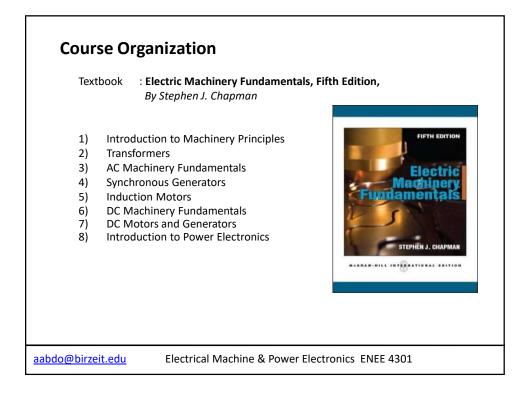
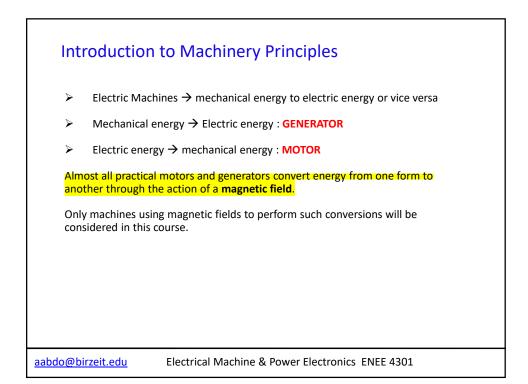
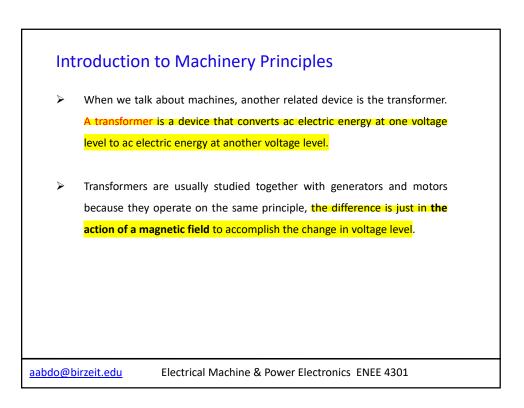


Course C	Organization	
Office Section Textbook :	 Dr. Ali Abdo Masri 119 M,W 11:00 – 12:20 T, R 11:00 – 12:20 Electric Machinery Fundament By Stephen J. Chapman 	Aqaad 421
aabdo@birzeit.edu		ower Electronics ENEE 4301

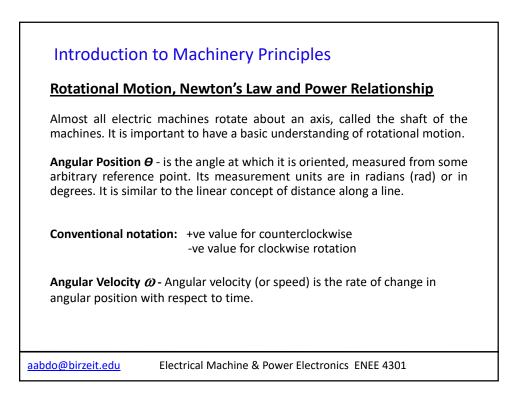


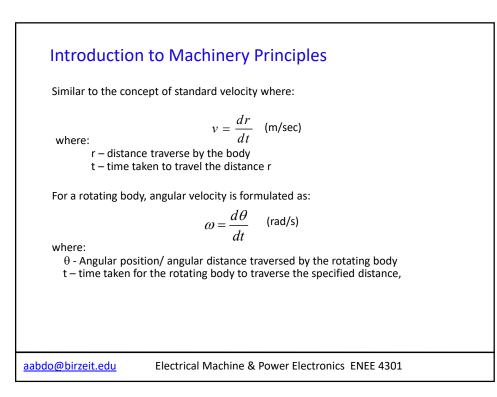
Course Organization		
Grading:		
Midterm Exam	35 %	
Final Exam	40 %	
Class Work	25 %	
	100 %	
do@birzeit.edu	Electrical Machine & Power Electronics ENEE 4301	

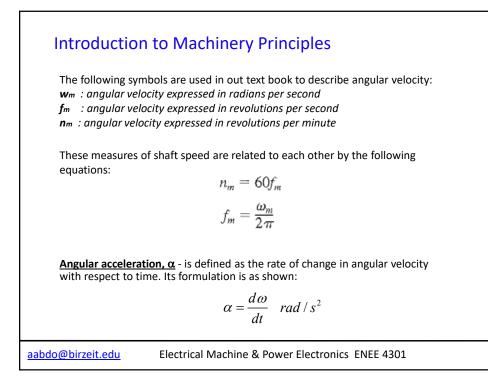


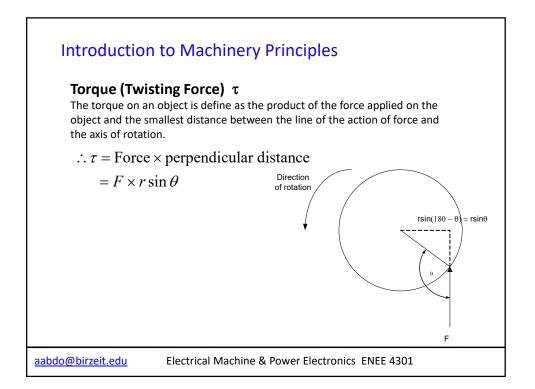


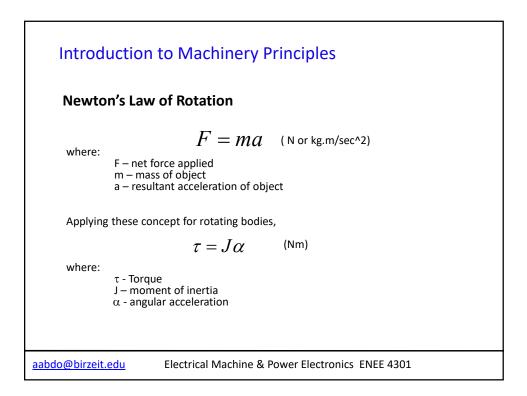
	_
Introduction to Machinery Principles	
Why are electric motors and generators so common?	
 Electric power is a clean and efficient energy source that is easy to transmit over long distances and easy to control. 	
An electric motor does not require constant ventilation and fuel the way that an internal-combustion engine does, so the motor is very well suited for use in environments where the pollutants associated with combustion are not desirable.	
aabdo@birzeit.edu Electrical Machine & Power Electronics ENEE 4301	

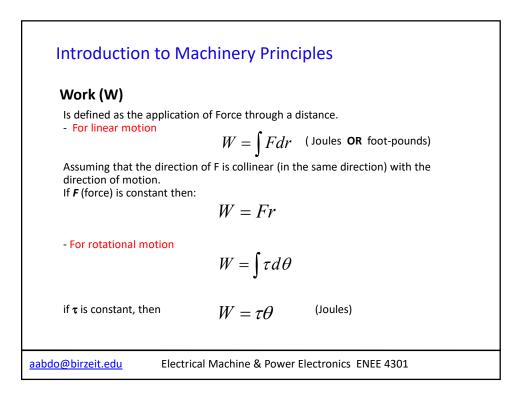


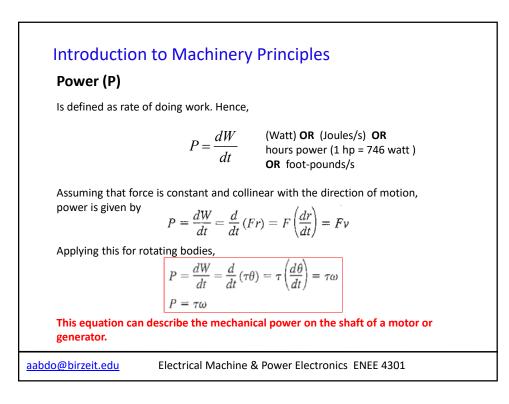


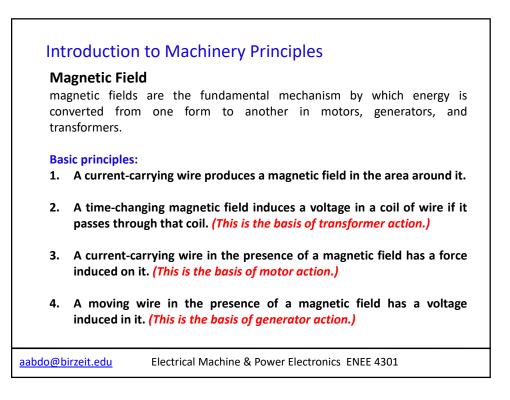


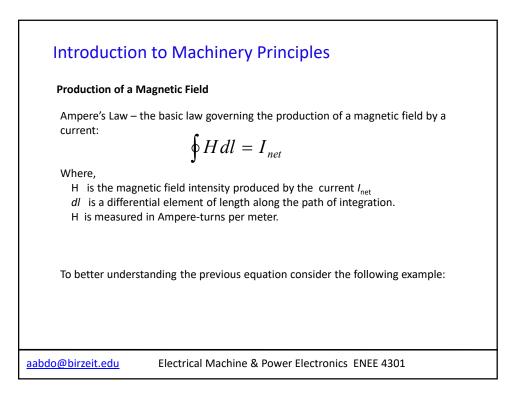


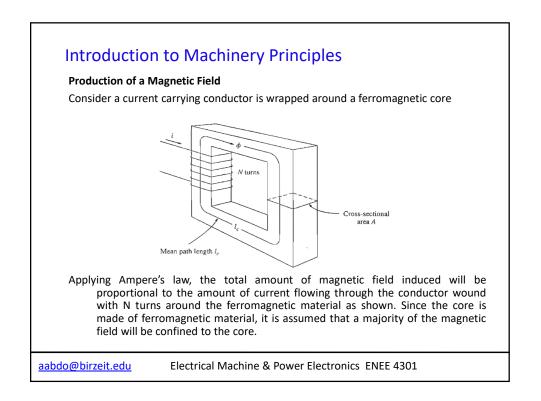


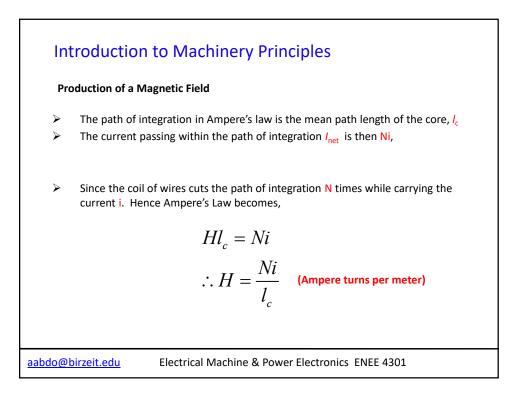


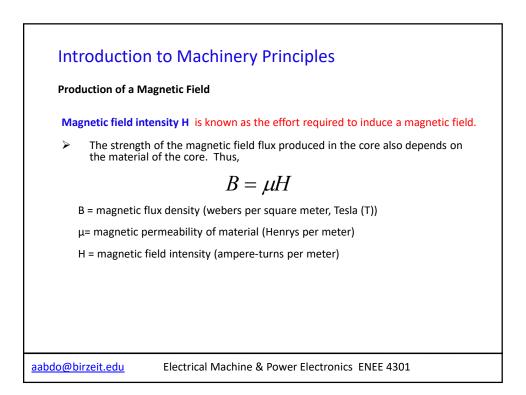


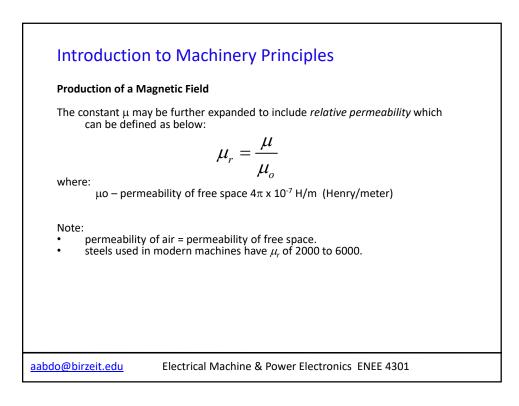


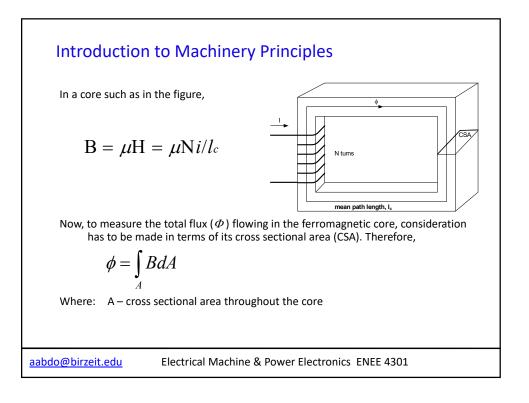


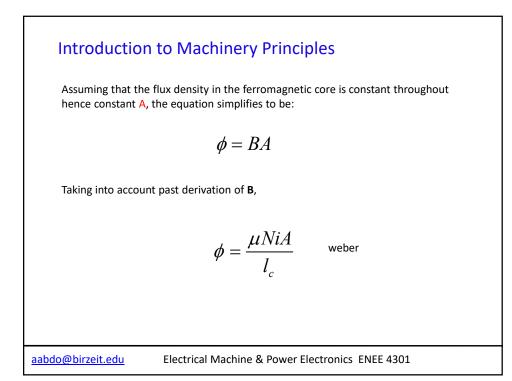




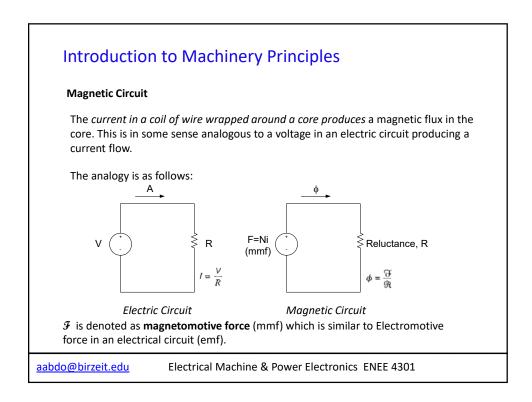


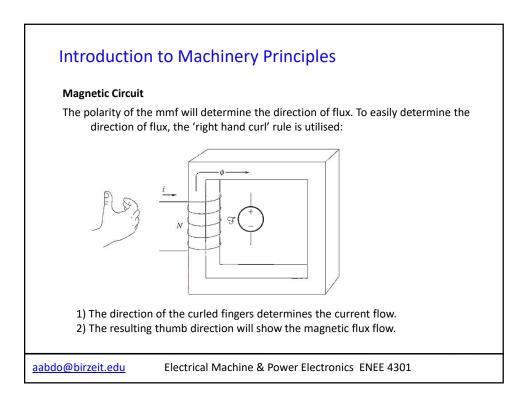


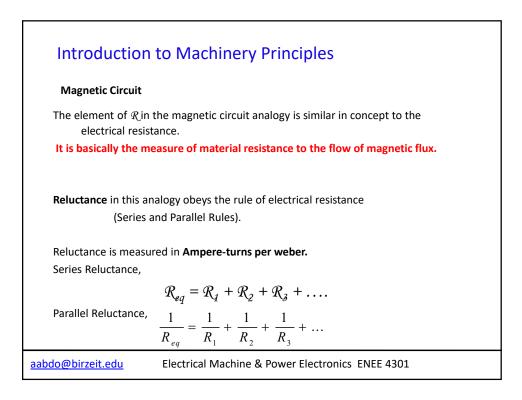


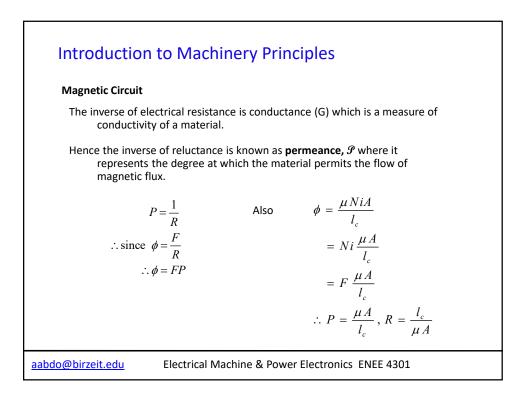


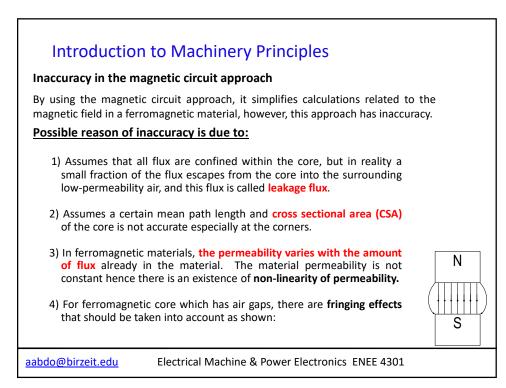
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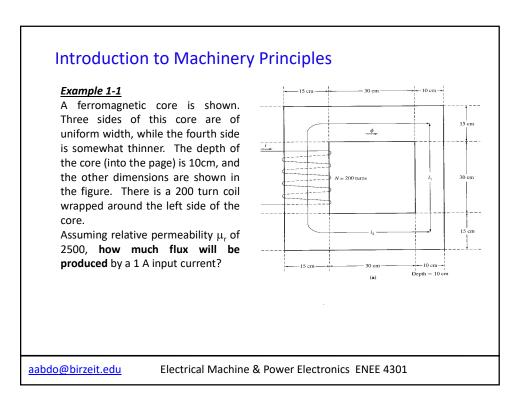


