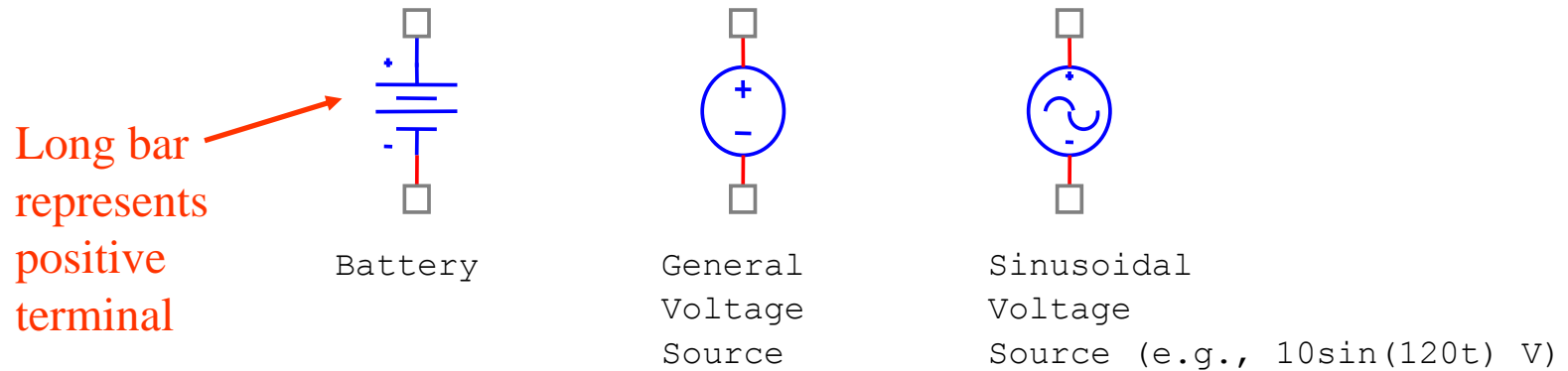
$$i_L(t) = i_L(0^-) + \frac{1}{L} \int_{0^-}^t V_L(t) dt \quad \text{for } t \geq 0$$

L is called the inductance of the coil and is measured in units of the henry (H)



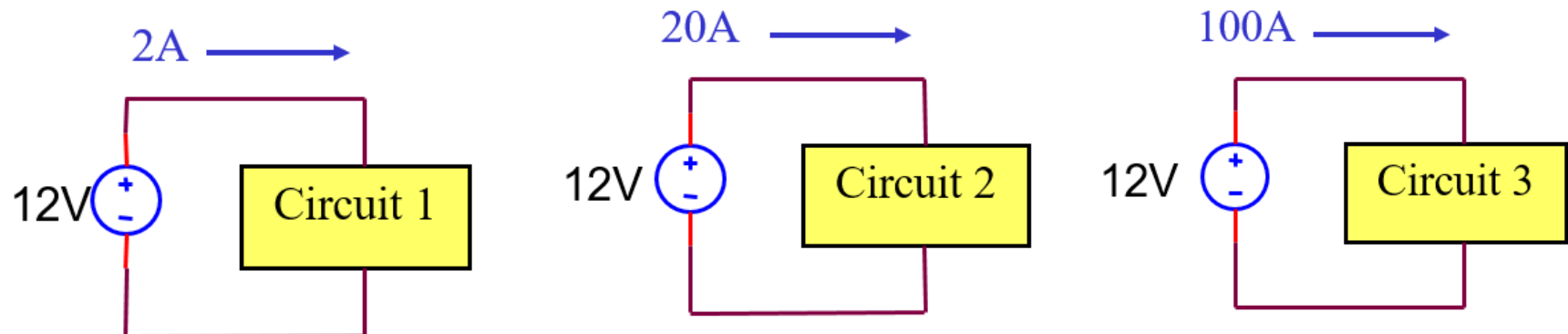
**Independent voltage source** – A circuit element in which the voltage across its terminals is completely independent of the current through it .

**Symbols:**



- The symbols shown above are from PSPICE. The boxes on the ends of the wires are simply for connecting wires or other components to the sources.
- Voltage sources have a specified voltage, but the current depends on the circuit and is determined through analysis.

