

## CH600 Three-phase Induction Motor

- ⊗ The distinguishing feature of induction motor is that no field circuit current is required to run the machine <sup>①</sup> advantage
- ⊗ The construction of induction motor.

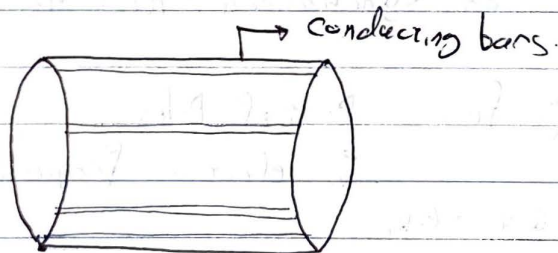
- it has the same stator construction of synchronous motor, with different construction Rotor

- The induction motor has two rotor types:

- ① Squirrel cage rotor
- ② Wound rotor.

### ① Cage Rotor

it consists of series conducting bars laid into slots carved by large short rings ~~are either~~ <sup>1</sup>

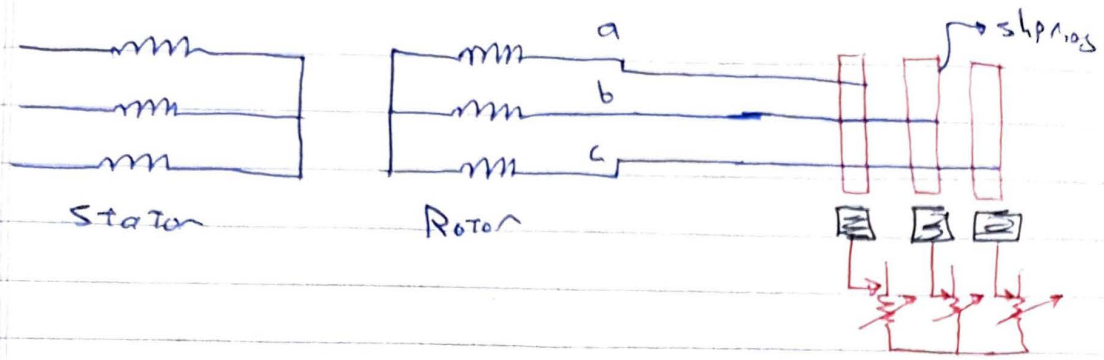


in the face of rotor and shorted at either

### ② Wound Rotor

its consists of a set of 3 $\phi$  windings that are mirror to the stator winding. The winding are usually Y connected. The terminal a, b, c are tied to the sliprings on the rotor's shaft.

The terminal are shorted via brushes.



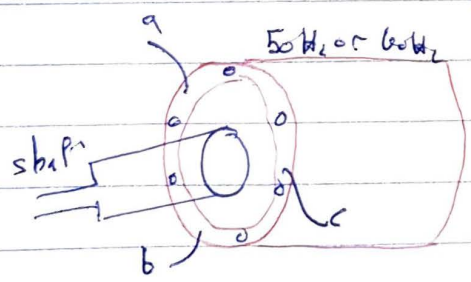
- Notes
- In wound rotor Type, an external resistor can be added to the rotor circuit to modify the Torque-speed characteristic.
  - The wound Rotor is more expensive & it requires much more maintenance.

### Operating Principle of Induction motors.

- A set of three- $\phi$  voltage is applied to the ~~stator~~ stator windings to cause a set of 3- $\phi$  current to flow in stator windings.
- The current will produce a rotating stator magnetic field  $\vec{B}_s$  which rotates at synchronous speed  $\omega_s$ , where  $\omega_s$  is given by

$$\omega_s = \frac{120}{P} f_e$$

$P$ : # of Poles  
 $f_e$ : electric frequency



- The Rotating magnetic field will pass over the conducting ~~bar~~ bars and induces voltage on them.
- $$e_{ind} = (\vec{v} \times \vec{B}_s) \cdot \vec{L}$$
- where  $\vec{v}$  is relative velocity of bars with respect to the speed of  $\vec{B}_s$





- ⊗ The induced voltage will produce a rotor current  $\vec{I}_r$
- ⊗  $\vec{I}_r$  produces  $\vec{B}_r$
- ⊗  $\vec{B}_r$  interact with  $\vec{B}_s$  to produce the induced Torque in the machine  
 $T_{ind} = k \vec{B}_r \times \vec{B}_s$

Note: The Rotor can speed up to synchronous speed, but it can never reach it [to keep emf to]

Speed of  $\vec{B}_s$ :  $\omega_s$   
 speed of  $\vec{B}_r$ :  $\omega_m$ , where  $\omega_m < \omega_s$   
 speed of Rotor:  $\omega_m$

### ⊗ Concept of slip $\alpha$

slip speed  $\omega_a$ : it's the difference between  $\omega_s$  & rotor speed

$$\omega_a = \omega_s - \omega_m \quad \text{or} \quad \omega_a = \omega_s - \omega_m$$

synchronous speed  $\omega_s$       mechanical speed  $\omega_m$

slip ( $\alpha$ ): it's the Ratio of slip speed and synchronous speed

$$\alpha = \frac{\omega_a}{\omega_s} \Rightarrow \boxed{\omega_a = \alpha \omega_s}$$

$$\alpha = \frac{\omega_a}{\omega_s} \Rightarrow \boxed{\omega_a = \alpha \omega_s}$$

$$\alpha = \frac{\omega_a}{\omega_s} = \frac{\omega_s - \omega_m}{\omega_s} = \frac{\omega_s - \omega_m}{\omega_s} \Rightarrow \alpha \omega_s = \omega_s - \omega_m$$

$$\boxed{\omega_m = \omega_s (1 - \alpha)} \quad \omega_s \alpha = \omega_s - \omega_m$$

$$\omega_m = \omega_s (1 - \alpha)$$

## Rotor frequency ( $f_r$ )

when the Rotor is locked ( $\omega_m = 0, a = 1$ )  $\Rightarrow f_r = f_e$

when the Rotor turns at  $\omega_s$  ( $a = 0$ )  $\Rightarrow f_r = 0$

at any other speed than  $\omega_s$ , the rotor frequency is proportional to the slip

$$f_r = a f_e$$

$$\omega_s = \frac{120}{P} f_e \Rightarrow \left[ f_e = \frac{P \omega_s}{120} \right], f_r = (a) \left( \frac{P}{120} \right) \omega_s$$

$$f_r = \frac{P}{120} \omega_m = \frac{P}{120} (\omega_s - \omega_m)$$

Ex

A 208 V, 10 hp, four pole, 60 Hz,  $\Delta$ -connected induction motor has a full load slip of 5%.

- what is the synchronous speed of this motor?
- what is the Rotor speed of this motor?
- what is the Rotor frequency of this motor at rated speed?
- what is the shaft torque of this motor at rated load?

Solution

$$a) \omega_s = \frac{120}{P} f_e = 1800 \text{ rpm}$$

$$b) \omega_m = (1 - a) \omega_s = (1 - 0.05)(1800) = 1710 \text{ rpm}$$

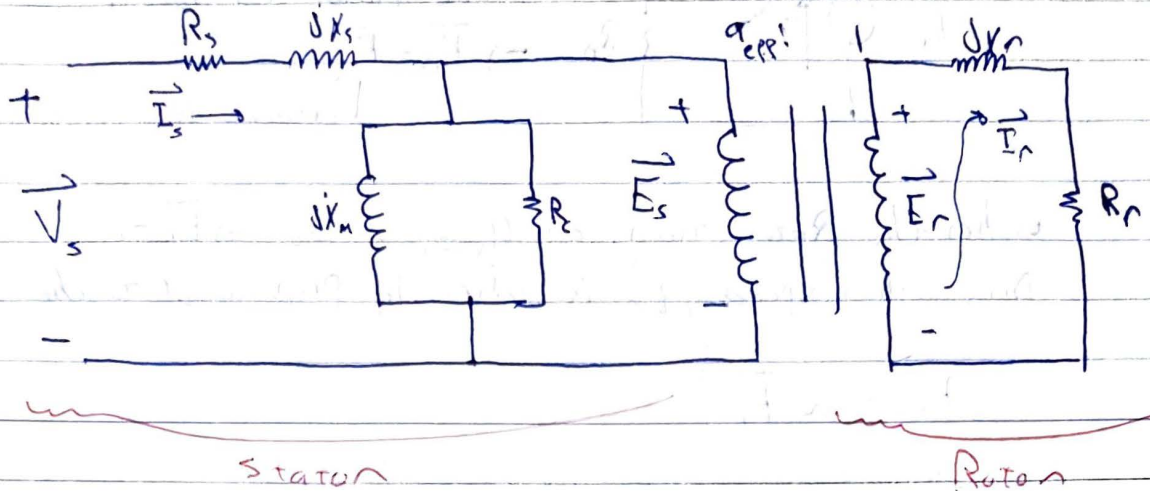
$$c) f_r = a f_e = (0.05)(60) = 3 \text{ Hz}$$

$$d) T_r = \frac{P_r}{\omega_{m,r}} = \frac{(10)(746)}{(1710)(2\pi)} = 41.7 \text{ N.m}$$



## Equivalent circuit of Induction Motors:

its very similar to the per-phase equivalent circuit of Transformer.