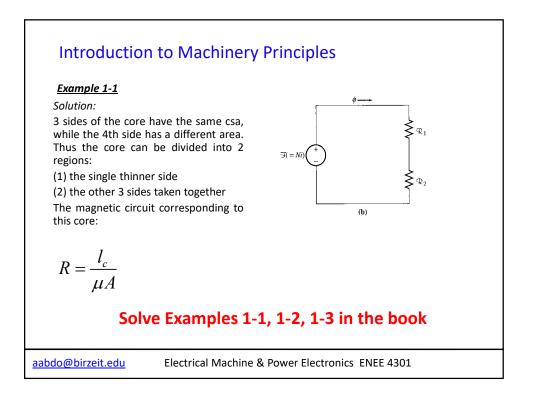


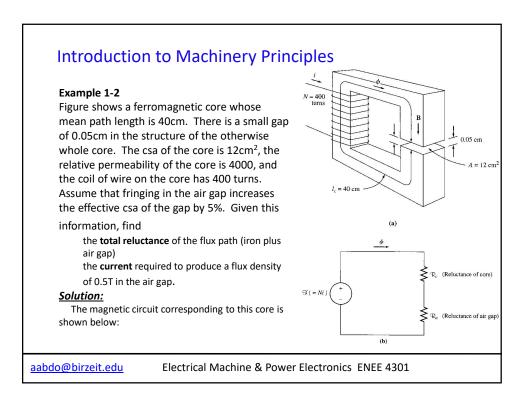


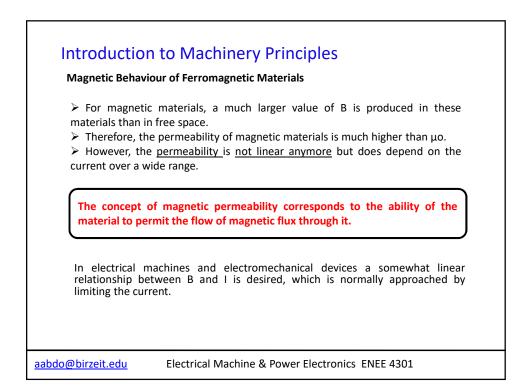


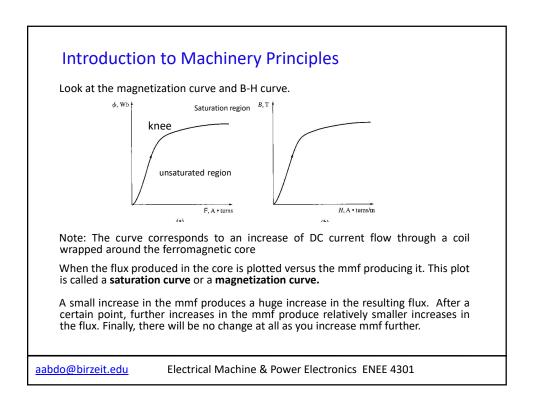


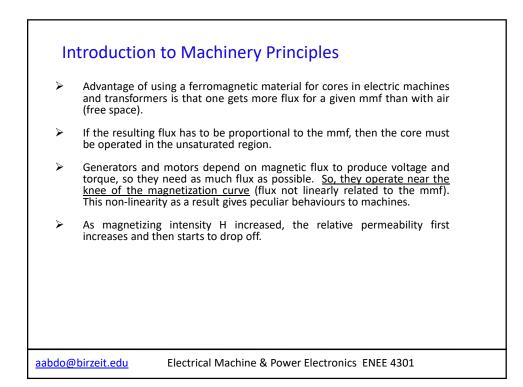


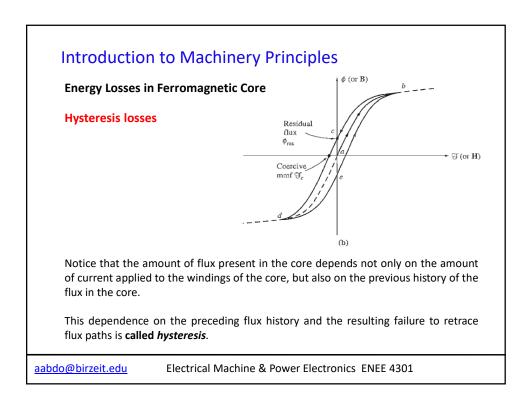


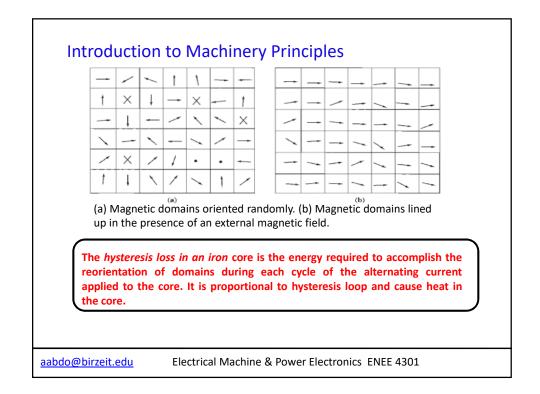


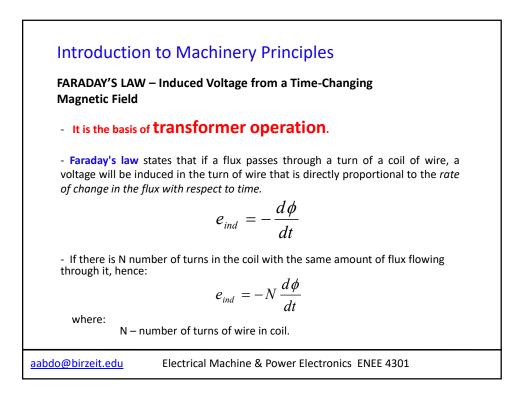


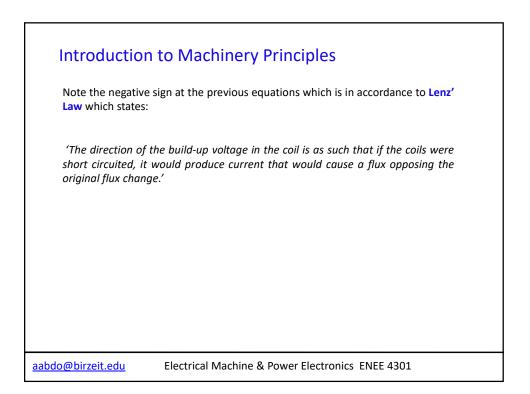


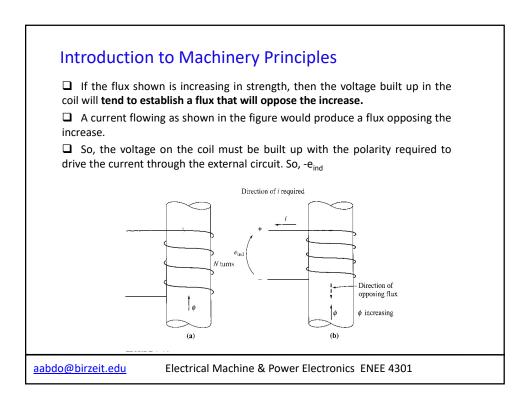


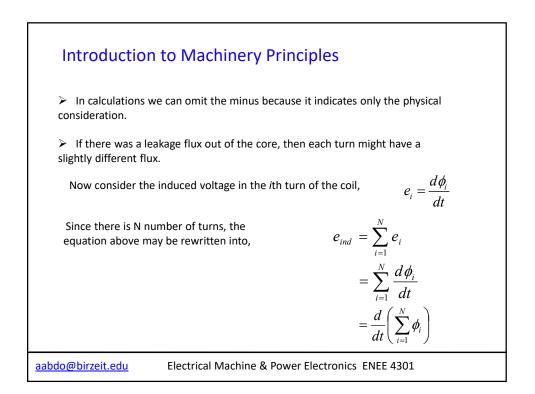


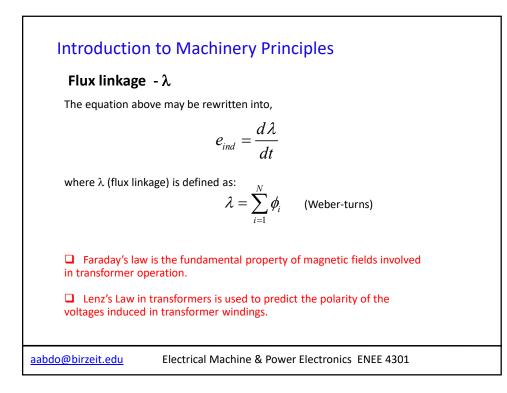


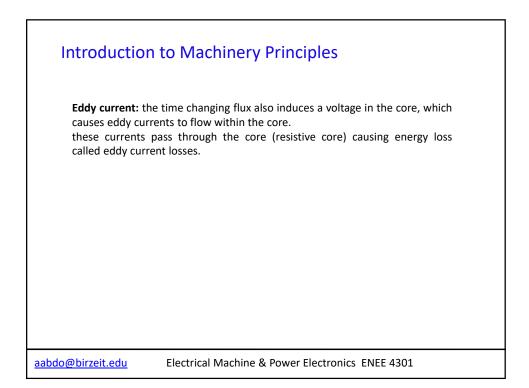


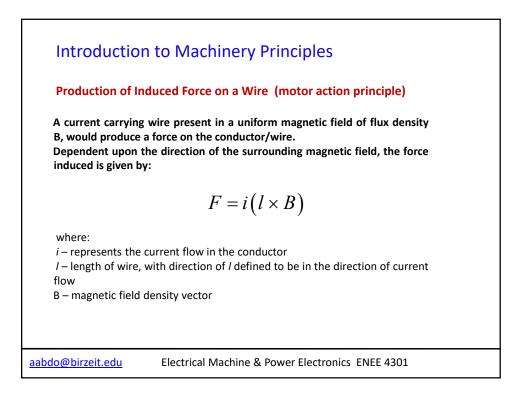


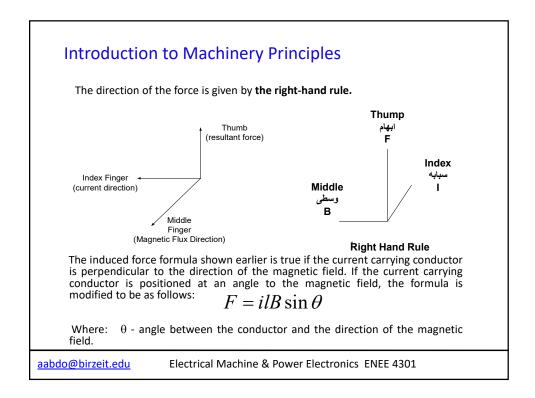


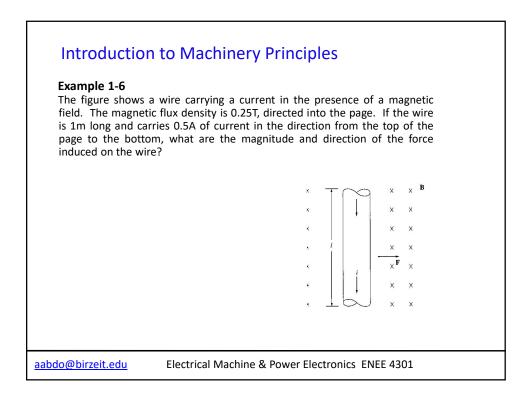


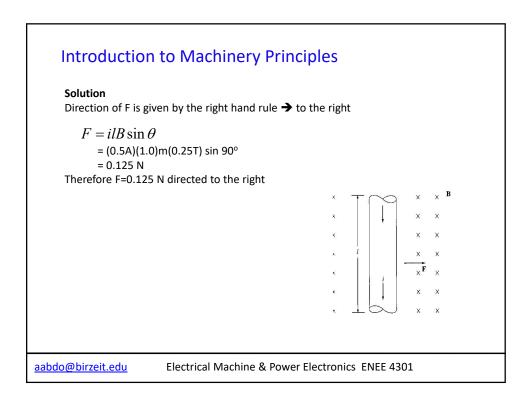


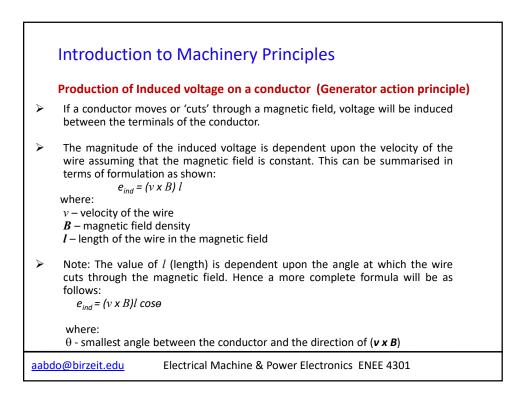


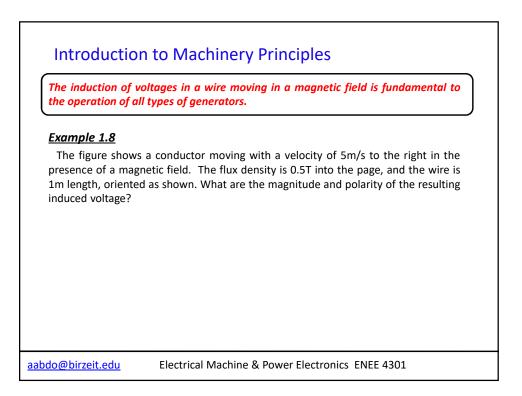


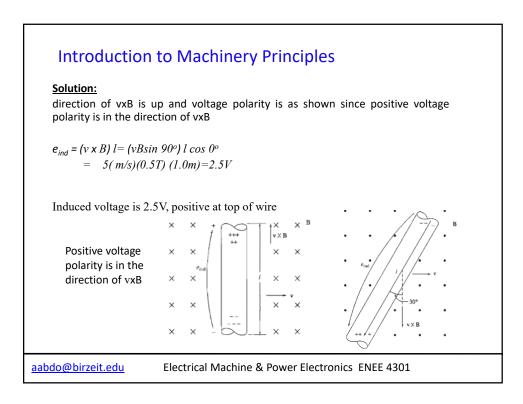


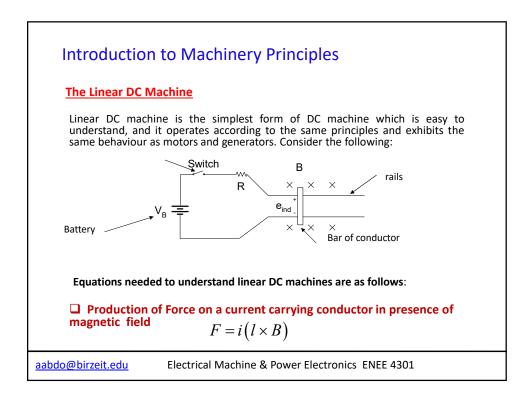


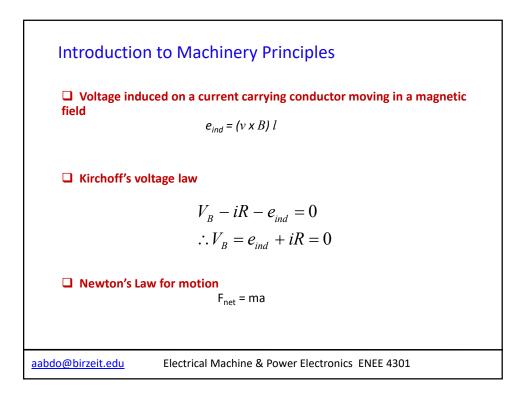


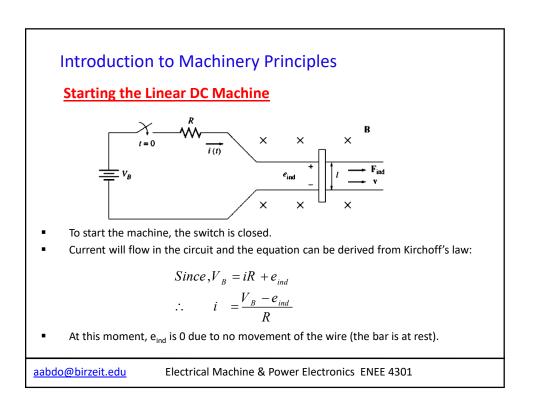


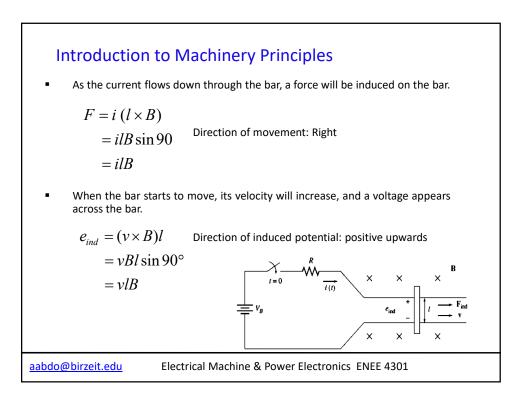


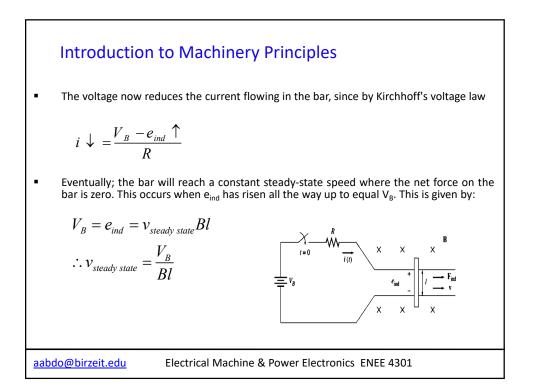


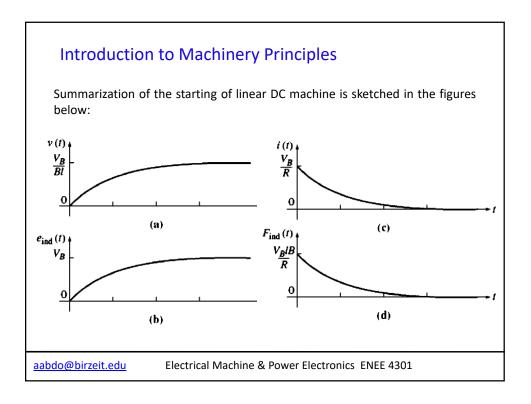


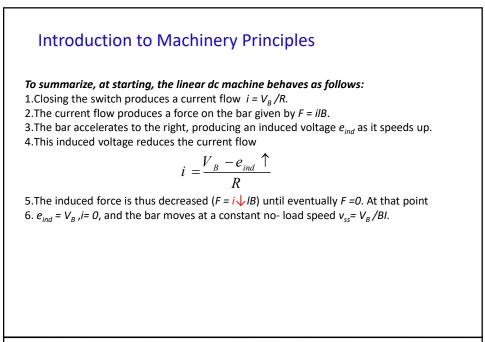








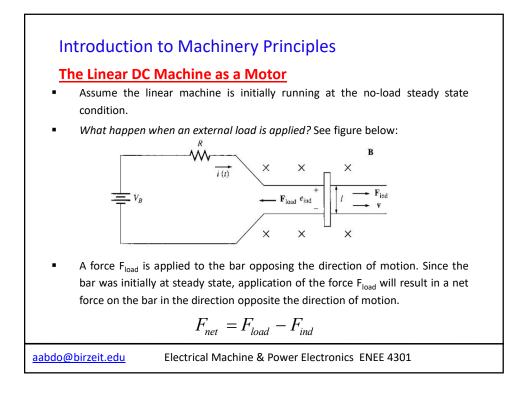


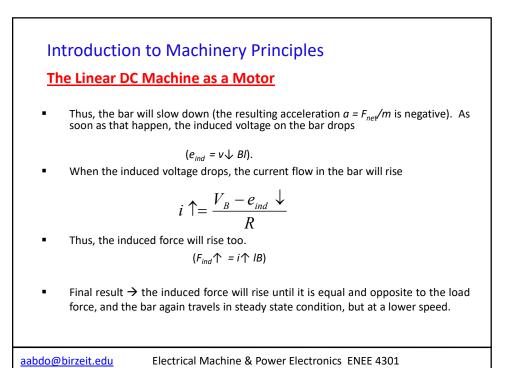


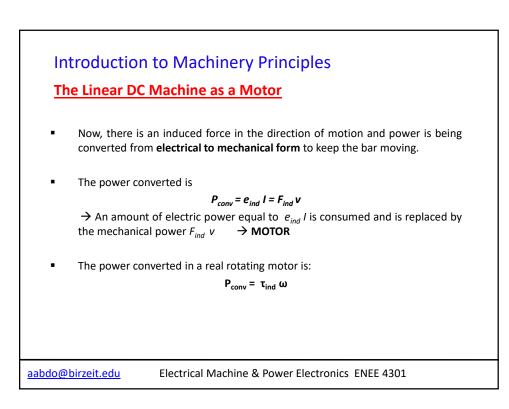
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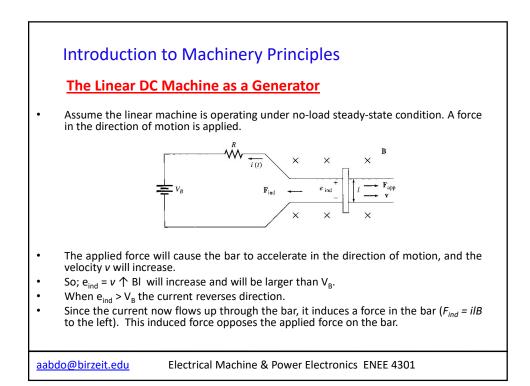
Electrical Machine & Power Electronics ENEE 4301

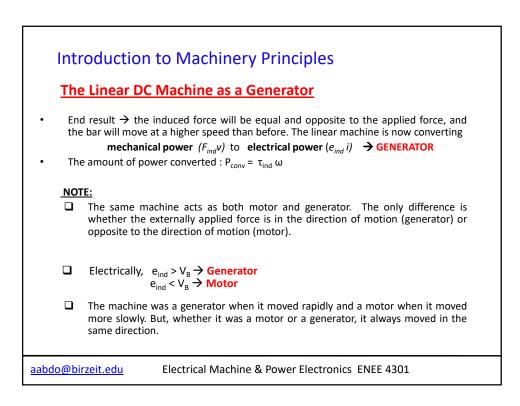
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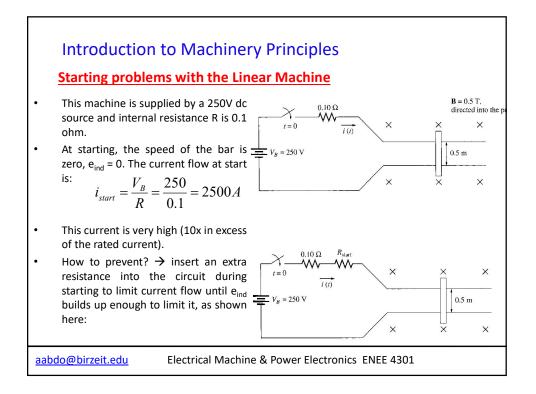


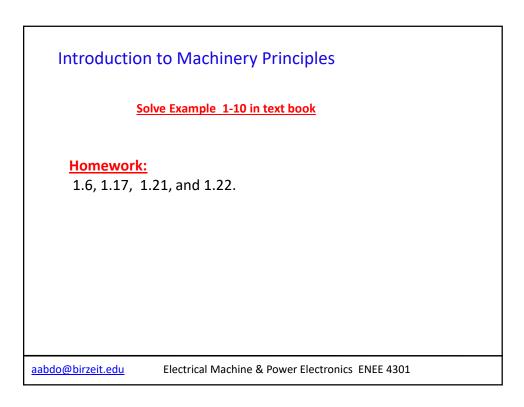


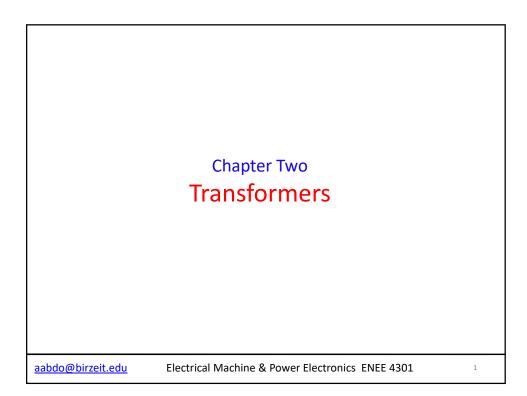




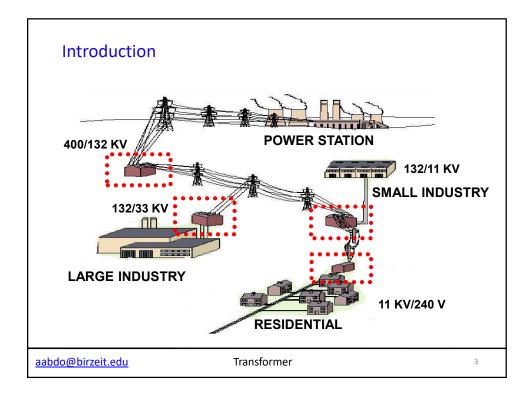




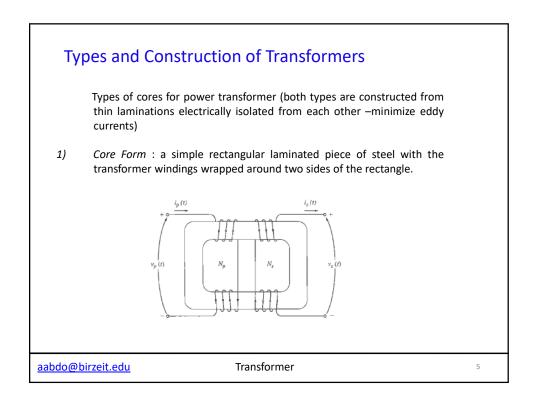


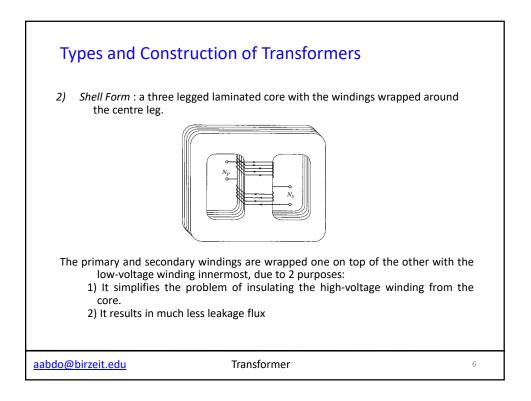


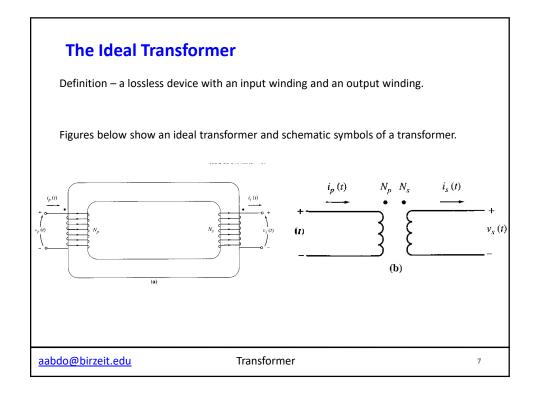
Ir	ntroduction	
	A transformer is a device that changes ac electric power at one frequency and voltage level to ac electric power at the same frequency and another voltage level through the action of a magnetic field.	
	It operates based on Faraday's Law : <i>induced voltage on a conductor/coil from a time changing magnetic field.</i>	
	It consist of two or more coils wrapped around a common Ferromagnetic core.	
aabdo@birzeit.edu Transformer		2



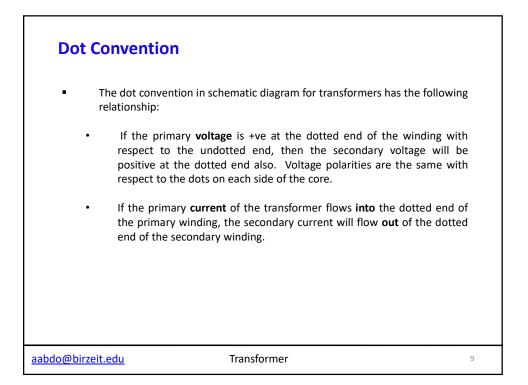
Туј	pes of Transformers
	Step up/Unit transformers – Usually located at the output of a generator. Its function is to step up the voltage level so that transmission of power is possible.
	Step down/Substation transformers – Located at main distribution or secondary level transmission substations. Its function is to lower the voltage levels for distribution 1st level purposes.
	Distribution Transformers – located at small distribution substation. It lowers the voltage levels for 2nd level distribution purposes.
	Special Purpose Transformers - E.g. Potential Transformer (PT) , Current Transformer (CT).
	Isolation and Impedance Matching Transformers.
aabdo@b	irzeit.edu Transformer 4
<u>aanno@n</u>	

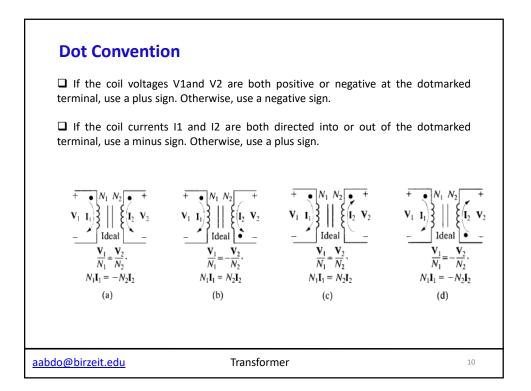


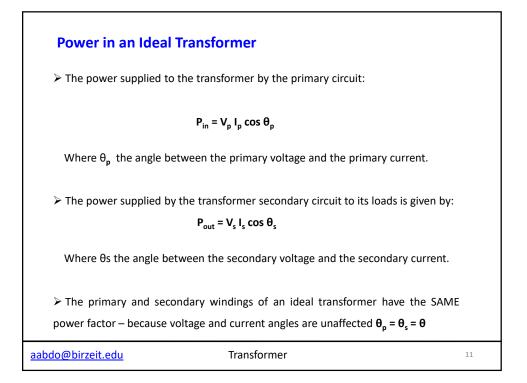




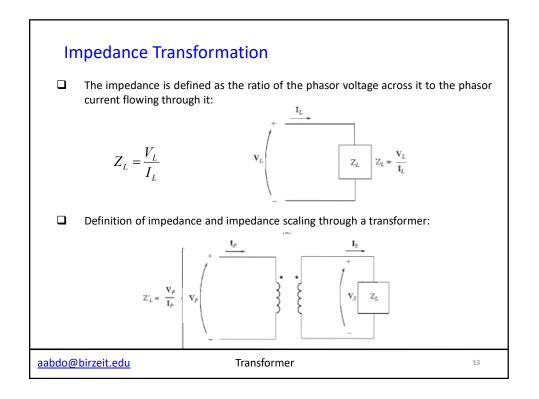
The Ideal Transformer The transformer has N_p turns of wire on its primary side and N_s turns of wire on its secondary sides. The relationship between the primary and secondary voltage is as follows: $\frac{v_p(t)}{v_s(t)} = \frac{N_p}{N_s} = a$ where *a* is the turns ratio of the transformer. The relationship between primary and secondary current is: $N_p i_p(t) = N_s i_s(t)$ $\frac{i_p(t)}{i_s(t)} = \frac{1}{a}$ Note that since both type of relations gives a constant ratio, hence the transformer changes ONLY the magnitude value of current and voltage. Phase angles are not affected. aabdo@birzeit.edu Transformer 8

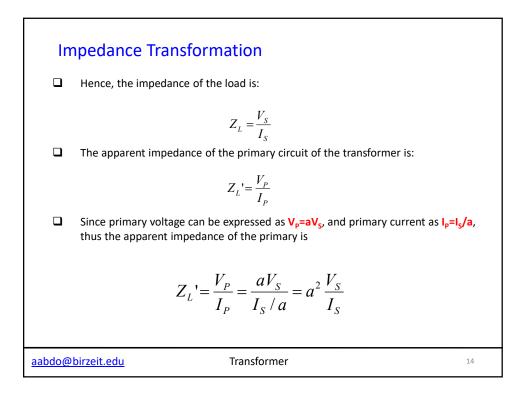




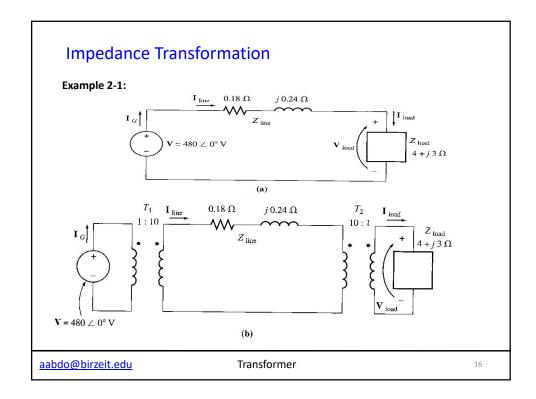


Power in an Ideal Transformer	
Input and output power in ideal transformer:	
$P_{out} = V_s I_s \cos \theta$	
We know that, $V_s = V_p / a$ and $I_s = a I_p$	
$P_{out} = \frac{V_p}{a} (aI_p) \cos \theta$	
$P_{out} = V_p I_p \cos \theta = P_{in}$	
Output Power = Input Power	
The same idea can be applied for reactive power Q and apparent power S.	
aabdo@birzeit.edu Transformer	12



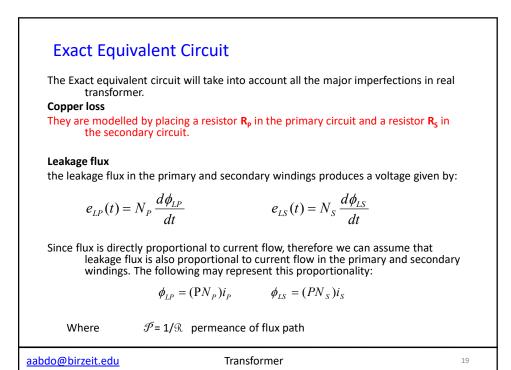


Impedance Transforma	ation	
Example 2-1:		
o	Hz is connected a transmission line with ar e end of the transmission line there is a load o	
	as described above in Figure (a), what will the vill the transmission line losses be?	е
transmission line and a 10:1 step-d	former is placed at the generator end of the own transformer is placed at the load end of the voltage be now? What will the transmission line	е
aabdo@birzeit.edu	Transformer	15

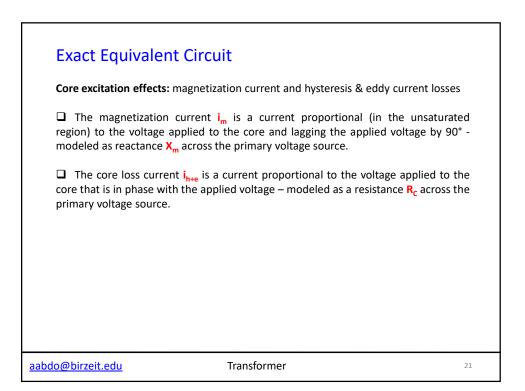


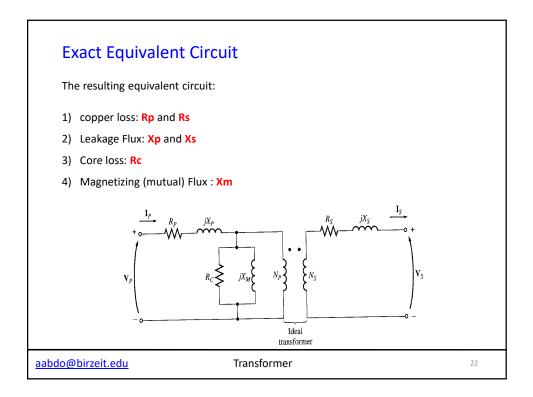
Real and Ideal Transformer	
What assumptions are required to convert a real transformer into the They are as follows:	ideal transformer?
1. The core must have no hysteresis or eddy currents.	
2. The magnetization curve must have the shape in the following figure Notice that for an unsaturated core the net magnetomotive force that $N_{\rho}i_{\rho} = N_s i_s$.	Fnet = 0, implying
3. The leakage flux in the core must be zero, implying that all the flux in the core couples both windings.	
4. The resistance of the transformer windings must	€, A • turns
aabdo@birzeit.edu Transformer	17

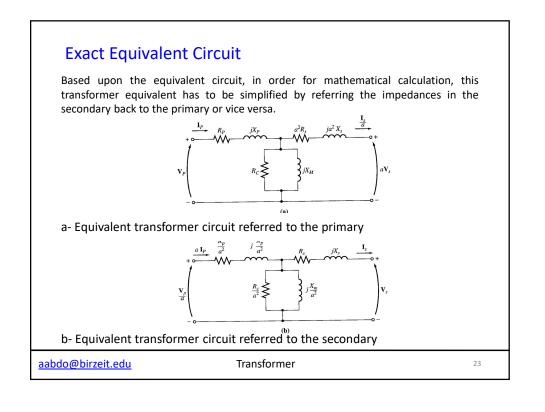
		-
Th	e Equivalent Circuit of a Transformer	
Taking	into account real transformer, there are several losses that has to be taken into account in order to accurately model the transformer, namely:	
1.	Copper (I²R) Losses – Resistive heating losses in the primary and secondary windings of the transformer.	
2.	Eddy current Losses – resistive heating losses in the core of the transformer. The are proportional to the square of the voltage applied to the transformer.	y
3.	Hysteresis Losses – these are associated with the rearrangement of the magnetic domains in the core during each half-cycle. They are complex, non-linear function of the voltage applied to the transformer.	с
4. Leakage flux – The fluxes and which escape the core and pass through only one of the transformer windings are leakage fluxes. They then produced self-inductance in the primary and secondary coils.		
<u>aabdo@b</u>	pirzeit.edu Transformer 18	3

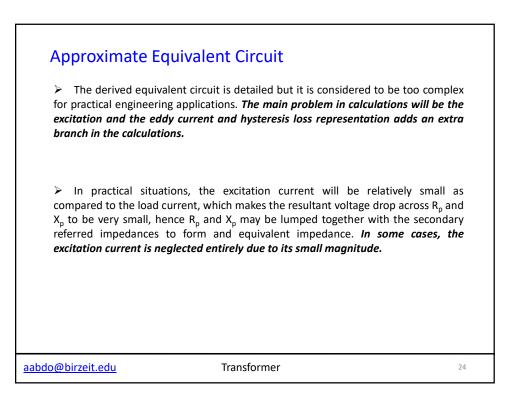


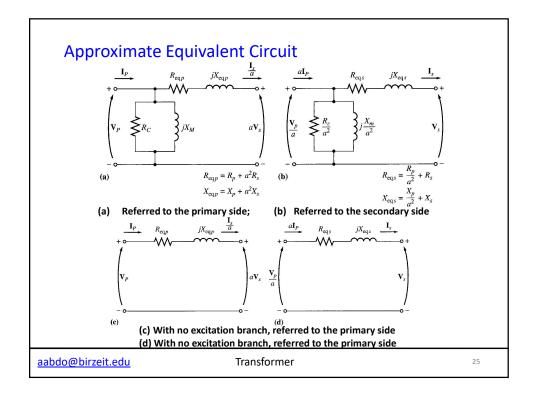
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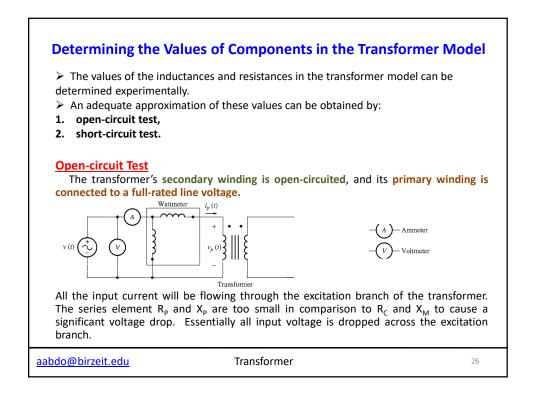


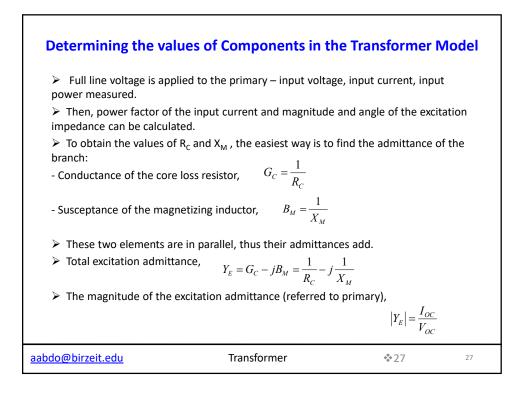


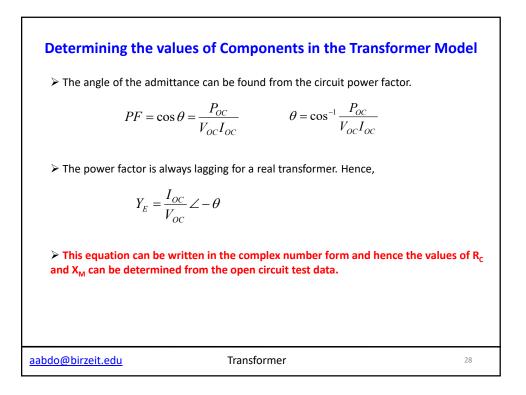


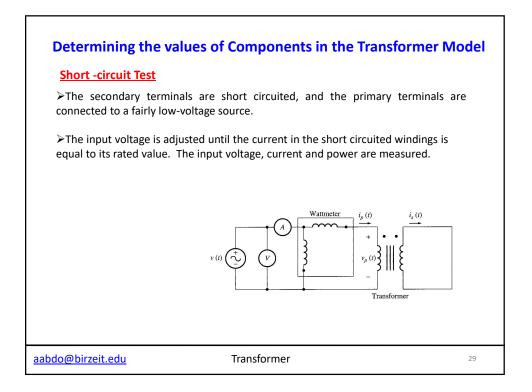




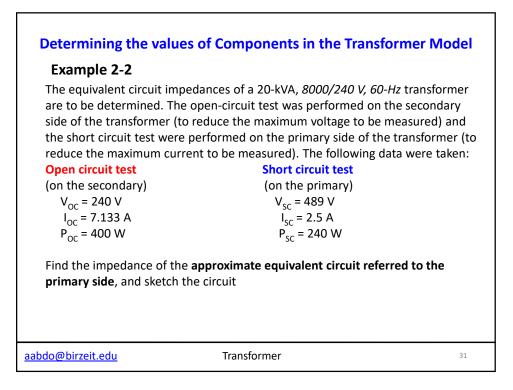


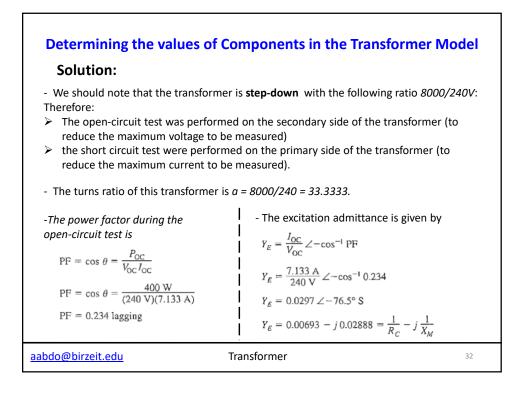


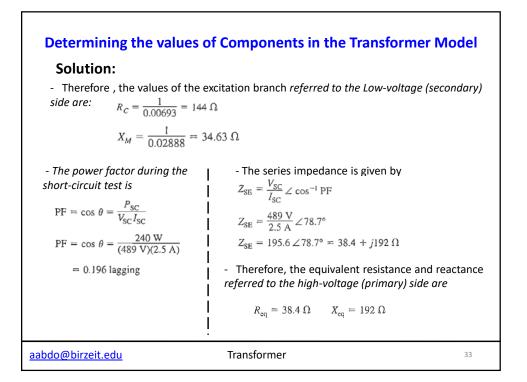


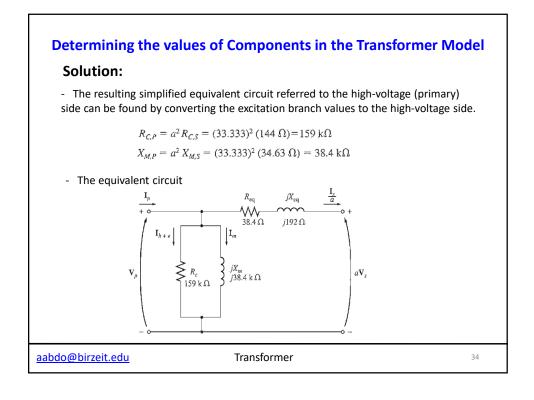


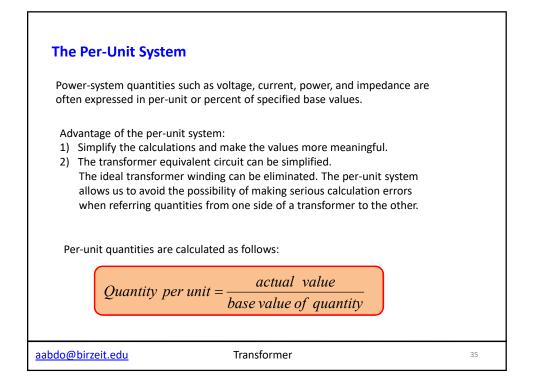
Determining the values of Components in the Transformer Model> The excitation branch is ignored, because negligible current flows through it
due to low input voltage during this test. Thus, the magnitude of the series
impedances referred to the primary is:
$$|Z_{SE}| = \frac{V_{SC}}{I_{SC}}$$
> Power factor, (lagging) $PF = \cos \theta = \frac{P_{SC}}{V_{SC}I_{SC}}$ Therefore, $Z_{SE} = \frac{V_{SC} \angle 0^{\circ}}{I_{SC} \angle - \theta} = \frac{V_{SC}}{I_{SC}} \angle \theta^{\circ}$ > The series impedance $Z_{SE} = R_{eq} + jX_{eq}$
 $= (R_p + a^2R_S) + j(X_P + a^2X_S)$ abdo@birzeit.edu

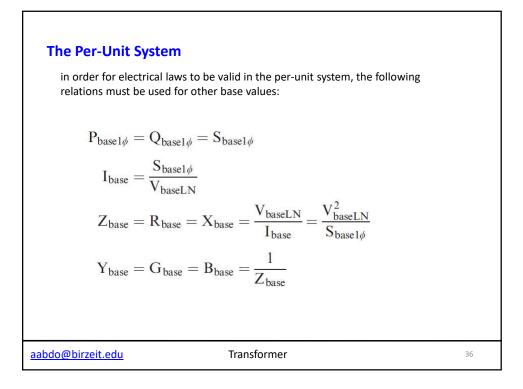






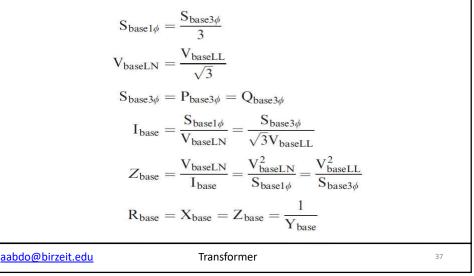


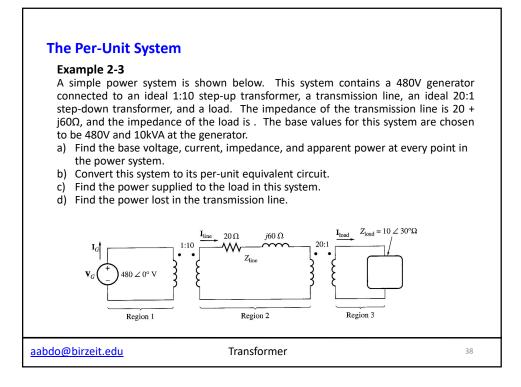






Balanced three-phase circuits can be solved in per-unit on a per-phase basis after converting Δ -load impedances to equivalent Y impedances.





The Per-Unit System

> If more than one machine and one transformer are included in a single power system, the system base voltage and power may be chosen arbitrarily, but the *entire system must have the same base.*

> One common procedure is to choose the system base quantities to be equal to the base of the largest component in the system.

> Per-unit values given to another base can be converted to the new base by converting them to their actual values (volts, amperes, ohms, etc.) as an inbetween step. Alternatively, they can be converted directly by the equations

$$(P, Q, S)_{\text{pu on base } 2} = (P, Q, S)_{\text{pu on base } 1} \frac{S_{\text{base } 1}}{S_{\text{base } 2}}$$

$$V_{\text{pu on base } 2} = V_{\text{pu on base } 1} \frac{V_{\text{base } 1}}{V_{\text{base } 2}}$$

$$(R, X, Z)_{\text{pu on base } 2} = (R, X, Z)_{\text{pu on base } 1} \frac{(V_{\text{base } 1})^2 (S_{\text{base } 2})}{(V_{\text{base } 2})^2 (S_{\text{base } 1})}$$

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Transformer

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Transformer Voltage Regulation and Efficiency

>The output voltage of a transformer varies with the load even if the input voltage remains constant. This is because a real transformer has series impedance within it.