**Example:** The current provided by the 12V source below varies in each case.

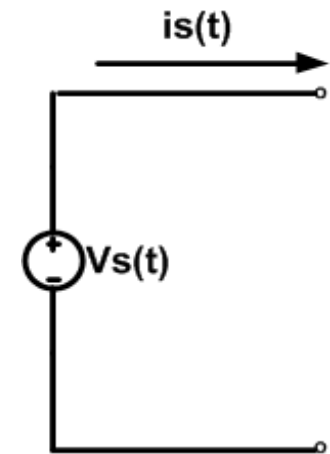


Voltage Source

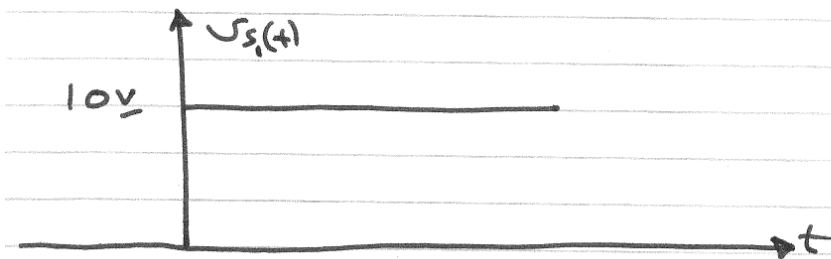
$$V_{s1}(t) = 10 \text{ V (DC)}$$

$$V_{s2}(t) = 5 \sin \omega t \text{ V (ac)}$$

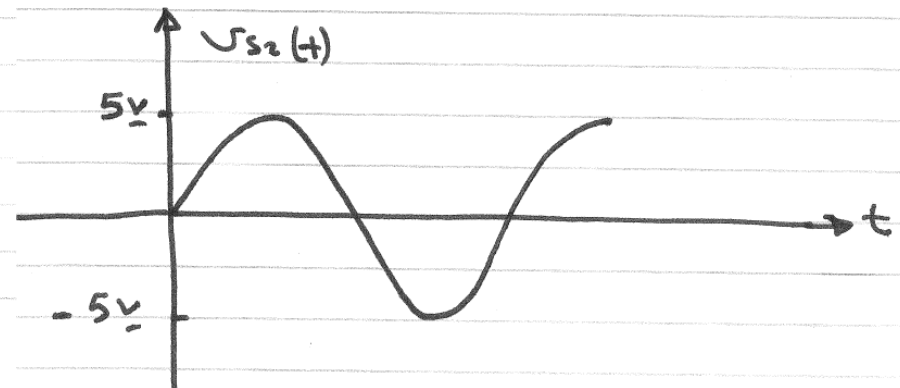
$$V_{s3}(t) = 10 e^{-t} \text{ V}$$



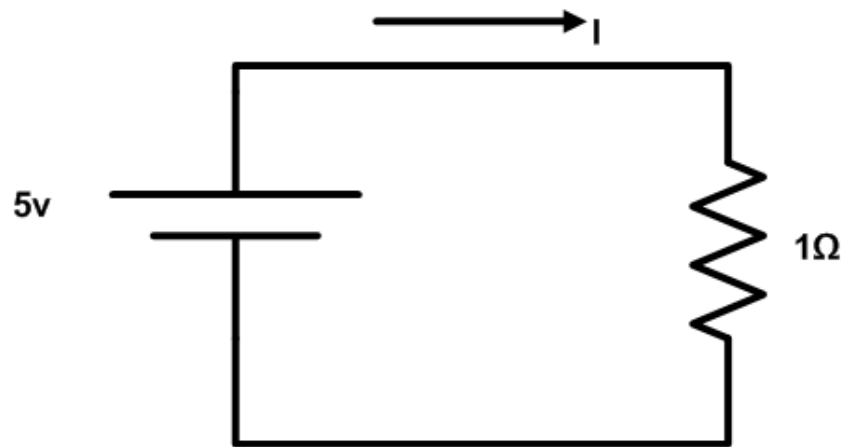
$$V_{s1}(t) = 10 \text{ V (DC)}$$



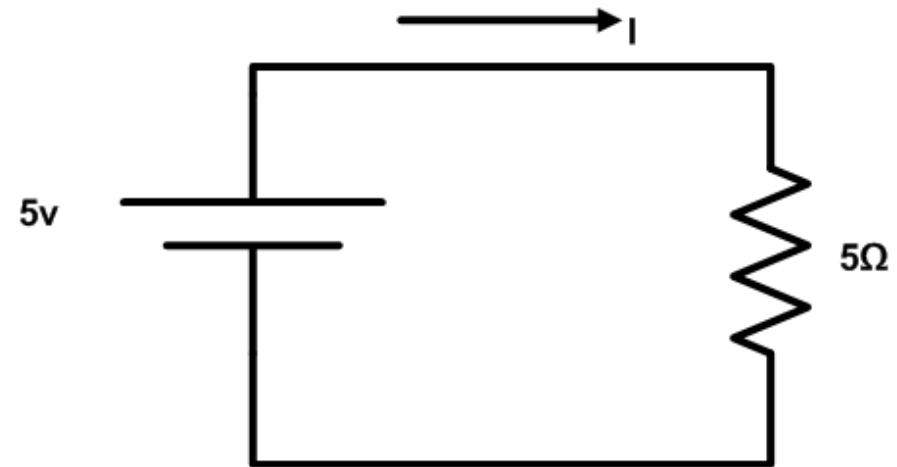
$$V_{s2}(t) = 5 \sin \omega t \text{ V (ac)}$$







$$I = \frac{5v}{1\Omega} = 5A$$

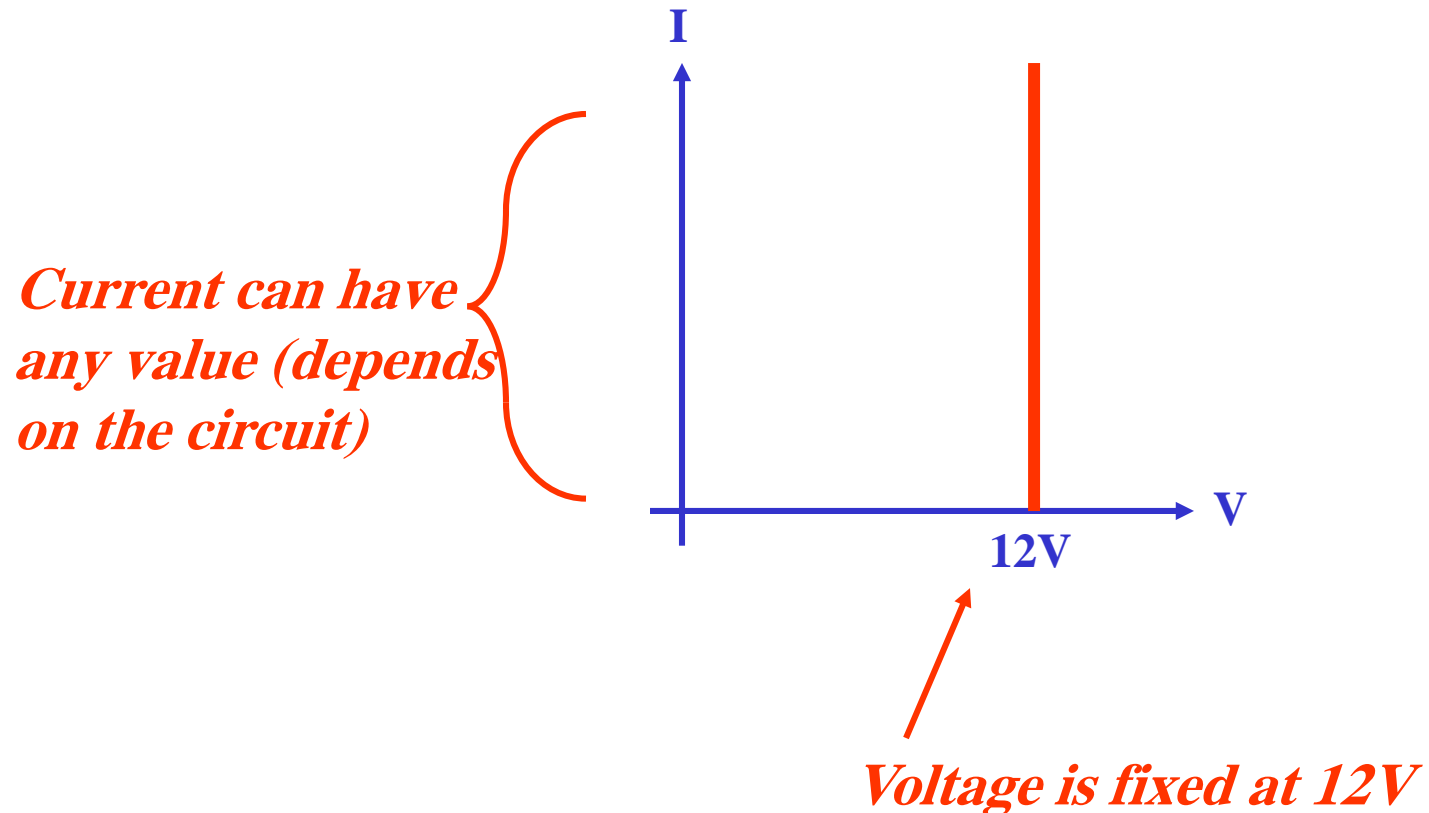


$$I = \frac{5v}{5\Omega} = 1A$$

## Independent voltage source characteristics

The “characteristics” of a device typically refers to a graph of  $I$  versus  $V$  which illustrates the behavior of the device.

The characteristics of an ideal independent 12 V voltage source are shown below.