$R_s$  % Resistance of stator winding

$R_r$  % Resistance of rotor bar or winding

$X_s$  % stator Leakage Reactance

$X_r$  % rotor Leakage Reactance

$X_m$  % Magnetizing Reactance

$R_c$  % Resistance of core accounting for eddy current & hysteresis

$a_{eff}$  % its the effective turns ratio of the motor which couples between  $\vec{E}_s$  &  $\vec{E}_r$ .

Note % we can easily find it in the core of wound Rotor <sup>(a<sub>eff</sub>)</sup>

$\vec{E}_s$  % Internal stator voltage

$\vec{E}_r$  % rotor induced voltage

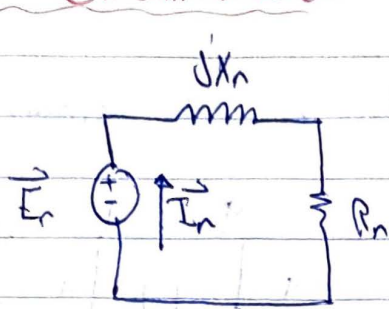
$I_r$  % rotor current

$I_s$  % stator or source phase current

$V_s$  % stator or source phase voltage

Frequency of rotor is same as stator frequency - eq circuit is same ⊗

## Rotor Circuit Model



$$R_{on} \vec{E}_r = 0$$

The Rotor is locked

$$\Rightarrow \vec{E}_r = \vec{E}_{r0}$$

↳ maximum Rotor Voltage

when the Rotor turns at  $\omega_s \Rightarrow \alpha = 0 \Rightarrow \vec{E}_r = 0$

Any other speed,  $\vec{E}_r$  is directly proportional to the slip

$$\boxed{\vec{E}_r = \alpha \vec{E}_{r0}}$$

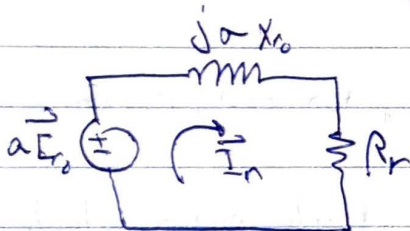
$$R_{on} \vec{X}_r$$

$$X_r = \omega L_r = 2\pi f_r L_r = 2\pi (\alpha f_e) L_r = \alpha X_{r0}$$

where  $X_{r0} = 2\pi f_e L_r$

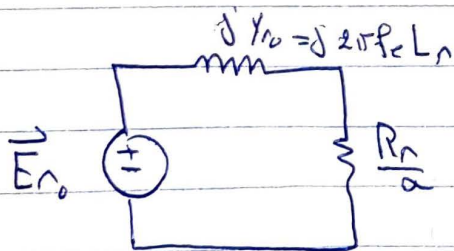
↓  
Maximum leakage rotor reactance

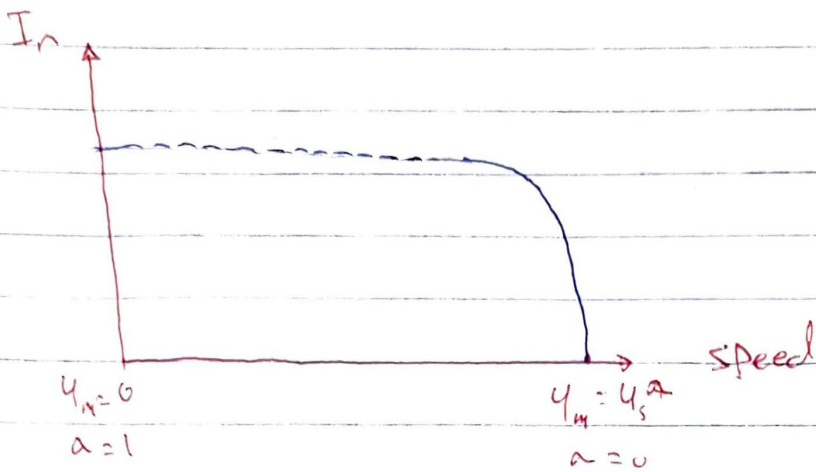
So



By applying KVL in the Rotor circuit.

$$\vec{I}_r = \frac{\alpha \vec{E}_{r0}}{R_r + (jX_{r0})\alpha} \Rightarrow \vec{I}_r = \frac{\vec{E}_{r0}}{\frac{R_r}{\alpha} + jX_{r0}}$$





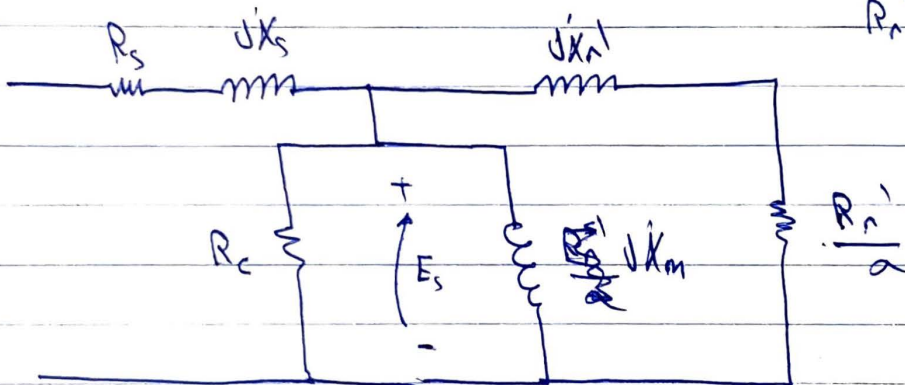
when  $a$  is small 
$$I_r = \frac{E_r}{\frac{R_r}{a} + X_{r0}} \approx \frac{E_r}{\frac{R_r}{a}} \approx \frac{a E_r}{R_r}$$

Note At starting the Rotor current is usually high compared with the motor nominal current.

Final equivalent circuit  $\omega$

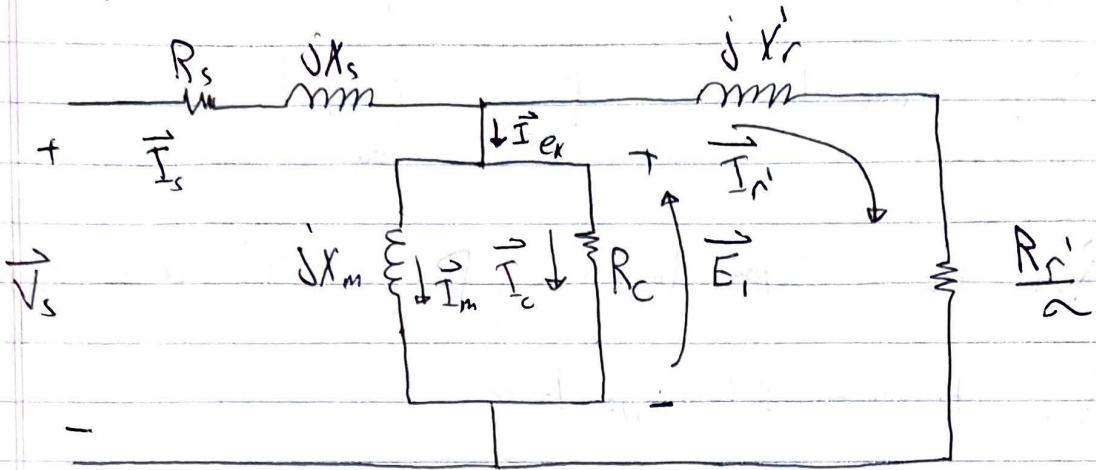
$$X_{r1}' = \frac{X_{r0}}{a} = a^2 X_{r0}$$

$$R_{r1}' = a^2 R_{r0}$$





# Equivalent Circuit of Induction Motor.

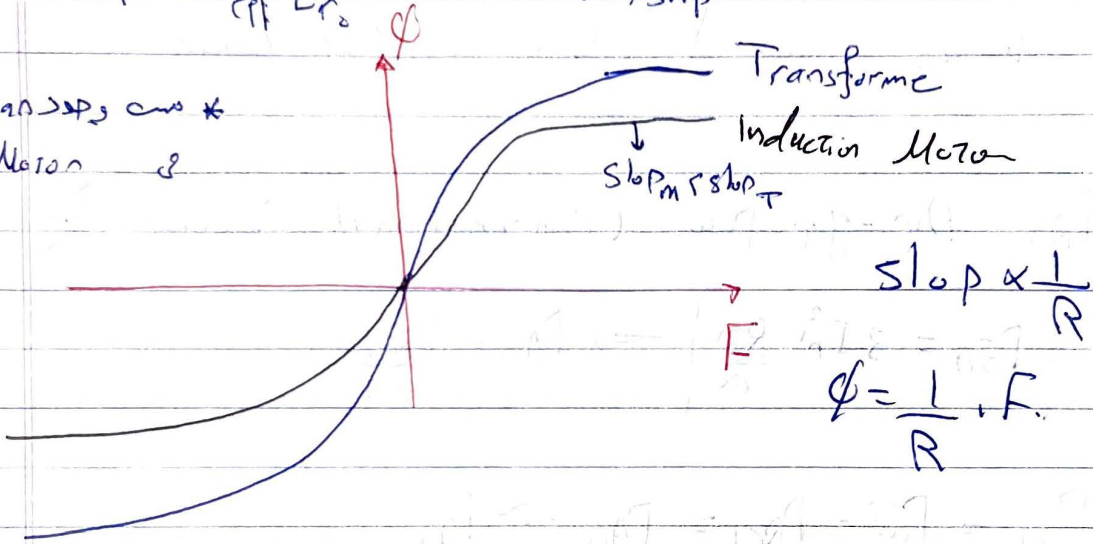


$$R_r' = a_{eff}^2 R_r \quad X_r' = a_{eff}^2 X_r \quad \vec{I}_r' = \frac{1}{a_{eff}} \vec{I}_r$$

