

L16 : Part 2 : FET ac analysis \Rightarrow

Common-Source (CS) Self Bias Effect of R_i

here $V_g = \frac{R_G}{R_G + R_i} \cdot V_i$

$V_{gs} = V_g - V_s$

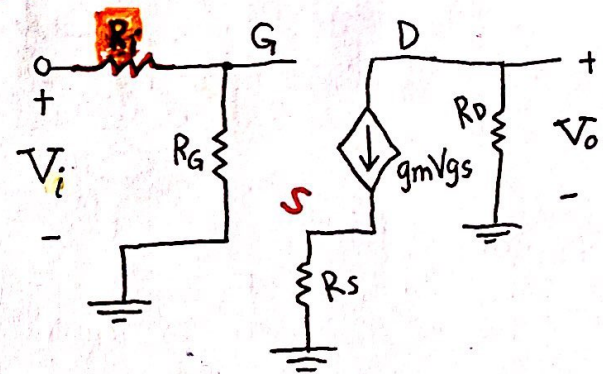
$V_{gs} = \frac{R_G}{R_G + R_i} \cdot V_i - g_m V_{ss} R_s$

$V_i = V_{gs} (1 + g_m R_s) \frac{R_G + R_i}{R_G}$

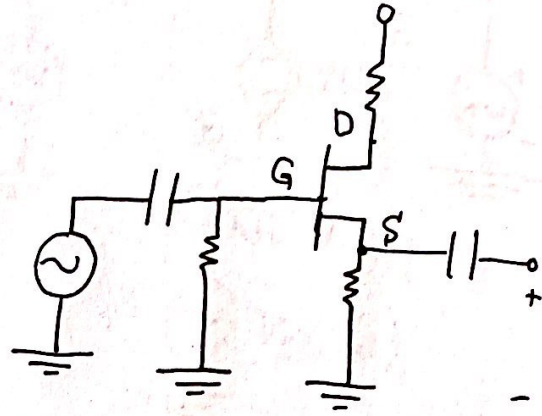
$V_o = -g_m V_{gs} R_D$

$A_v = \frac{V_o}{V_i} = \frac{-g_m R_D}{1 + g_m R_s} \left[\frac{R_G}{R_G + R_i} \right]$

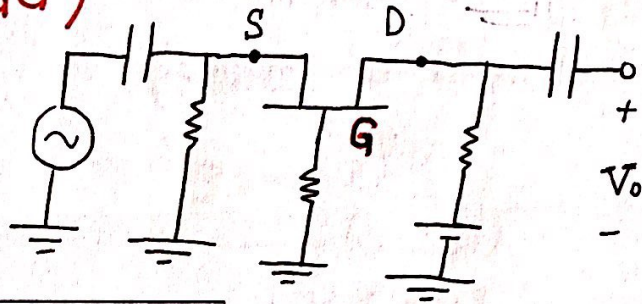
AV is reduced Further due to R_i



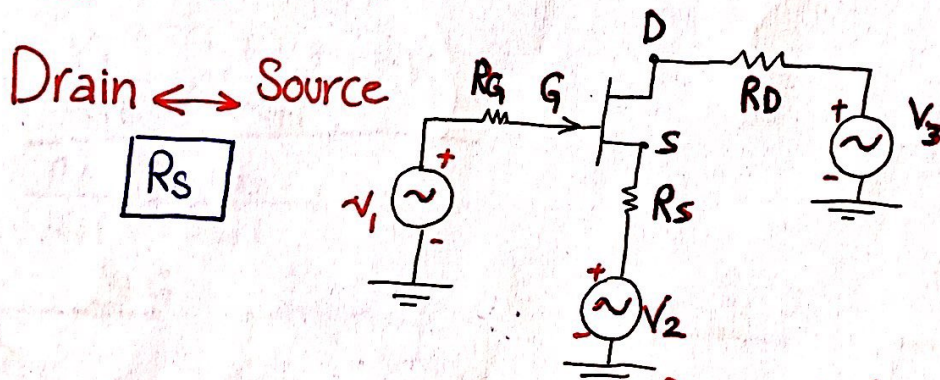
2] Common drain (CD)