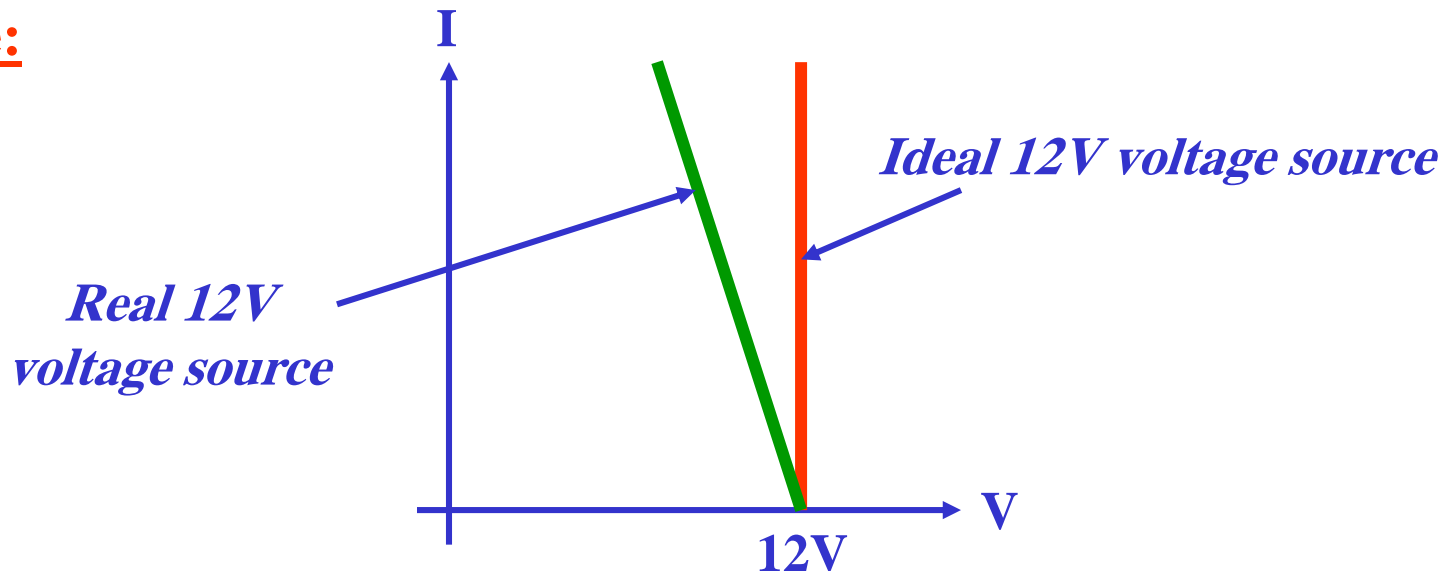


## Real versus ideal independent voltage sources

The voltage delivered by an **real voltage source** (or practical voltage source) will typically drop as the current required by the source increases. For example:

- The 1.5V across a D-cell in a flashlight drops when the light is turned on.
- The 12V across a car battery drops when the car is started.
- The voltage from a power company drops during peak load hours (the voltage typically ranges from 115V - 130V in North America).

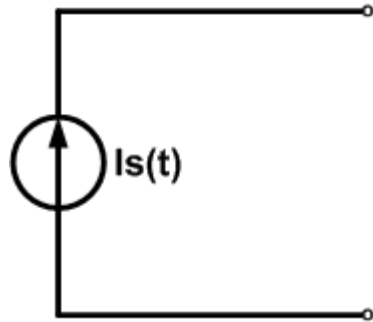
### Example:



Note: Any voltage source shown in the text is assumed to be ideal.

**Independent current source** – A circuit element in which the current through it is completely independent of the voltage across its terminals. (This device is not as common in everyday use as the independent voltage source.)

Symbol:

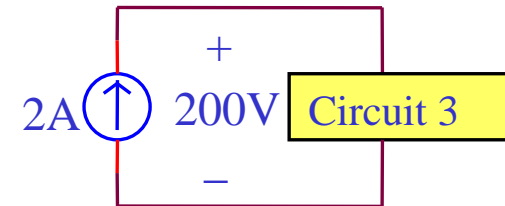
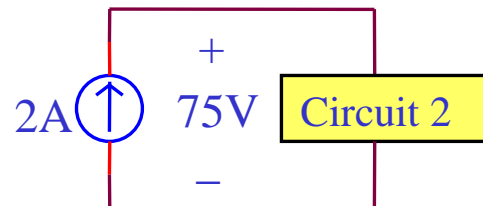
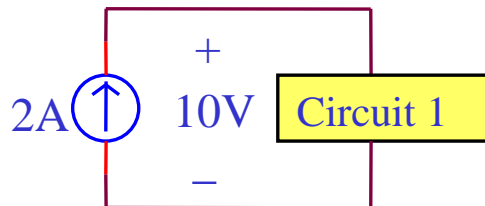


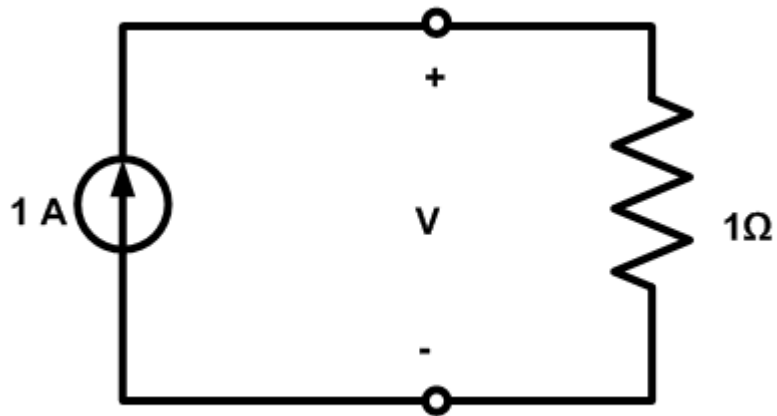
$$i_s(t) = 10 \sin wt \text{ A}$$

$$i_s(t) = 20 \text{ A}$$

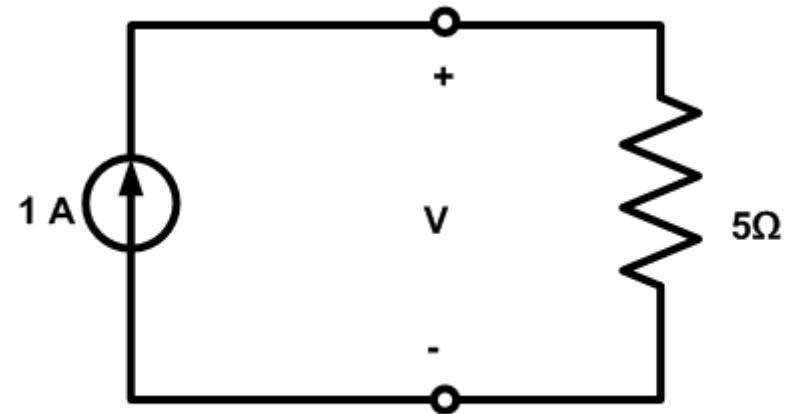
- Current sources have a specified current, but the voltage depends on the circuit and is determined through analysis.

**Example:** The voltage provided by the 2A source below varies in each case.





$$V = (1 A) \cdot (1 \text{ ohm}) = 1 V$$

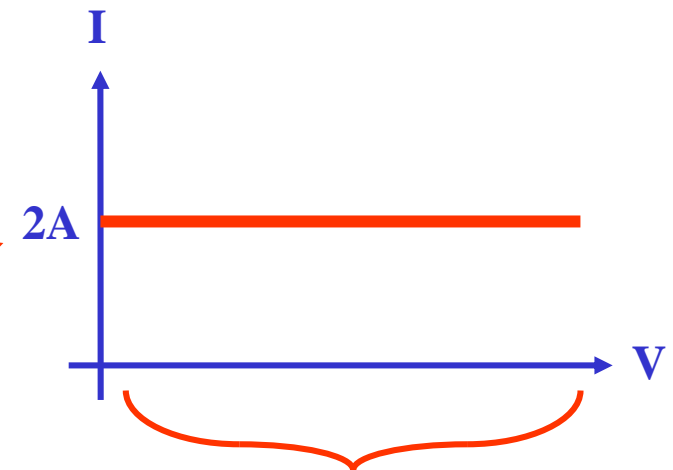


$$V = (1 A) \cdot (5 \text{ ohm}) = 5 V$$

## Independent current source characteristics

The characteristics of an ideal independent 2A current source are shown.