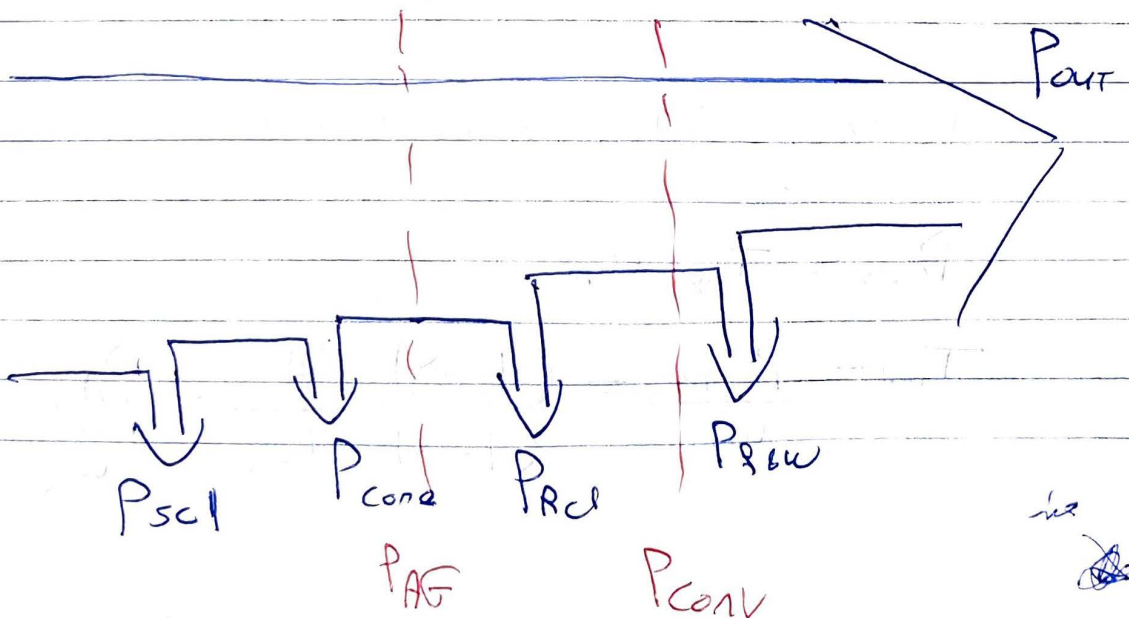
$$\vec{E}_1 = a_{eff} \vec{E}_r$$

$\omega$ , slip

Anggapan \*  
Motor &



## Power calculations





$P_{sc1}$ : stator copper losses  $P_{sc1} = 3I_c^2 R_s$

$P_{core}$ : Core losses  $P_{core} = \frac{3E_1^2}{R_c}$

$P_{rc1}$ : Rotor copper losses  $P_{rc1} = 3I_r'^2 R_r' = 3I_r'^2 R_r$

$P_{f&w}$  = Friction & windage losses

$P_{conv}$  = converted power to mechanical

$$P_{conv} = T_{ind} \omega_m$$

Induced Torque  $\leftarrow$   $\leftarrow$  Rotor (mechanical speed)

$P_{AG}$ : Air-gap power (consumed in the resistor  $\frac{R_r'}{s}$ )

$$P_{AG} = 3I_r'^2 \frac{R_r'}{s} \Rightarrow P_{AG} = \frac{P_{rc1}}{s}$$

$$P_{conv} = P_{AG} - P_{rc1} = P_{AG} - s P_{AG}$$

$$P_{conv} = (1-s) P_{AG}$$

$$P_{out} = T_{load} \omega_m$$

$$P_{out} = P_{conv} - P_{f&w}$$

Induced Torque equation

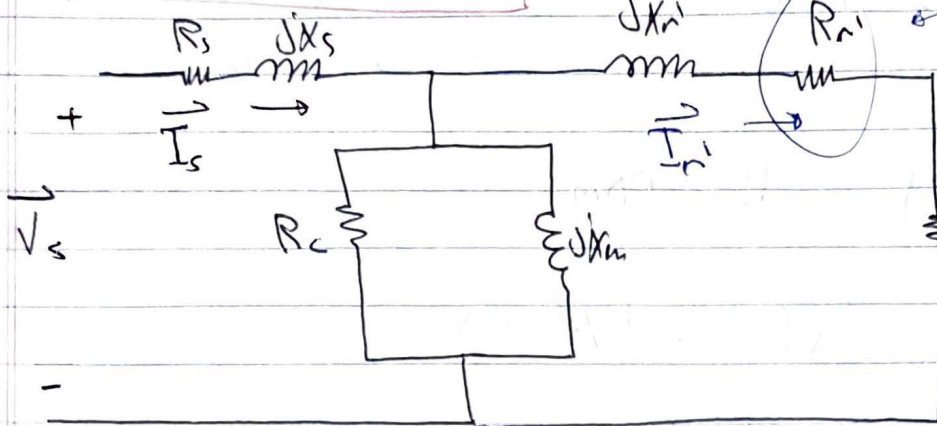
$$P_{conv} = T_{ind} \omega_m$$

$$T_{ind} = \frac{P_{conv}}{\omega_m} = \frac{(1-s) P_{AG}}{(1-s) \omega_s} = \frac{P_{AG}}{\omega_s}$$

$$T_{ind} = \frac{3 I_r'^2 R_r'}{\omega_s}$$

Leq AP  $\omega_s$  slip

$$\frac{R_r'}{a} = \frac{R_r'}{a} - R_r' \cdot \frac{R_r'}{a}$$



$$\left(\frac{1-a}{a}\right) R_r' = R_{conv}$$

Converted to Power

$$P_{conv} = (1-a) P_{AG} = (1-a) \frac{3 I_r'^2 R_r'}{a}$$

Motor efficiency

$$= 3 I_r'^2 R_{conv}, \quad R_{conv} = \frac{1-a}{a} R_r'$$

$$\eta = \frac{P_{out}}{P_{in}}$$

$$P_{in} = 3 V_s I_s \text{ PF} = \sqrt{3} V_L I_L \text{ PF}$$

Rotor efficiency

$$\eta_r = \frac{P_{conv}}{P_{AG}} = \frac{(1-a) P_{AG}}{P_{AG}} = 1-a$$

Example

A 460V, 25 hp, 60 Hz, 4 poles, Y-connected induction motor has the following impedances in ohms, per phase referred to the stator circuit:

$$R_s = 0.641 \Omega, \quad R_r' = 0.332 \Omega$$

$$X_s = 1.106 \Omega, \quad X_r' = 0.464 \Omega, \quad X_m = 26.3 \Omega$$

The Total Rotational losses are 1.1 kW and assumed to be constant, for a rotor slip of 2.2% at the rated voltage & rated frequency, find the motor's

a) speed b) current c) PF d)  $P_{conv}$  &  $P_{AO}$

e)  $T_{ind}$  &  $T_{load}$   $\eta(\%)$



a) speed,  $\omega_m$

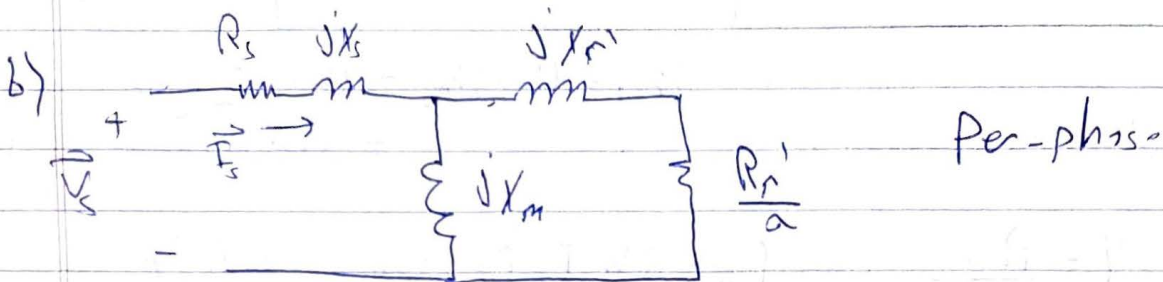
$$a = \frac{\omega_s - \omega_m}{\omega_s} = 1 - \frac{\omega_m}{\omega_s}$$