3] Common Gate (CG)



Impedance Reflection



KVL :

$$V_3 + \mu V_{gs} = I_D r_{ds} + I_D R_D + I_D R_S + V_2 \dots (*)$$

$$V_{gs} = V_g - V_s \dots [1]$$

$$= V_g - (I_D R_S + V_2) \dots [2]$$

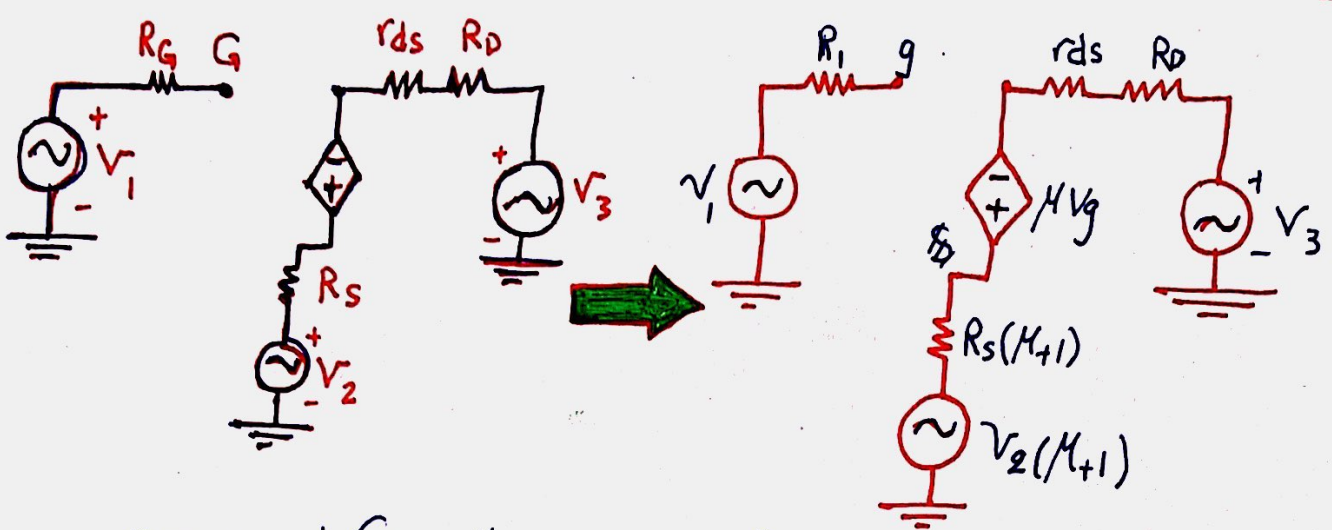
$$V_s = I_D R_S + V_2 \dots \rightarrow \text{at } [1]$$