*Current is fixed at 2A*

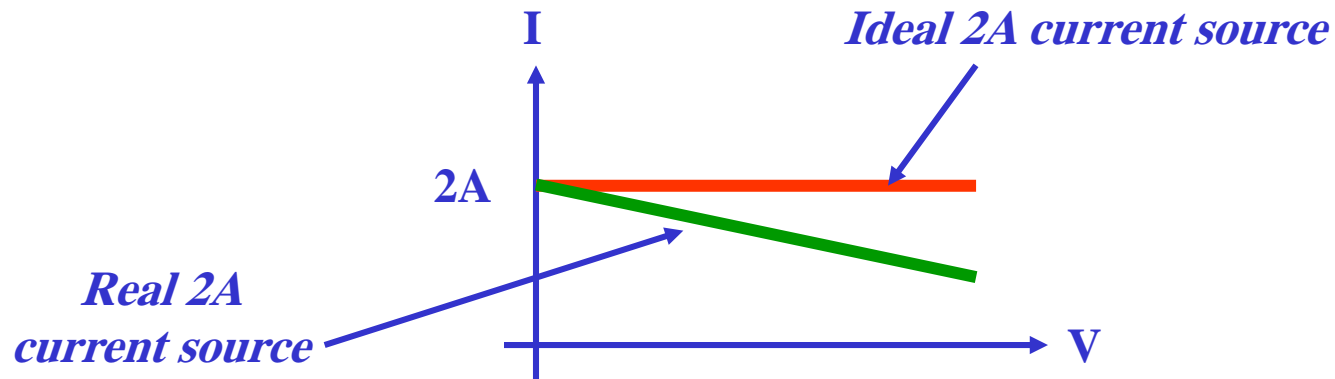


*Voltage can have any value  
(depends on the circuit)*

## Real versus ideal independent current sources

The current delivered by an real current source (or practical current source) will typically drop as the voltage required by the source increases.

### Example:

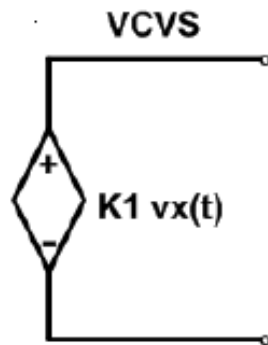


Note: Any current source shown in the text is assumed to be ideal.

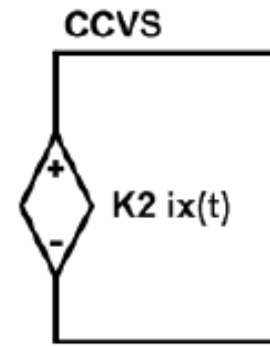
# Dependent Sources

- Are sources in which the source voltage (or current) **depend** upon a current or voltage elsewhere in the circuit .