$$\omega_m = (1 - a)\omega_s$$

$$\omega_m = (1 - a)\omega_e$$

$$\omega_s = \frac{120}{p} f_e = 1800 \text{ rpm}$$

$$\omega_m = (1 - 0.022) \times 1800 = 1760 \text{ rpm}$$



$$\vec{I}_s = \frac{\vec{V}_s}{Z_{eq}}, \quad Z_{eq} = 14.07 \angle 33.6^\circ \Omega$$

$$\vec{I}_s = \frac{(460/\sqrt{3}) \angle 0^\circ}{14.07 \angle 33.6^\circ} \Rightarrow \vec{I}_s = 18.28 \angle -33.6^\circ \text{ A}$$

c)  $PF = \cos(\theta_{V_s} - \theta_{I_s}) = \cos(0 - (-33.6))$

$$= \cos(33.6) = 0.833 \text{ lagging}$$

d) we can use current divide to find  $I_r$  but there is easiest way.

$$P_{in} = 3 V_s I_s PF = 3 \left( \frac{460}{\sqrt{3}} \right) (18.28) (0.833) = 12.53 \text{ kW}$$

$$P_{sc1} = 3 I_s^2 R_s = 3 (18.28)^2 (0.641)$$

$$P_{sc1} = 0.685 \text{ kW}$$



$$P_{AG} = P_{in} - P_{core} - P_{sc1} = 12.53 - 0.681 \Rightarrow P_{AG} = 11.845 \text{ kW}$$

$$P_{conv} = (1 - a) \cdot P_{AG} = 11.585 \text{ kW}$$

e)

$$P_{conv} = T_{ind} \omega_m$$

$$T_{ind} = \frac{P_{conv}}{\omega_m} = \frac{11.585}{1760 \frac{\pi}{30}} = \frac{56.9}{62.8} \text{ N.m}$$

$$P_{out} = T_{Load} \omega_m$$

$$P_{out} = P_{conv} - P_{p2k} = 11.585 - 1.1 = 10.485 \text{ kW}$$

$$T_{Load} = \frac{10.485}{1760 \left(\frac{\pi}{30}\right)} = 56.9 \text{ N.m}$$

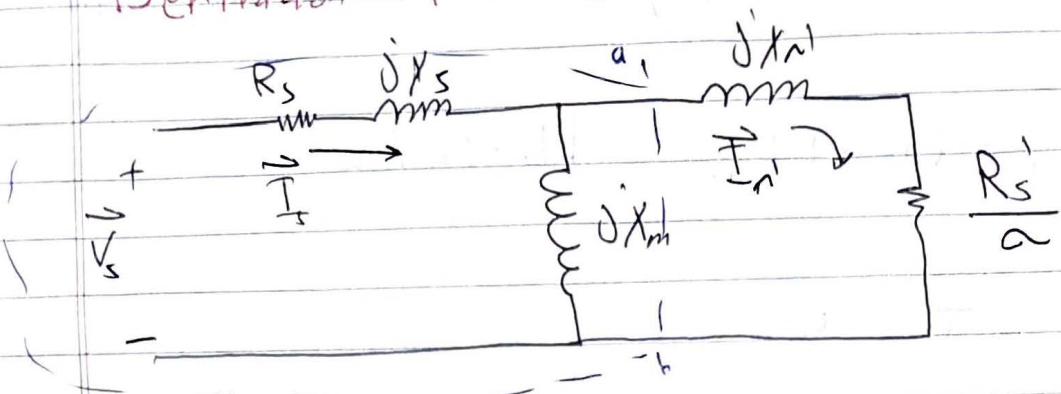
f)

$$\eta = \frac{P_{out}}{P_{in}} = \frac{10.485}{12.53} = 83.7\%$$

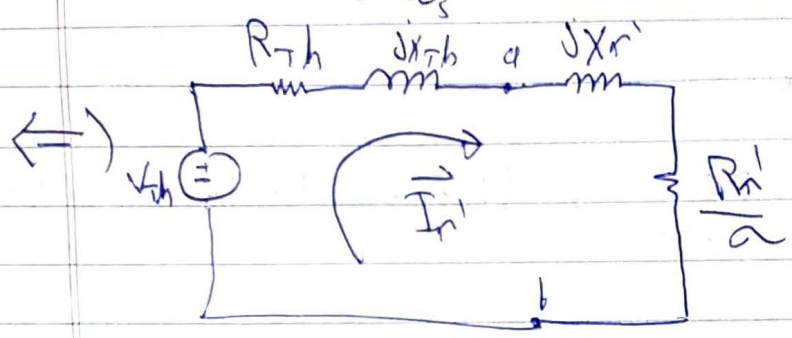
$$\eta_r = 1 - a = 1 - 0.022$$

\*) لدریافت توان القایی و Torque در موتور القایی پارامترهای زیر را در نظر بگیرید

### Derivation of Induced Torque equation



$$T_{ind} = \frac{3 I_r'^2 R_r'}{a \omega_s} = \frac{P_{AG}}{\omega_s}$$



$$\vec{V}_{th} = \vec{V}_{oc} = \frac{jX_m}{R_s + j(X_s + X_m)} \cdot \vec{V}_s$$

$$X_m + X_s \gg R_s \Rightarrow \vec{V}_{th} \approx \frac{X_m}{X_m + X_s} \cdot \vec{V}_s$$

$$Z_{th} = (R_s + jX_s) \parallel jX_m$$

$$Z_{th} = \frac{(R_s + jX_s)(jX_m)}{R_s + j(X_s + X_m)}$$

$$X_s + X_m \gg R_s \Rightarrow Z_{th} \approx \frac{(R_s + jX_s)(jX_m)}{j(X_s + X_m)}$$

$$Z_{Th} = R_s \left( \frac{X_m}{X_m + X_s} \right) + j X_s \left( \frac{X_m}{X_s + X_m} \right) = R_{Th} + j X_{Th}$$

$$R_{Th} = R_s \left( \frac{X_m}{X_m + X_s} \right) \quad , \quad X_{Th} = X_s \left( \frac{X_m}{X_m + X_s} \right) \approx X_s$$

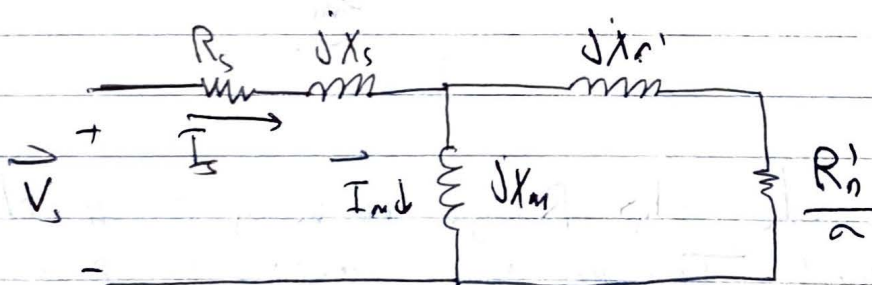
$$\vec{I}_r = \frac{\vec{V}_{Th}}{(R_{Th} + \frac{R_r'}{a}) + j(X_{Th} + X_r')}$$

$$I_r' = \frac{V_{Th}}{\sqrt{(R_{Th} + \frac{R_r'}{a})^2 + (X_{Th} + X_r')^2}}$$

done

$$T_{ind} = \frac{(3) V_{Th}^2}{\omega_s \left[ \left( R_{Th} + \frac{R_r'}{a} \right)^2 + \left( X_{Th} + X_r' \right)^2 \right]} \cdot \frac{R_r'}{a}$$