 \succ Full load Voltage Regulation is a quantity that compares the output voltage at no load with the output voltage at full load, defined by this equation:

$$VR = \frac{V_{S,nl} - V_{S,fl}}{V_{S,fl}} \times 100\%$$

≻At no load, $V_s = V_p/a$ thus,

$$VR = \frac{\left(V_{P} / a\right) - V_{S,fl}}{V_{S,fl}} \times 100\%$$

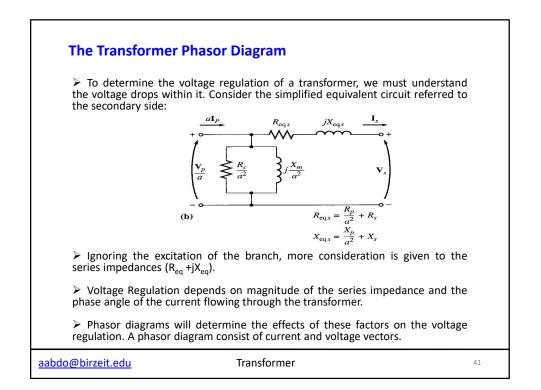
➢In per-unit system,

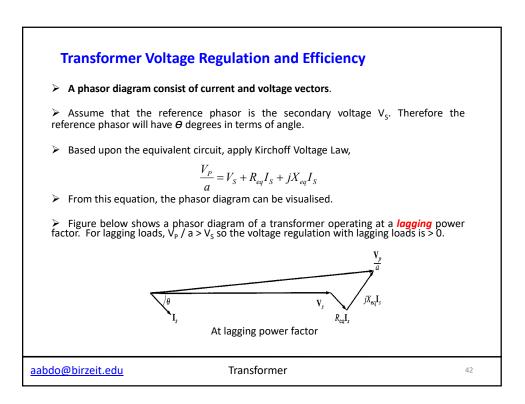
$$VR = \frac{V_{P,pu} - V_{S,fl,pu}}{V_{S,fl,pu}} \times 100\%$$

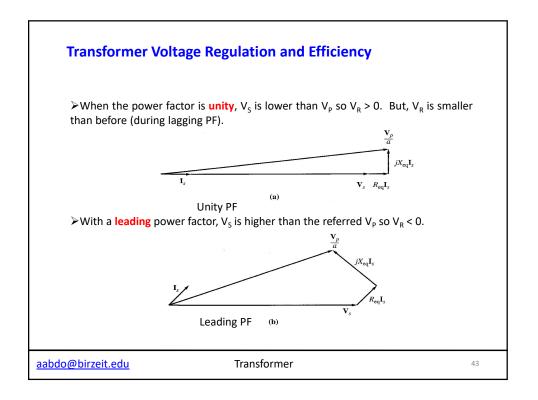
➢Ideal transformer, VR = 0%.

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Transformer







Tra	Transformer Voltage Regulation and Efficiency			
≻ In	summary:			
	Lagging PF	Unity PF	Leading PF	
	$V_p/a > V_s$	$V_p / a > V_s$	$V_{s} > V_{p} / a$	
	VR > 0	VR > 0 (smaller than VR lag)	VR < 0	
Due to the fact that transformer is usually operated at lagging pf, hence there i approximate method to simplify calculations.				
	irzeit.edu	Transformer		

Transformer Efficiency

> Transformer efficiency is defined as (applies to motors, generators and transformers):

$$\eta = \frac{P_{out}}{P_{in}} \times 100\% \qquad \qquad \eta = \frac{P_{out}}{P_{out} + P_{loss}} \times 100\%$$

> Types of losses incurred in a transformer:

1) Copper I²R losses

2) Hysteresis losses

3) Eddy current losses

> Therefore, for a transformer, efficiency may be calculated using the following:

$$\eta = \frac{V_S I_S \cos \theta}{P_{Cu} + P_{core} + V_S I_S \cos \theta} \times 100\%$$

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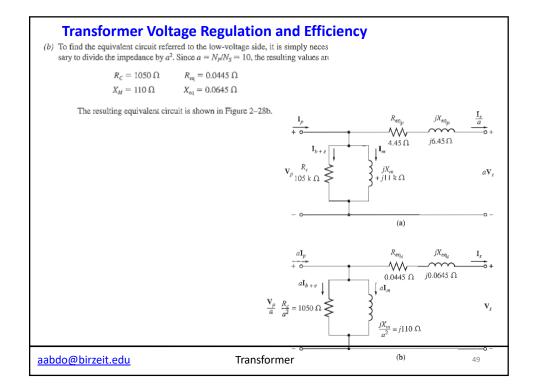
Transformer

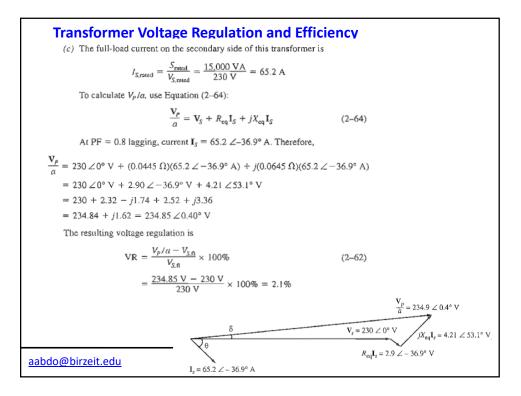
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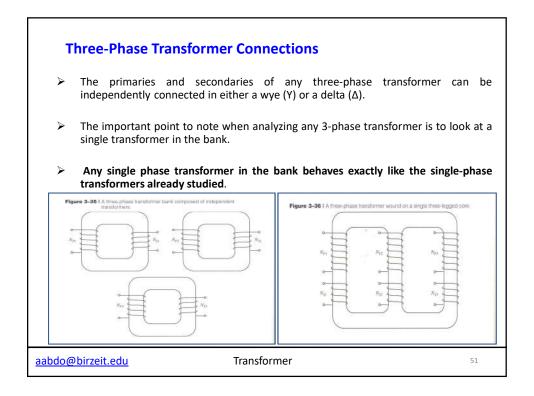
branch componer	30 V transformer is its, its series imped e been taken from the	ances, and its vo	etermine its excitation Itage regulation. The
	Open-circuit test (low voltage side)	Short-circuit test (high voltage side)	
	$V_{\rm OC} = 230 \text{ V}$	$V_{\rm SC}=47~{ m V}$	•
	$I_{\rm OC} = 2.1 {\rm A}$	$I_{\rm SC}=6.0{\rm A}$	
	$V_{\rm OC} = 50 \ { m W}$	$P_{SC} = 160 \text{ W}$	
 Find the e Calculate Cale leadin Plot the very power face 	g PF.	red to the low volta regulation at 0.8 la bad is increased fror 0, and 0.8 leading.	
In	portant example y	ou need to solve	it

Transformer Voltage Regulation and Efficiency (a) The turns ratio of this transformer is a = 2300/230 = 10. The excitation branch values of the transformer equivalent circuit referred to the secondary (low voltage) side can be calculated from the open-circuit test data, and the series elements referred to the primary (high voltage) side can be calculated from the short-circuit test data. From the open-circuit test data, the open-circuit impedance angle is $\theta_{\rm OC} = \cos^{-1} \frac{P_{\rm OC}}{V_{\rm OC} I_{\rm OC}}$ $\theta_{\rm OC} = \cos^{-1} \frac{50 \,\rm W}{(230 \,\rm V)(2.1 \,\rm A)} = 84^{\circ}$ The excitation admittance is thus $Y_E = \frac{I_{\rm OC}}{V_{\rm OC}} \angle -84^\circ$ $Y_E = \frac{2.1 \text{ A}}{230 \text{ V}} \angle -84^{\circ} \text{ S}$ $Y_E = 0.00913 \angle -84^\circ S = 0.000954 - j0.00908 S$ The elements of the excitation branch referred to the secondary are $R_{C,S} = \frac{1}{0.000954} = 1050 \,\Omega$ $X_{M,S} = \frac{1}{0.00908} = 110 \Omega$ aabdo@birzeit.edu Transformer 47

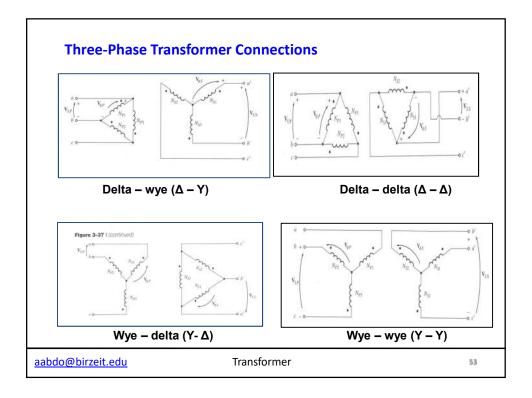
Transformer Voltage Regulation and Efficiency From the short-circuit test data, the short-circuit impedance angle is $\theta_{\rm SC} = \cos^{-1} \frac{P_{\rm SC}}{V_{\rm SC} I_{\rm SC}}$ $\theta_{\rm SC} = \cos^{-1} \frac{160 \text{ W}}{(47 \text{ V})(6 \text{ A})} = 55.4^{\circ}$ The equivalent series impedance is thus $Z_{\rm SE} = \frac{V_{\rm SC}}{I_{\rm SC}} \angle \theta_{\rm SC}$ $Z_{\rm SE} = \frac{47 \text{ V}}{6 \text{ A}} \angle 55.4^{\circ} \Omega$ $Z_{\rm SE} = 7.833 \angle 55.4^\circ = 4.45 + j6.45 \,\Omega$ The series elements referred to the primary side are $R_{eq,P} = 4.45 \ \Omega$ $X_{eq,P} = 6.45 \ \Omega$ The resulting simplified equivalent circuit referred to the primary side can be found by converting the excitation branch values to the primary side. $R_{C,P} = a^2 R_{C,S} = (10)^2 (1050 \ \Omega) = 105 \ k\Omega$ $X_{M,F} = a^2 X_{M,S} = (10)^2 (110 \ \Omega) = 11 \ k\Omega$ This equivalent circuit is shown in Figure 2-28a. aabdo@birzeit.edu Transformer 48



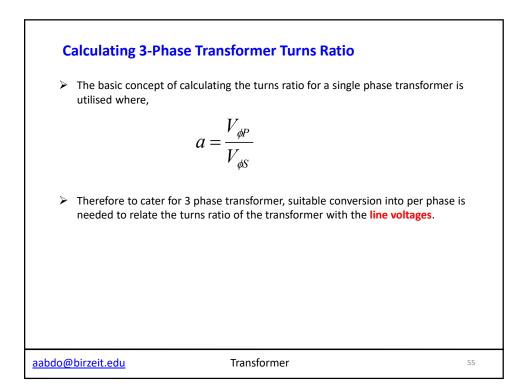


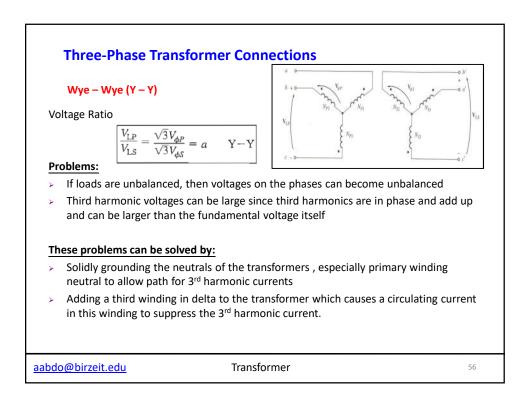


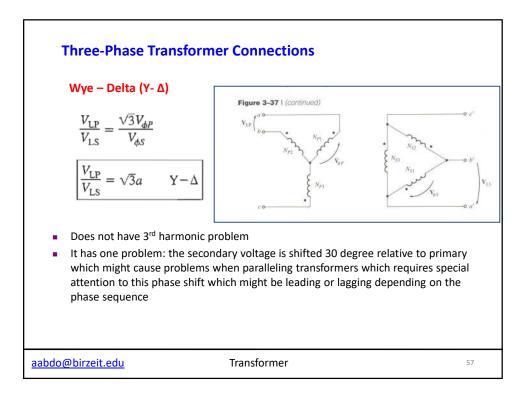


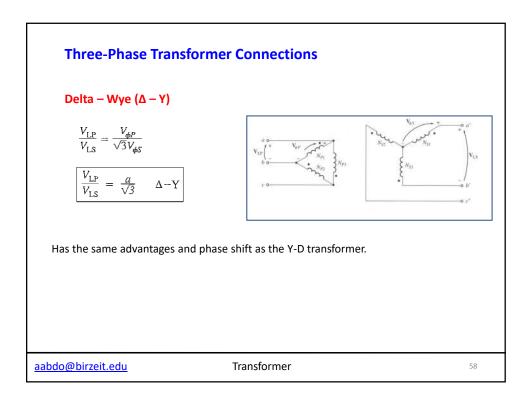


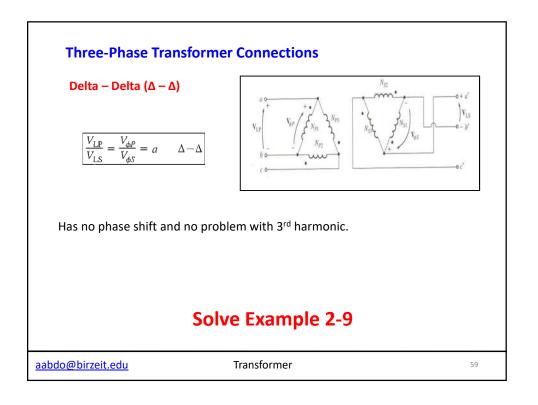
Three-Phase Transformer Connections The impedance, voltage regulation, efficiency, and similar calculations for three ≻ phase transformers are done on a per-phase basis, using same techniques as single-phase transformers. A simple concept that all students must remember is that, for a Delta ≻ configuration, $V_{\phi P} = V_{L}$ $I_{\phi P} = \frac{I_{L}}{\sqrt{3}}$ $S_{\phi P} = \frac{S}{3}$ For Wye configuration,(for balanced case $I_N=0$ and neutral can be left open and ≻ only 3 wires are required) $V_{\phi P} = \frac{V_L}{\sqrt{3}} \qquad \qquad I_{\phi P} = I_L \qquad \qquad S_{\phi P} = \frac{S}{3}$ aabdo@birzeit.edu Transformer 54





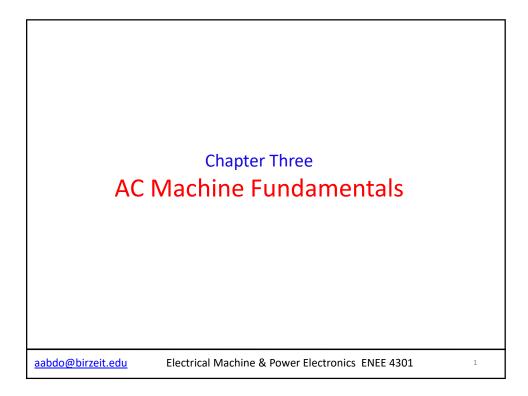


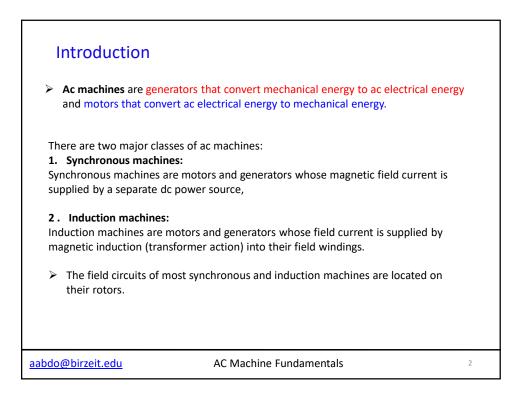


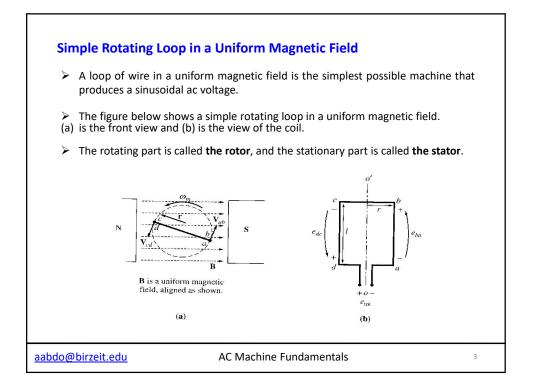


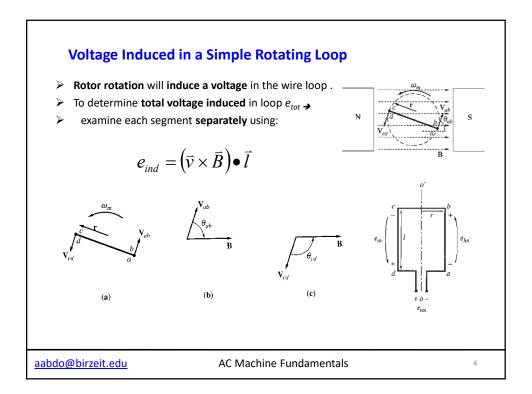
I	nstrument Transformers	
>	Special transformers used to take measurements: Potential Transformer (PT) and Current Transformer (CT)	
>	PT is a specially wound transformer with high-voltage primary and low-voltage secondary. It has a very low power rating and it is used to provide a an accurate sample of the power system voltage to the monitoring instrument without affecting the true voltage values	
>	CT sample the current an a line and reduce it to safe and measurable level.	
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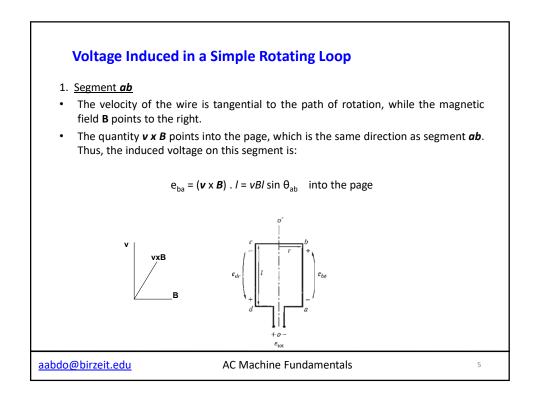
Но	mework	
>	Homework problems are: 2.1, 2.6, 2.12 and 2.24;	
۶	These problems are from the 5th edition text book.	
<u>aabdo@b</u>	irzeit.edu Transformer	61

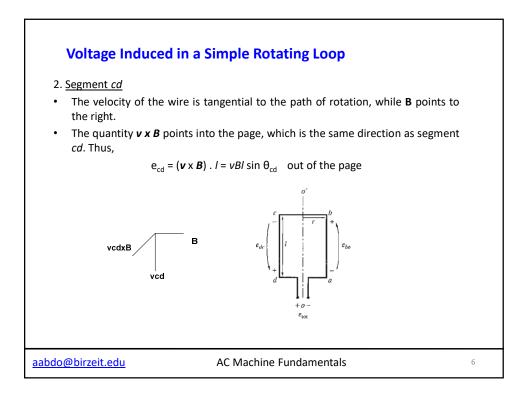


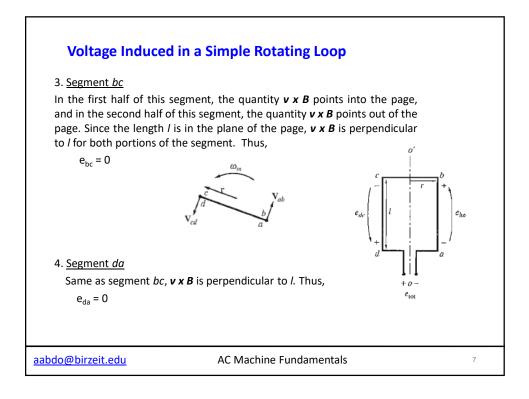


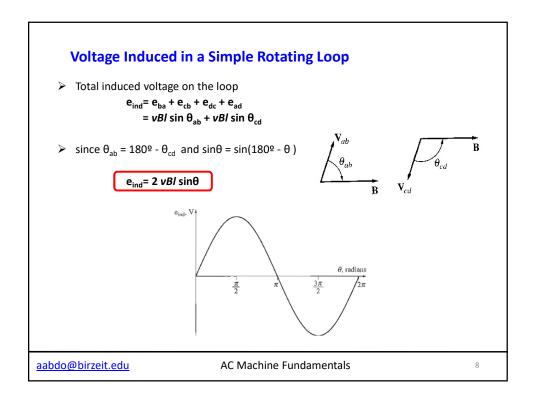


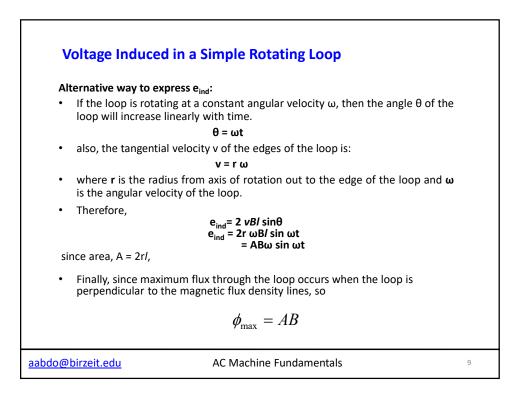


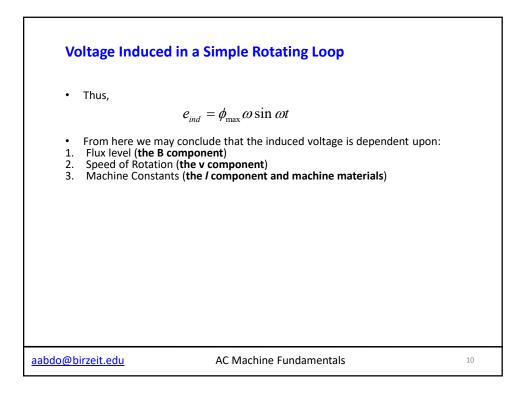


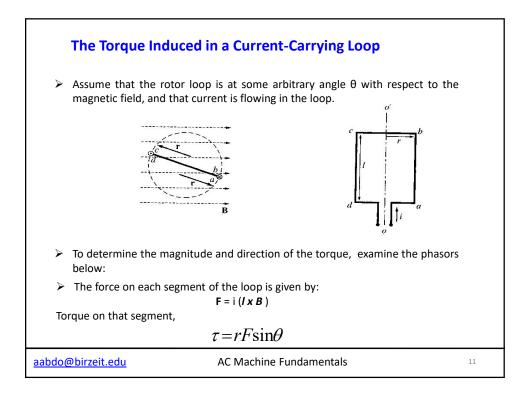


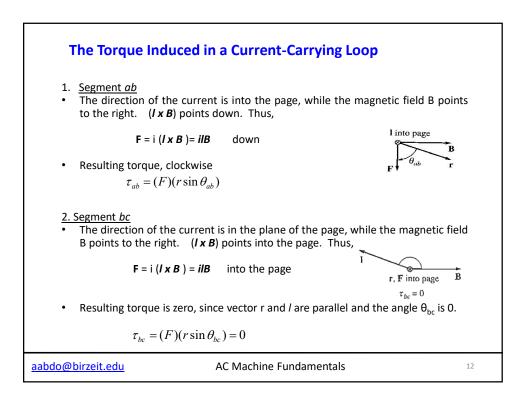


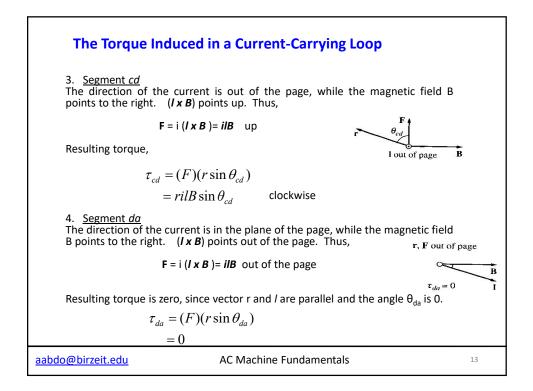


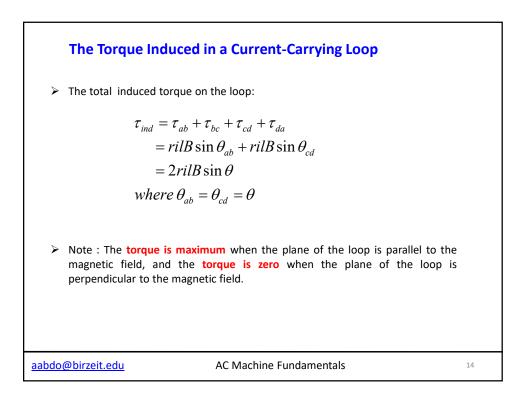


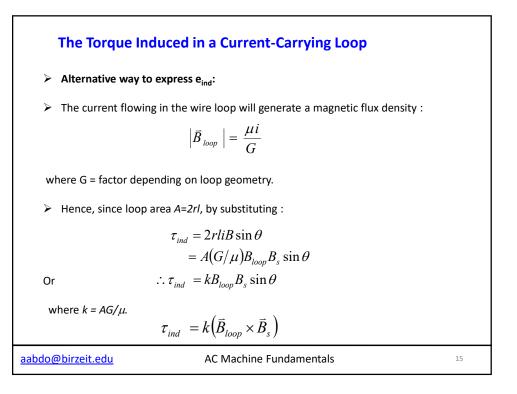


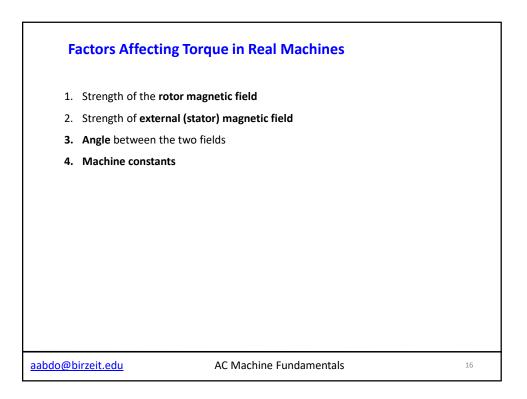


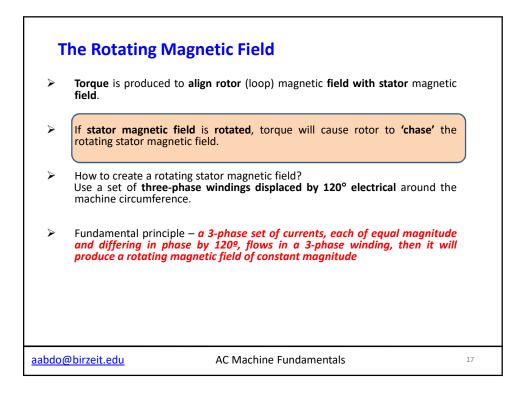


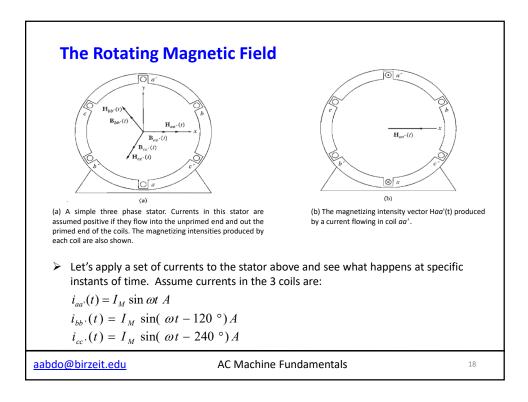


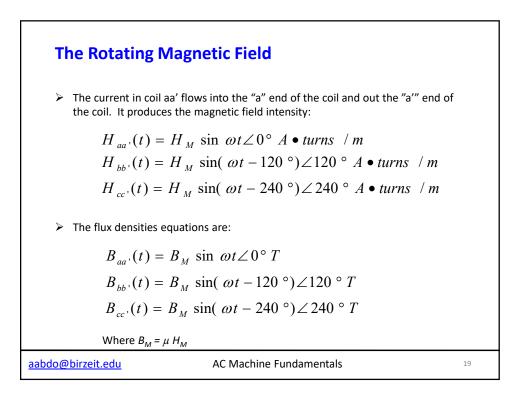




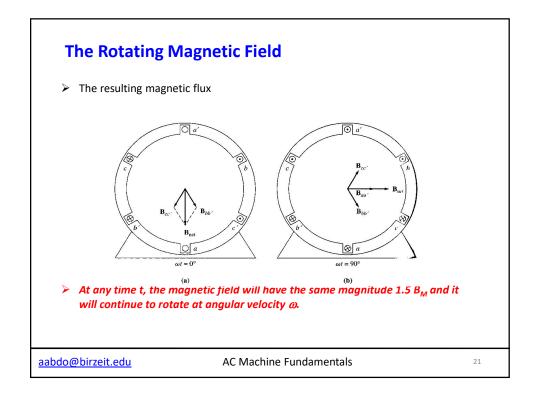


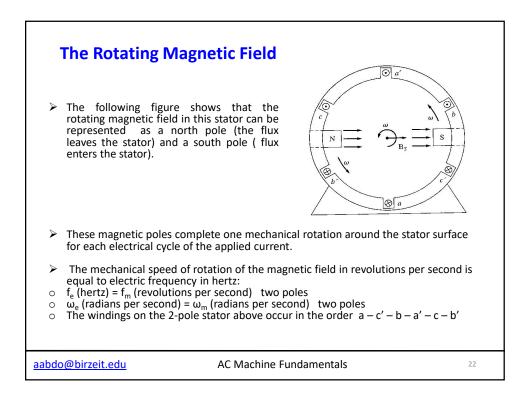


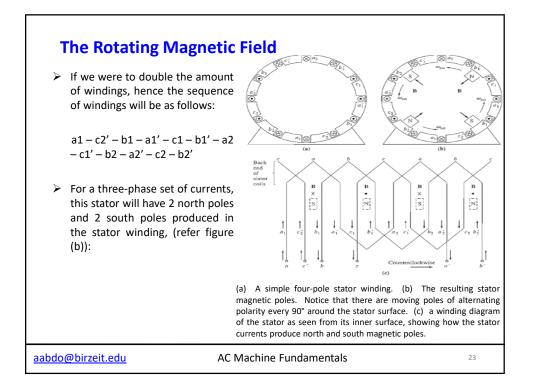




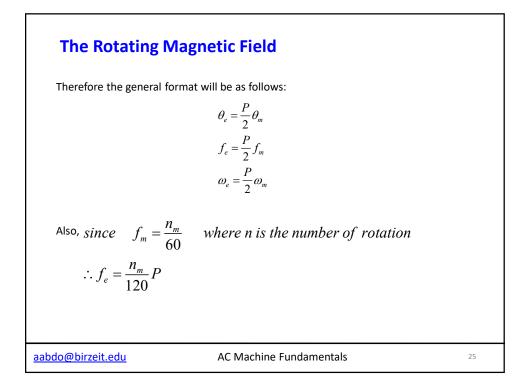
The Rotating Magnetic Field		
At $\omega t = 0^{\circ}$ $B_{aa'} = 0$ $B_{bb'} = B_M \sin(-120^{\circ}) \angle 120^{\circ} T$ $B_{cc'} = B_M \sin(-240^{\circ}) \angle 240^{\circ} T$ The total magnetic field from all three coils added together will be $B_{net} = B_{aa'} + B_{bb'} + B_{cc'}$ $= 0 + \left(-\frac{\sqrt{3}}{2}B_M\right) \angle 120^{\circ} + \left(\frac{\sqrt{3}}{2}B_M\right) \angle 240^{\circ}$ $= 1.5B_M \angle -90^{\circ}$	$\omega t = 90^{\circ}$ $B_{aa'} = B_M \angle 0^{\circ}$ $B_{bb'} = -0.5 B_M \angle 120^{\circ} T$ $B_{cc'} = -0.5 B_M \angle 240^{\circ} T$ The total magnetic field from all three coils added together will be $B_{net} = B_{aa'} + B_{bb'} + B_{cc'}$ $= B_M + (-0.5B_M) \angle 120^{\circ} + (-0.5B_M) \angle 240^{\circ}$ $= 1.5B_M \angle 0^{\circ}$	
aabdo@birzeit.edu AC Machine	e Fundamentals 20	

