



BIRZEIT UNIVERSITY
BIRZEIT UNIVERSITY
Faculty of Engineering
Electrical Engineering Department
Signals and Systems - ENEE334
First Exam

Instructors: Mr. A Rimawi

Dec.9, 2012

Problem 1 (10 pts):

State whether each of the following statements is True or False, justify your answer

- a. If a signal $f(t)$ is odd then $-f(-t)$ is an even signal.
- b. A time-invariant system must also be linear.
- c. A periodic signal $f(t)$ is equal to its Fourier series representation for all $t \in \mathbb{R}$.
- d. The signal $x(t) = \cos(\sqrt{2} \pi t) + \sin(2\sqrt{2} \pi t)$ is periodic.
- e. Periodic signals are always finite energy signals.

Problem 2 (20pts):

Let H be a continuous-time Linear-Invariant system (LTI), such that the system's response to a pulse input $p(t) = u(t) - u(t - 1)$ is $H\{p(t)\} = y_p(t)$. Both signals are depicted in Figure 1(a).

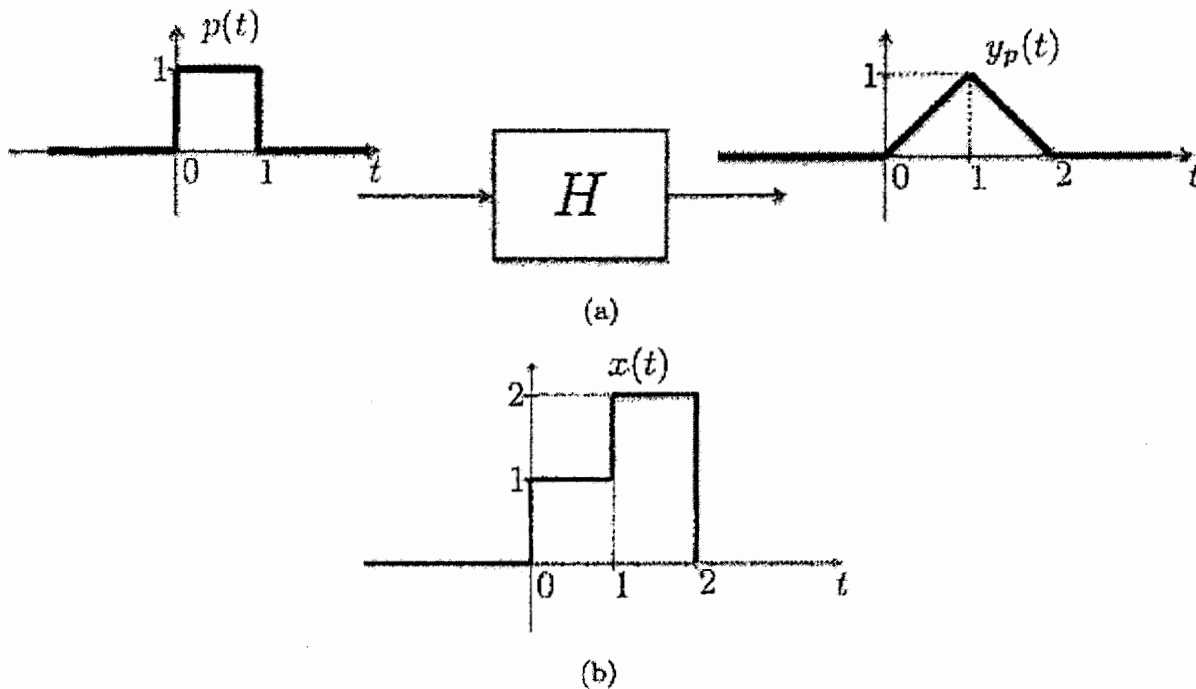


Figure 1

Given only the information above we want to calculate the system's response input $x(t)$ depicted in Figure 1(b). Let's break down the problem into two parts.

- a. Note that $x(t)$ can be written as a sum of scaled and time-shifted versions of $p(t)$. In particular

$$x(t) = a p(t) + b p(t - t_0)$$

Find the adequate values of a , b and t_0

- b. Use what you know about the system and the result of part (a) to plot the system's response to input $x(t)$.

Problem 3 (20pts):

Consider the periodic signal $x(t)$ given by the expression

$$x(t) = (2 + 2j)e^{-j3t} - 3je^{-j2t} + 5 + 3j e^{j2t} + (2 - 2j)e^{j3t}$$

- What is the period and fundamental frequency of $x(t)$.
- Justify that $x(t)$ is a real signal and write the corresponding compact trigonometric Fourier series representation.
- Sketch both the exponential Fourier spectra and trigonometric Fourier spectra of the signal.
- What is the power of $x(t)$.