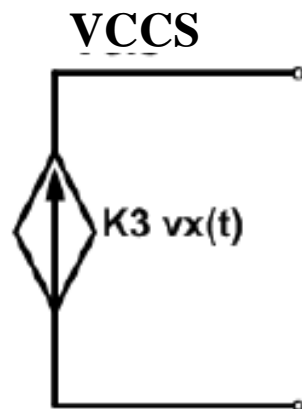
Voltage  
Controlled  
Voltage  
Source



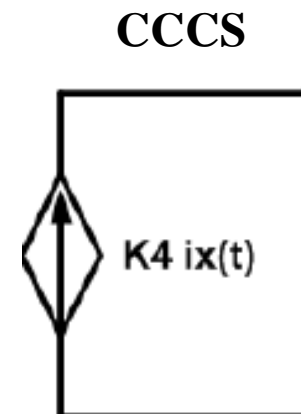
Current  
Controlled  
Voltage  
Source



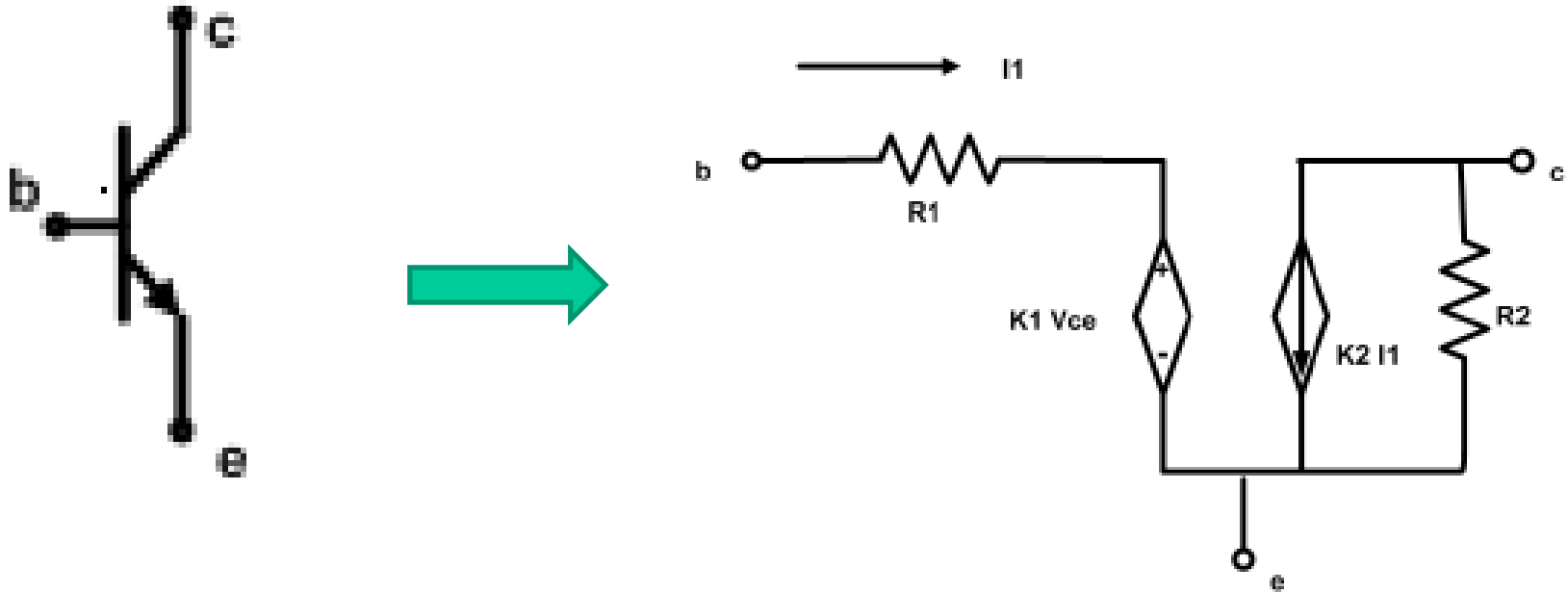
Voltage  
Controlled  
Current  
Source



Current  
Controlled  
Current  
Source



# Transistor Model example



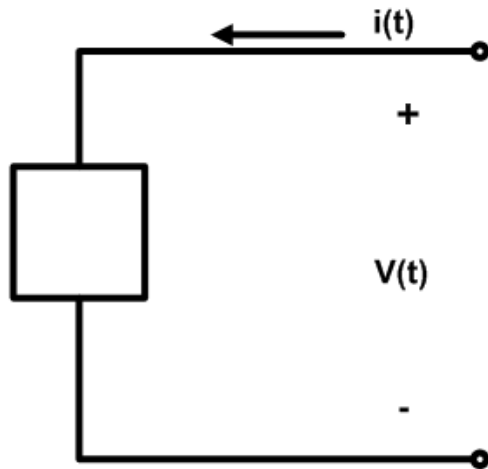


# Power and Energy

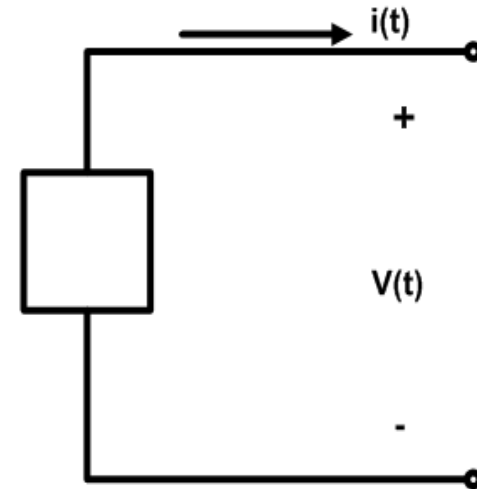
- Why Power & Energy are important in circuit analysis?
  - Although current and voltage are useful in analysis & design of electrical systems, the useful **output of the system often is non-electric**, & this output is usually expressed in terms of power & Energy.
  - Also, all **practical devices have limitations** on the amount of power that they can handle.

# Power and Energy

$$p(t) = \frac{dw(t)}{dt}$$



$$p(t) = +v(t)i(t) \text{ absorbing}$$



$$p(t) = -v(t)i(t) \text{ supplying}$$

**Power:** is defined as the time rate of supplying or absorbing energy.

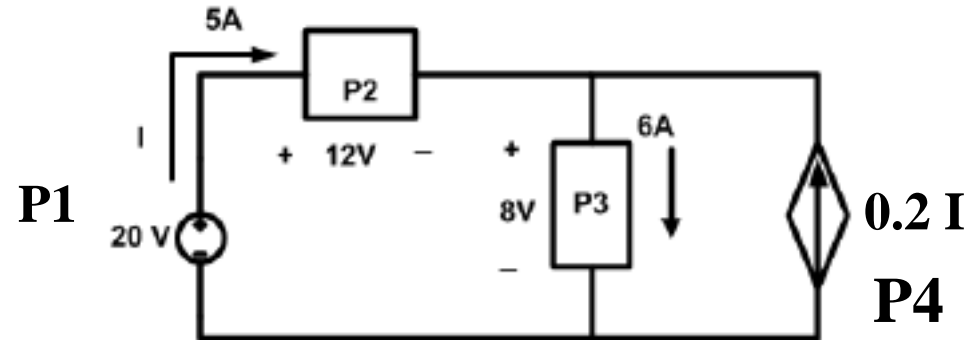
“a water pump rated 75 kW can deliver more liters per second than one rated 7.5 kW”

# Conservation of Energy

- The law of conservation of energy must be obeyed in any electric circuit .
- The algebraic sum of power in a circuit at any instant of time , must be zero.

$$\sum p(t) = 0$$

- Calculate power supplied or absorbed by each element



$$p_1 = (20)(-5) = -100 \text{ w} \quad \textit{supplied power}$$

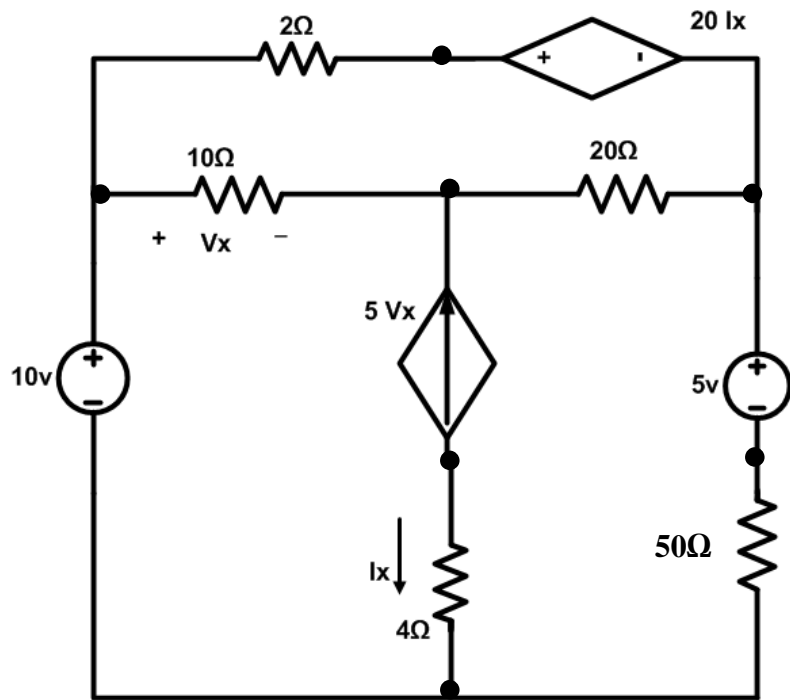
$$p_2 = (12)(5) = 60 \text{ w} \quad \textit{absorbed power}$$

$$p_3 = (8)(+6) = 48 \text{ w} \quad \textit{absorbed power}$$

$$p_4 = (8)(-0.2 \times 5) = -8 \text{ w} \quad \textit{supplied power}$$

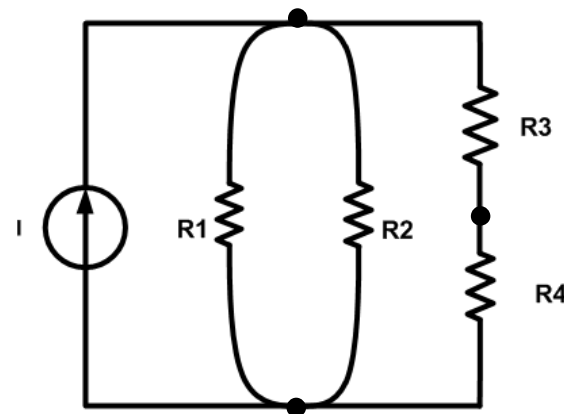
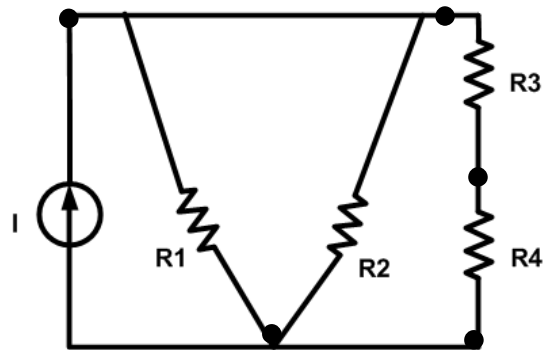
$$p \textit{ absorbed} = p \textit{ supplied}$$