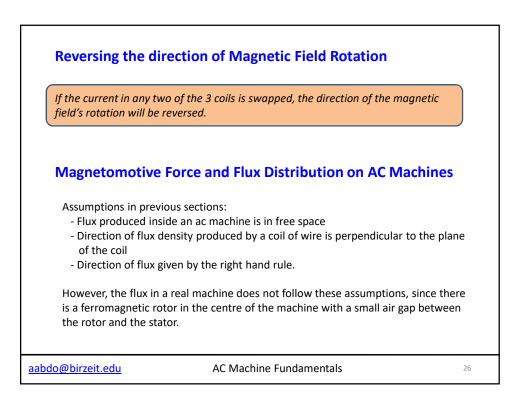


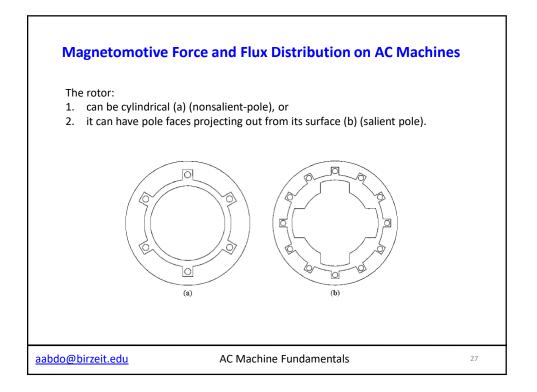


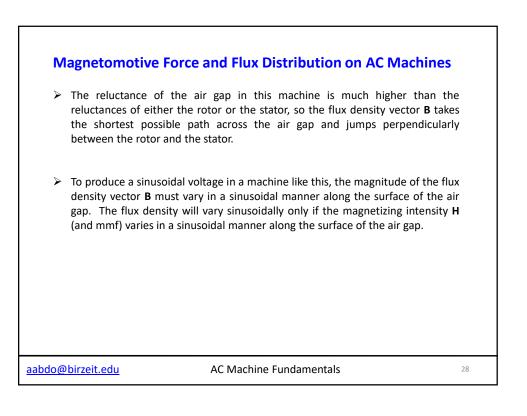


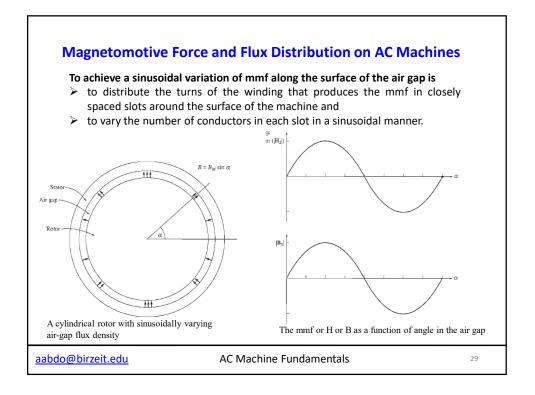
The Rotating Magnetic Field > In this winding, a pole moves only halfway around the stator surface in one electrical cycle. ≻ Since one electrical cycle is 360 electrical degrees, and mechanical motion is 180 mechanical degrees, the relationship between the electrical angle $\boldsymbol{\theta}_{e}$ and the mechanical $\boldsymbol{\theta}_m$ in this stator is $\theta s_e = 2\theta s_m$ Thus, for a four pole winding, the electrical frequency of the current is twice the \geq mechanical frequency of rotation: $f_e = 2f_m$ $\omega_e = 2\omega_m$ aabdo@birzeit.edu **AC Machine Fundamentals** 24

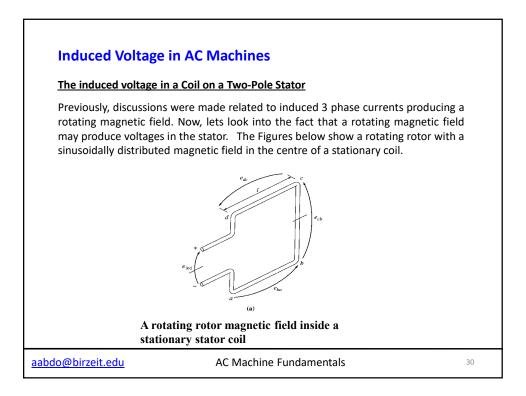


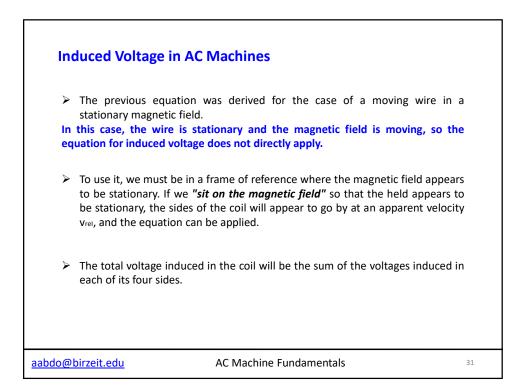




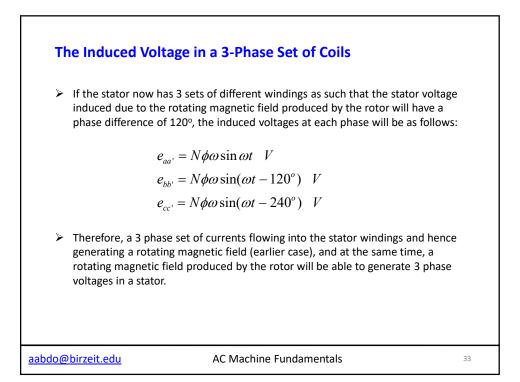


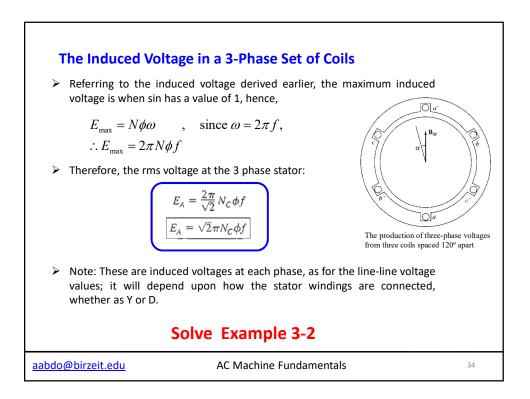


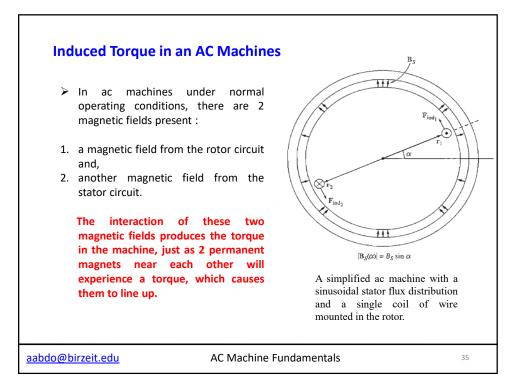


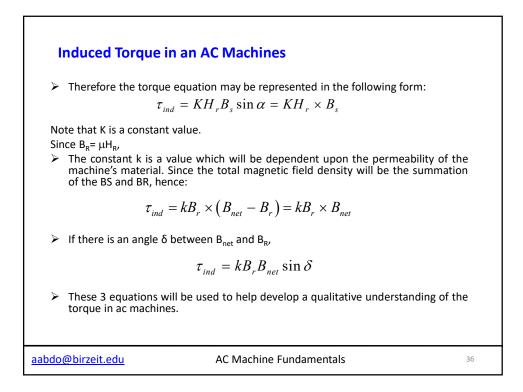


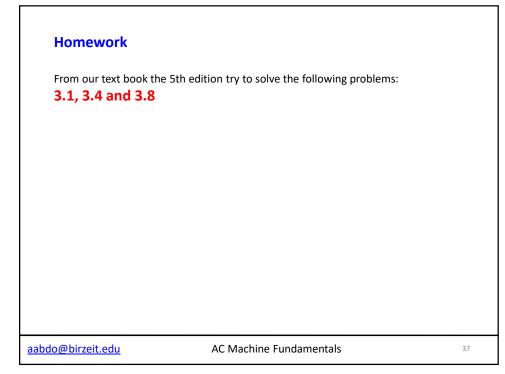
Induced Voltage in AC Machines Therefore, the total voltage on the coil will be $e_{induced} = e_{ba} + e_{dc} = 2VB_M l \cos \omega_m t$ Since, $v = r\omega_{m}$ Therefore, $e_{induced} = 2rlB_M \omega_m \cos \omega_m t$ $\phi = 2rlB_m$ Since, And the angular mechanical velocity should be equal to the angular electrical velocity, $e_{induced} = \phi \omega \cos \omega t$ or (taking into account number of turns of windings), $e_{induced} = N_c \phi \omega \cos \omega t$ aabdo@birzeit.edu **AC Machine Fundamentals** 32

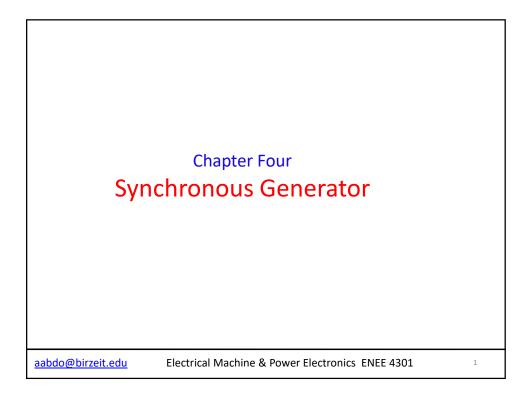


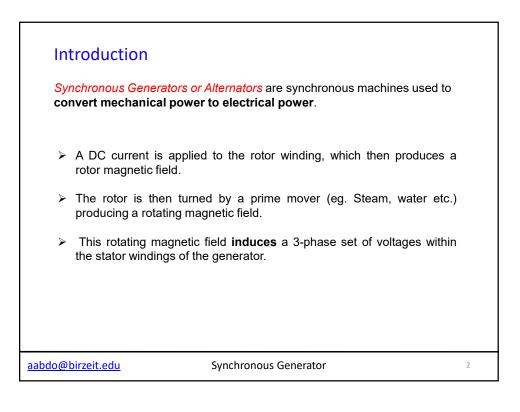


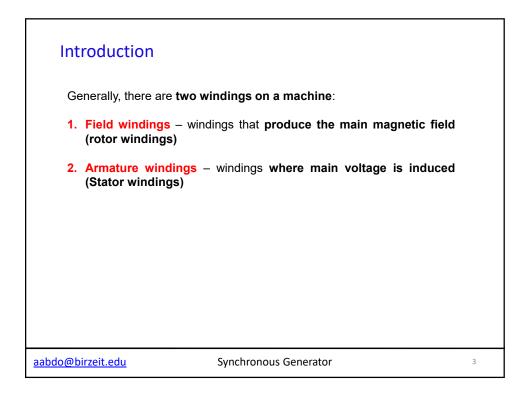


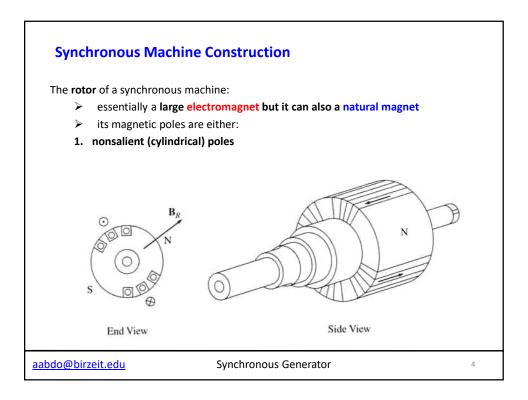


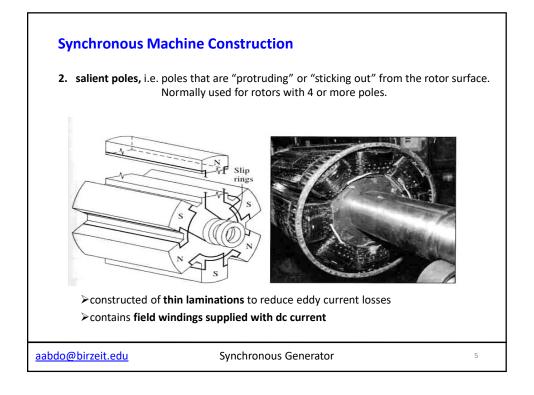


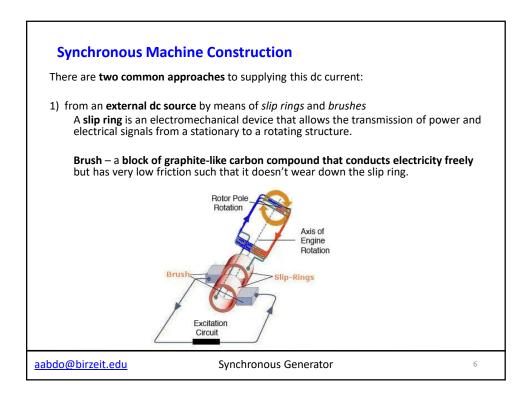




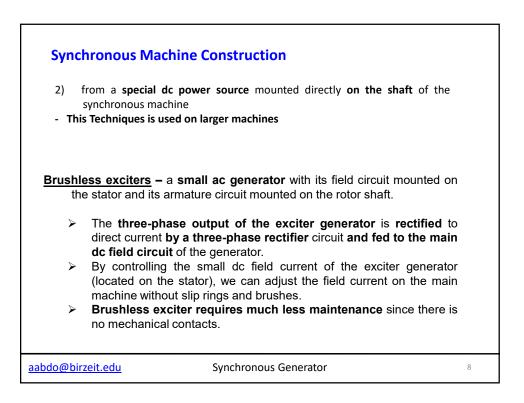


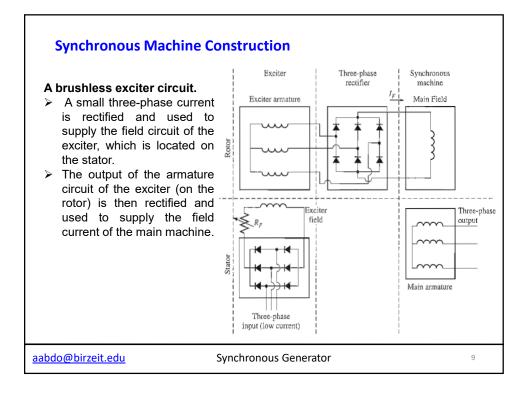


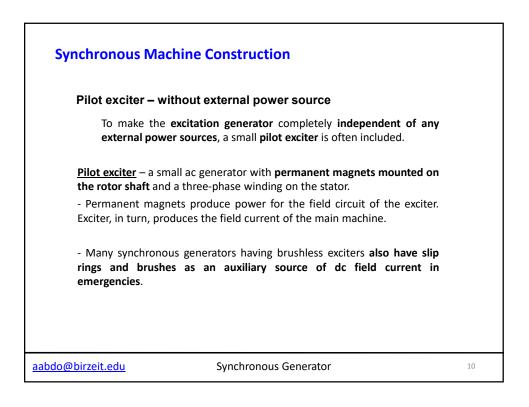


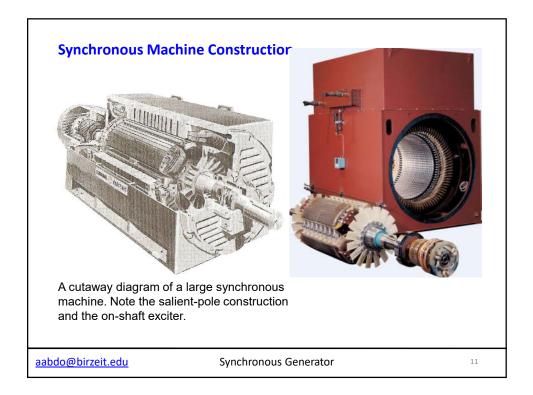


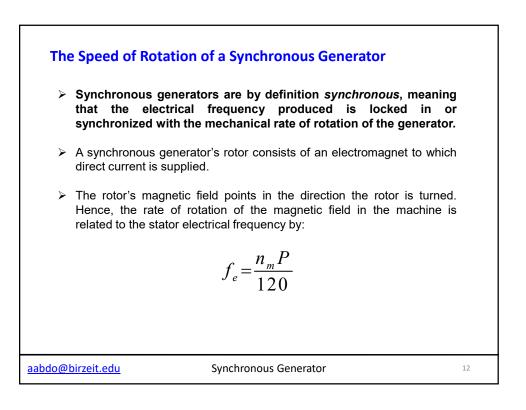
- (synchronous machine, one end of the dc rotor winding is tied to each of the two slip rings, and a stationary brush rides on each slip ring.
	 If positive end of a dc voltage source is connected to one brush and the negative end is connected to the other, then the same dc voltage will be applied to the field winding at all times regardless of the angular position or speed of rotor.
Pro	blems with slip rings and brushes:
1.	Increased maintenance required – check brushes for wear regularly.
2.	Brush voltage drop can cause significant power losses on machines with larger field currents.
The	refore, slip rings and brushes are used on all small synchronous machines

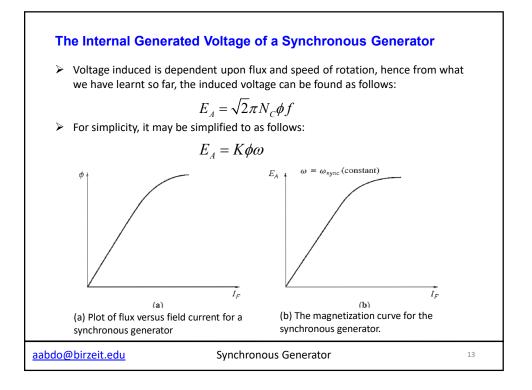


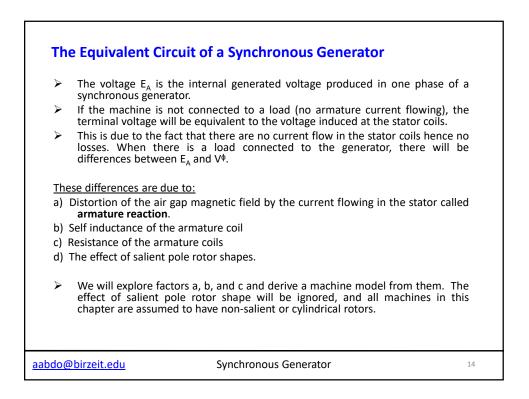


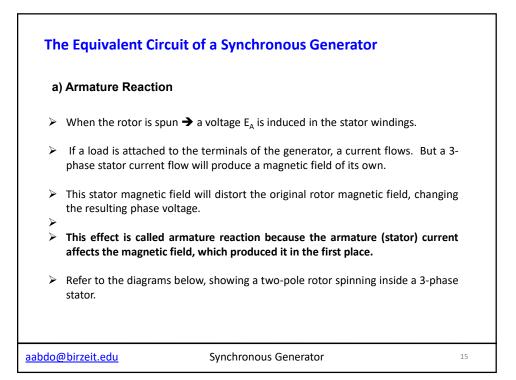


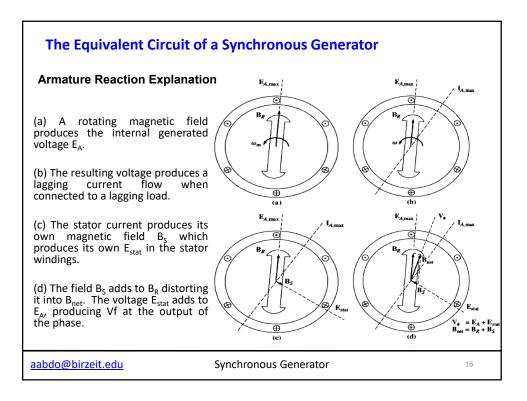


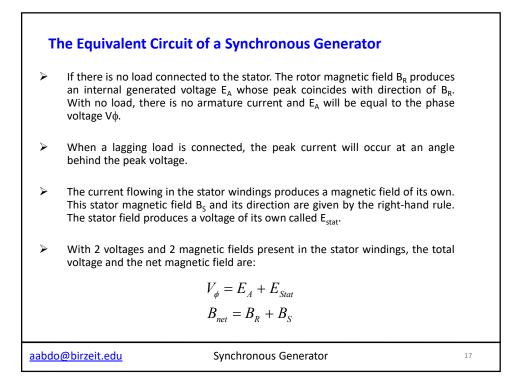


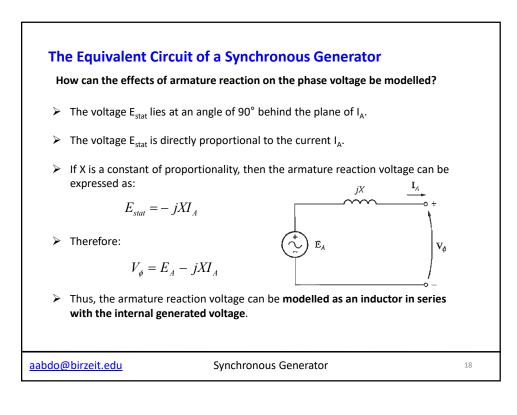


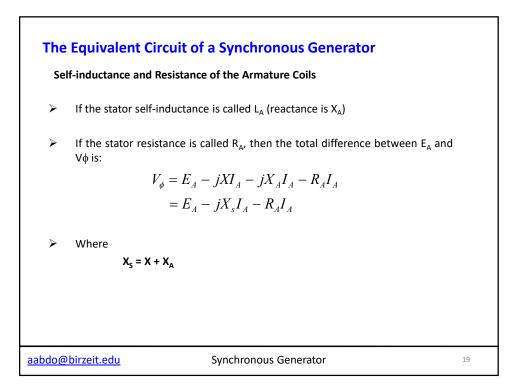


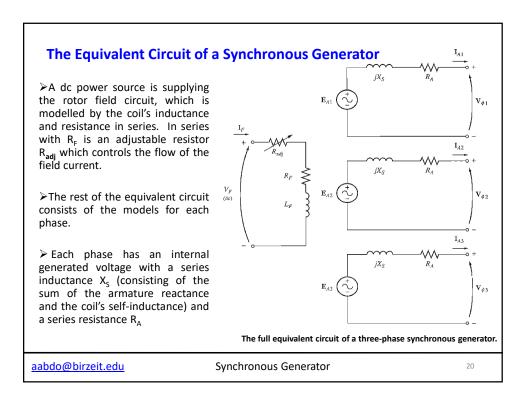


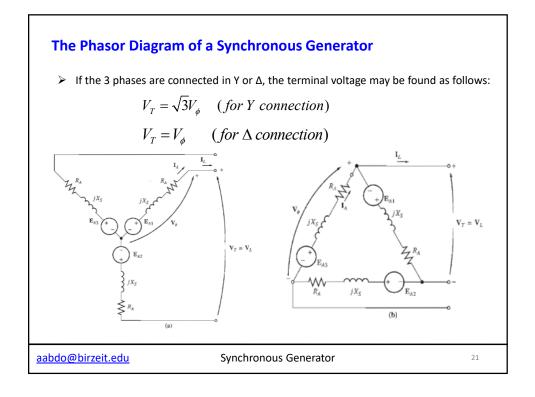


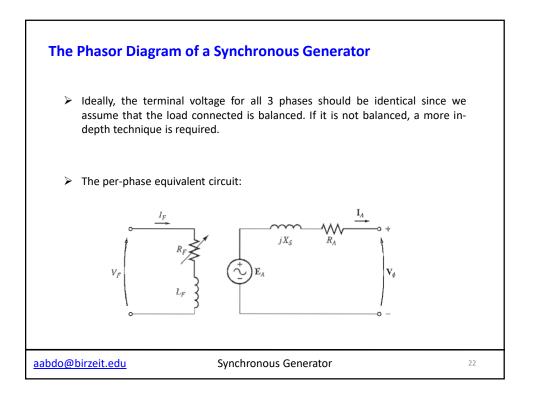


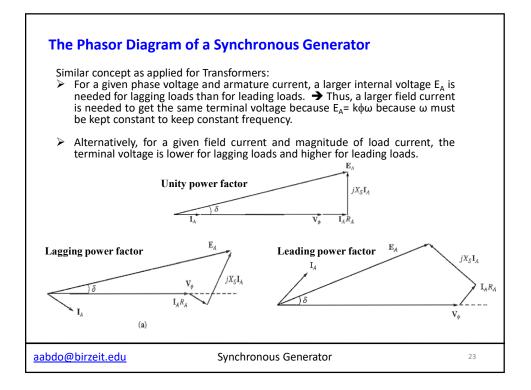


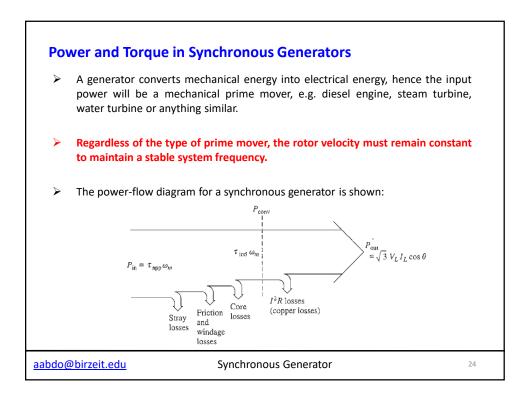


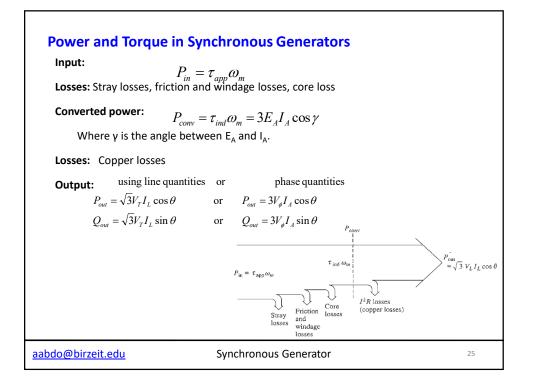


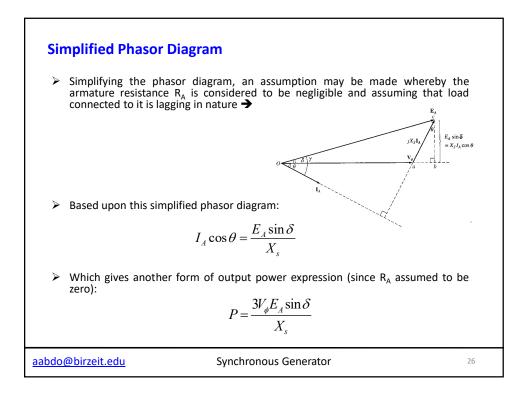




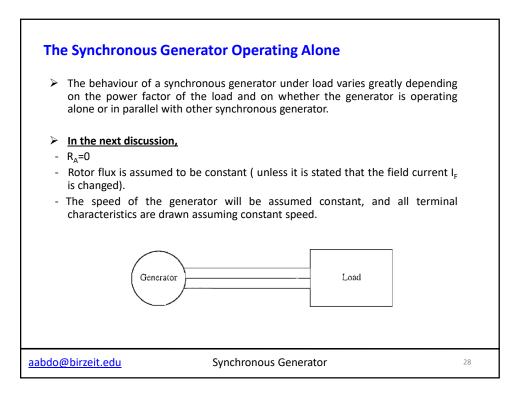


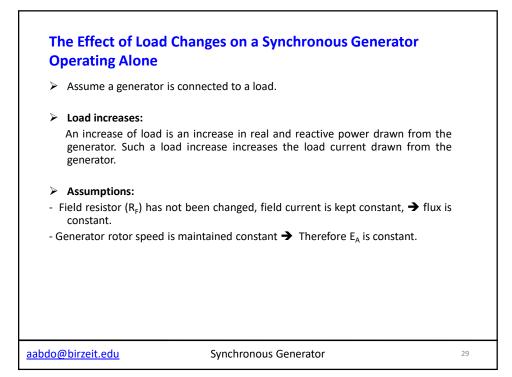


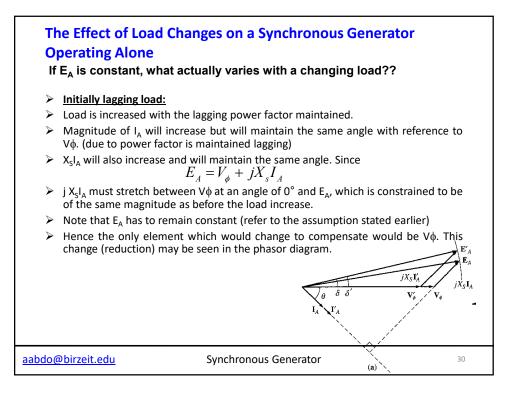


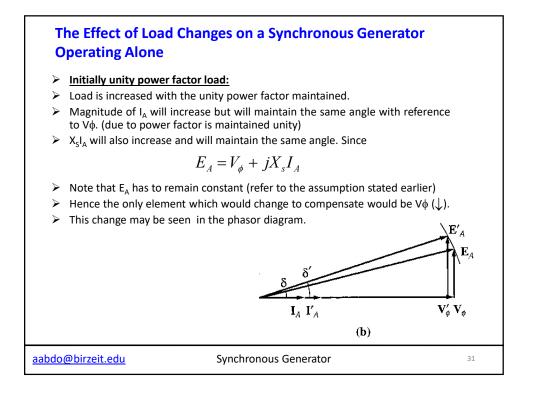


Simplified Phasor Diagram From the above equation, it can be seen that power is dependent upon: ⊳ The angle between V ϕ and E_A which is δ . ≻ δ is known as the torque angle of the machine. ⊳ ≻ maximum torque may be found when sin δ is 1 which gives the maximum power (a.k.a. static stability limit) to be: $P_{\max} = \frac{3V_{\phi}E_A}{X_c}$ The basic torque equation: ⊳ $\tau_{ind} = kB_{R} \times B_{s} = kB_{R} \times B_{net} = kB_{R}B_{net}\sin\delta$ An alternative expression can be derived from the power expression since $P_{out}=P_{conv}$ when R_A assumed to be zero. Because $P_{conv}=\tau_{ind}\omega_m$, the induced torque is: ≻ $\tau_{ind} = \frac{3V_{\phi}E_A\sin\delta}{\omega_m X_s}$ aabdo@birzeit.edu Synchronous Generator 27







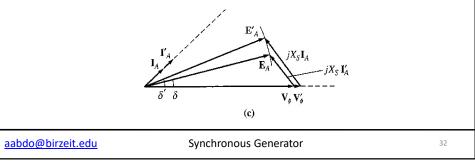


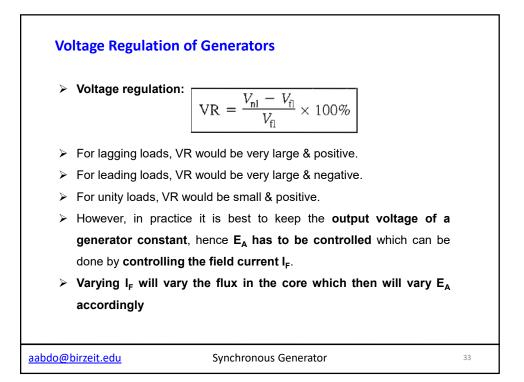
The Effect of Load Changes on a Synchronous Generator Operating Alone Initially leading power factor Load

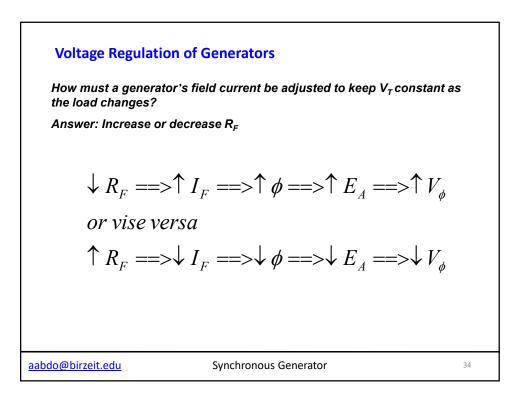
- > Load is increased with the leading power factor maintained.
- > Magnitude of I_A will increase but will maintain the same angle with reference to V ϕ . (due to power factor is maintained leading)
- > X_sI_A will also increase and will maintain the same angle. Since

$$E_A = V_\phi + jX_s I_A$$

- > Note that E_A has to remain constant (as assumed earlier)
- \blacktriangleright Hence the only element which would change to compensate would be V ϕ .







Example 4-2

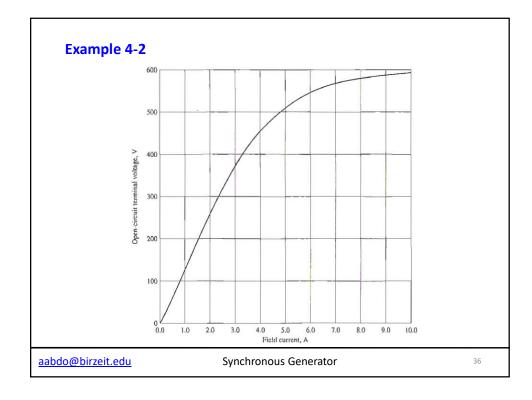
A 480-V, 60-Hz, Δ -connected, four-pole synchronous generator has the *OCC* shown in Figure 4-23a. This generator has a synchronous reactance of 0.1 Ω and an mature resistance of 0.0 15 Ω , At full load, the machine supplies 1200 A at 0.8 PF lagging. Under full-load conditions, the friction and windage losses are 40 kW, and the core losses are 30 kW. Ignore any field circuit losses.

- (a) What is the speed of rotation of this generator?
- (b) How much field current must be supplied to the generator to make the terminal voltage 480 V at no load?
- (c) If the generator is now connected to a load and the load draws 1200 A at 0.8 PF lagging, how much field current will be required to keep the terminal voltage equal to 480 V?
- (d) How much power is tile generator now supplying? How much power is supplied to the generator by the prime mover? What is this machine's overall efficiency?
- (e) If the generator's load were suddenly disconnected from the line, what would happen to its terminal voltage?
- (f) Finally, suppose that the generator is connected to a load drawing 1200 A at 0.8 PF leading. How much field current would be required to keep VT at 480 V?

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Example 4-2

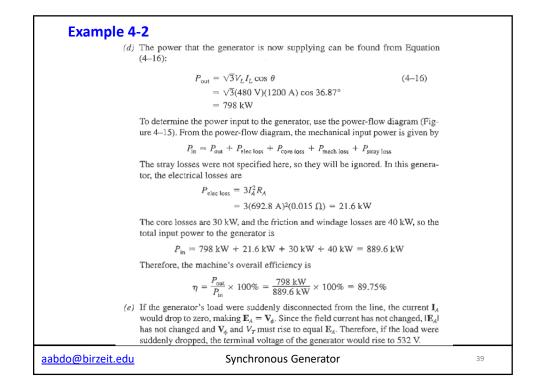
Solution

This synchronous generator is Δ -connected, so its phase voltage is equal to its line voltage $V_{\phi} = V_T$, while its phase current is related to its line current by the equation $I_L = \sqrt{3}I_{\phi}$. (a) The relationship between the electrical frequency produced by a synchronous generator and the mechanical rate of shaft rotation is given by Equation (3–34): $f_{se} = \frac{n_m P}{120}$ (3–34) Therefore, $n_m = \frac{120f_{se}}{P}$ $= \frac{120(60 \text{ Hz})}{4 \text{ poles}} = 1800 \text{ r/min}$ (b) In this machine, $V_T = V_{\phi}$. Since the generator is at no load, $I_A = 0$ and $E_A = V_{\phi}$. Therefore, $V_T = V_{\phi} = E_A = 480 \text{ V}$, and from the open-circuit characteristic, $I_F = 4.5 \text{ A}$.