GOOD LUCK ☺

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Dec.22, 2013

In all Questions assume the system diagram as shown in figure 1

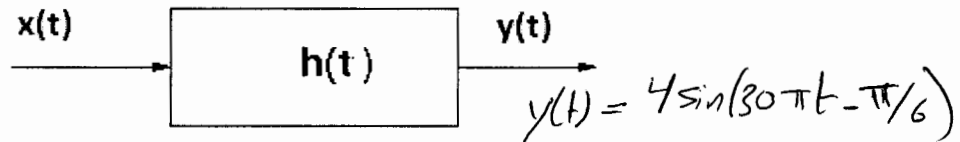
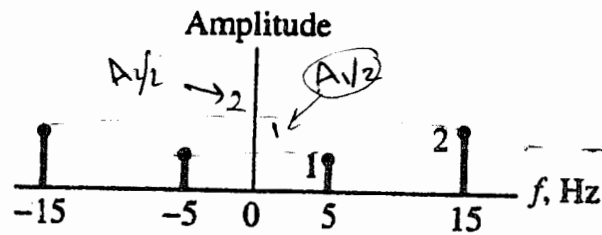


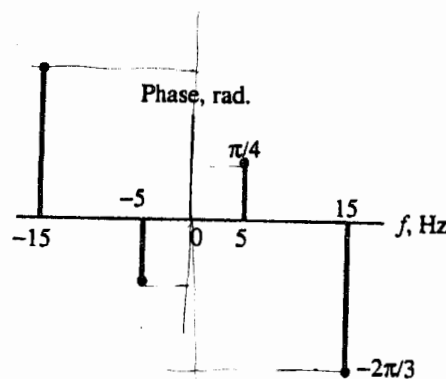
Fig1

Problem 1 (30pts):

For the following double-sided amplitude and phase spectrum of the input signal, $x(t)$ is shown in figure 2



$$\begin{aligned}
 f_1 &= 5 & T_1 &= \frac{1}{5} \\
 f_2 &= 15 & T_2 &= \frac{1}{15}
 \end{aligned}$$



$$\begin{aligned}
 y(t) &= h(t-2) \int_{-\infty}^{\infty} x(\lambda) d\lambda \\
 y(t) &= h(t-2) \left[\int_{-\infty}^{-5} 2 \cos(\pi\lambda t + \pi/4) d\lambda + \int_{-5}^5 1 \cos(\pi\lambda t + \pi/4) d\lambda + \int_5^{15} 2 \cos(\pi\lambda t - 2\pi/3) d\lambda \right]
 \end{aligned}$$

Fig 2

- Find $x(t)$
- Find $h(t)$, $H(f)$
- Calculate the average power of the input signal $x(t)$, and output signal $y(t)$
- Design the LTI system, $h(t)$

Problem 2 (35pts):

Consider the input signal; $x(t)$, and amplitude and phase spectrum of the system, $h(t)$ are shown in figure 3, and figure 4, respectively

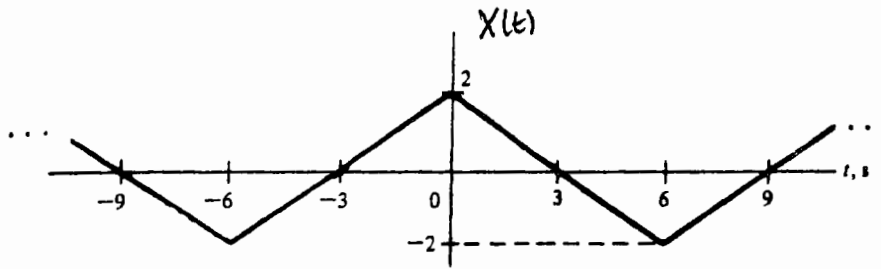


Fig3

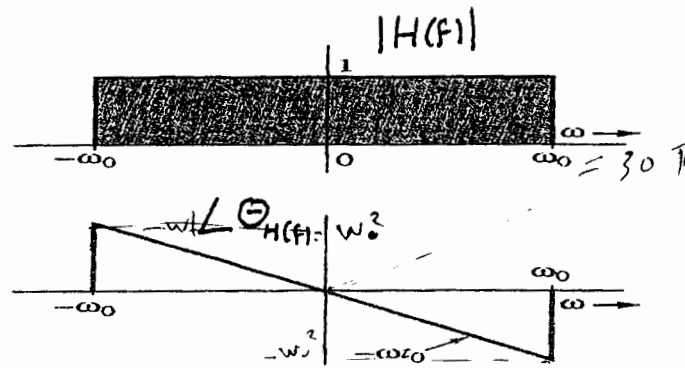


Fig4

$\frac{2}{5}x = 2$
 $(-6, -2)$
 $(0, 2)$
 $\text{slope} = \frac{4}{6} = \frac{2}{3}$
 $y - 2 = \frac{2}{3}(x)$
 $y = \frac{2}{3}x + 2$
 $y = \frac{2}{3}(x + \frac{3}{2})$

$(6, -2)$
 $\text{slope} = \frac{4}{-6} = -\frac{2}{3}$
 $y - 2 = -\frac{2}{3}x$
 $y = -\frac{2}{3}x + 2$

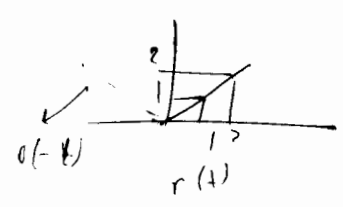
$y(t) = -\omega t$

$-r(t + \omega_0)$

$-\omega t_0 + 0$

$-\omega(t + \omega_0)$

$-\omega r(t)$



- Find $x(t)$, and $X(f)$
- Plot the input spectrum signal, $X(f)$
- Find the system response, $h(t)$
- Find the output signal, $y(t)$, and its spectrum, $Y(f)$

Problem 3 (30pts):

Consider the system response, $h(t)$ is given as

$h(t) = u(t) + e^{-3t}u(t)$

- Find the Laplace Transform of the system response, $h(t)$
- Find the Region of Convergence ROC
- Plot the s-plane for the system
- Design the system

$\mathcal{L}\left(e^{j(10\pi t + \frac{\pi}{4})} + e^{-j(10\pi t + \frac{\pi}{4})} \right)$