$$60 + 48 = 100 + 8$$



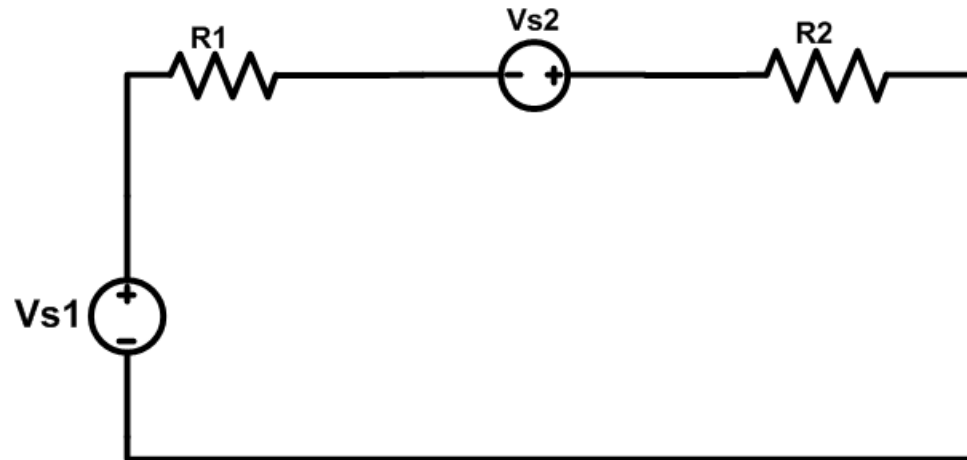
## Definitions

- Node : A point of connection of two or more circuit elements.
- Loop: Any closed path through the circuit in which no node is crossed more than once.
- Mesh : Any loop that doesn't contain within it another loop.



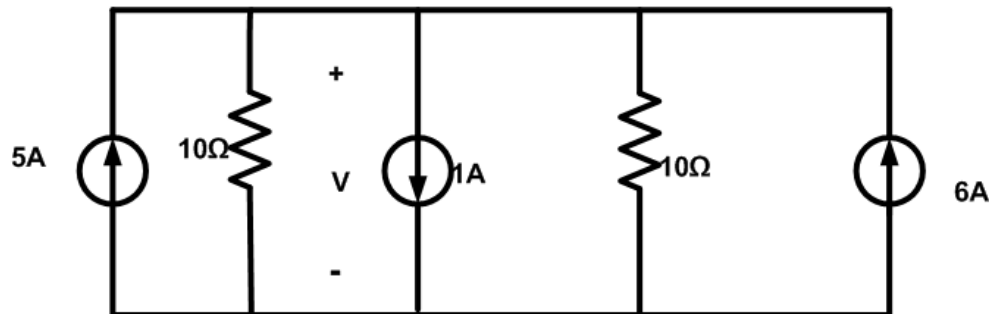
# Series connections

- All of the elements in the circuit shown below carry the same current then said to be connected in series.



# Parallel Connection

- Elements in a circuit having a common voltage across them are said to be connected in parallel.



**Two key laws for analyzing circuits:**

Kirchhoff's Voltage Law (KVL)

Kirchhoff's Current Law (KCL)

**Kirchhoff's Voltage Law (KVL)**

Definition: “The algebraic sum of the voltages around any closed path equals zero.”

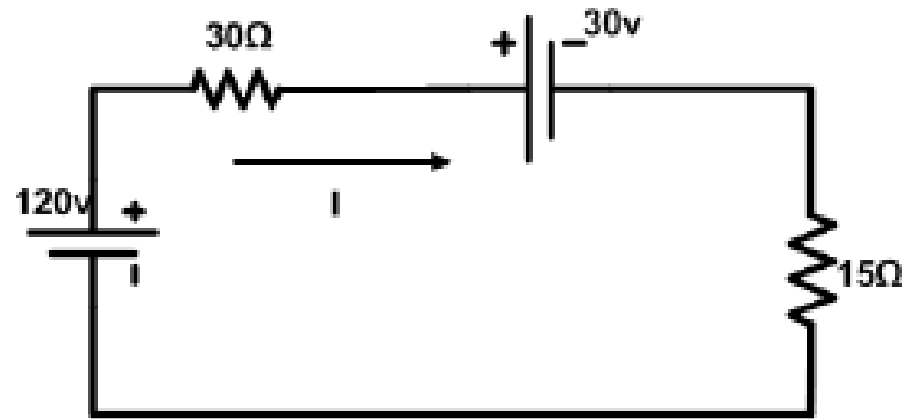
**Notes:**

- Start at any point in a path
- Go around the loop in either direction until you return to the starting point
- Use a consistent sign convention



# Analysis of a single- loop circuit

Find I?

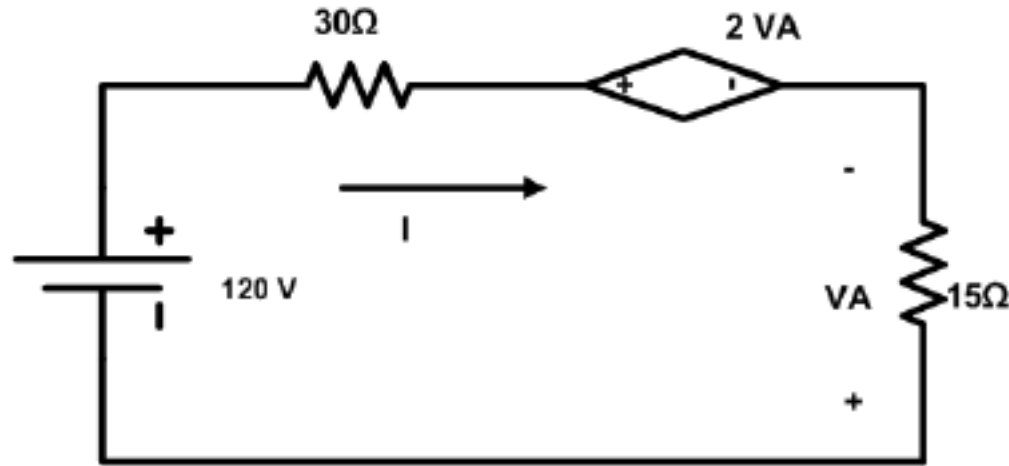


KVL

- $30 I + 30 + 15 I - 120 = 0 \rightarrow$
- $45 I = 90 \rightarrow I = 2 \text{ A}$
- $V(30\Omega) = (30 \Omega) \cdot (2 \text{ A}) = 60 \text{ V}$
- $V(15\Omega) = (15 \Omega) (2 \text{ A}) = 30 \text{ V}$