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Synchronous Generator

Example 4-2 (c) If the generator is supplying 1200 A, then the armature current in the machine is $I_{\rm A} = \frac{1200 \,\rm A}{\sqrt{3}} = 692.8 \,\rm A$ The phasor diagram for this generator is shown in Figure 4-23b. If the terminal voltage is adjusted to be 480 V, the size of the internal generated voltage \mathbf{E}_A is given by $\mathbf{E}_A = \mathbf{V}_{\phi} + R_A \mathbf{I}_A + j X_S \mathbf{I}_A$ $= 480 \angle 0^{\circ} \text{V} + (0.015 \ \Omega)(692.8 \angle -36.87^{\circ} \text{ A}) + (j0.1 \ \Omega)(692.8 \angle -36.87^{\circ} \text{ A})$ $= 480 \angle 0^{\circ} V + 10.39 \angle -36.87^{\circ} V + 69.28 \angle 53.13^{\circ} V$ $= 529.9 + i49.2 V = 532 \angle 5.3^{\circ} V$ To keep the terminal voltage at 480 V, \mathbb{E}_A must be adjusted to 532 V. From Figure 4-23, the required fie v, кù $I_A = 692.8 \angle - 36.87^\circ \text{ A}$ aabdo@birzeit.edu Synchronous Generator 38



Example 4-2	
(f) If the generator were loaded down with 1200 A at 0.8 PF leading while the ter- minal voltage was 480 V, then the internal generated voltage would have to be	
$\mathbf{E}_{A} = \mathbf{V}_{\phi} + R_{A}\mathbf{I}_{A} + jX_{S}\mathbf{I}_{A}$	
= $480 \angle 0^{\circ} V + (0.015 \Omega)(692.8 \angle 36.87^{\circ} A) + (j0.1 \Omega)(692.8 \angle 36.87^{\circ} A)$ = $480 \angle 0^{\circ} V + 10.39 \angle 36.87^{\circ} V + 69.28 \angle 126.87^{\circ} V$ = $446.7 + j61.7 V = 451 \angle 7.1^{\circ} V$	
Therefore, the internal generated voltage E_A must be adjusted to provide 451 V if V_T is to remain 480 V. Using the open-circuit characteristic, the field current would have to be adjusted to 4.1 A.	
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Example 4-3 A 480V, 50Hz, Y-connected, 6-pole synchronous generator has a per-phase synchronous reactance of 1Ω . Its full-load armature current is 60A at 0.8PF lagging. This generator has friction and windage losses of 1.5kW and core losses of 1 kW at 50Hz at full load. Since the armature resistance is being ignored, assume that the I^2R losses are negligible. The field current has been adjusted so that the terminal voltage is 480V at no load. (a) What is the speed of rotation of this generator? (b) What is the terminal voltage of this generator if the following are true? 1. It is loaded with the rated current at 0.8 PF lagging. 2. It is loaded with the rated current at 1.0 PF. 3. It is loaded with the rated current at 0.8 PF leading. (c) What is the efficiency of this generator (ignoring the unknown electrical losses) when it is operating at the rated current and 0.8 PF lagging? (d) How much shaft torque must applied by the prime mover at full load? How large is the induced counter-torque? (e) What is the voltage regulation of this generator at 0.8 PF lagging? At 1.0 PF? At 0.8 PF leading? 41 aabdo@birzeit.edu Synchronous Generator

Example 4-3

Solution

This generator is Y-connected, so its phase voltage is given by $V_{\phi} = V_T / \sqrt{3}$. That means that when V_T is adjusted to 480 V, $V_{\phi} = 277$ V. The field current has been adjusted so that $V_{T,nl} = 480$ V, so $V_{\phi} = 277$ V. At *no load*, the armature current is zero, so the armature reaction voltage and the $I_A R_A$ drops are zero. Since $I_A = 0$, the internal generated voltage $E_A = V_{\phi} = 277$ V. The internal generated voltage $E_A (= K\phi\omega)$ varies only when the field current changes. Since the problem states that the field current is adjusted initially and then left alone, the magnitude of the internal generated voltage is $E_A = 277$ V and will not change in this example.

(a) The speed of rotation of a synchronous generator in revolutions per minute is given by Equation (3–34):

$$f_{se} = \frac{n_m P}{120}$$
(3–34)

Therefore,

$$n_m = \frac{120f_{se}}{P}$$
$$= \frac{120(50 \text{ Hz})}{6 \text{ poles}} = 1000 \text{ r/min}$$

Alternatively, the speed expressed in radians per second is

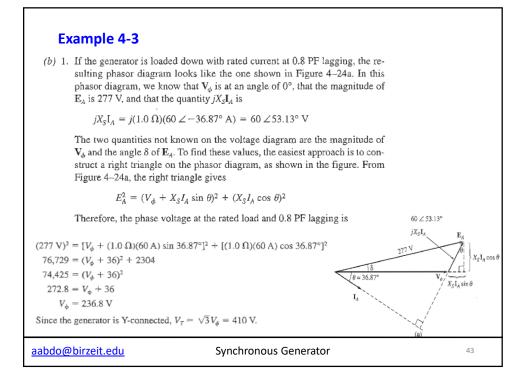
$$\omega_m = (1000 \text{ r/min}) \left(\frac{1 \text{ min}}{60 \text{ s}}\right) \left(\frac{2\pi \text{ rad}}{1 \text{ r}}\right)$$

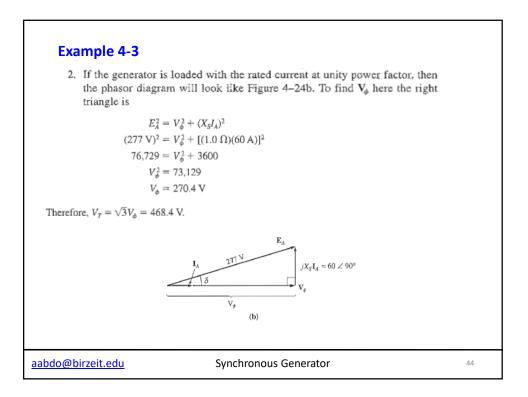
= 104.7 rad/s

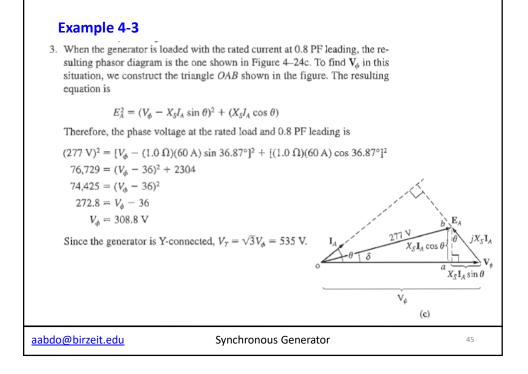
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Example 4-3	
(c) The output power of this generator at 60 A and 0.8 PF lagging is $P_{out} = 3V_{\phi} I_A \cos \theta$ $= 3(236.8 \text{ V})(60 \text{ A})(0.8) = 34.1 \text{ kW}$ The mechanical input power is given by $P_{in} = P_{out} + P_{elec \log s} + P_{core \log s} + P_{mech \log s}$ $= 34.1 \text{ kW} + 0 + 1.0 \text{ kW} + 1.5 \text{ kW} = 36.6 \text{ kW}$ The efficiency of the generator is thus	
$\eta = \frac{P_{\text{out}}}{P_{\text{in}}} \times 100\% = \frac{34.1 \text{ kW}}{36.6 \text{ kW}} \times 100\% = 93.2\%$ (d) The input torque to this generator is given by the equation $P_{\text{in}} = \tau_{\text{app}}\omega_m$	
so $\tau_{app} = \frac{P_{in}}{\omega_m} = \frac{36.6 \text{ kW}}{125.7 \text{ rad/s}} = 291.2 \text{ N} \cdot \text{m}$ The induced countertorque is given by $P_{conv} = \tau_{ind}\omega_m$ so $\tau_{ind} = \frac{P_{conv}}{\omega_V} = \frac{34.1 \text{ kW}}{125.7 \text{ rad/s}} = 271.3 \text{ N} \cdot \text{m}$	
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Example 4-3

(e) The voltage regulation of a generator is defined as

$$VR = \frac{V_{nl} - V_{fl}}{V_{fl}} \times 100\%$$
 (3-67)

By this definition, the voltage regulation for the lagging, unity, and leading power-factor cases are

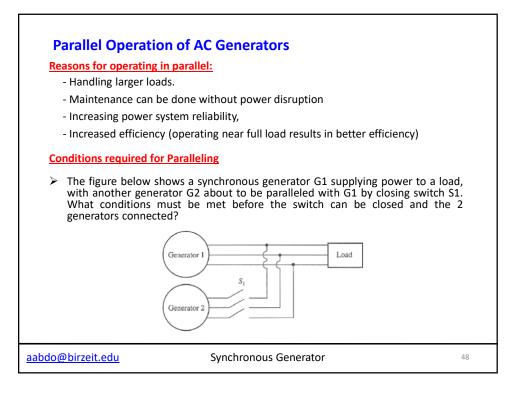
- 1. Lagging case: VR = $\frac{480 \text{ V} 410 \text{ V}}{410 \text{ V}} \times 100\% = 17.1\%$
- 2. Unity case: VR = $\frac{480 \text{ V} 468 \text{ V}}{468 \text{ V}} \times 100\% = 2.6\%$
- 3. Leading case: VR = $\frac{480 \text{ V} 535 \text{ V}}{535 \text{ V}} \times 100\% = -10.3\%$

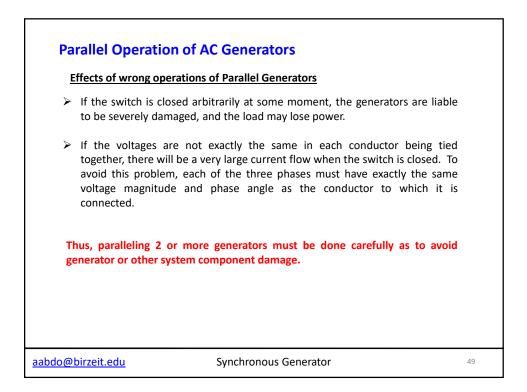
In Example 4–3, lagging loads resulted in a drop in terminal voltage, unitypower-factor loads caused little effect on V_{7} , and leading loads resulted in an increase in terminal voltage.

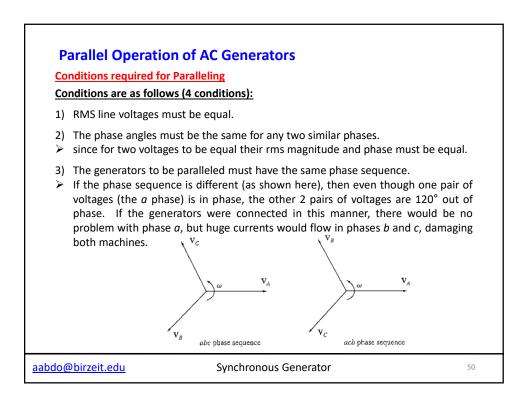
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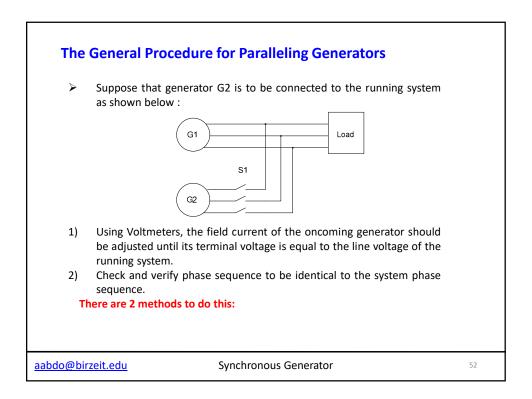
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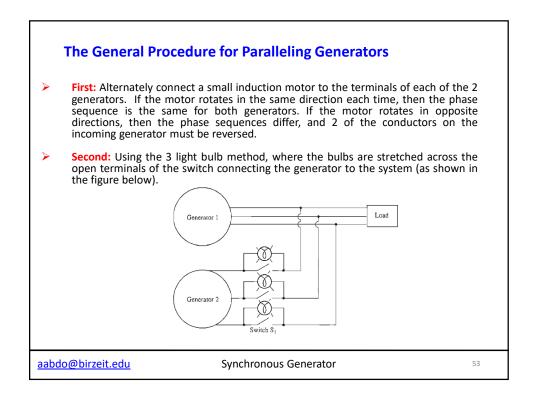


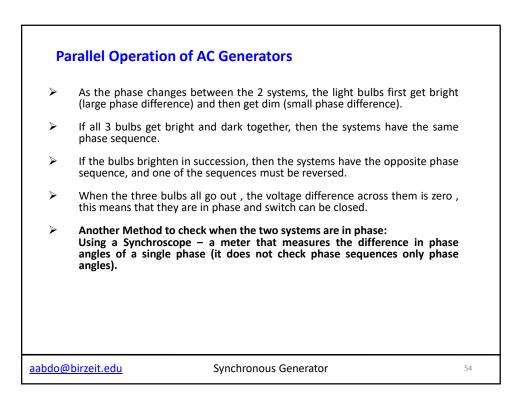




Par	allel Operation of AC Generators	
<u>Co</u>	nditions are as follows (4 conditions):	
4)	The oncoming generator (the new generator) must have a slightly higher operating frequency as compared to the system frequency.	
>	This is done so that the phase angles of the incoming machine will change slowly with respect to the phase angles of the running system.	
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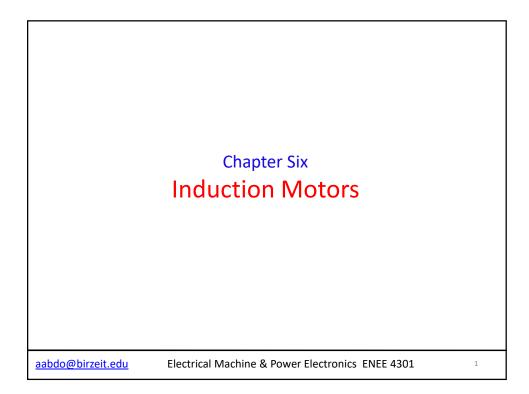


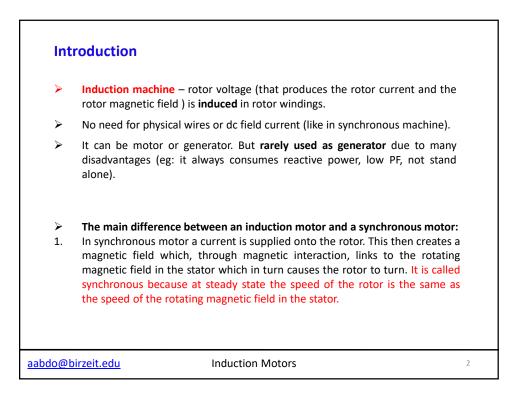


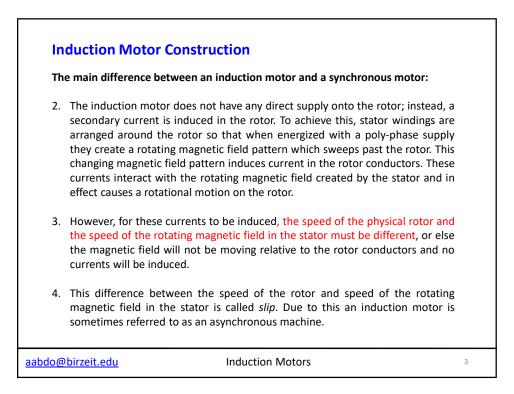


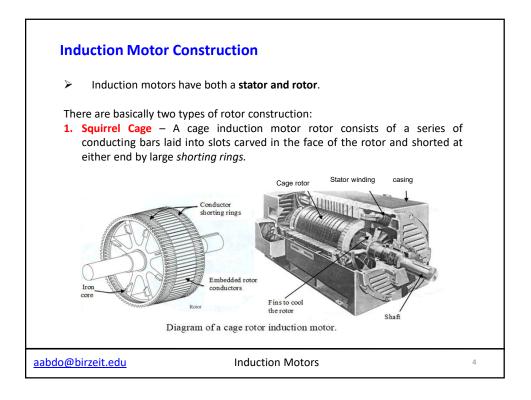
Parallel Operation of AC Generators 3) Check and verify generator frequency to be slightly higher than the system frequency. This is done by watching a frequency meter until the frequencies are close and then by observing changes in phase between the systems. 4) Once the frequencies are nearly equal, the voltages in the 2 systems will change phase with respect to each other very slowly. The phase changes are observed, and when the phase angles are equal, the switch connecting the 2 systems is shut. > In Large generators belonging to power systems, this whole process of paralleling is automated and a computer does this job. > For smaller generators an operator goes through the paralleling process described. aabdo@birzeit.edu Synchronous Generator 55

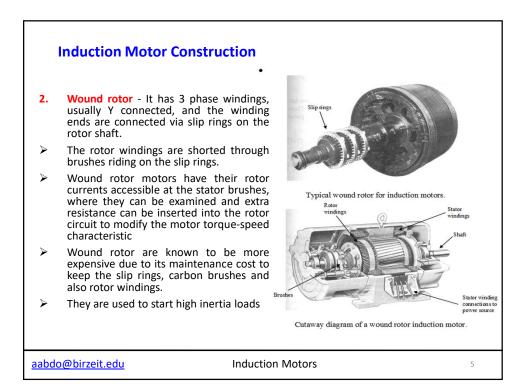
-	n of AC Generators	
Suggested question	ns to be solved:	
4.2(a,b,c,d,e,f), 4.	7, 4.27	
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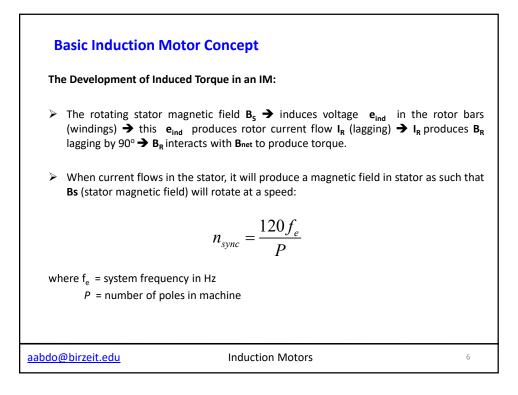


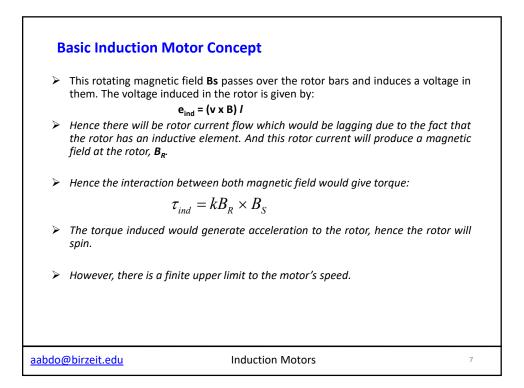


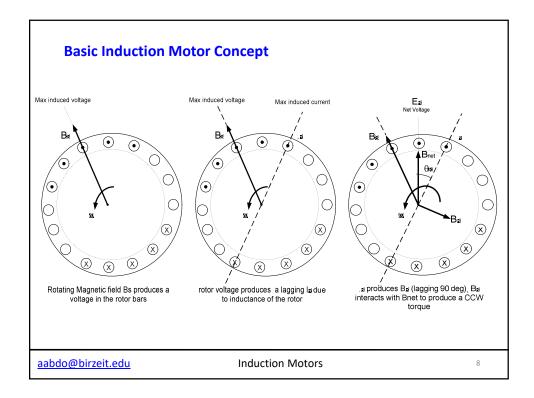


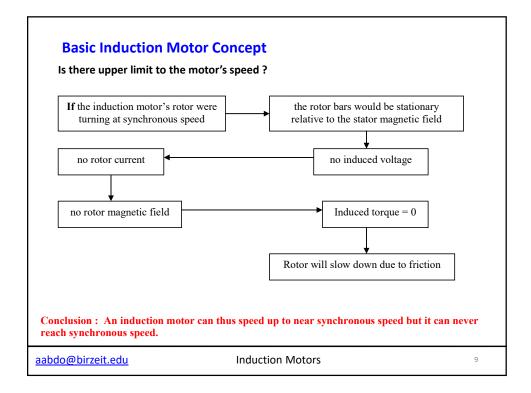


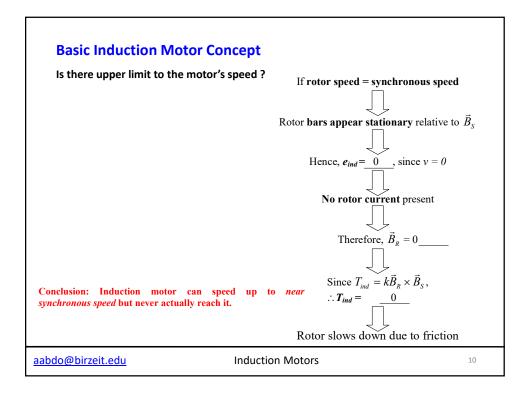


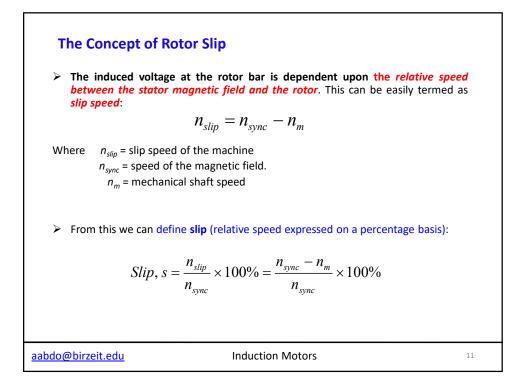




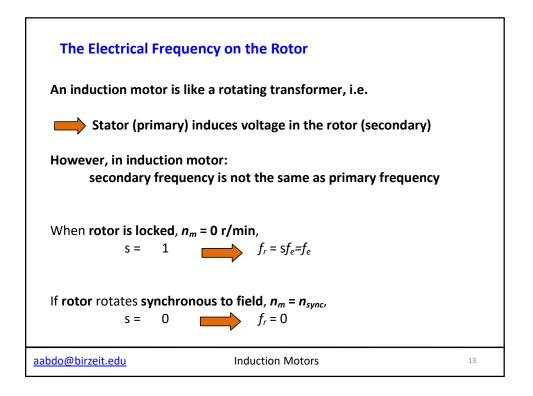




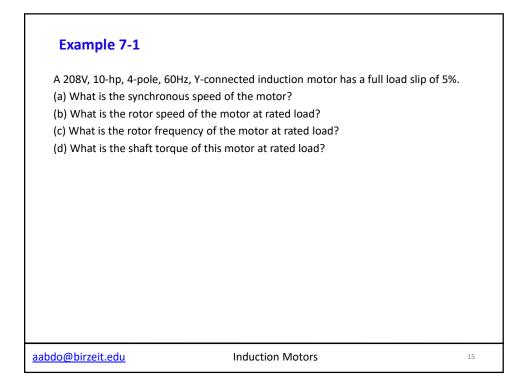


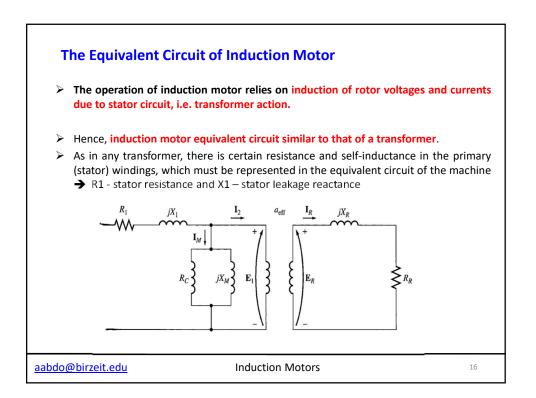


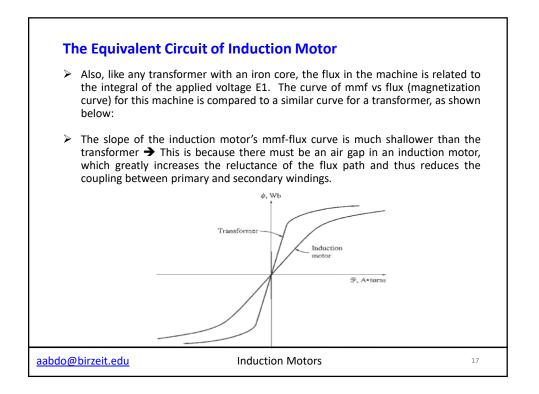
The Concept of Rotor Slip Slip may also be described in terms of angular velocity, ω . ≻ $s = \frac{\omega_{sync} - \omega_m}{\omega_{sync}} x100\%$ Using the ratio of slip, we may also determine the rotor speed: \geq $n_m = (1-s)n_{sync}$ or $\omega_m = (1-s)\omega_{sync}$ \triangleright Notice: rotor rotates at synchronous speed, s = 0 1. rotor is stationary, s = 1 2. 3. All normal motor speeds fall between s = 0 and s = 1 aabdo@birzeit.edu Induction Motors 12

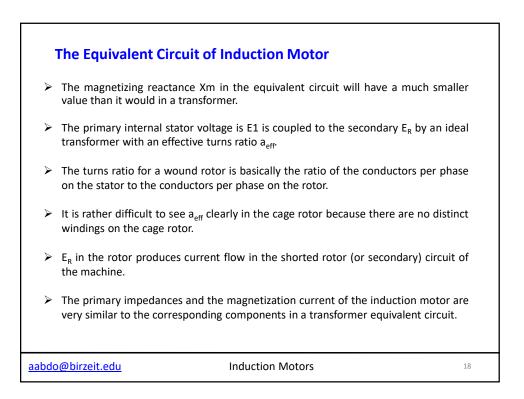


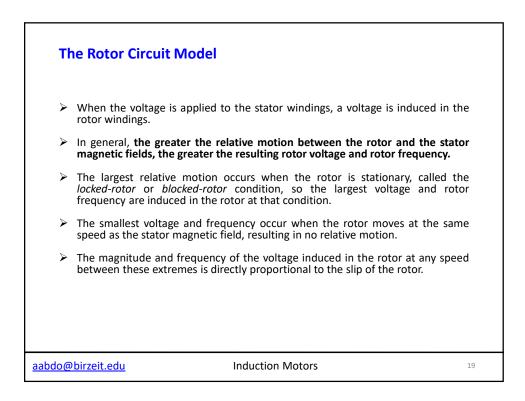
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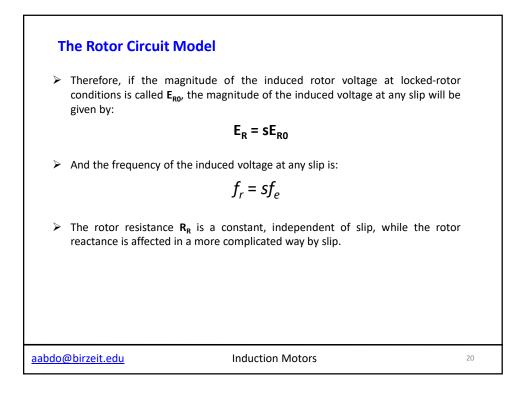


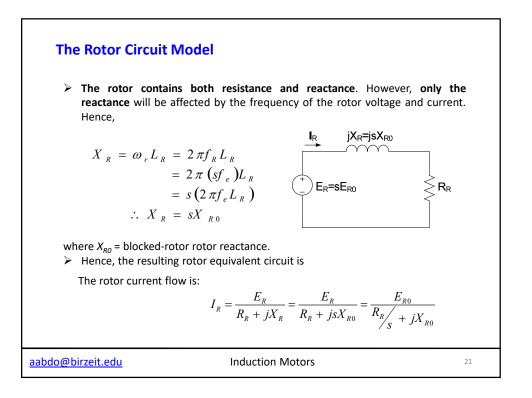


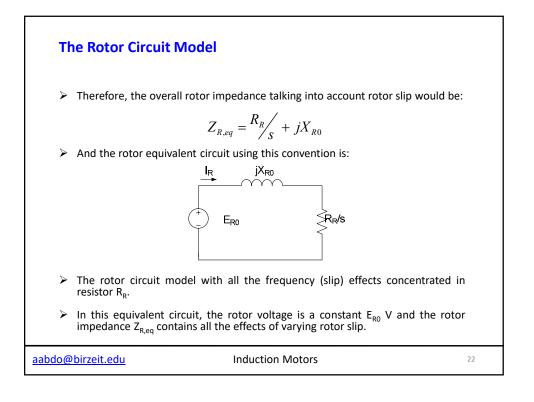


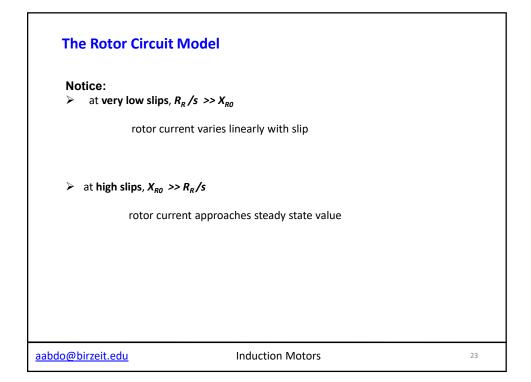


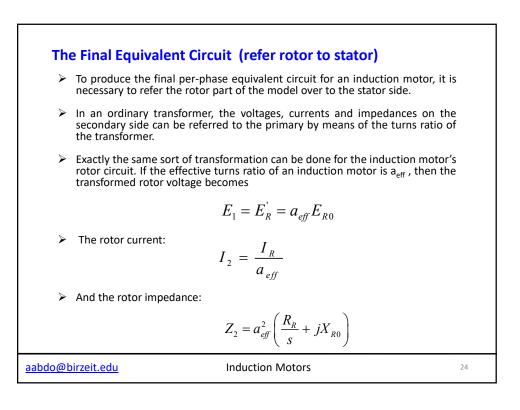


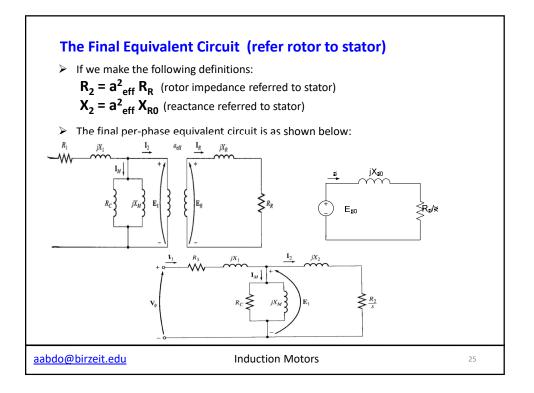




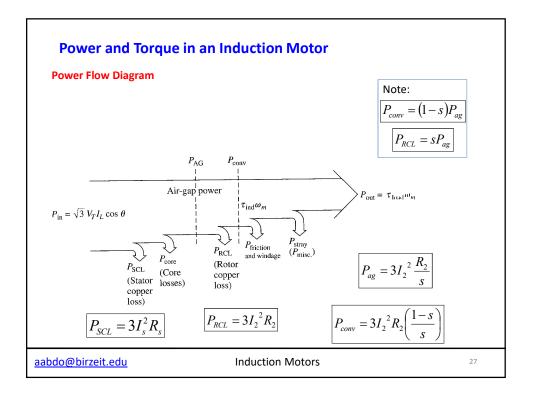






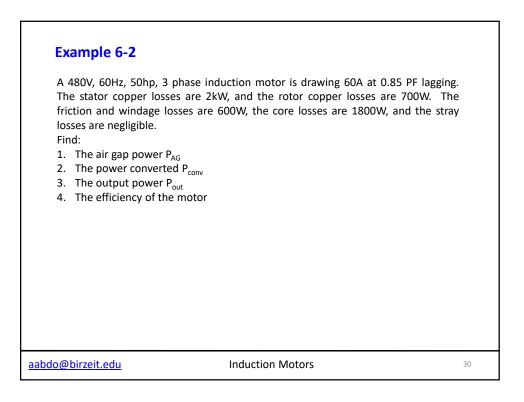


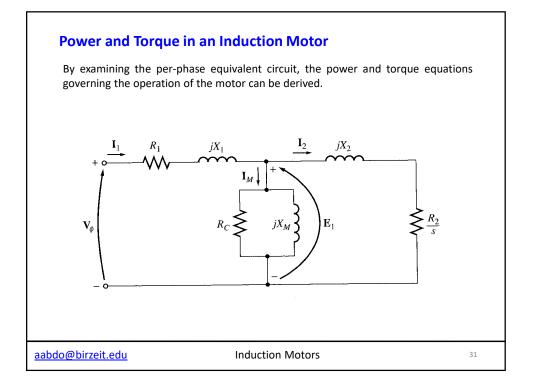
Power and Torque in an Induction Motor Losses and Power-Flow diagram > An induction motor can be basically described as a rotating transformer. Its input is a 3 phase system of voltages and currents. ≻ ≻ For an ordinary transformer, the output is electric power from the secondary windings. > The secondary windings in an induction motor (the rotor) are shorted out, so no electrical output exists from normal induction motors. Instead, the output is mechanical. ≻ The relationship between the input electric power and the output mechanical power of this motor is shown below: aabdo@birzeit.edu Induction Motors 26

