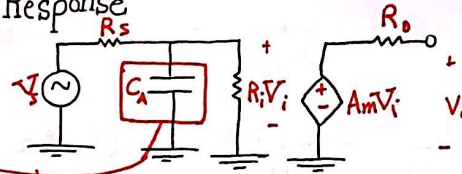


# Electronics 236 - L23, Part 1 & 2 - Frequency Response

## Shunt Caps & high Frequency Response

بين G و S  
او بين B و E



$$V_o = A_m V_i, \text{ Am Gain @ mid band}$$

$$V_i = \frac{R_i // \frac{1}{j\omega C_A}}{R_i + \frac{1}{j\omega C_A} + R_s} \times V_s$$

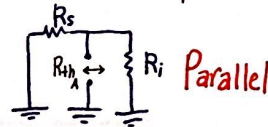
$$A(j\omega) = A_m \left( \frac{R_i}{R_i + R_s} \right) \cdot \left( \frac{1}{1 + j\omega C_A (R_s // R_i)} \right)$$

$$|A(j\omega)| = A_m \frac{R_i}{R_i + R_s} \frac{1}{\sqrt{1 + [\omega C_A (R_s // R_i)]^2}}; \text{ @ } \omega = \omega_{CA}$$

$$\therefore |A(j\omega_{CA})| = A_v(\text{mid}) \frac{1}{\sqrt{2}}$$

$$\therefore \rightarrow \omega_{HCA} (R_s // R_i) = 1 \Rightarrow \omega_H = \frac{1}{CA (R_s // R_i)} \leftarrow \text{high freq. corner freq.}$$

$(R_s // R_i) \equiv R_{th}$  thevenin's impedance seen by CA  
 $V_s = 0$



[For  $A_v(\text{mid}) = A_m = 1$ ]

$$\text{@ } \omega = \omega_{CA} \rightarrow 20 \log | | = 20 \log \frac{1}{\sqrt{2}} = -3 \text{ dB}$$

$$\text{@ } \omega = 10 \omega_{CA} \rightarrow 20 \log 10 = -20 \text{ dB}$$

$\therefore$  This is LPF



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# Notes

1 If there is one Cap of this type we find  $W_{CA} = \frac{1}{R_{TH} C_A}$ ; &  $W_H = W_{CA}$

2 If there is two Caps  $C_A$  &  $C_B \Rightarrow A(j\omega) = A_{v(mid)} \frac{1}{(1 + \frac{j\omega}{W_{CA}})} \frac{1}{(1 + \frac{j\omega}{W_{CB}})}$   
 To find  $W_H$  "على فرض انهم لا تتوازي ولا تتوالي - بماد عن بعض" LPF

$$|A(j\omega_H)| = \frac{A_{m(mid)}}{\sqrt{2}} = \frac{A_v(mid)}{\sqrt{(1 + \frac{j\omega}{W_{CA}})(1 + \frac{j\omega}{W_{CB}})}}$$

By solving For  $|A(j\omega_H)|$  @  $\omega = W_H$ , we get an approximate expression to Evaluate  $W_H$

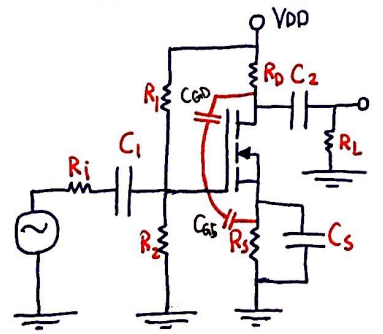
- Assuming  $W_{CA} > W_{CB}$

$$1 / (\frac{1}{W_{CA}} + \frac{1}{W_{CB}}) < W_H < W_{CB}$$

$$\frac{W_{CA} \cdot W_{CB}}{W_{CA} + W_{CB}} < W_H < W_{CB}$$

$$\text{lower limit} < W_H < \min(W_S)$$

## Example - high Freq. $W_H$ ?



اول سؤال هو متو هم الكابستز التي بالهوا بقيمة  $W_H$   
 $[C_{GD}, C_{GS}]$

$C_1, C_2, C_s \rightarrow$  Short  
 $C_{GD}, C_{GS} \rightarrow$  are considered one @ a time while all other high freq are open

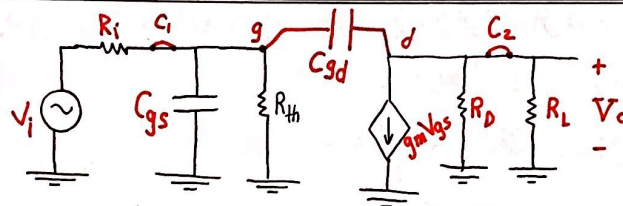
# Example - High Freq.

- high Freq. ss Eq. Circuit.
  - ↳  $C_1, C_2, C_s \rightarrow$  Short
  - ↳  $C_{gs}, C_{gd} \rightarrow 1$  @ a time, while others high freq. open!