(*) بـ [2] نعوض

$$V_3 + \mu (V_g - (I_D R_S + V_2)) = I_D (r_{ds} + R_D + R_S) \dots [6]$$

$$I_D = \frac{V_3 + \mu V_g - V_2 (\mu + 1)}{R_D + r_{ds} + R_S (\mu + 1)}$$

$$i = \frac{\Delta V}{\Sigma R}$$



Original Circuit

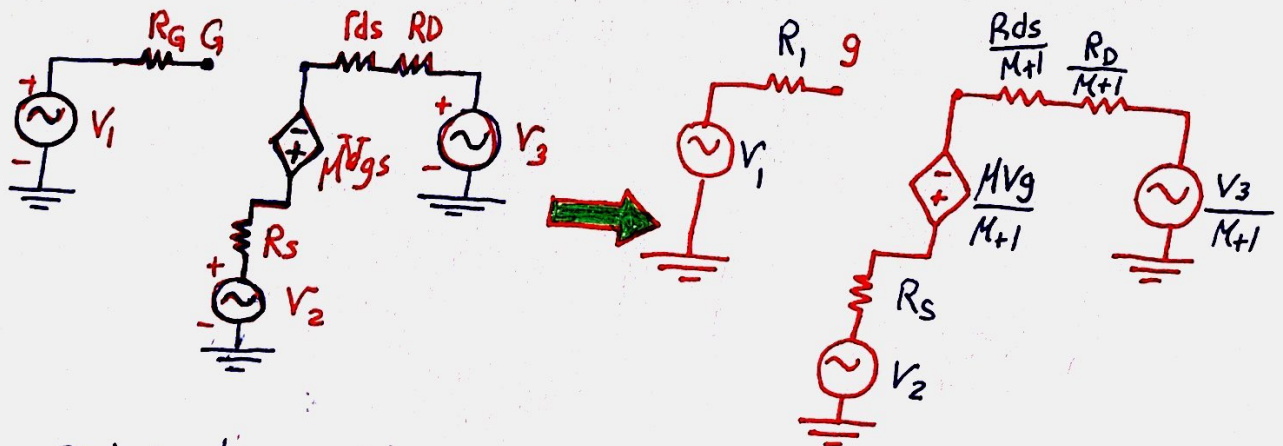
Drain Equ. Circuit
(Source to Drain)

$$\begin{aligned} \mu V_{gs} &\rightarrow \mu V_g \\ R_S &\rightarrow R_S(\mu+1) \\ V_2 &\rightarrow V_2(\mu+1) \end{aligned}$$

$M+1$ etc (convert)

$$I_D = \frac{V_3}{\mu+1} + \frac{\mu V_g}{\mu+1} - V_2$$

$$\frac{R_D}{\mu+1} + \frac{r_{ds}}{\mu+1} + R_S$$



Original circuit

Source Eq. Circuit
(Drain to Source)

$$\begin{aligned} \mu V_{gs} &\rightarrow \frac{\mu V_g}{\mu+1} & R_D &\rightarrow \frac{R_D}{\mu+1} \\ V_3 &\rightarrow \frac{V_3}{\mu+1} & r_{ds} &\rightarrow \frac{r_{ds}}{\mu+1} \end{aligned}$$

7.

Example : Phase splitting Circuit

Two outputs : treated one @ time

Find $A_{V_1}, A_{V_2}, Z_i, Z_{O1}, Z_{O2}$

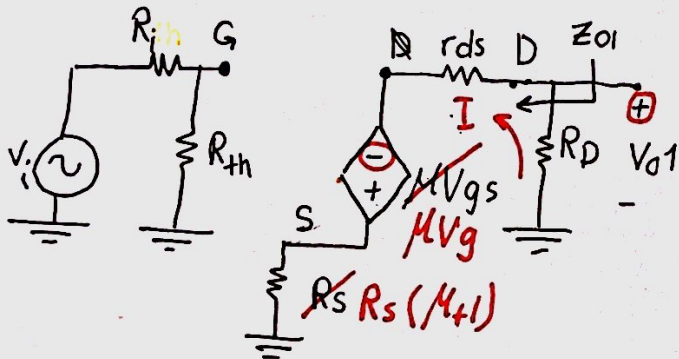
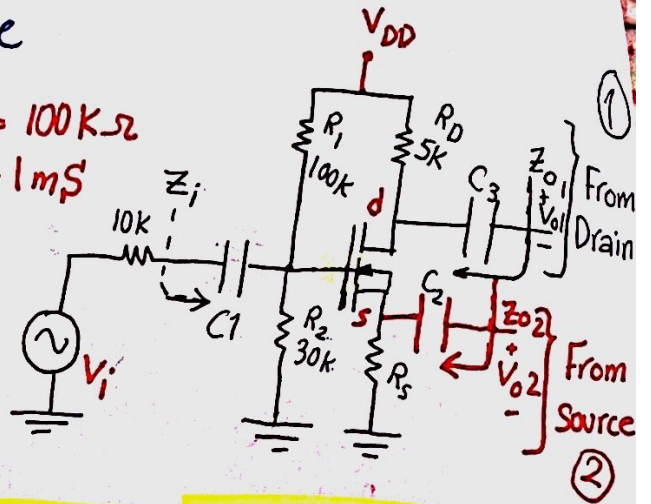
$r_{ds} = 100k\Omega$
 $g_m = 1mS$