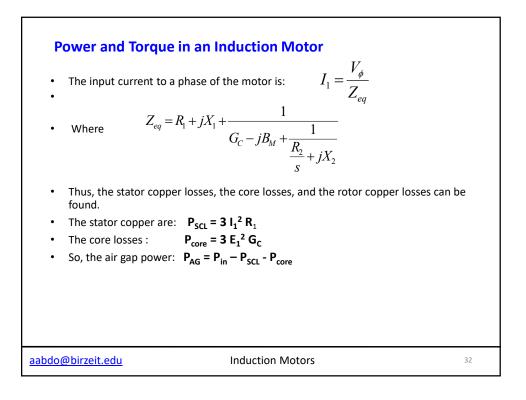


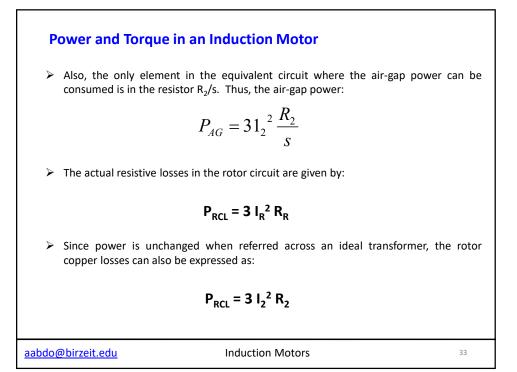
Power and Torque in an Induction Motor	
The input power (electrical) of an induction motor:	
$P_{\rm in} = \sqrt{3} V_T I_L \cos \theta$	
Losses encountered on stator side:	
- Stator copper loss P _{sct} , i.e. I ² R loss in stator windings.	
- Hysteresis and eddy current losses P _{core}	
- Air gap power $P_{AG} \Rightarrow$ power transferred to the rotor across the air gap	
 Losses encountered on rotor side: Rotor copper loss P_{RCL}, i.e. I²R loss in rotor windings. 	
> What is left?	
Power converted from electrical to mechanical form, P _{conv} .	
 Final losses: Friction and windage losses, P_{F&W} Stray losses, P_{misc} 	
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Dower and Torque in an Induction Motor	
Power and Torque in an Induction Motor	
The output power (mechanical) of the induction motor:	
$P_{out} = \tau_{load} w_m$	
Special note on P _{core} :	
> The core losses do not always appear after P_{SCL} .	
P _{core} comes partially from the stator circuit and partially from the rotor circuit. Usually the rotor core losses are very small compared to the stator core losses.	
> P_{core} are represented in the induction motor equivalent circuit by the resistor R_c (or the conductance G_c).	
If R _c is not given but P _{core} = X watts is given, then often add it together with P _{F&W} at the end of the power flow diagram.	
Note: P _{core} , P _{F&W} and P _{misc} are sometimes lumped together and called rotational losses P _{rot} .	
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Power and Torque in an Induction Motor

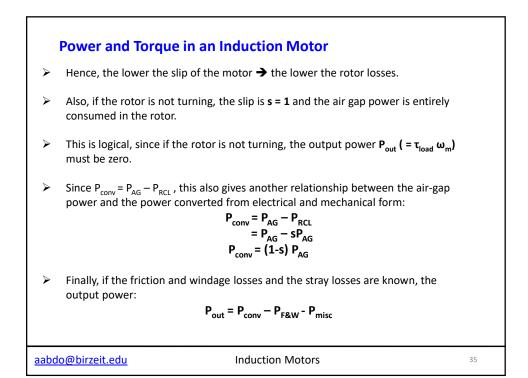
After stator copper losses, core losses and rotor copper losses are subtracted from the input power to the motor, the remaining power is converted from electrical to mechanical form. The power converted, which is called developed mechanical power is given as:

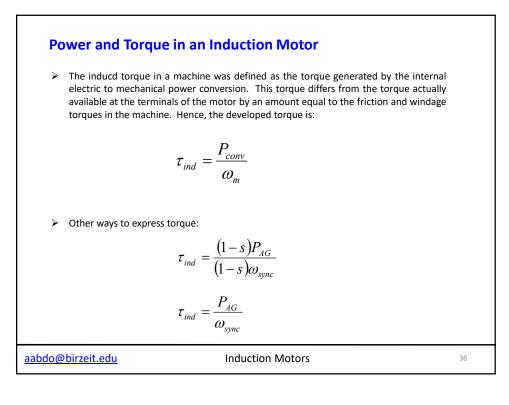
$$P_{conv} = P_{AG} - P_{RCL}$$

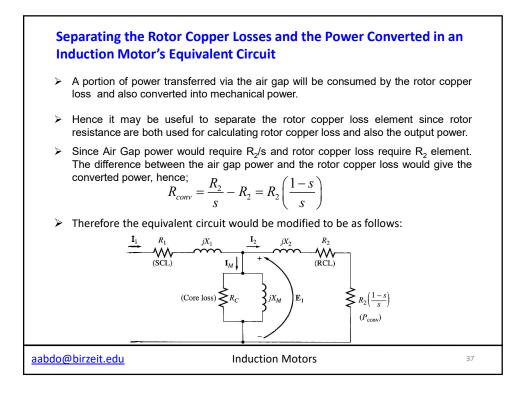
= $3I_2^2 \frac{R_2}{s} - 3I_2^2 R_2$
= $3I_2^2 R_2 \left(\frac{1}{s} - 1\right)$
 $P_{conv} = 3I_2^2 R_2 \left(\frac{1-s}{s}\right)$

 $\succ\,$ And the rotor copper losses are noticed to be equal to the air gap power times the slip $\rightarrow\,$ P_{RCL} = S P_{AG}

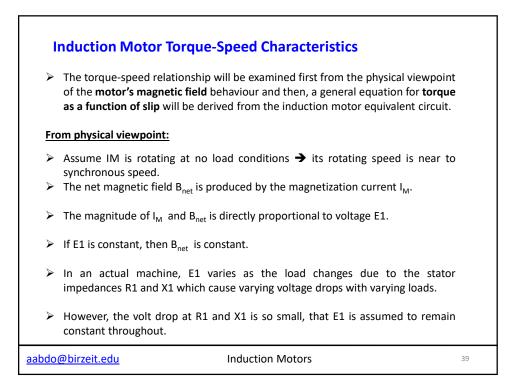
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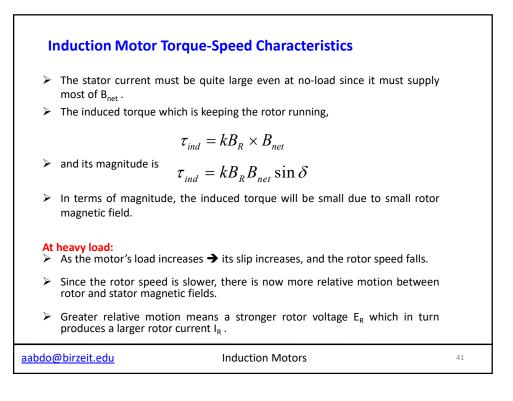


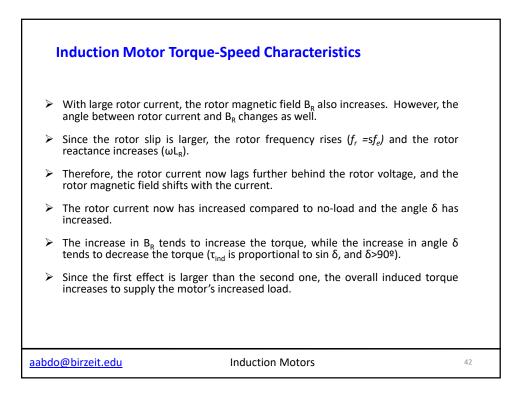


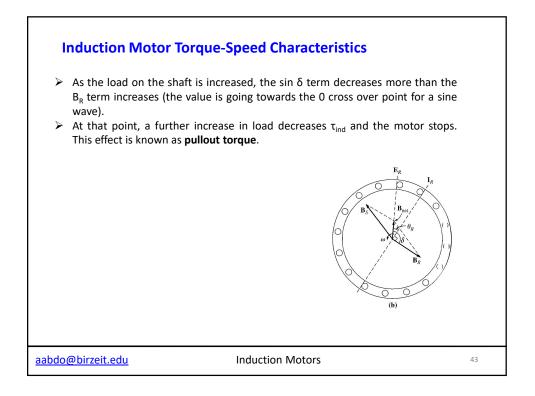
Example 6-3		
	4 pole, Y-connected induct per phase referred to the state	tion motor has the following or circuit:
R1 = 0.641 Ω	R2 = 0.332 Ω	
X1 = 1.106 Ω	X2 = 0.464 Ω	Xm = 26.3 Ω
loss is lumped in with		med to be constant. The core rotor slip of 2.2% at the rated
(a) speed		
(b) stator current		
(c) power factor		
(d) Pconv and Pout		
(e) tind and tload		
(d) efficiency		
See	the solution form the	text book
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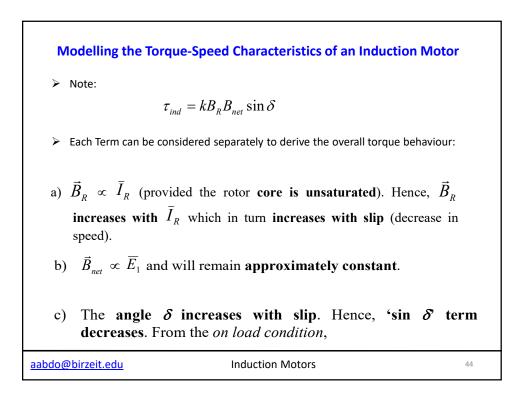


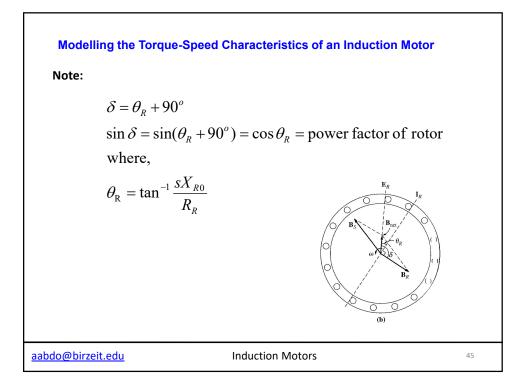
In	duction Motor Torque-Speed Characteristics	
>	At no-load, slip is very small, and so the relative motion between rotor and magnetic field is very small, and f_r is also very small.	
۶	Since the relative motion is small, ${\bf E_R}$ induced in the bars of the rotor is very small, and ${\bf I_R}$ is also very small.	
۶	Since f_r is small, the reactance of the rotor is nearly zero, and the max rotor current I_R is almost in phase with the rotor voltage E_R .	
~	The rotor current produces a small magnetic field B_R at an angle slightly greater than 90 degrees behind B_{net} .	
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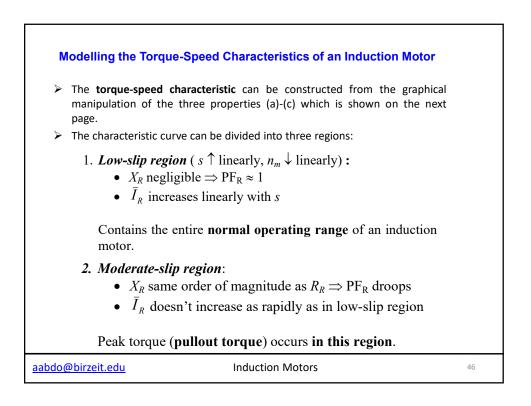


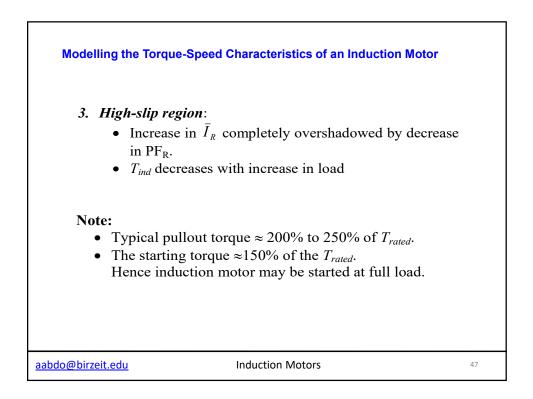


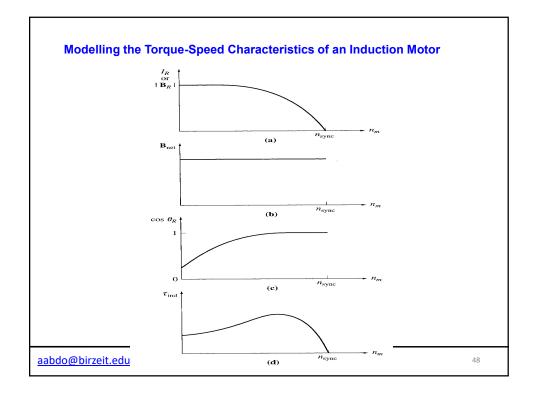


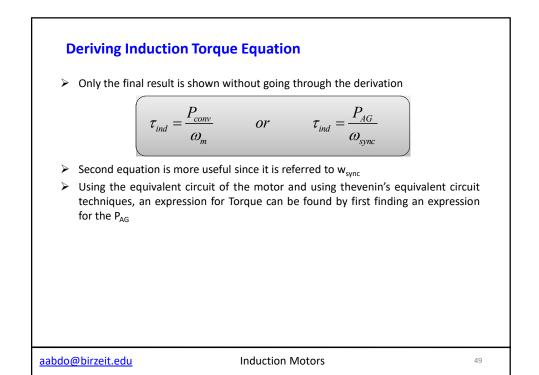


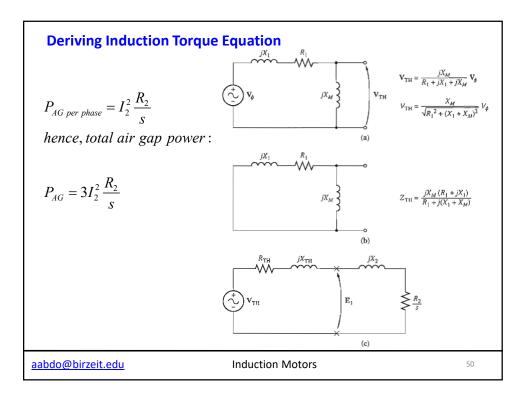












Deriving Induction Torque Equation

1. Derive the thevenin voltage (potential divider rule):

$$V_{TH} = V_{\phi} \frac{jX_m}{R_1 + jX_1 + jX_m}$$

> Hence the magnitude of thevenin voltage:

$$V_{TH} = V_{\phi} \frac{X_{m}}{\sqrt{R_{1}^{2} + (X_{1} + X_{m})^{2}}}$$

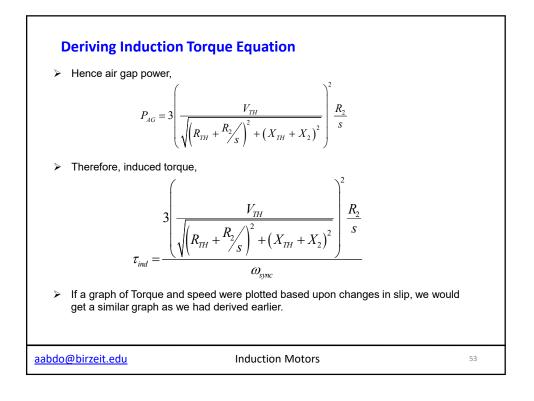
Since X_m >> X₁, X_m >> R₁, therefore the magnitude may be approximated to:

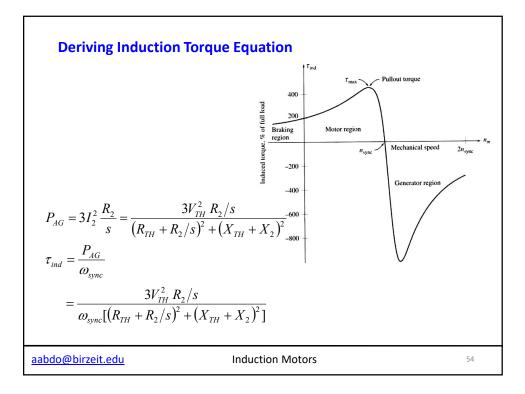
$$V_{TH} \approx V_{\phi} \frac{X_m}{X_1 + X_m}$$

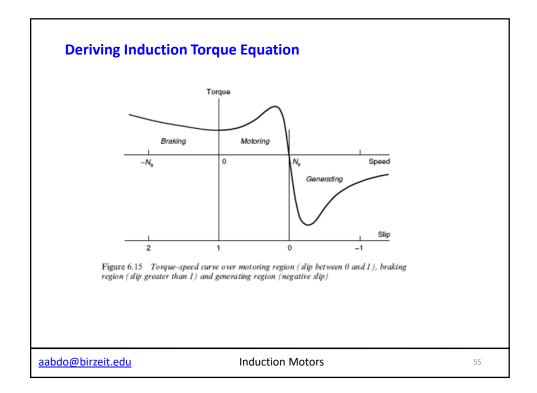
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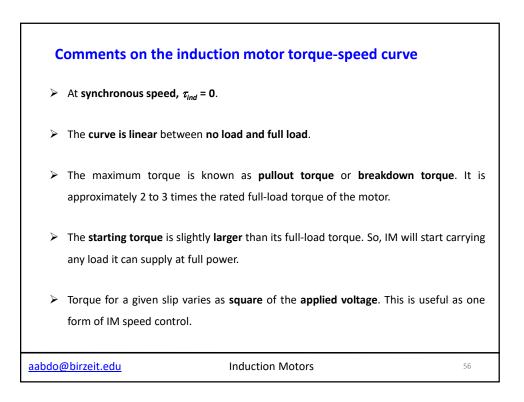
Induction Motors

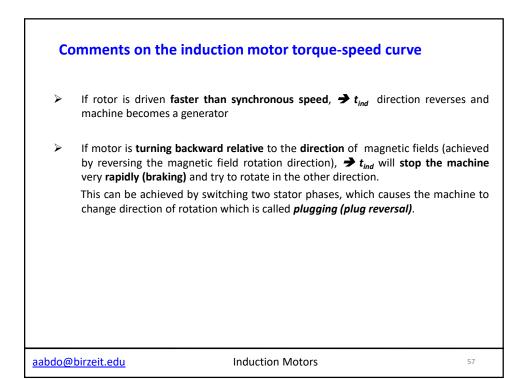
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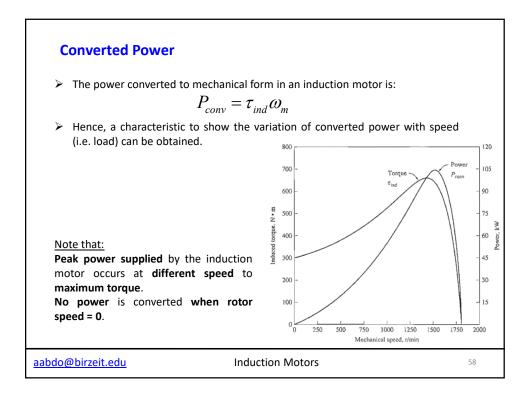














- Since induced torque is equal to P_{AG} / ω_{sync} , the maximum pullout torque may be found by finding the maximum air gap power. And maximum air gap power is during which the power consumed by the R_2/s resistor is the highest.
- Based upon the maximum power transfer theorem, maximum power transfer will be achieved when the magnitude of source impedance matches the load impedance. Since the source impedance is as follows:

$$Z_{source} = R_{TH} + jX_{TH} + jX_2$$

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Maximum (Pullout) Torque in an Induction Motor

Hence maximum power transfer occurs during:

$$\frac{R_2}{s} = \sqrt{R_{TH}^2 + (X_{TH} + X_2)^2}$$

Hence max power transfer is possible when slip is as follows:

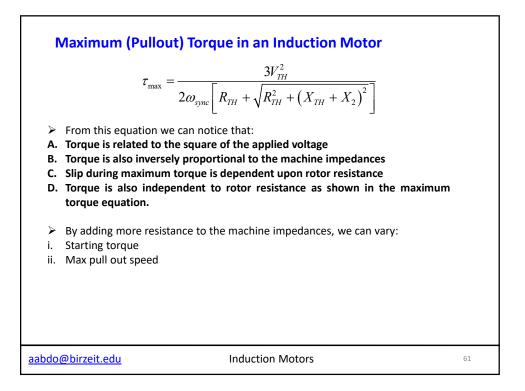
$$s_{\max} = \frac{R_2}{\sqrt{R_{TH}^2 + (X_{TH} + X_2)^2}}$$

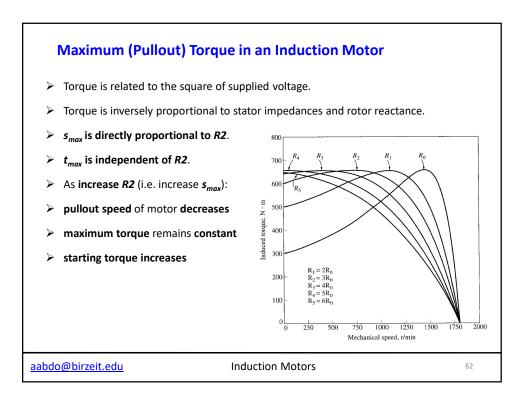
Put in the value of S_{max} into the torque equation,

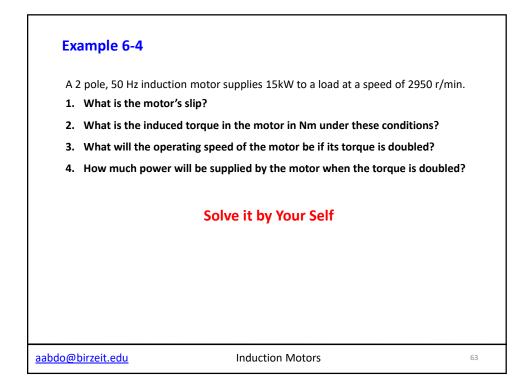
$$\tau_{\max} = \frac{3V_{TH}^2}{2\omega_{sync} \left[R_{TH} + \sqrt{R_{TH}^2 + (X_{TH} + X_2)^2} \right]}$$

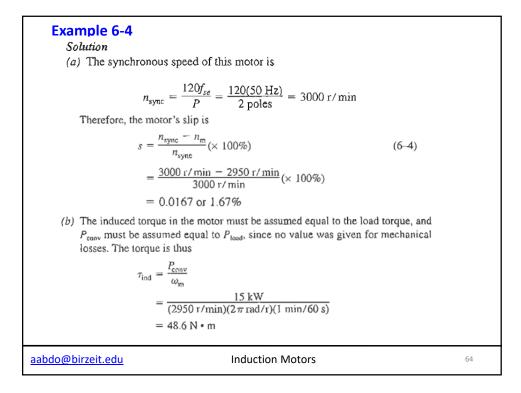
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Example 6-4

(c) In the low-slip region, the torque-speed curve is linear, and the induced torque is directly proportional to slip. Therefore, if the torque doubles, then the new slip will be 3.33 percent. The operating speed of the motor is thus

 $n_m = (1 - s)n_{\text{sync}} = (1 - 0.0333)(3000 \text{ r/min}) = 2900 \text{ r/min}$

(d) The power supplied by the motor is given by

$$P_{\rm conv} = \tau_{\rm ind} \omega_m$$

= $(97.2 \text{ N} \cdot \text{m})(2900 \text{ r/min})(2\pi \text{ rad/r})(1 \text{ min/60 s})$

= 29.5 kW

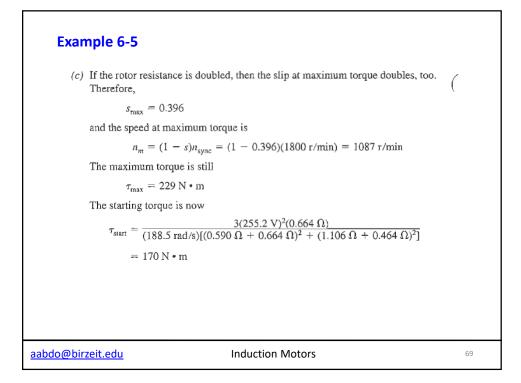
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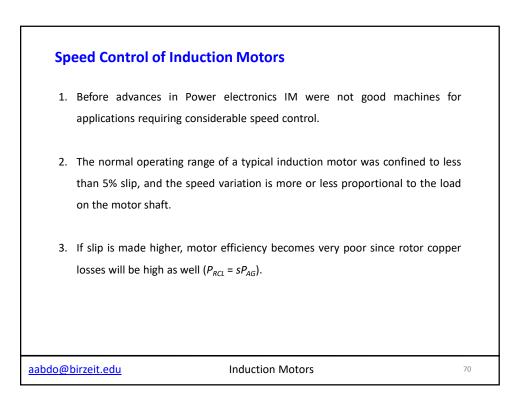
Induction Motors

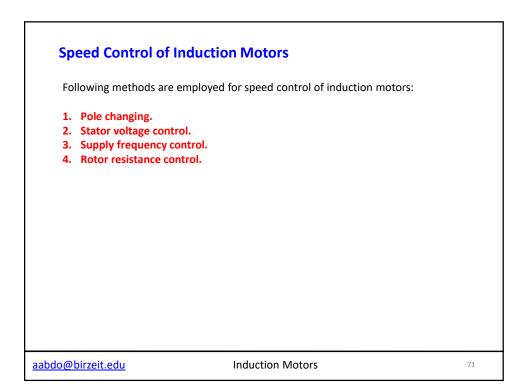
Example 6-5 A 460V, 25hp, 60Hz, 4-pole, Y-connected wound rotor induction motor has the following impedances in ohms per-phase referred to the stator circuit: R1 = 0.641 Ω R2 = 0.332 Ω Xm = 26.3 Ω $X1 = 1.106 \Omega$ X2 = 0.464 Ω 1. What is the max torque of this motor? At what speed and slip does it occur? 2. What is the starting torque? 3. When the rotor resistance is doubled, what is the speed at which the max torque now occurs? What is the new starting torque? Solve it by Your Self aabdo@birzeit.edu Induction Motors 66

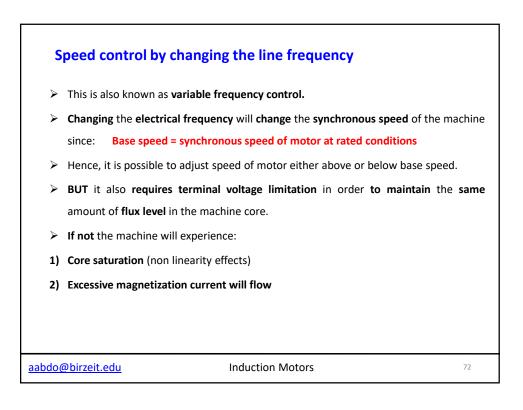
Example 6-5 Solution The Thevenin voltage of this motor is $V_{\rm TH} = V_{\phi} \frac{X_M}{\sqrt{R_1^2 + (X_1 + X_M)^2}}$ (6–41a) $=\frac{(266 \text{ V})(26.3 \Omega)}{\sqrt{(0.641 \Omega)^2 + (1.106 \Omega + 26.3 \Omega)^2}} = 255.2 \text{ V}$ The Thevenin resistance is $R_{\rm TH} \approx R_{\rm l} \left(\frac{X_M}{X_{\rm I} + X_M} \right)^2$ (6–44) $\approx (0.641 \ \Omega) \left(\frac{26.3 \ \Omega}{1.106 \ \Omega + 26.3 \ \Omega} \right)^2 = 0.590 \ \Omega$ The Thevenin reactance is $X_{\rm TH} \approx X_1 = 1.106 \,\Omega$ (a) The slip at which maximum torque occurs is given by Equation (6-53): $s_{\rm max} = \frac{R_2}{\sqrt{R_{\rm TH}^2 + (X_{\rm TH} + X_2)^2}}$ (6–53) $= \frac{0.332 \,\Omega}{\sqrt{(0.590 \,\Omega)^2 + (1.106 \,\Omega + 0.464 \,\Omega)^2}} = 0.198$ aabdo@birzeit.edu Induction Motors 67

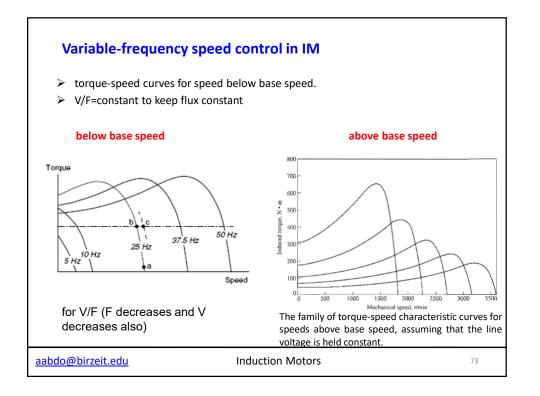
Example 6-	-5	
This corresp	ponds to a mechanical speed of	
n _m	$= (1 - s)n_{sync} = (1 - 0.198)(1800 r/min) = 1444 r/min$	
The torg	ue at this speed is	
$ au_{ m max} =$	$\frac{3V_{\rm TH}^2}{2\omega_{\rm sync}[R_{\rm TH} + \sqrt{R_{\rm TH}^2 + (X_{\rm TH} + X_2)^2}]} $ (6–54)	
=	3(255.2 V) ²	
	2(188.5 rad/s)[0.590 Ω + $\sqrt{(0.590 \Omega)^2 + (1.106 \Omega + 0.464 \Omega)^2}$]	
=	229 N • m	
(b) The star	ting torque of this motor is found by setting $s = 1$ in Equation (6–50)	
$ au_{ m start} =$	$\frac{3V_{\rm TH}^2 R_2}{\omega_{\rm sync}[(R_{\rm TH} + R_2)^2 + (X_{\rm TH} + X_2)^2]}$	
	$\frac{3(255.2 \text{ V})^2(0.332 \Omega)}{(188.5 \text{ rad/s})[(0.590 \Omega + 0.332 \Omega)^2 + (1.106 \Omega + 0.464 \Omega)^2]}$ 104 N • m	
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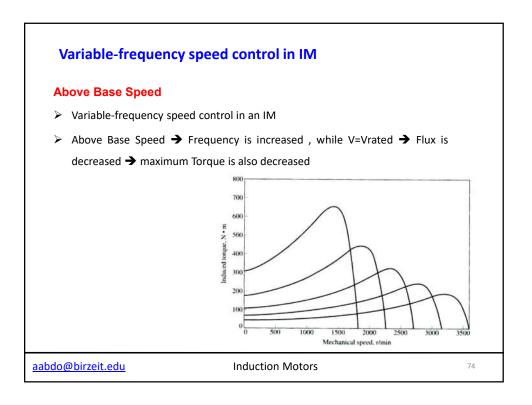