Induced Torque equation



Per-Phase equivalent circuit

$$T_{ind} = \frac{PAG}{\omega_s} \quad ; \quad PAG = 3 I_r'^2 \frac{R_r'}{a}$$

$$T_{ind} = \frac{3 I_r'^2 R_r'}{a \omega_s}$$



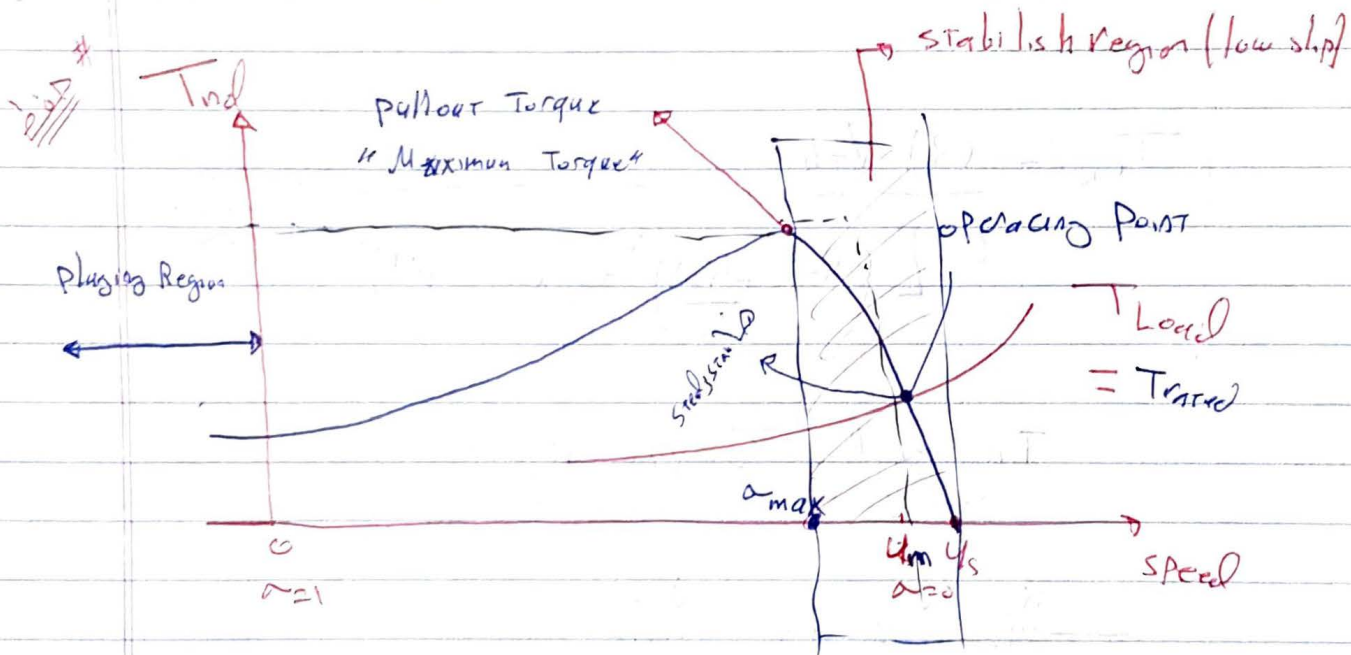
$$\vec{V}_{Th} = \frac{jX_m}{R_s + j(X_m + X_s)} \cdot \vec{V}_s$$

$$V_{Th} = X_m$$

$$T_{ind} = \frac{3 V_{Th}^2}{\omega_s \left[ R_{Th} + \frac{R_r'}{a} \right]^2 + (X_{mTh} + X_r')^2} \cdot \frac{R_r'}{a}$$

$$T_{ind} = f(\alpha) = g(\gamma_m)$$

$$\gamma_m = (1 - \alpha) K$$



Note: when the slip Range is very small, the Induced Torque is approximately proportional to the slip (linear relationship)

$$T_{ind} \approx \frac{3 V_{Th}^2}{\omega_s \left[ \left( \frac{R_r'}{a} \right)^2 \right]} \cdot \frac{R_r'}{a} = \frac{3 V_{Th}^2 \cdot a \cdot K a}{\omega_s R_r'}$$

لأنه في المنطقة الصغيرة من الانزلاق

$$T_{ind} - T_{load} = J \frac{d\omega}{dt}$$

under steady state (speed = constant)

$$\Rightarrow T_{ind} = T_{load}$$

## Plugging Region

its used to stop the motor rapidly by switching any two of 3 phases.

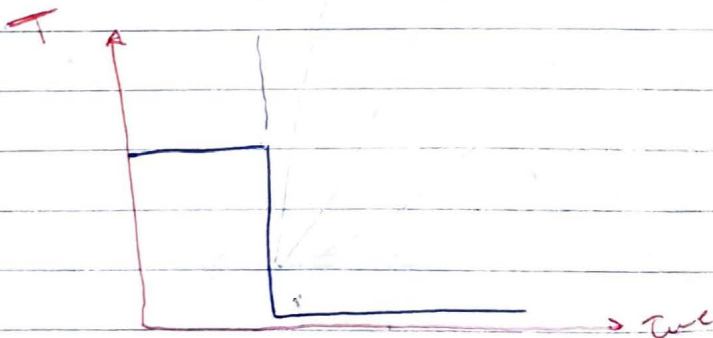
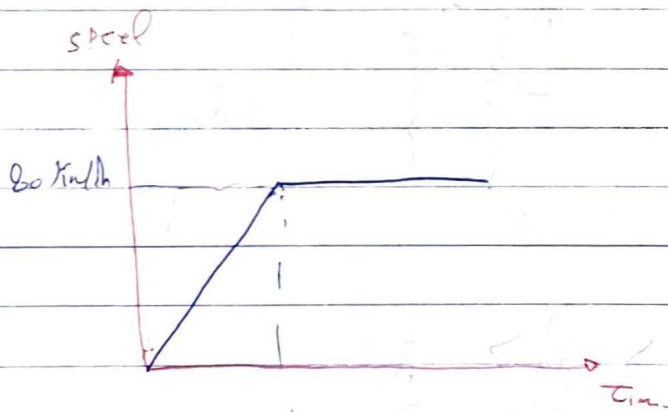
المسكدة عند التخليج ذكره في كتابه

$T_{start}$  = Starting Torque

$T_{start}$  is slightly higher than the motor rated Torque

$T_{max}$  = pullout or maximum Torque.

$$T_{max} = (2-3) T_{rated}$$





$$\frac{dT_{ind}}{da} = 0$$

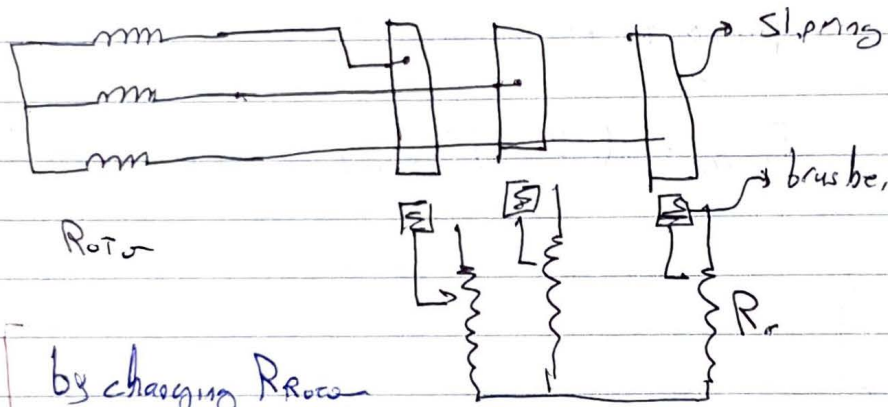
$$a_{max} = \frac{R_r'}{\sqrt{R_{Th}^2 + (X_{Th} + X_{r1})^2}} \quad \text{--- (1)}$$

عق

$$T_{max} = \frac{3 V_{Th}^2}{2 \omega_s \left[ R_{Th} + \sqrt{R_{Th}^2 + (X_{Th} + X_{r1})^2} \right]}$$

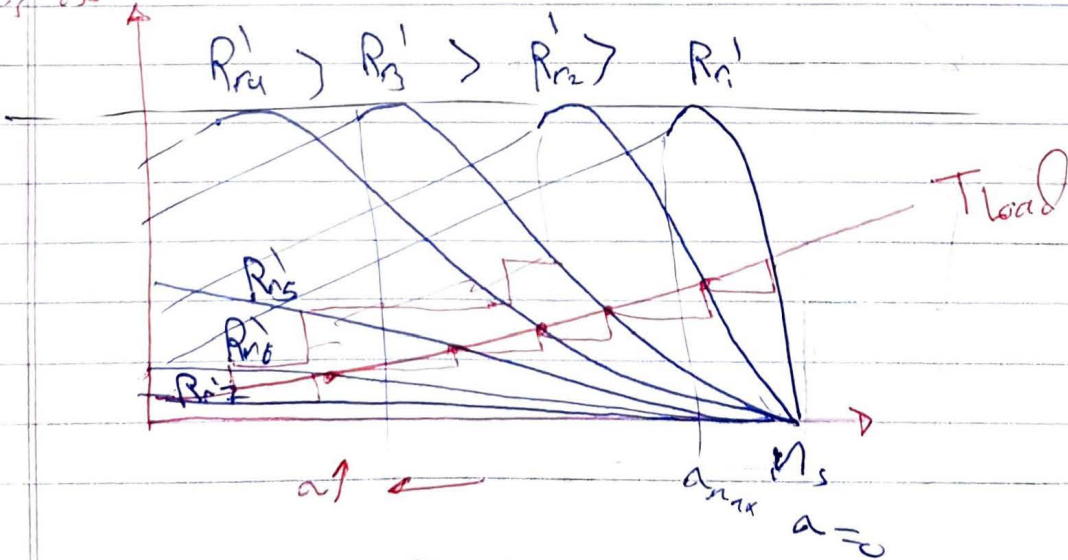


Wound Rotor Induction Motor ... مع هذا النوع دة ان لا يفتح ان اعبر  $R_r$  فيه



amplitude to be  
with a small up  
rotor winding and  
=  $V_r$  cos

by changing  $R_{Rocor}$



$\rightarrow X_m \uparrow$

$Y_{Rocor} = \text{load}$   $Y_{eff} \text{ عتة}$   $R_{r1}$   $\text{للس لول}$   $\text{عكسكبي}$



$$\textcircled{1} R_a' \leq R_a' \leq R_{a2}' \Rightarrow R_a' \uparrow \Rightarrow a_{max} \uparrow$$

$$a \uparrow \Rightarrow \text{speed} \downarrow \Rightarrow (\eta_m = 1 - a) \downarrow$$

$$\text{efficiency} \Rightarrow \eta \downarrow \Rightarrow T_{start} \uparrow$$

$$\textcircled{2} R_a' > R_{a2}' \Rightarrow T_{start} \downarrow \Rightarrow \eta \downarrow$$