# Analysis of a circuit containing a dependent source .

- Find  $I$ ?  
and calculate power absorbed by each circuit element



$$30I + 2V_A + 15I - 120 = 0$$

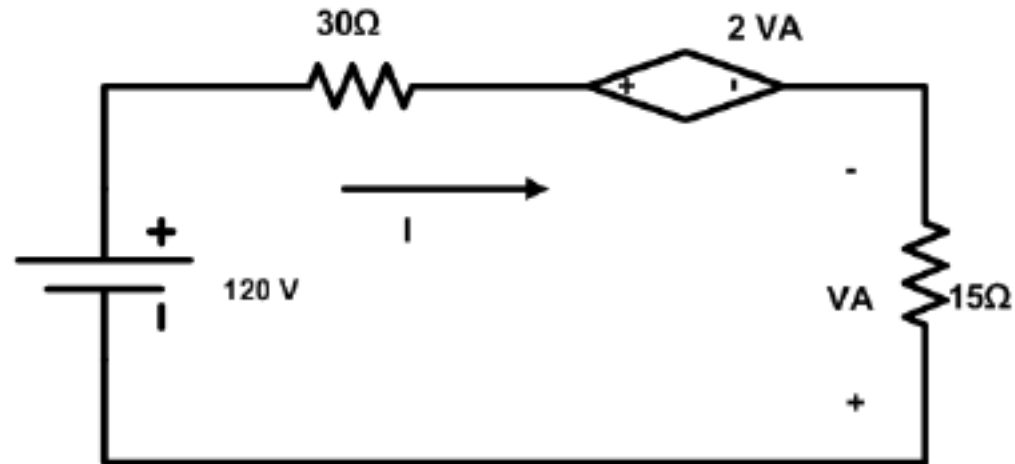
$$\rightarrow V_A = -15 I$$

$$\rightarrow I = 120/15 = 8A$$

$$\rightarrow V_A = -120 V$$

# Analysis of a circuit containing a dependent source

- Find  $I$ ?  
and calculate power absorbed by each circuit element

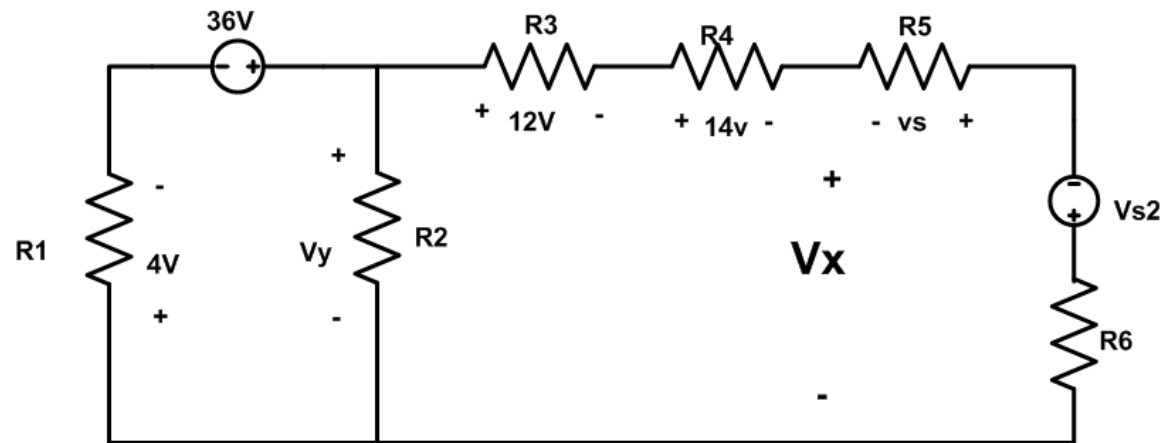


$$I = 120/15 = 8\text{A}$$

$$V_A = -120\text{V}$$

- Answers:
- $P(120\text{V}) = -960\text{ W}$
- $P(2V_A) = -1920\text{ W}$
- $P(30\Omega) = 1920\text{ W}$
- $P(15\Omega) = 960\text{ W}$

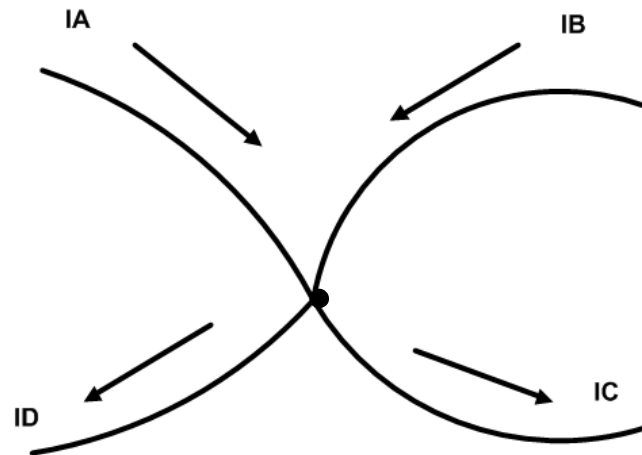
# Applying KVL



- Find  $V_x$  and  $V_y$
- KVL for 1-st loop:  $4 - 36 + V_y = 0$   
 →  $V_y = 36 - 4 = 32 \text{ V}$
- KVL for second loop:  $-V_y + 12 + 14 + V_x = 0$   
 →  $V_x = -14 - 12 + 32 = 6 \text{ V}$

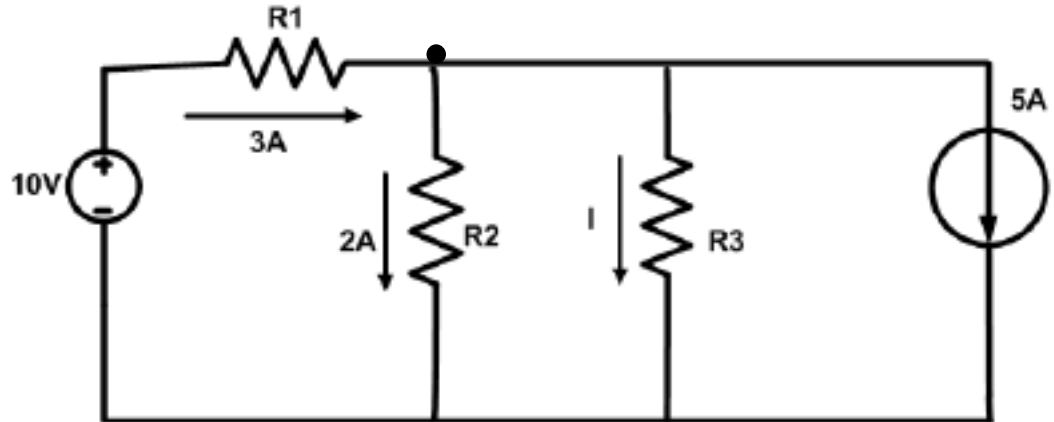
# Kirchhoff's current law : KCL

- KCL : the algebraic sum of the current entering any node is zero
- $I_A + I_B - I_C - I_D = 0$
- KCL: Alternative form
- Sum of Currents In = Sum of Currents out
- $I_A + I_B = I_C + I_D$