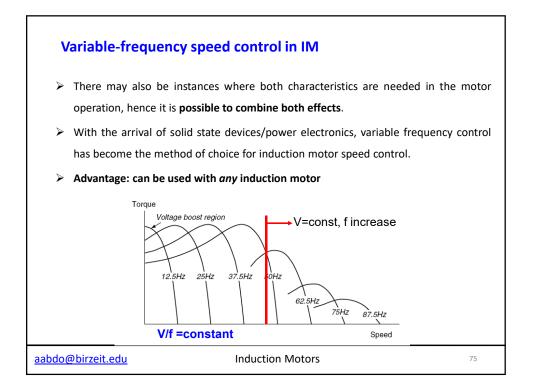


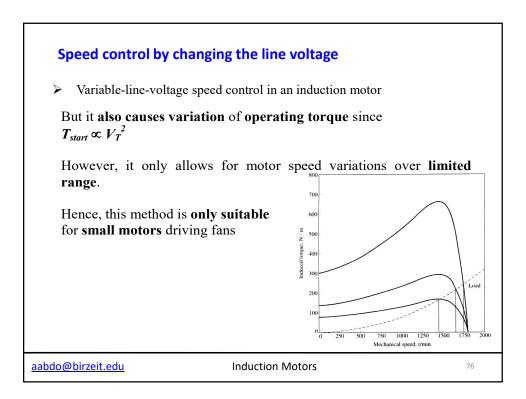


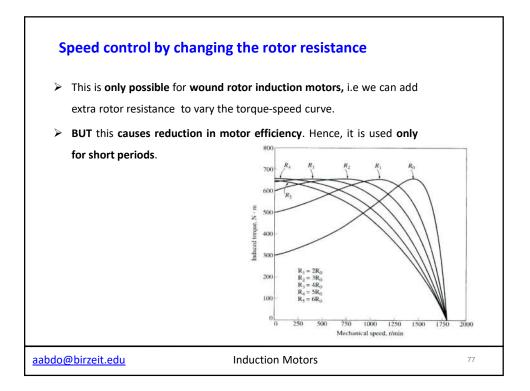


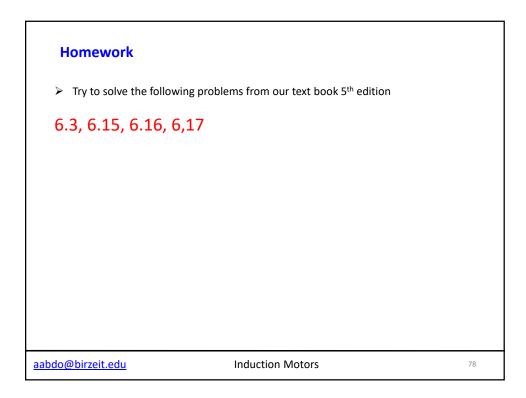


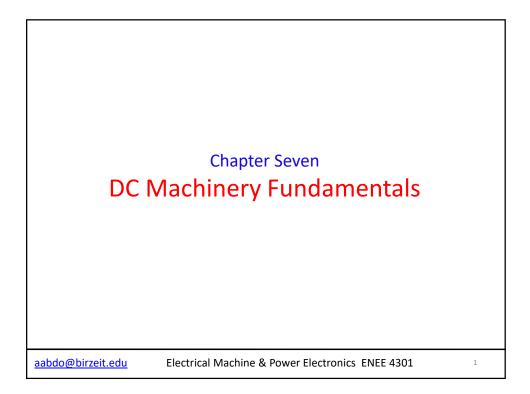


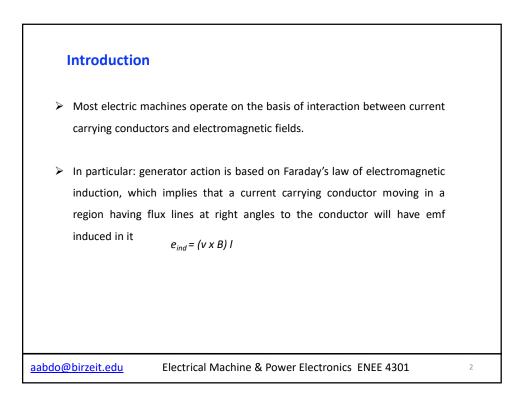


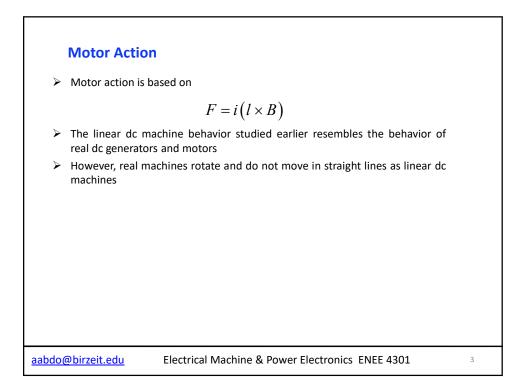


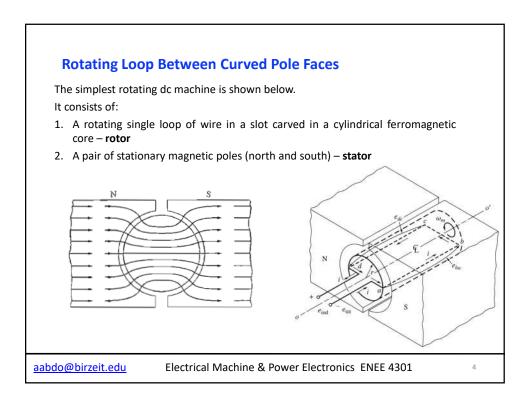


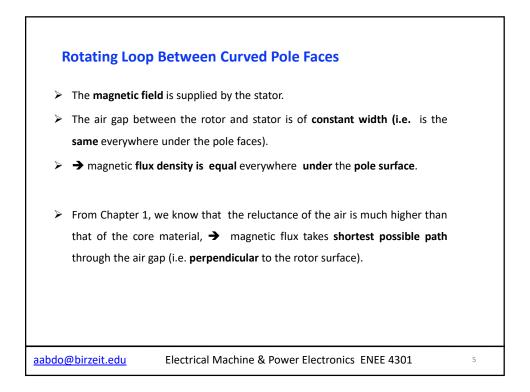


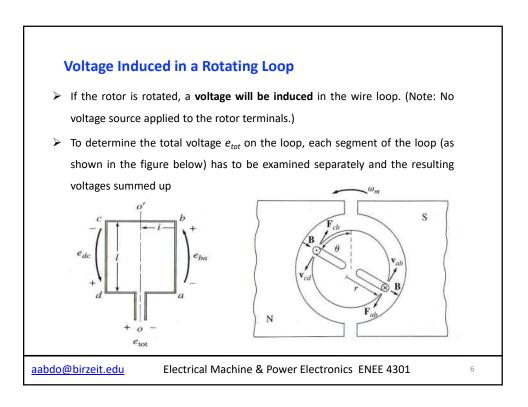


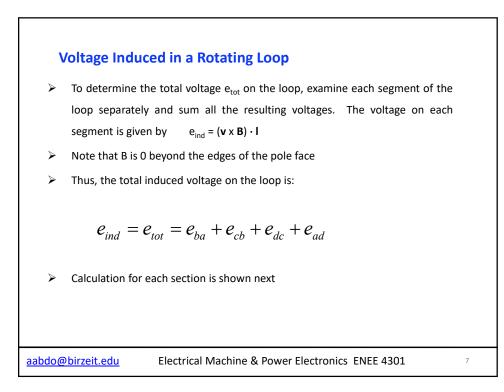


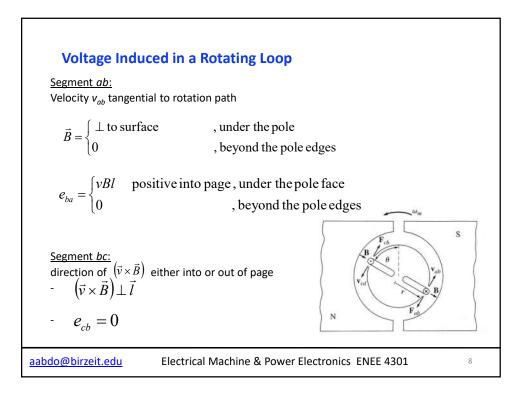


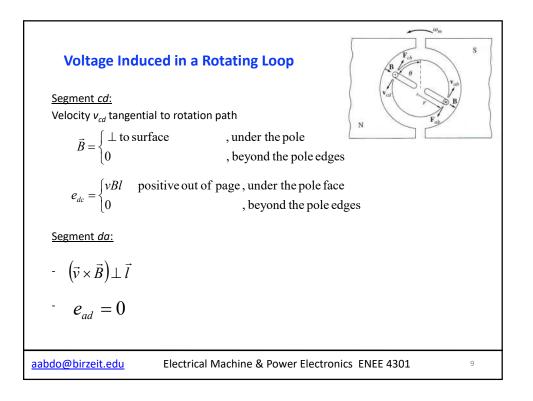


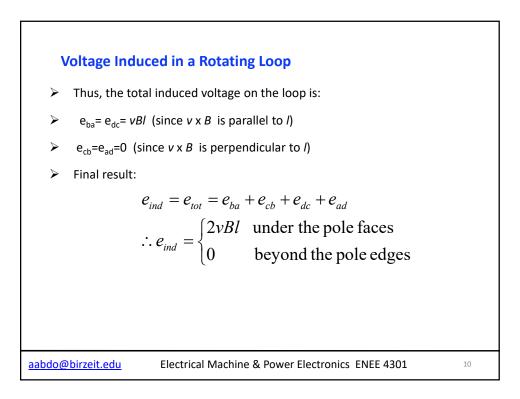


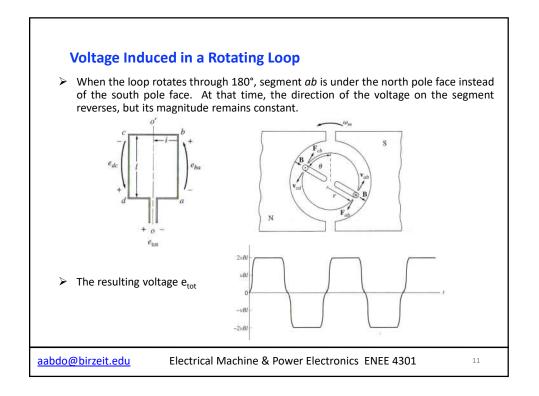


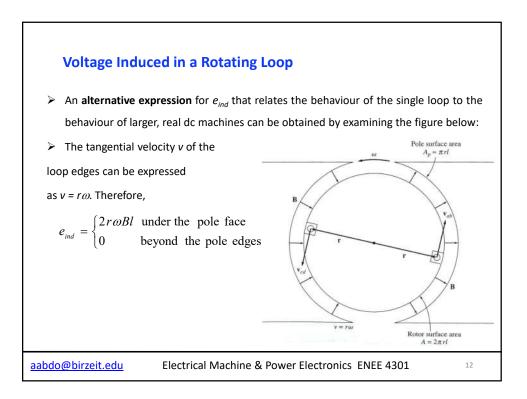












Voltage Induced in a Rotating Loop

For a 2-pole machine, if we assume that the gap between the poles is negligible (the gaps at the top and bottom of the diagram) then the surface area of the pole can be written as (area of cylinder /2) :

$$A_P = \frac{2\pi rl}{2} = \pi rl$$

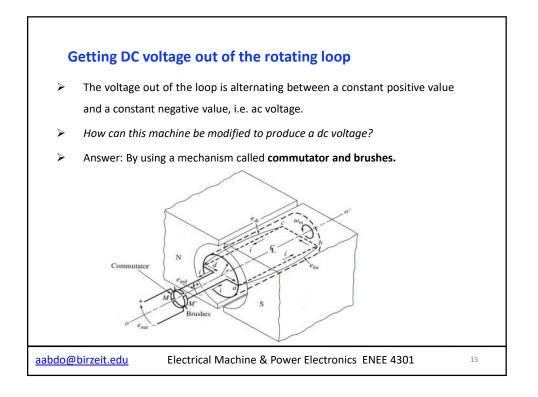
Therefore,

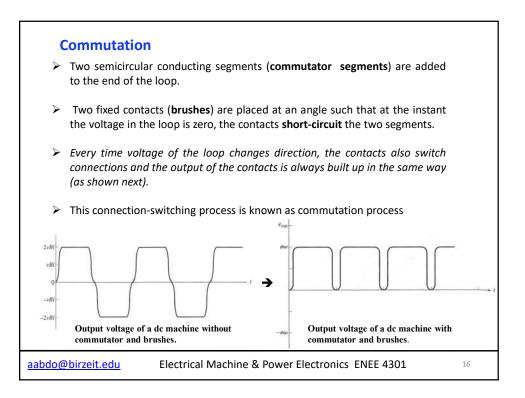
$$e_{ind} = \begin{cases} \frac{2}{\pi} A_p B \omega & \text{under the pole face} \\ 0 & \text{beyond the pole edges} \end{cases}$$

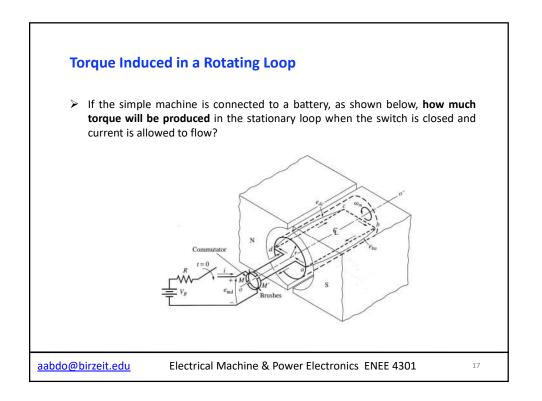
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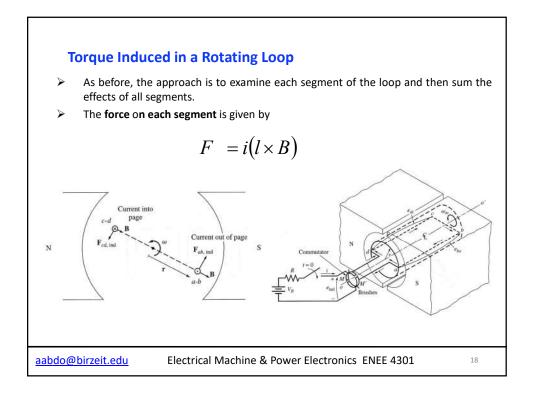
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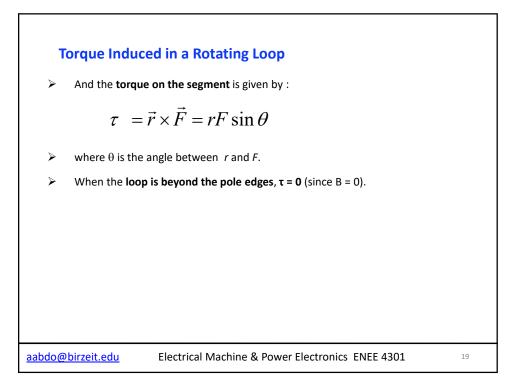
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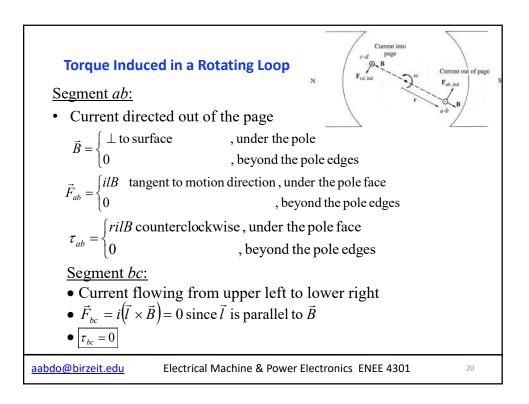


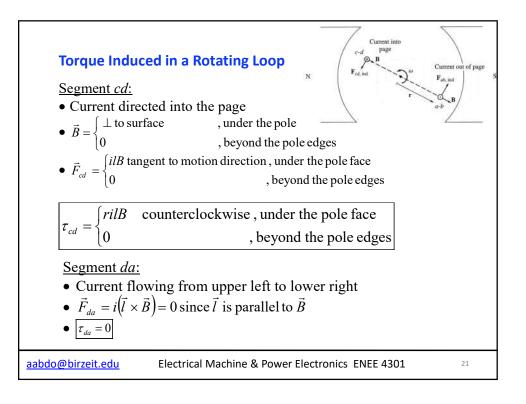


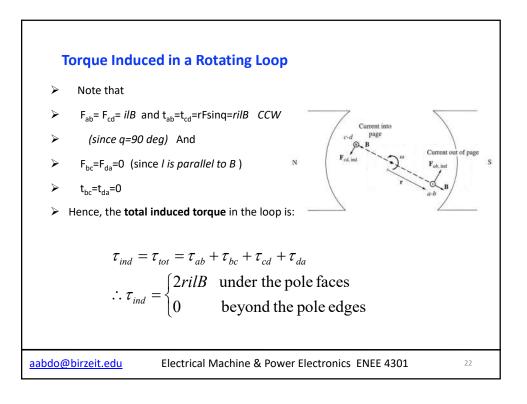


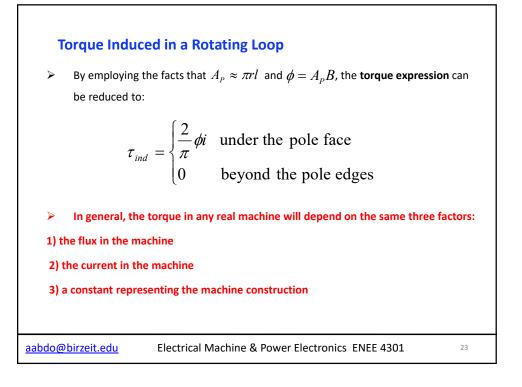




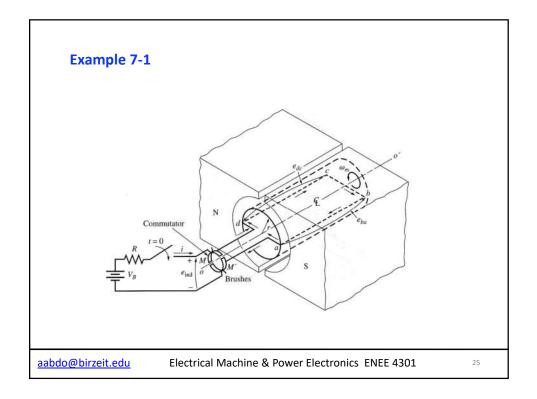








E	kample 7-1		
	A simple rotating loop between curved pole faces connected to a battery and a resistor through a switch. The physical dimensions and characteristics of the machine are:		
	r=0.5m; /=1m; R=0.3 ohm; B=0.25T; V _B =120V		
(a)	What happens when switch is closed?		
(b)	What is the machine's maximum starting current? What is the steady-state angular velocity at no load?		
(c)	Suppose load torque=10 N.m, what is the new steady-state speed? How much power is supplied to the shaft? How much power is being supplied by the battery? is the machine a motor or a generator?		
(d)	Suppose the machine is unloaded again, and a torque =7.5 N.m is applied to the shaft in the direction of motion. What is the new steady-state speed? Is the machine acting as a motor or generator?		
(a)	Suppose the machine is running unloaded, what would be the final steady- state speed of the rotor be if the flux density were reduced to 0.2 T?		
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Example 7-1

Solution

(a) When the switch in Figure 7-6 is closed, a current will flow in the loop. Since the loop is initially stationary, $e_{ind} = 0$. Therefore, the current will be given by

$$i = \frac{V_B - e_{\text{ind}}}{R} = \frac{V_B}{R}$$

This current flows through the rotor loop, producing a torque

$$\tau_{ind} = \frac{2}{\pi} \phi i$$
 CCW

This induced torque produces an angular acceleration in a counterclockwise direction, so the rotor of the machine begins to turn. But as the rotor begins to (turn, an induced voltage is produced in the motor, given by

$$e_{\rm ind} = \frac{2}{\pi} \phi \omega_m$$

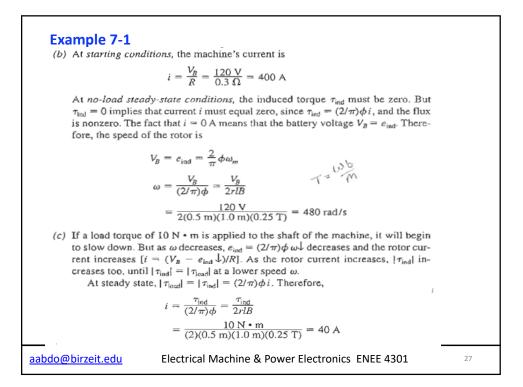
so the current *i* falls. As the current falls, $\tau_{ind} = (2/\pi)\phi i \downarrow$ decreases, and the machine winds up in steady state with $\tau_{ind} = 0$, and the battery voltage $V_B = e_{ind}$. This is the same sort of starting behavior seen earlier in the linear dc machine.

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Example 7-1 By Kirchhoff's voltage law, $e_{ind} = V_B - iR$, so $e_{ind} = 120 \text{ V} - (40 \text{ A})(0.3 \Omega) = 108 \text{ V}$ Finally, the speed of the shaft is $\omega = \frac{e_{\rm ind}}{(2/\pi)\phi} = \frac{e_{\rm ind}}{2rlB}$ $=\frac{108 \text{ V}}{(2)(0.5 \text{ m})(1.0 \text{ m})(0.25 \text{ T})} = 432 \text{ rad/s}$ The power supplied to the shaft is $P = \tau \omega_m$ $= (10 \text{ N} \cdot \text{m})(432 \text{ rad/s}) = 4320 \text{ W}$ The power out of the battery is $P = V_R i = (120 \text{ V})(40 \text{ A}) = 4800 \text{ W}$ This machine is operating as a motor, converting electric power to mechanical power. aabdo@birzeit.edu Electrical Machine & Power Electronics ENEE 4301 28

Example 7-1

(d) If a torque is applied in the direction of motion, the rotor accelerates. As the speed increases, the internal voltage e_{ind} increases and exceeds V_{θ} , so the current flows out of the top of the bar and into the battery. This machine is now a *generator*. This current causes an induced torque opposite to the direction of motion. The induced torque opposes the external applied torque, and eventually $|\tau_{load}| = |\tau_{ind}|$ at a higher speed ω_m .

The current in the rotor will be

$$i = \frac{\tau_{\text{ind}}}{(2/\pi)\phi} = \frac{\tau_{\text{ind}}}{2rlB}$$
$$= \frac{7.5 \text{ N} \cdot \text{m}}{(2)(0.5 \text{ m})(1.0 \text{ m})(0.25 \text{ T})} = 30 \text{ A}$$

The induced voltage eind is

$$e_{ind} = V_B + iR$$

= 120 V + (30 A)(0.3 Ω)
= 129 V

Finally, the speed of the shaft is

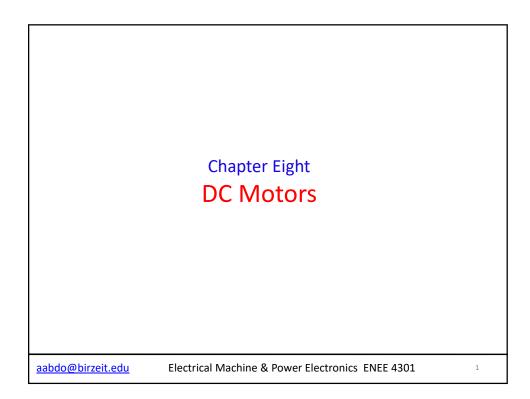
$$\omega = \frac{e_{\text{ind}}}{(2/\pi)\phi} = \frac{e_{\text{ind}}}{2rlB}$$
$$= \frac{129 \text{ V}}{(2)(0.5 \text{ m})(1.0 \text{ m})(0.25 \text{ T})} = 516 \text{ rad/s}$$

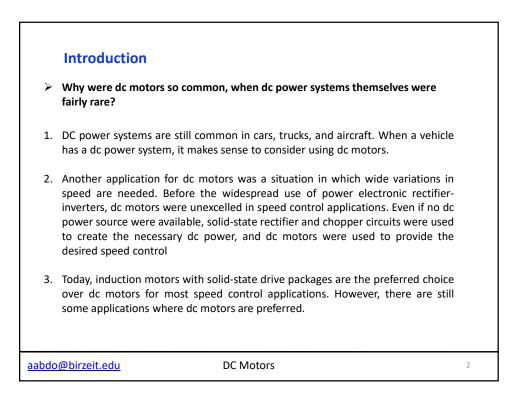
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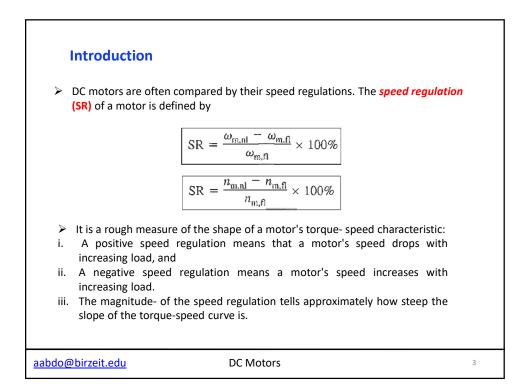
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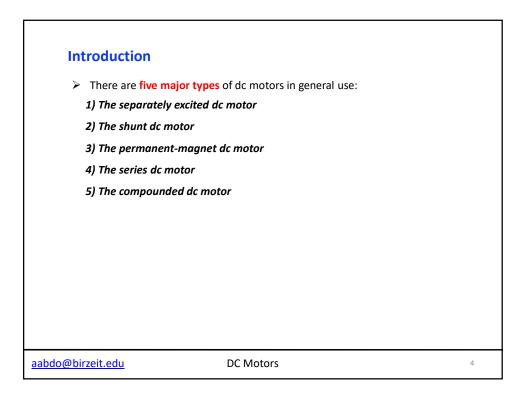
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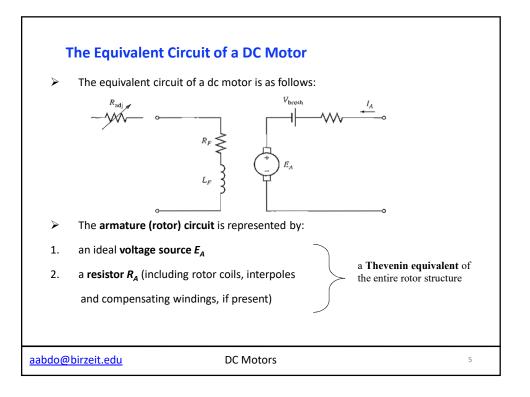
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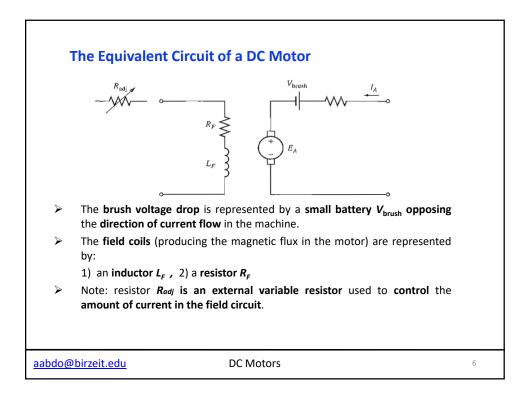


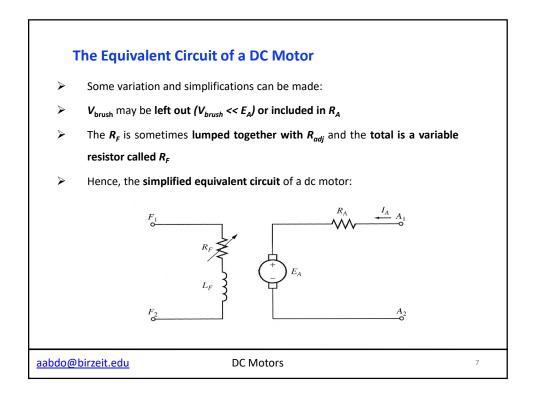


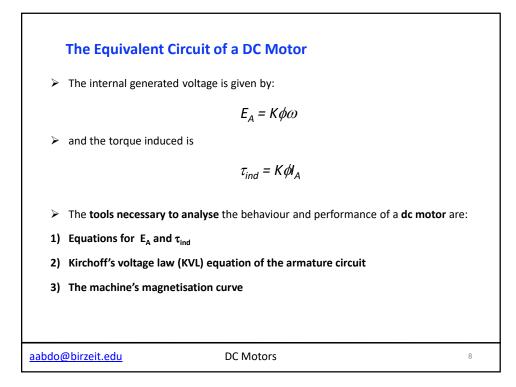


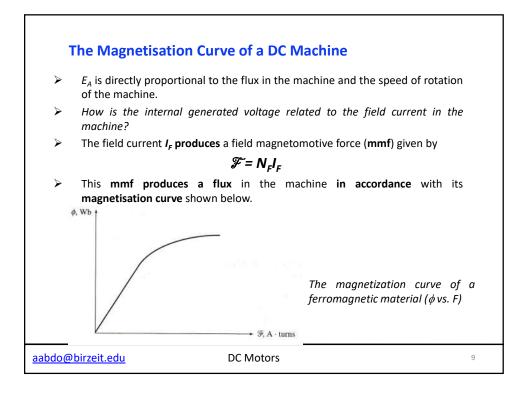


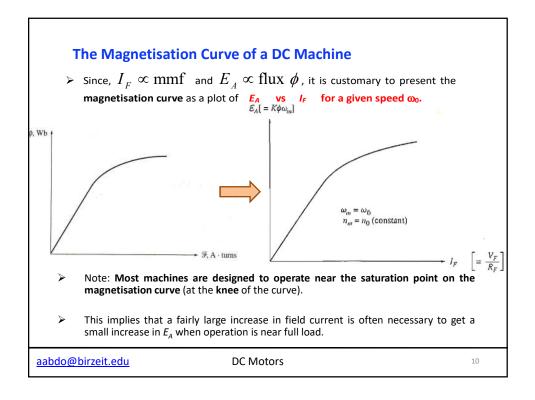


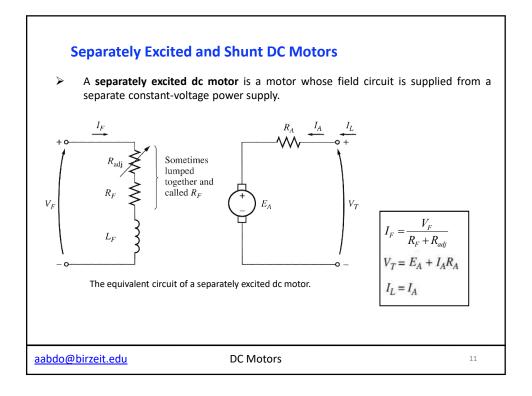


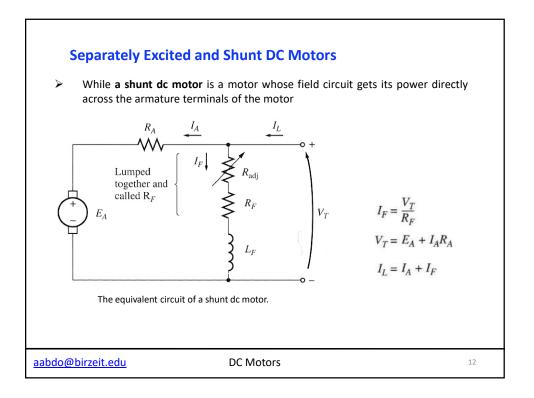


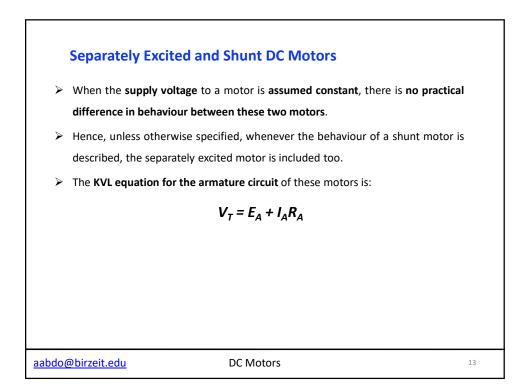


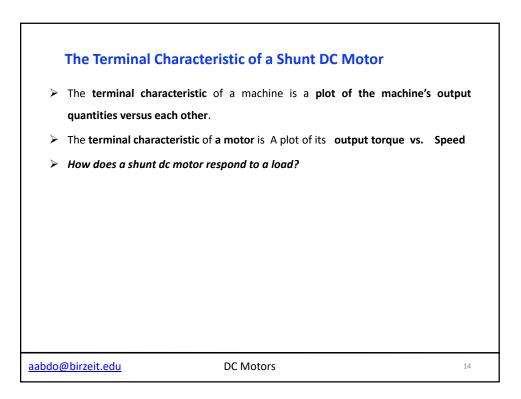


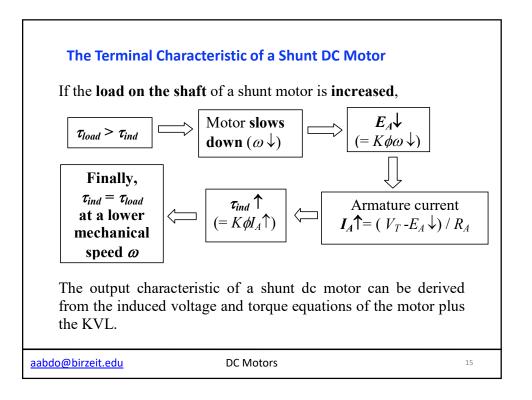




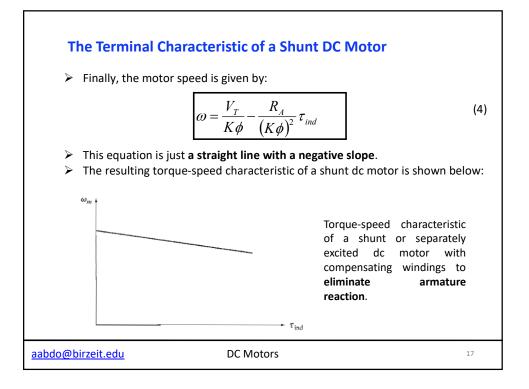


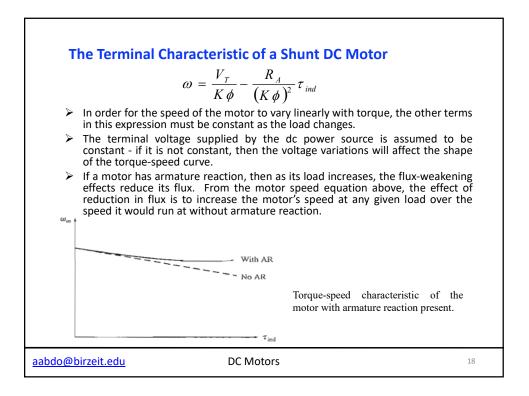


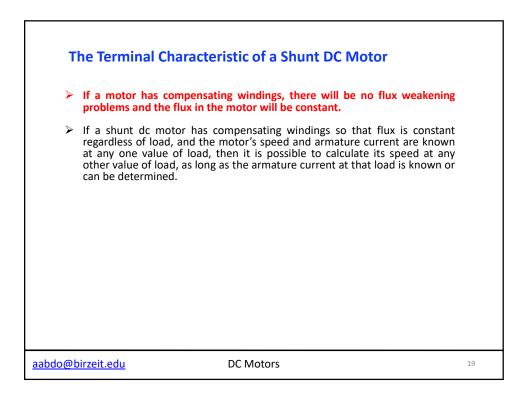


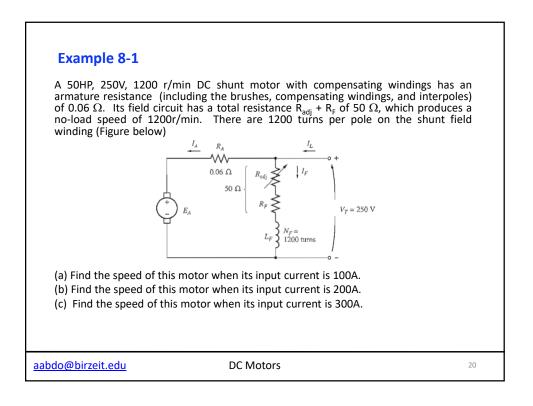


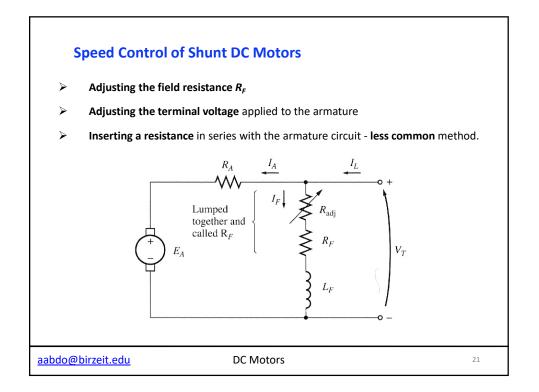
The Terminal Characteristic of a Shunt DC Motor	
From KVL, $V_T = E_A + I_A R_A$.	
The induced voltage $E_A = K \phi \omega$, so	
$V_{T} = K\phi\omega + I_{A}R_{A}$	(1)
Since $\tau_{ind} = K \phi I_A$, current I_A can be expressed as $I_A = \frac{\tau_{ind}}{K \phi}$	(2)
Combining equations (1) and (2) yields $V_T = K\phi\omega + \frac{\tau_{ind}}{K\phi}R_A$	(3)
aabdo@birzeit.edu DC Motors	16