Example A 460 V, 25 hp, 4 pole,  $Y_m$  connected, wound rotor IM has the following impedances

$$R_s = 0.641 \Omega, R_a' = 0.332 \Omega$$

$$X_m = 1.106 \Omega, X_a' = 0.464 \Omega, X_m = 26.1 \Omega$$

- What is  $T_{max}$ ? At what speed (8 slip) does it occur?
- What is  $T_{start}$ ?
- If  $R_a'$  is doubled, what is the speed at which  $T_{max}$  occurs? What is the new  $T_{start}$ ?

Solution

$$a) T_{max} = \frac{3 \sqrt{1.5}}{2 \omega_s [R_{Th} + \sqrt{R_{Th}^2 + (X_{Th} + X_m)^2}]}$$

$$R_{Th} = \left( \frac{Y_m}{X_m + X_s} \right) R_s \approx R_s, \quad X_{Th} \approx X_s$$

$$V_{Th} = \frac{X_m}{\sqrt{R_s^2 + (X_s + X_m)^2}} \cdot V_s$$

$$f = 60 \text{ Hz}$$

$$R_{Th} = 0.59 \Omega \quad X_{Th} = X_s = 1.806 \Omega \quad V_{Th} = \frac{480}{\sqrt{3}} = 277 \text{ V}$$

$$\omega_s = \left(\frac{2}{p}\right) \omega_e = 188.5 \text{ rad/s} \quad = 255.2 \text{ Volt}$$

$$T_{max} = 229 \text{ N.m}$$

$$a_{max} = \frac{R_r'}{\sqrt{R_{Th}^2 + (X_{Th} + X_r')^2}} = \frac{0.332}{\sqrt{\dots}} = 0.198$$

$$n_m = (1 - a_{max}) n_s = 1444 \text{ rpm}$$

b) max when  $a=1$

$$T_{start} = \frac{3 V_{Th}^2}{\omega_s [ \frac{R_r'}{a} + R_{Th} ]^2 + (X_{Th} + X_r')^2} \cdot \frac{R_r'}{a}$$

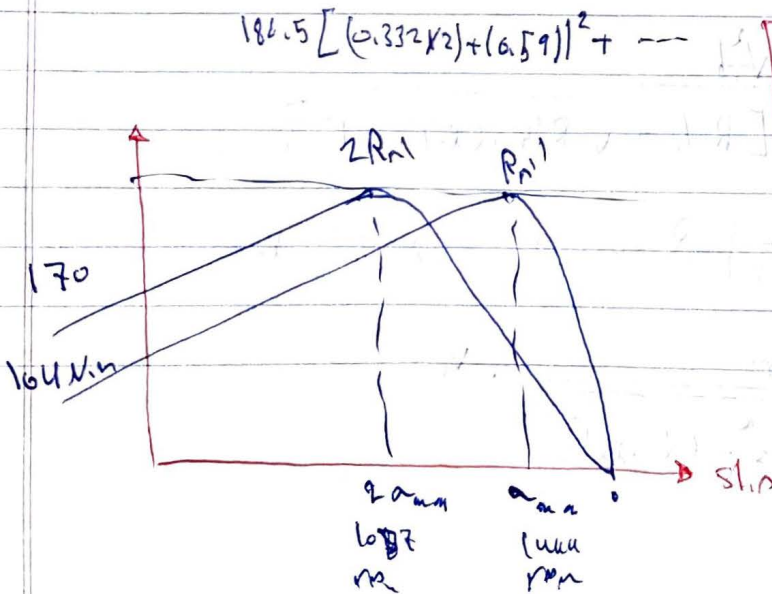
$$T_{start} = 164 \text{ N.m}$$

c)  $a_{max} = \frac{(2)(0.198)}{\dots} = 0.396$  since  $R_r' = 2R_r$

$$n_m = (1 - a_{max}) n_s = 1087 \text{ rpm}$$

only  $R_r' = 2R_r$

$$T_{start} = \frac{(3)(255.2)^2}{188.5 [ (0.332 \times 2) + (0.59) ]^2 + \dots} = 170 \text{ N.m}$$



Matlab

$$k = 0.000000000000000001$$

$$R_{Th} = 0.59$$

$$X_{Th} = 1.806$$

$$V_{Th} = 277$$

$$\omega_s = 188.5$$

$$p = 2$$

$$R_r = 0.166$$

$$R_r' = 2R_r$$

$$R_r' = 2R_r$$

$$g = \dots$$

plot(x,y)

plot(x,y)

hold on

## Calculation of starting current

$$I_{L\text{START}} = \frac{S_{\text{START}}}{\sqrt{3} V_L}$$

$$S_{\text{START}} = \text{Rated power} \times \text{code letter factor} \\ (\text{hp})$$

Nominal code letter	Locked Rotor [KVA/hp]
A	0 - 3.15
B	3.15 - 3.55
C	3.55 - 4.00
D	4.00 - 4.50
E	4.50 - 5
F	5 - 5.6
;	;

Ex What is the starting current of a 15 hp, 208V, code letter 3φ induction motor?

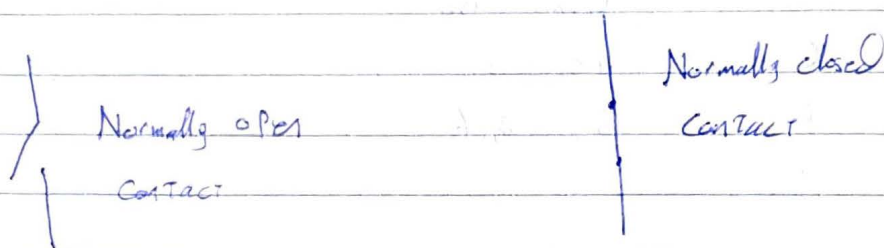
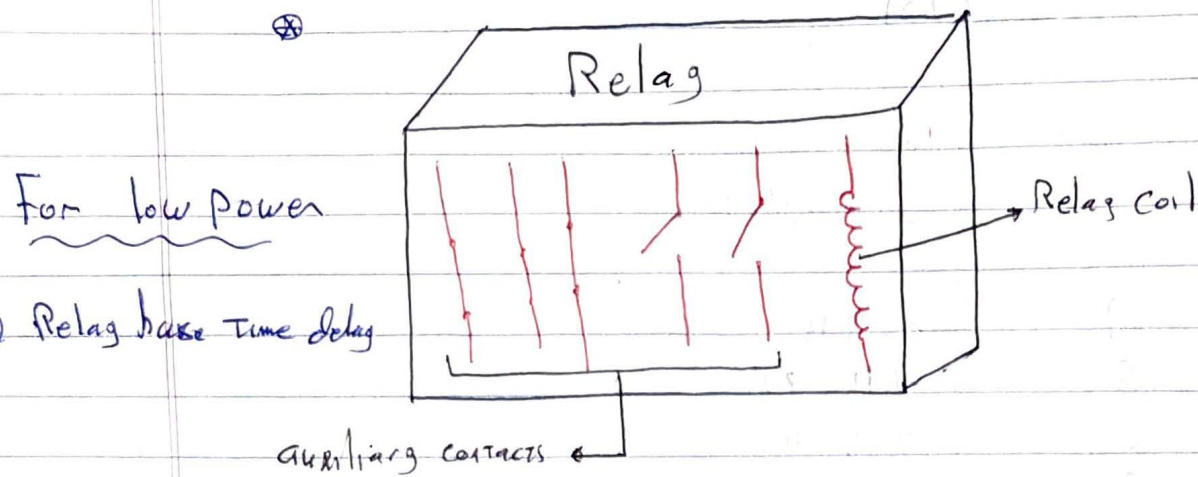
$$S_{\text{START}} = (15)(5.6) = 84 \text{ kVA}$$

$$I_{L\text{START}} = \frac{S_{\text{START}}}{\sqrt{3} V_L} = 233 \text{ A} \left[ \begin{array}{l} \text{Range of starting current:} \\ \text{The value will be} \\ \text{closed to it} \end{array} \right]$$