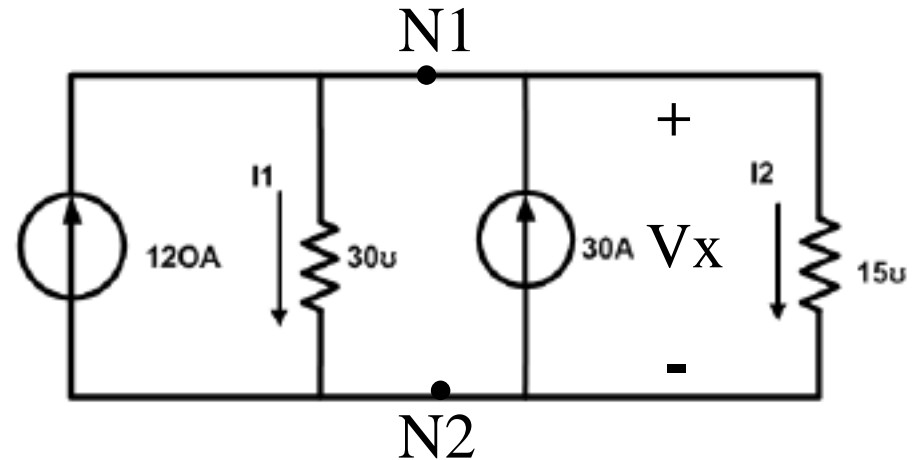
# KCL Application

- Find  $I$ ?
  - KCL :
  - $3 = 2 + I + 5$
- $I = -4A$**



# Single node-pair circuit

- Find  $V_X$ ?
- Remember  $I = G \cdot V$



- KCL at node1 :  $120 + 30 = I1 + I2$

$$120 + 30 = 30V_X + 15V_X$$

➔  $V_X = 3.33 \text{ V}$

- $I(30\text{u}) = 100 \text{ A}$
- $I(15\text{u}) = 50 \text{ A}$

# Analysis of circuit containing dependent sources

- Find  $V_X$

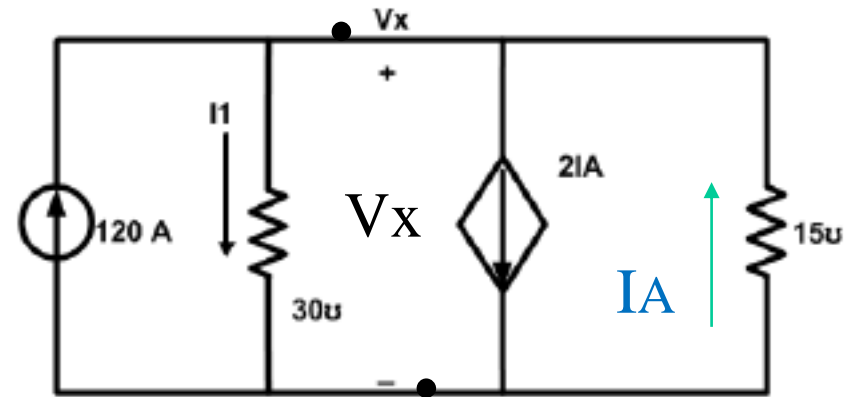
KCL ;

- $120 + I_A = I_1 + 2 I_A$

- $I_A = -15V_X$

- $I_1 = 30V_X$

**$\therefore V_X = 8 \text{ V}$**





# Applying KVL and KCL

- Solve for  $V_x$  and  $i_x$

- KVL :  $-60 + (5A)(8\ \Omega) + V_1 = 0$

- $\rightarrow V_1 = 60 - 40 = 20\text{ V}$

- $\rightarrow I_1 = 20/10 = 2\text{ A}$

- $\rightarrow$  KCL :  $I_2 = 5 - 2 = 3\text{ A}$

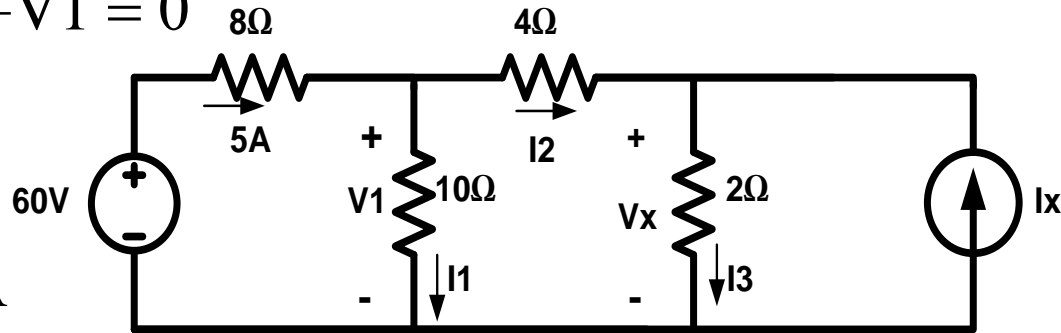
- $\rightarrow$  KVL :  $I_2(4\ \Omega) + V_x - V_1 = 0$

- $\rightarrow V_x = 8\text{ V}$

- $I_3 = 8/2 = 4\text{ A}$

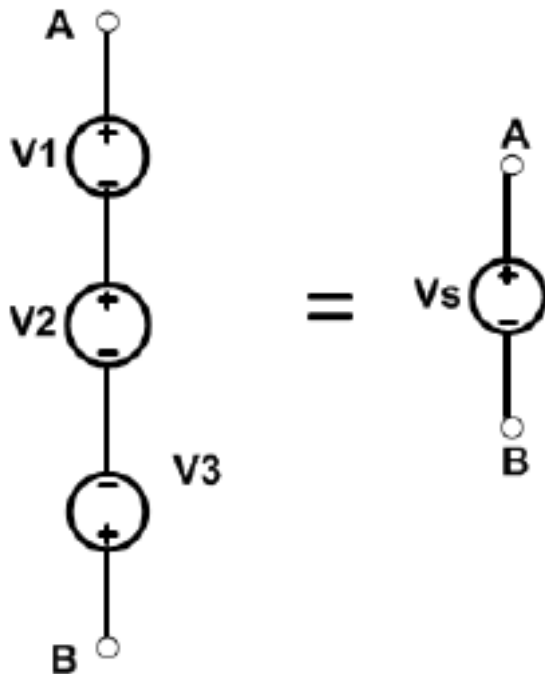
- KCL :  $i_x = I_3 - I_2 = 4 - 3 = 1\text{ A}$

- Answer :  $V_x = 8\text{ v}$  and  $i_x = 1\text{ A}$



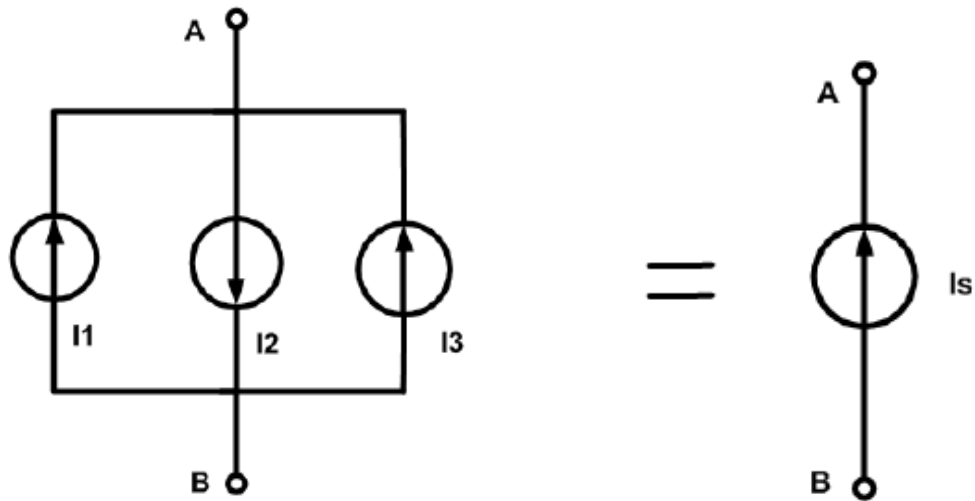
# Series and parallel sources

- Voltage sources connected in series can be combined into an Equivalent source :



$$V_s = V_1 + V_2 - V_3$$

- Current sources connected in parallel can be combined in to an equivalent current source :



$$I_S = I_1 - I_2 + I_3$$

# Impossible Circuit Configurations