Two outputs:

V_{O1} : Drain

V_{O2} : Source

(1)



(D) From S to D

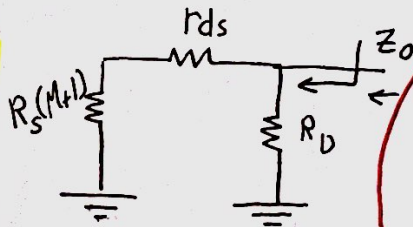
$$V_{O1} = \frac{R_D}{R_D + r_{ds} + R_S(M+1)} \cdot (-M V_g)$$

$$V_g = \frac{R_{th}}{R_{th} + R_i} \cdot V_i$$

$$A_{V_1} = \frac{V_{O1}}{V_g} \cdot \frac{V_g}{V_i} = \sqrt{\quad}$$

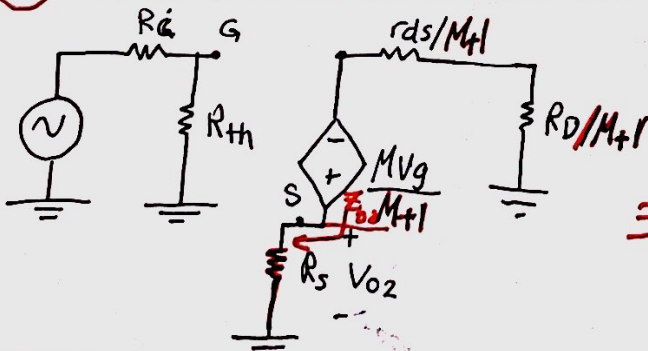
$$Z_{O1} = R_D \parallel (r_{ds} + R_S(M+1))$$

$V_i \rightarrow 0 \Rightarrow V_g = 0 \Rightarrow M V_g = 0$

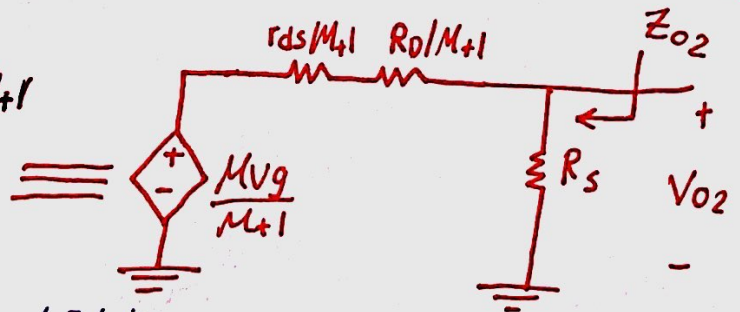


$$Z_i = R_{th}$$

(2) reflection from Drain to Source



$$V_{O2} = \frac{R_S}{R_S + \frac{r_{ds} + R_D}{M+1}} \cdot \frac{M V_g}{M+1}$$



$$V_g = \frac{R_{th}}{R_{th} + R_i} \cdot V_i$$

$$Z_{O2} = R_S \parallel \left(\frac{r_{ds} + R_D}{M+1} \right)$$

$V_i = 0 \Rightarrow V_g = 0$

.8. Back $\Rightarrow \infty = r_{ds}$ فرضاً

$$\mu = g_m r_{ds} \rightarrow \infty$$

$$Z_{o2} = R_s \parallel \left(\frac{r_{ds} + R_D}{\mu + 1} \right)$$

$$\left. \frac{r_{ds} + R_D}{\mu + 1} \right|_{r_{ds} \rightarrow \infty} = \frac{r_{ds} + R_D}{g_m r_{ds} + 1}$$

$$\left. Z_{o2} \right|_{r_{ds} \rightarrow \infty} = R_s \parallel \left. \frac{1}{g_m} \right|_{r_{ds} \rightarrow \infty}$$

$$\lim \frac{1 + \cancel{R_D/r_{ds}}}{g_m + \cancel{1/r_{ds}}} = \frac{1}{g_m}$$

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