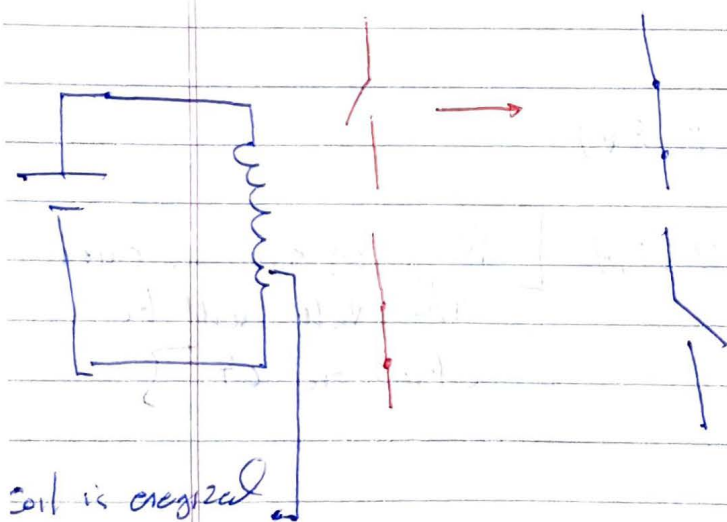


# Relay logic control of 3- $\phi$ induction motor (ON-OFF control)

Relay is an electro-magnet switch that has a coil and a set of auxiliary contacts. The contacts can be either normally open or normally closed.

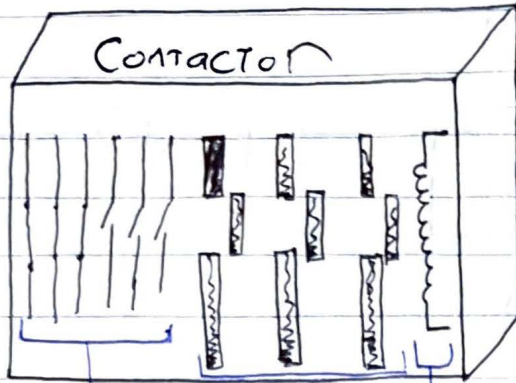


When the coil is energized, the normally open contact will close and the normally close contact will open.



CONTACTOR is an electro-magnet switch that has three main contacts with set of auxiliary contacts

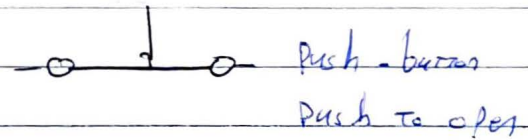
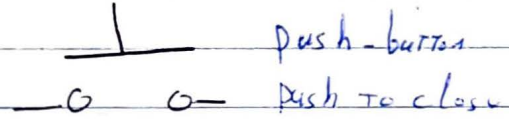
For 3 $\phi$  power  
3- $\phi$  IM



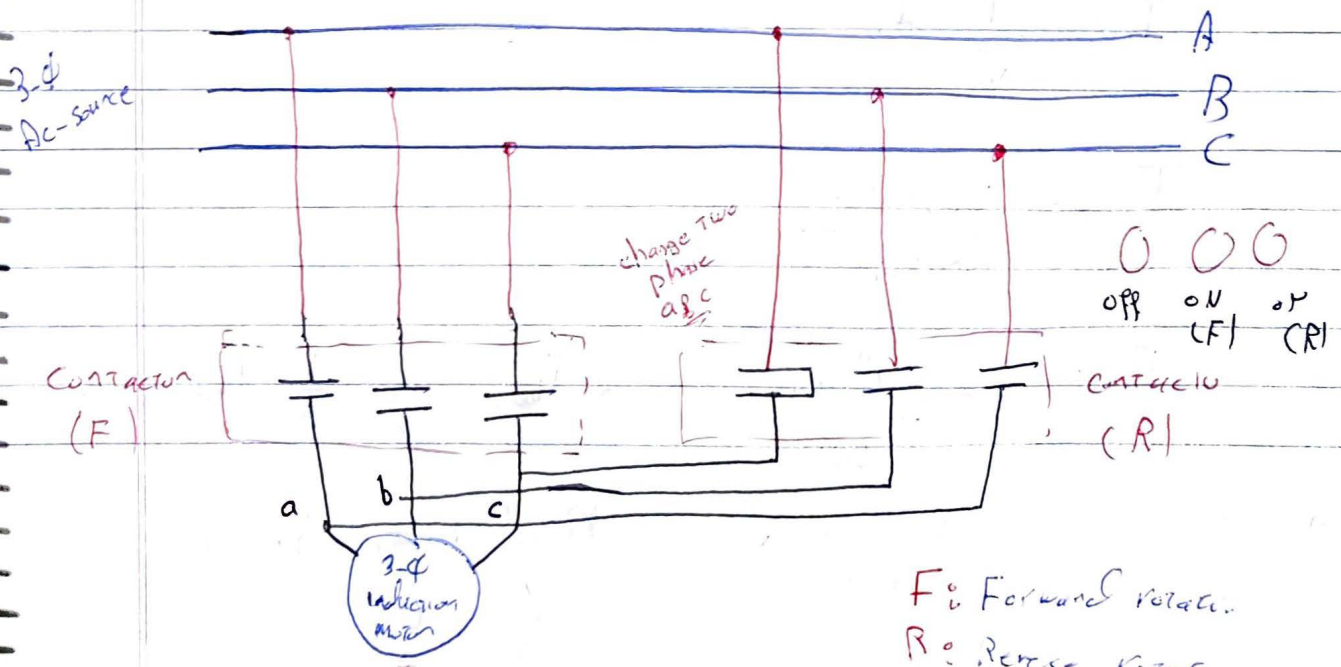
⇒ The auxiliary contact can be either normally open or normally closed

Auxiliary contacts      Main contacts      Coil

Symbols:



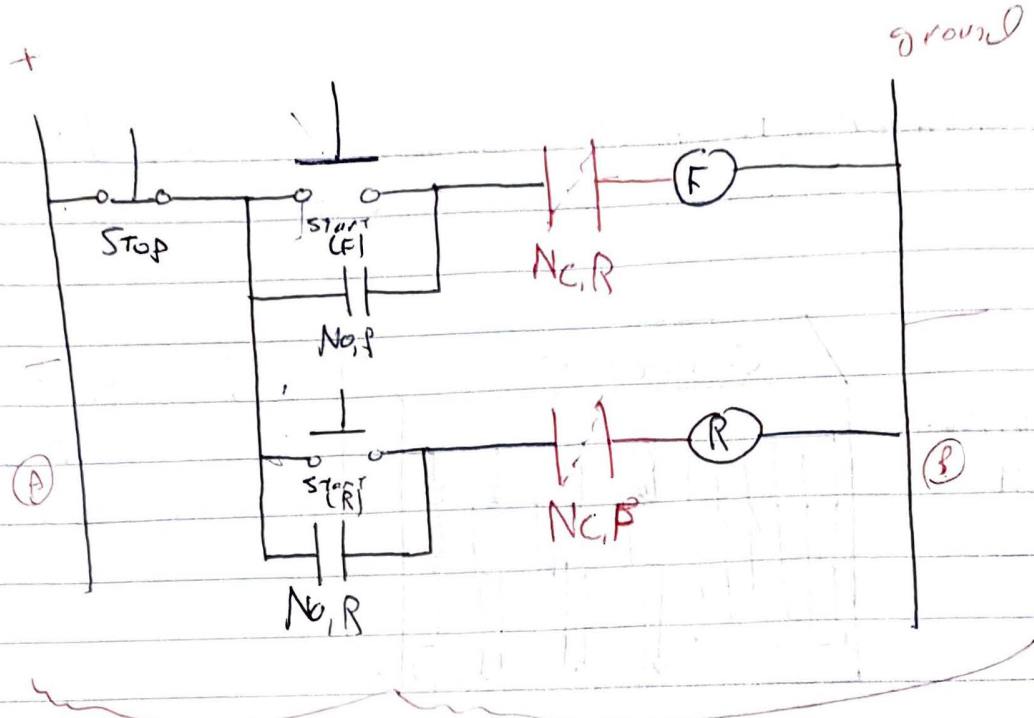
Example Control & power circuit to reverse the direction of motor





Ladder Diagram

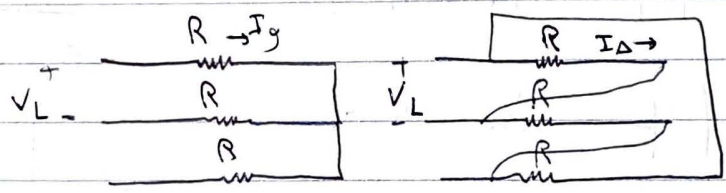
coil  
SI coil



### Control Circuit

\* Method to reduce the starting current of 3φ induction motor.