-  $\omega_H$  is estimated using Formmlula.

$$\frac{1}{\frac{1}{\omega_{CA}} + \frac{1}{\omega_{CB}}} \ll \omega_H \ll \min(\omega_n's)$$

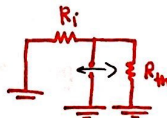
High Freq  
ss Eq. Circuit



1. Consider  $C_{gs}$  ( $C_{gd}$  open)

$$\omega_{C_{gs}} = \frac{1}{C_{gs} R_{gs}}$$

هي عبارة عن المقاومة التي تروى  
Indep. Sources الـ Cap  
Killed

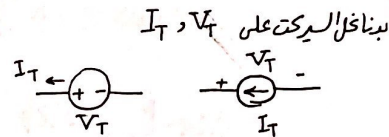
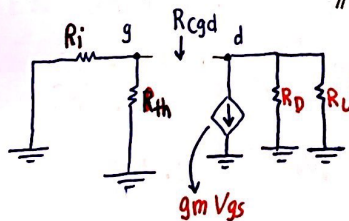


$$R_{gs} = R_i \parallel R_{th}$$

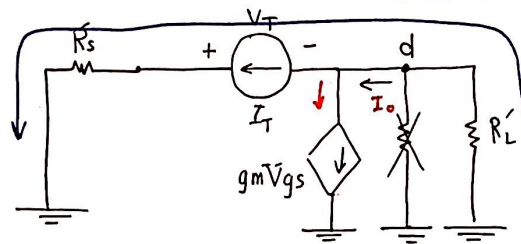
$V_i = 0$

$$\omega_{C_{gs}} = 668.45 \text{ M rad/sec} \quad // (6.28) = 2\pi \text{ لو بننا F بقدر نفس القيمة}$$

2.



$$R_{gd} \Big|_{V_i=0} = \frac{V_T}{I_T}$$



- $I_o = I_T + g_m V_{gs}$
- $V_{gs} = V_g = I_T R_s$
- $I_o R_L + I_T R_s = V_T$

$$\rightarrow (g_m V_{gs} + I_T) R_L + I_T R_s = V_T$$

$$(g_m I_T R_s + I_T) R_L + I_T R_s = V_T \Rightarrow g_m R_s R_L I_T + R_L I_T + R_s I_T = V_T$$

$$I_T (g_m R_s R_L + R_L + R_s) = V_T$$

$$\therefore \frac{V_T}{I_T} = g_m R_s R_L + R_L + R_s = R_{gs}$$

2.12.5

## 2. Consider $C_{gd}$ ( $C_{gs} \rightarrow$ open)

$$\omega_{gd} = \frac{1}{C_{gd} R_{gd}} \quad ; \quad R_{gd} \text{ is calculated using } \frac{V_T}{I_T} \text{ method.}$$

$$\omega_{gd} = \frac{1}{C_{gd} R_{gd}} = 48.54 \text{ M rad/sec.}$$

## 3. Estimation of $\omega_H$

$$\frac{668 \times 48}{668 + 48} \ll \omega_H \ll 48.58 \text{ Mrad/sec}$$

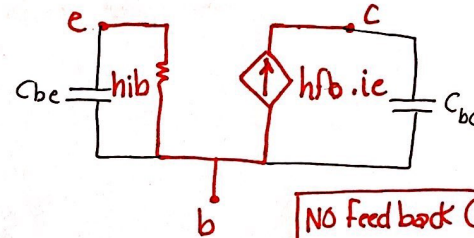
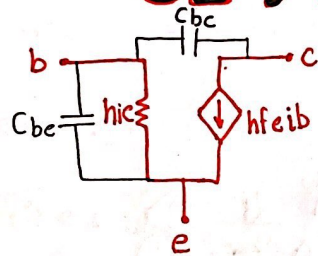
$$[45.25 \ll \omega_H \ll 48.58] \text{ Mrad/sec}$$

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# BJT's

CE, CC

CB



NO Feed back Cap 👍

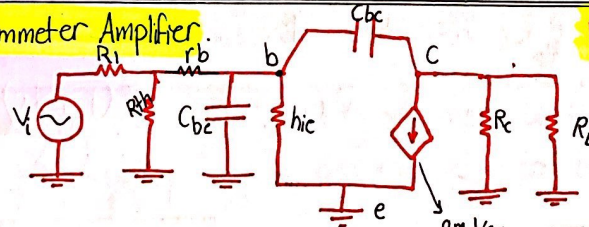
$$h_{fe} i_b = h_{fe} \cdot \frac{V_{be}}{h_{ie}}$$