① Y-Δ starter



$$I_{\Delta} = \frac{V_L}{R} \quad \rightarrow \quad I_y = \frac{V_L/\sqrt{3}}{R} = \frac{1}{\sqrt{3}} \frac{V_L}{R}$$

$$T_y = \frac{1}{\sqrt{3}} I_{\Delta}$$

$$T_{ind} = \frac{3 I_{\Delta}^2 R_{a1}}{\omega \omega_r}$$

$$T_{ind, start} = \frac{3 I_{\Delta}^2 R_{a1}}{\omega \omega_r}$$

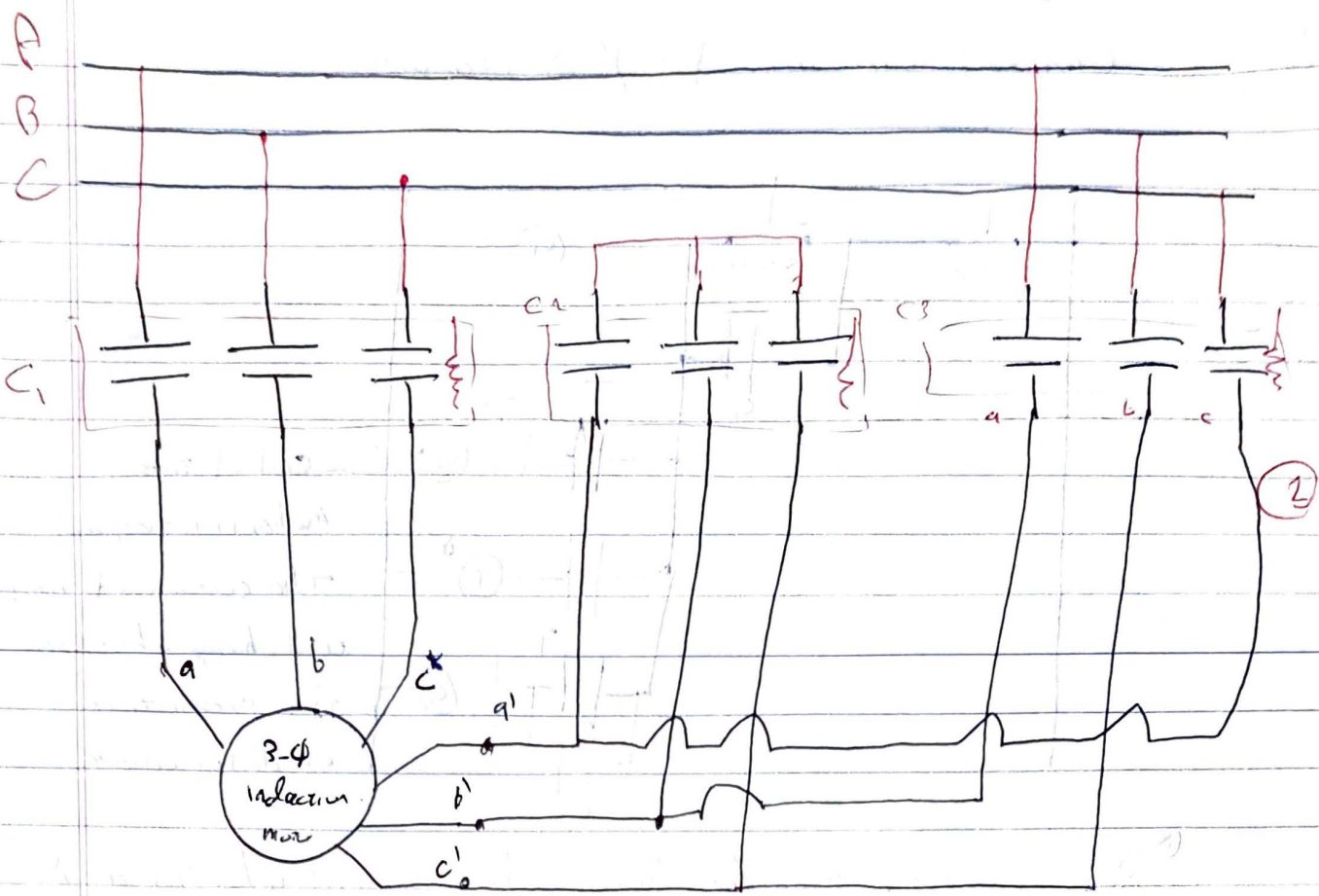
$$\rightarrow I_{ind, start, y} = \frac{1}{3} T_{ind, start, \Delta}$$

g d d s s starting current si haw h d \*

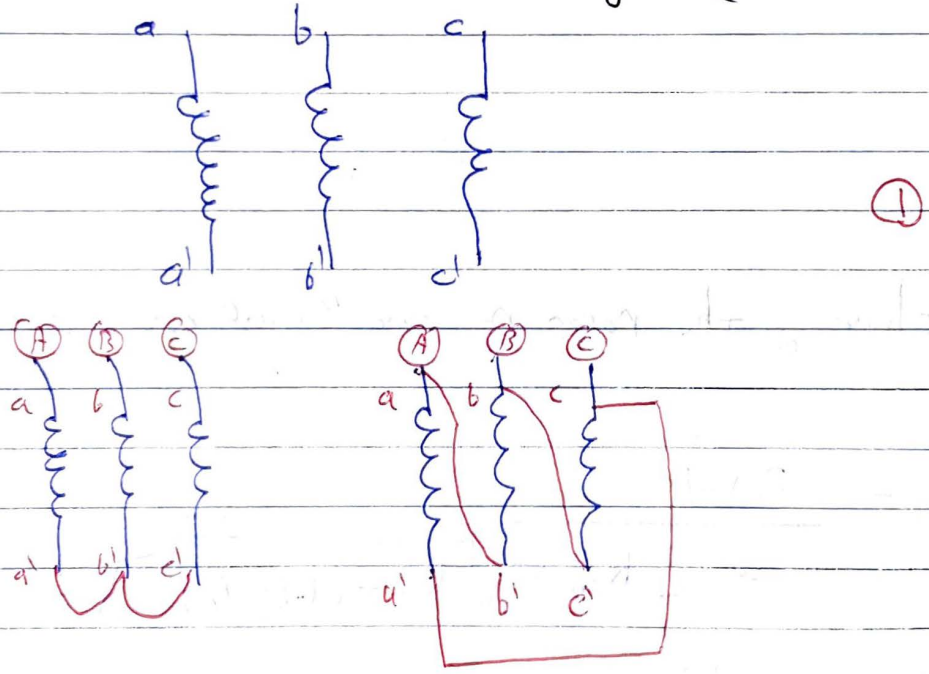
Rated voltage of motor

600/400  
Y



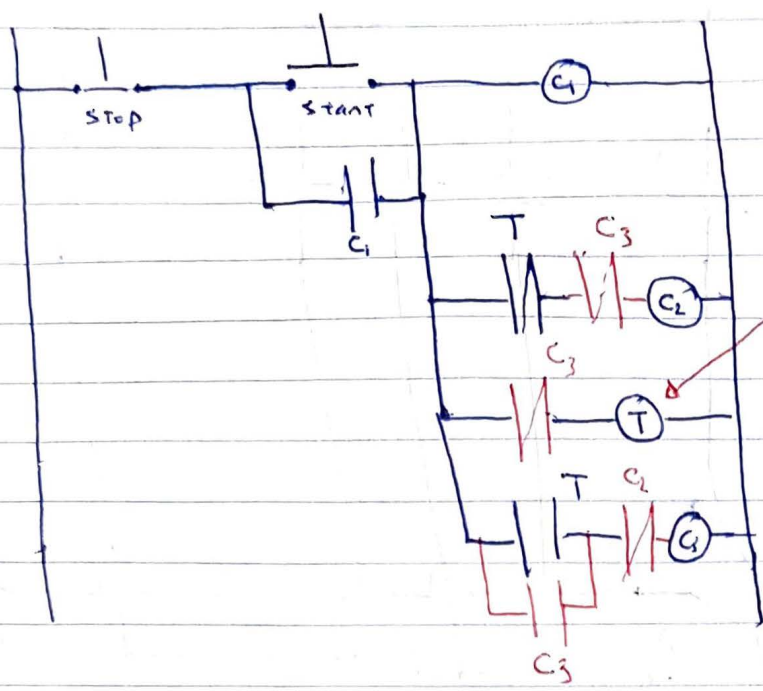


Stator windings (Must be before)



# Control circuit for $\Delta$ starter

3



Coil of timer  
 when it is energized  
 the contacts of timer  
 will change their state  
 after preset time  
 or delay time

\* Red Parameter using for Remove the timer coil when it is at  $\Delta$

\* Tag to add Reversed switch

② changing the rotor resistance "wound rotor induction machine"

$$T_{max} = \frac{3 V_{th}^2}{2 \omega_s [ R_{th} + \sqrt{R_{th}^2 + (X_{th} + X_r')^2} ]}$$

$$\cos \phi_{max} = \frac{R_r}{\sqrt{R_{th}^2 + (X_{th} + X_r')^2}}$$