$$= g_m \cdot V_{be}$$

$$g_m = \frac{h_{fe}}{h_{ie}}$$

\* Common Emitter Amplifier

\* Example



HF ac ss eq. Circuit

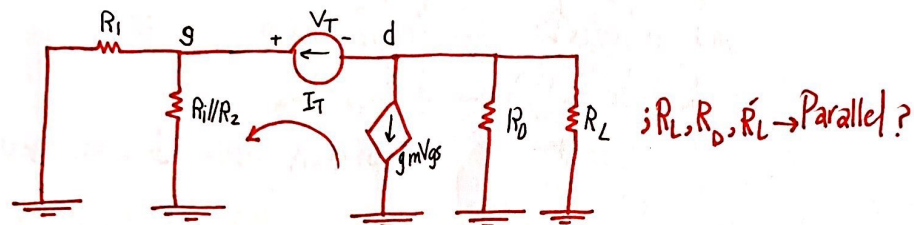
$$W_{be} = \frac{1}{C_{be} R_{be}}$$

$$R_{be} |_{V_i=0} = ([R_1 // R_{th}] + r_b)$$



2 Consider  $C_{gd}$  ( $C_{gs} \rightarrow$  open)

$\omega_{gd} = \frac{1}{C_{gd} R_{gd}}$  ;  $R_{gd}$  is calculated using  $\frac{V_T}{I_T}$  method.



Find  $\omega_H$ ?

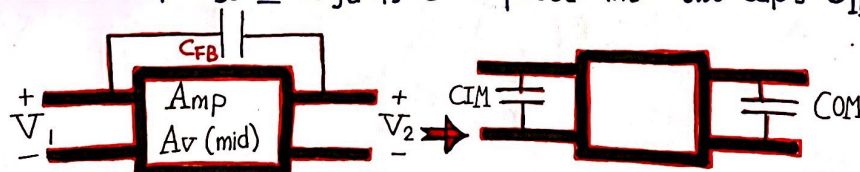
2) choose  $\omega_{bc} = \frac{1}{C_{bc} R_{bc}} = \dots$

$R_{bc} \Big|_{\omega=0} = R_s \parallel (R_1 \parallel R_{th}) + r_b$

**Note To Self:** FET  $\rightarrow$  has high Freq Response Better than BJT

**Miller Theorem:** used in Inverting amplifiers to find  $\omega_H$ .

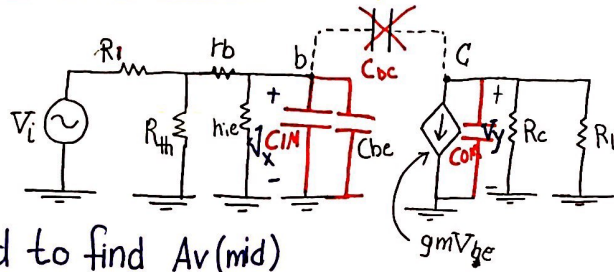
- Feedback Cap  $C_{bc}$  or  $C_{gd}$  is decomposed into two caps  $C_{IM}$   $C_{OM}$



$C_{IM} = C_{FB} [1 - A_v(\text{mid})]$

$C_{OM} = C_{FB} [1 - \frac{1}{A_v(\text{mid})}]$

# Back to Example @ Page 5



We need to find  $A_v(\text{mid})$

•  $A_v(\text{mid}) = \frac{V_y}{V_x}$  ,  $C_{FB} = C_{bc}$

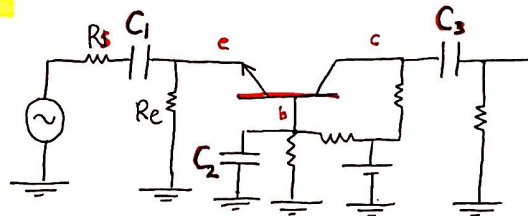
Miller Theorem

•  $\omega_L = \frac{1}{(C_{bc} + C_{in}) R_I}$

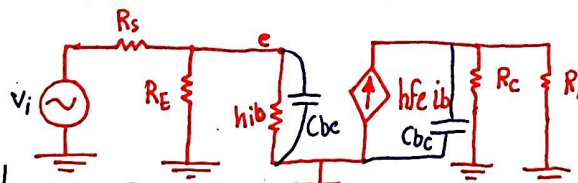
•  $R_I = R_{bc}$  "found earlier" =  $(R_i // R_{th}) + r_d$

•  $\omega_0 = \frac{1}{C_{out} R_o}$  ;  $R_o = R_c // R_L$   
 $V_i = 0$

## CB Example



$\omega_H$



$\omega_{bc} = \frac{1}{C_{bc} R_{bc}}$  ;  $R_{bc} |_{V_i=0} = R_s // R_E // h_{ie}$

$\omega_{bc} = \frac{1}{C_{bc} R_{bc}}$  ;  $R_{bc} |_{V_i=0} = R_c // R_L$

$\omega_H = \frac{\omega_{bc} \times \omega_{be}}{\omega_{bc} + \omega_{be}} \ll \omega_H \ll \min(\omega_s)$

# Homework →

Estimate the value of low & high frequency Corner frequencies & Calculate the mid-range voltage gain of the following Amplifier

**Important**

$$g_m = 1 \text{ mS}$$

$$C_{gs} = 5 \text{ pF}$$

$$C_{gd} = 2 \text{ pF}$$

$$R_L = 200 \text{ k}\Omega$$