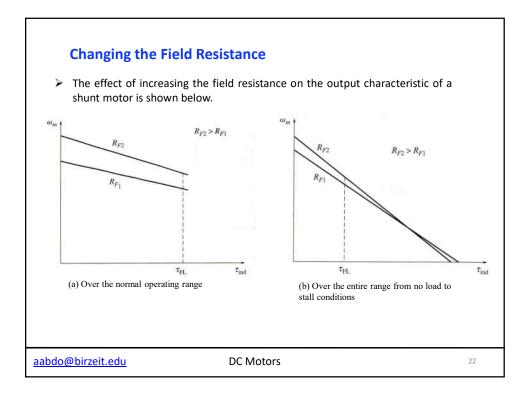


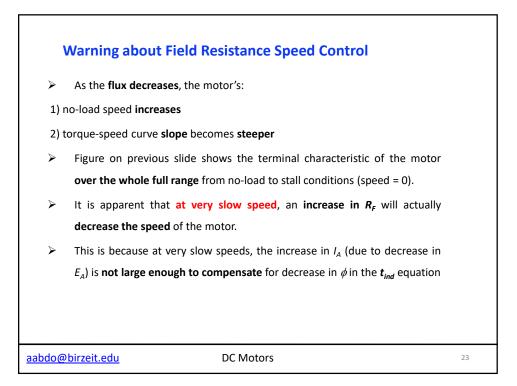


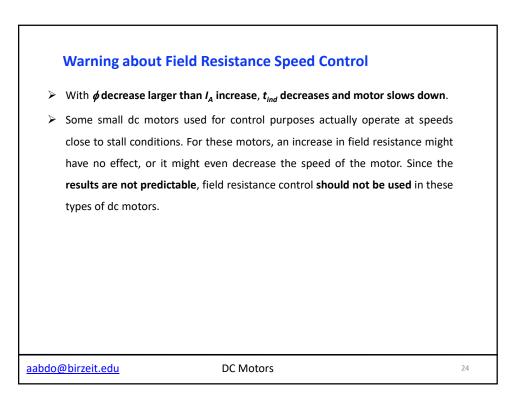


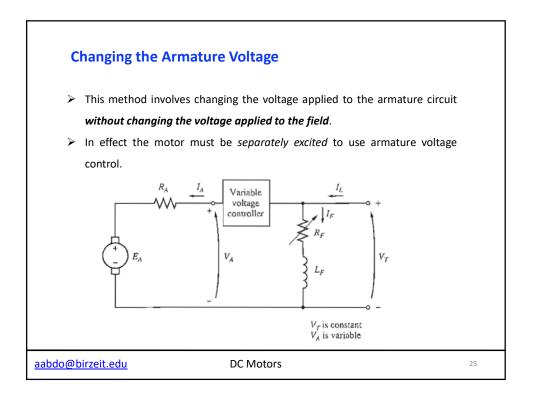


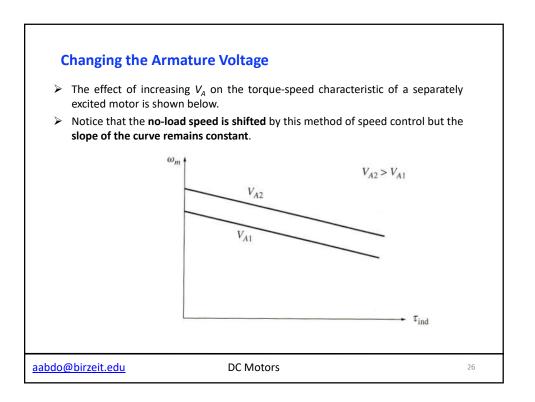


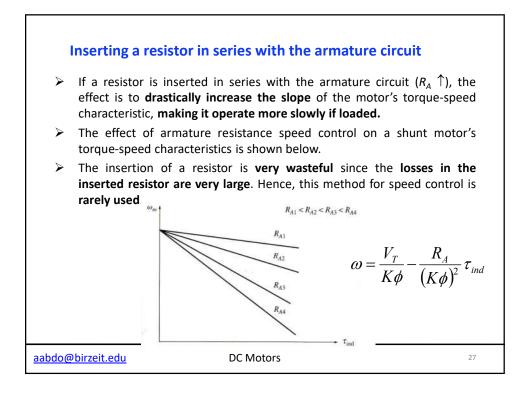


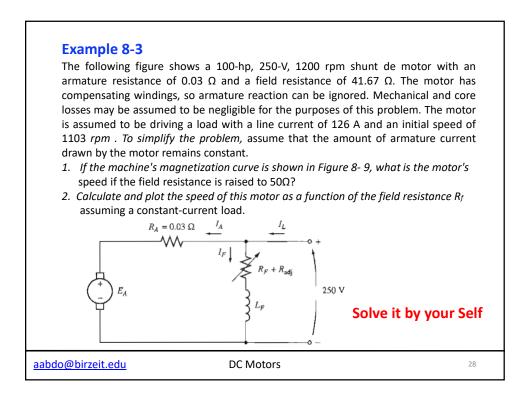


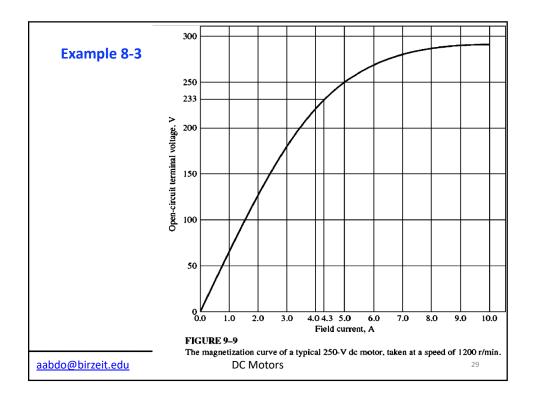


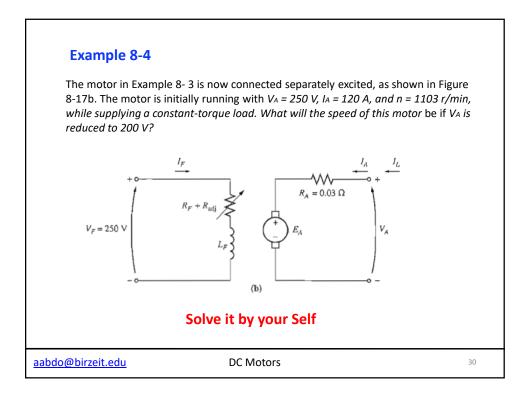


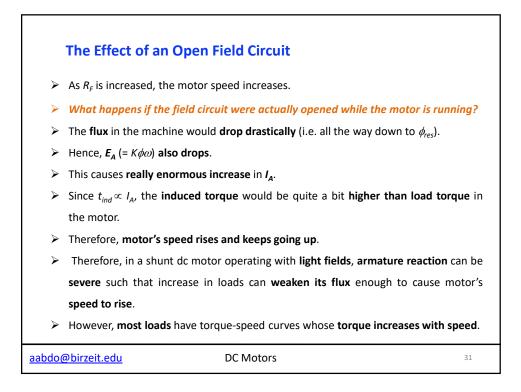


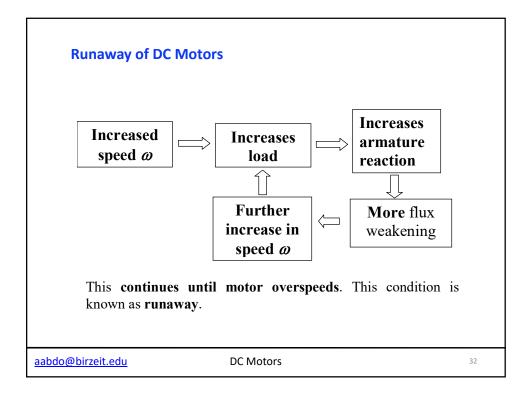


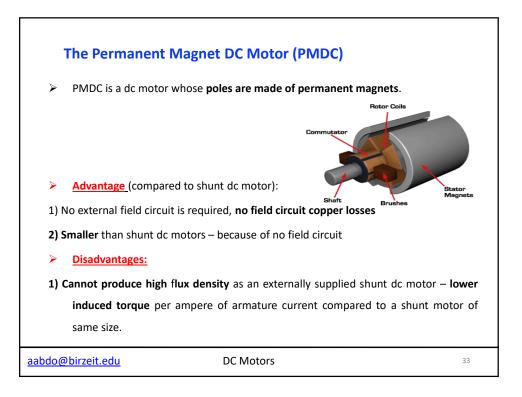




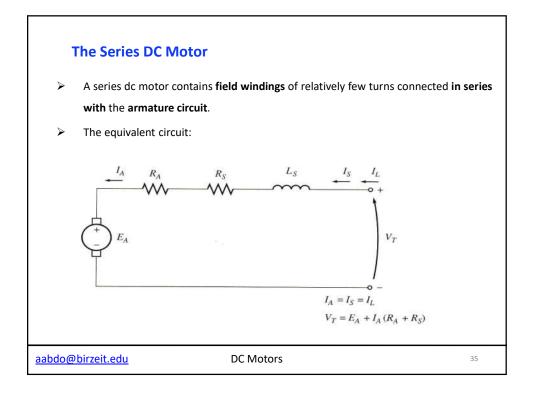


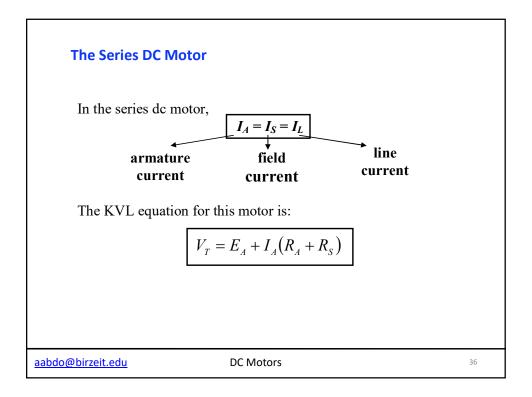


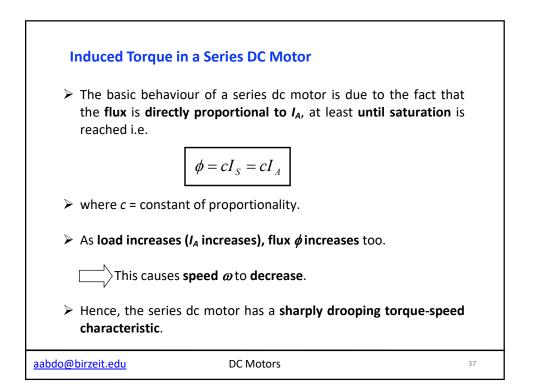


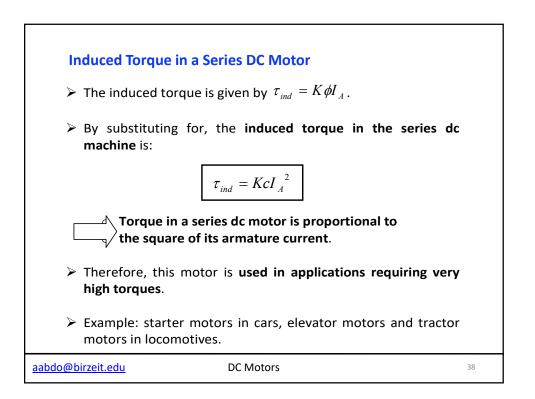


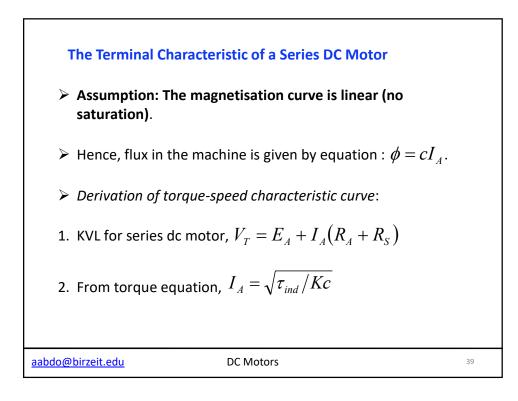
	The Permanent Magnet DC Motor (PMDC)		
2) Runs the risk of demagnetisation due to armature reaction or excessive heating			
	during prolonged periods of overload.		
\triangleright	The PMDC is basically the same machine as a shunt dc motor except the flux i	n the	
	PMDC motor is fixed.		
۶	Speed control through varying the field current or flux is not possible.		
\triangleright	Hence, speed control methods for PMDC motors are:		
1.	Armature voltage control		
2.	Armature resistance control		
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aabdo@	aabdo@birzeit.edu DC Motors 34		











The Terminal Characteristic of a Series DC Motor

1. Also, $E_A = K\phi\omega$. Hence, by substituting for E_A and I_A into the KVL equation:

$$V_T = K\phi\omega + \sqrt{\frac{\tau_{ind}}{Kc}} (R_A + R_S)$$

2. If the flux can be eliminated from this expression, it will directly relate the torque of a motor to its speed. Notice that $I_{_A}=\phi/c$,

thus
$$au_{ind}=ig(K/cig)\phi^2$$
 . Therefore,

$$\phi = \sqrt{\frac{c}{K}} \sqrt{\tau_{ind}}$$

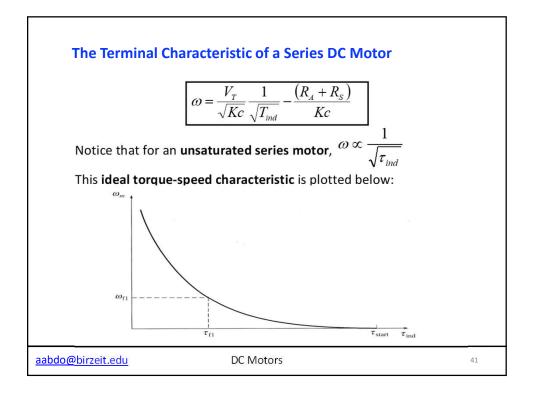
3. By substituting this flux expression into the equation in part 1 and solving for speed, the resulting **torque-speed relationship for the series dc motor** is:

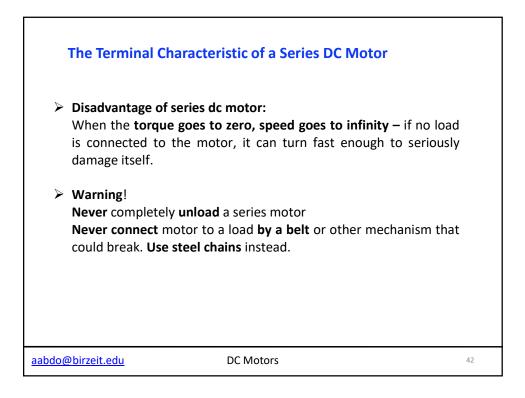
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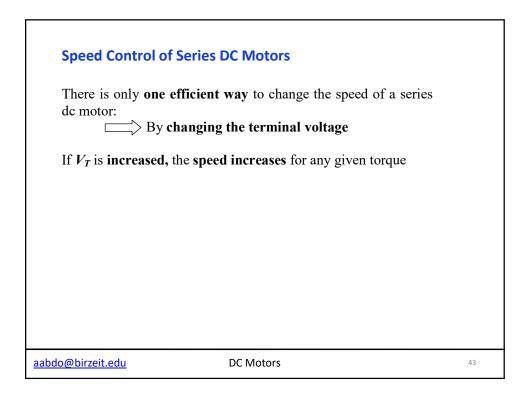
DC Motors

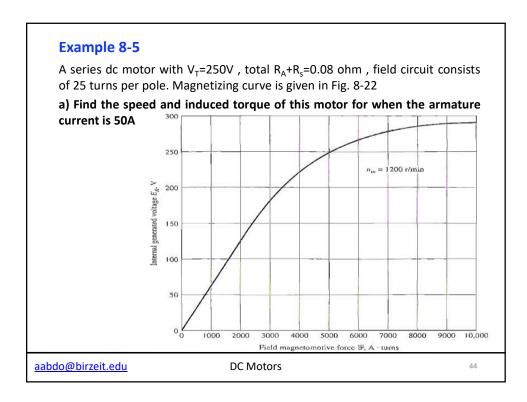
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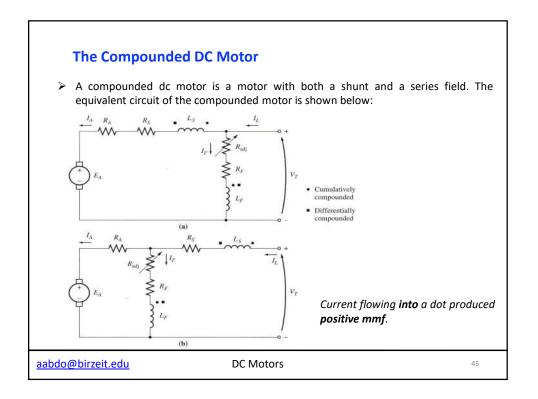
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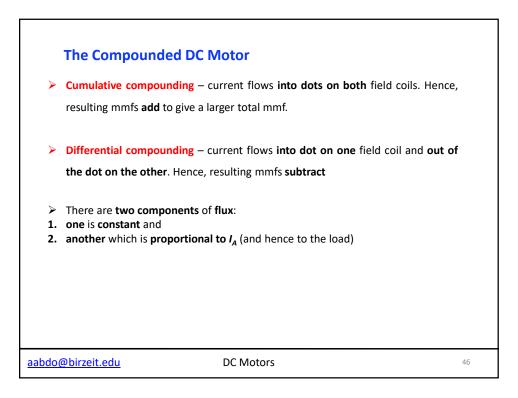


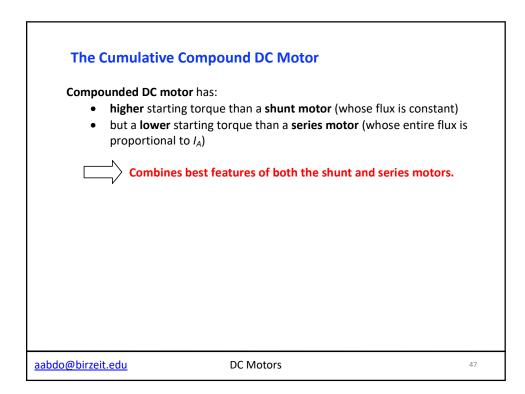


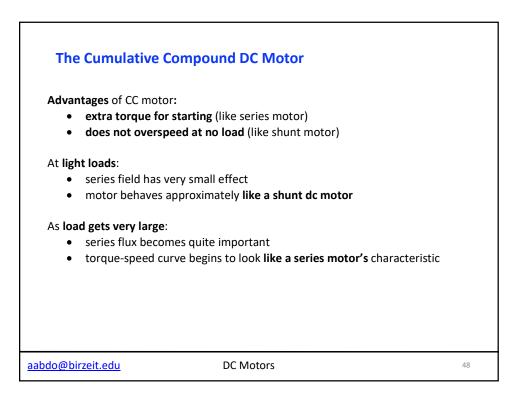


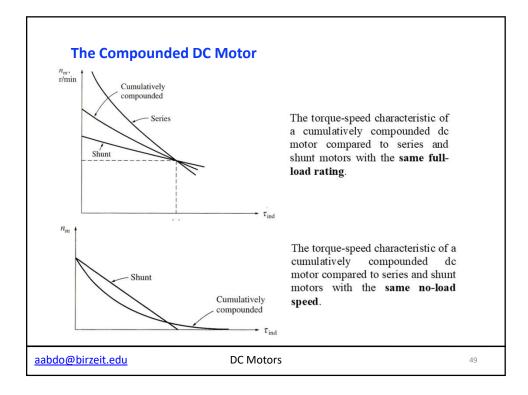


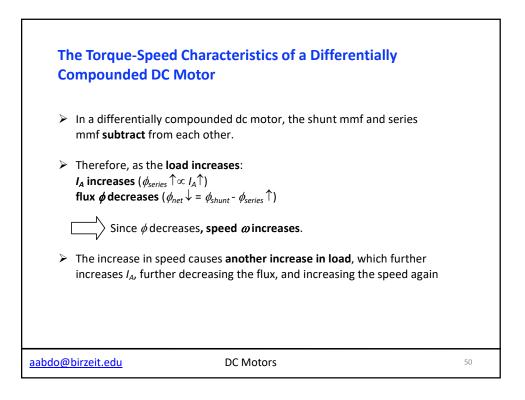


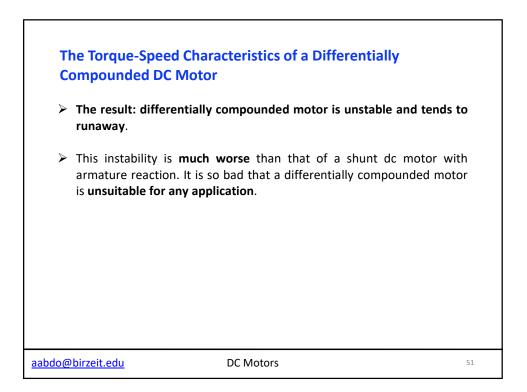


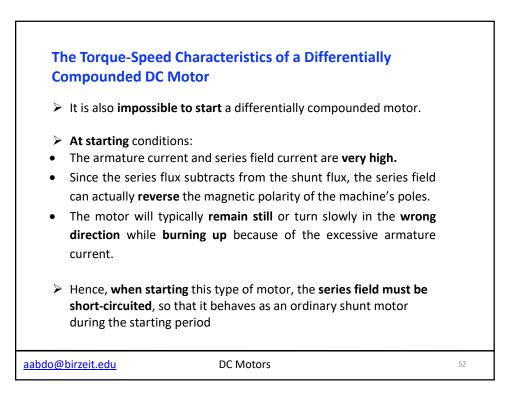


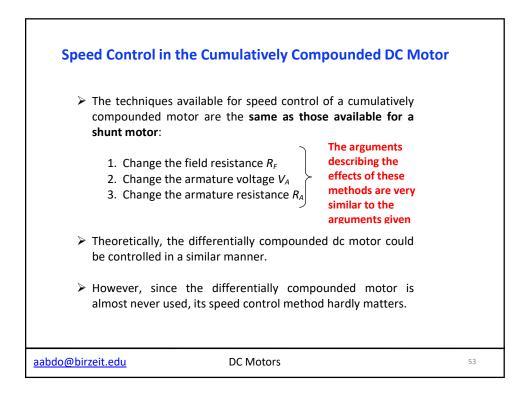


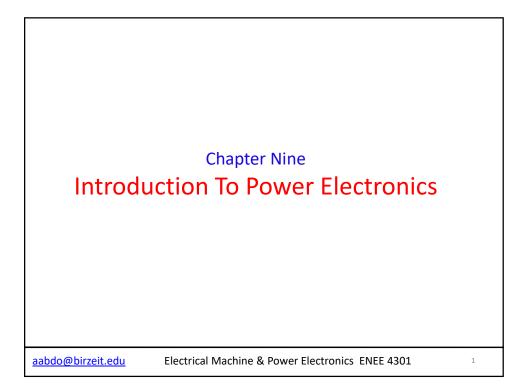




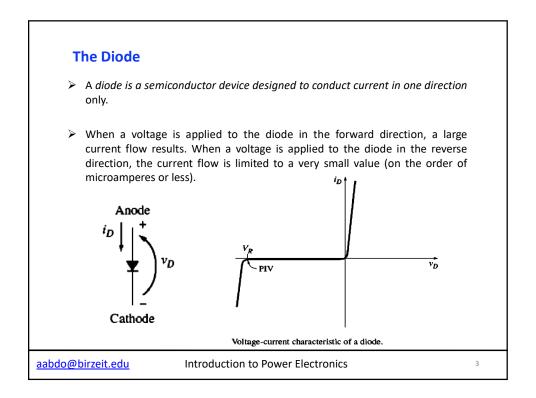




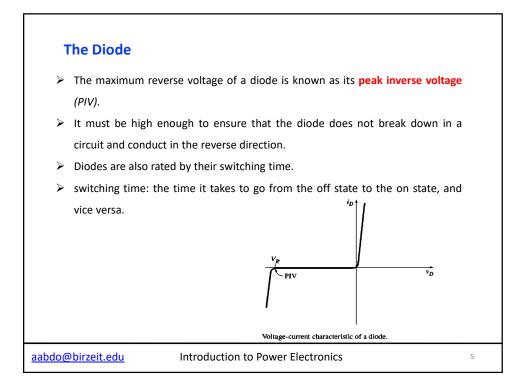


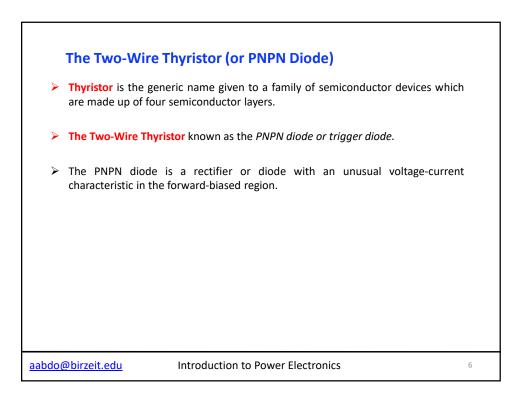


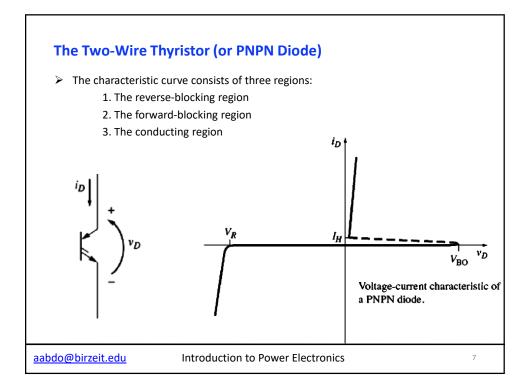
Introduction	
POWER ELECTRONIC COMPONENTS	
I. The Diode	
2. The Two-Wire Thyristor (or PNPN diode)	
3. The Three-Wire Thyristor (or silicon controlled rectifier (SCR))	
4. The Gate TurnOff (GTO) Thyristor	
5. The DIAC	
6. The TRIAC	
7. The Power Transistor (PTR)	
8. The Insulated-gate Bipolar Transistor (IGBT)	
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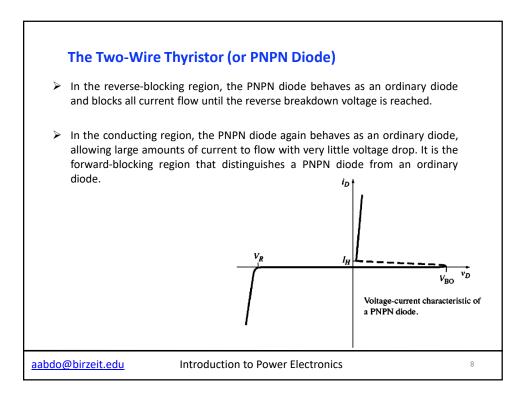


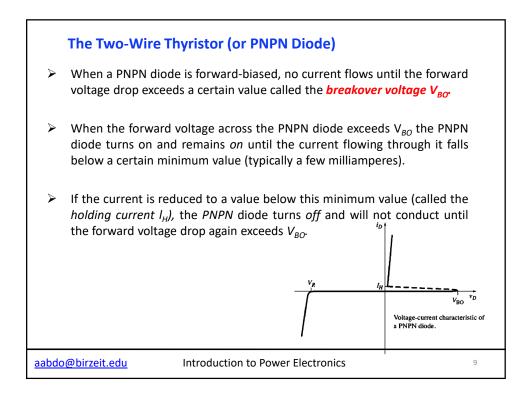
The Diode				
≻	Diodes are rated by:			
	1.	The amount of power they can safely dissipate.		
	2.	The maximum reverse voltage that they can take before breaking down.		
≻	The	e power dissipated by a diode during forward operation is equal to the		
	for	ward voltage drop across the diode times the current flowing through it.		
>	Thi	s power must be limited to protect the diode from overheating.		
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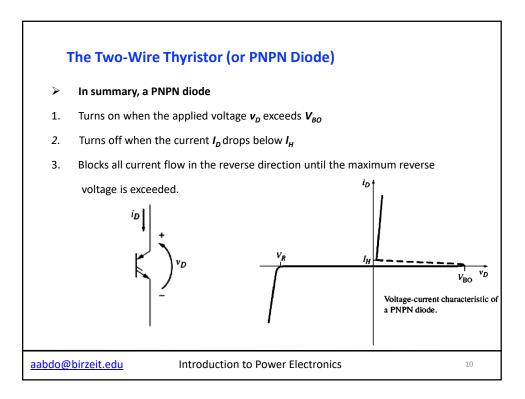


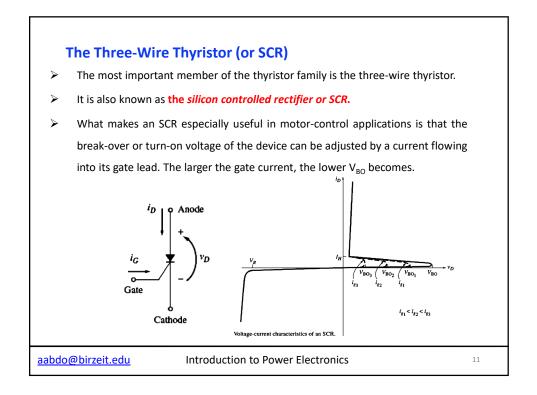


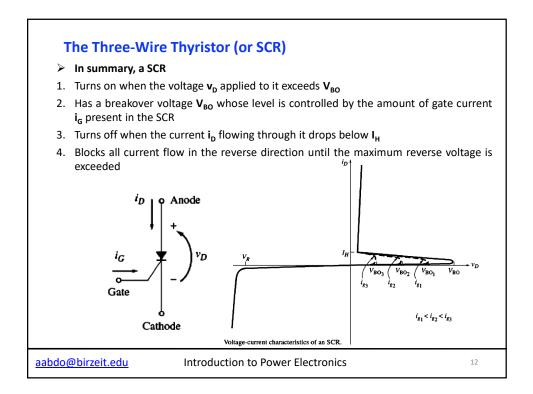


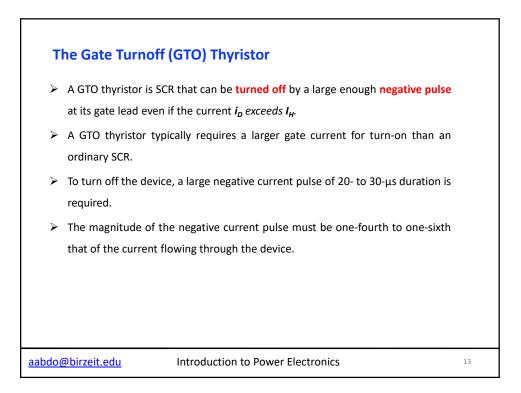


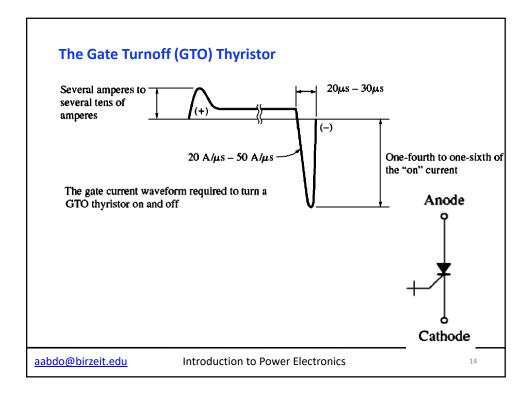


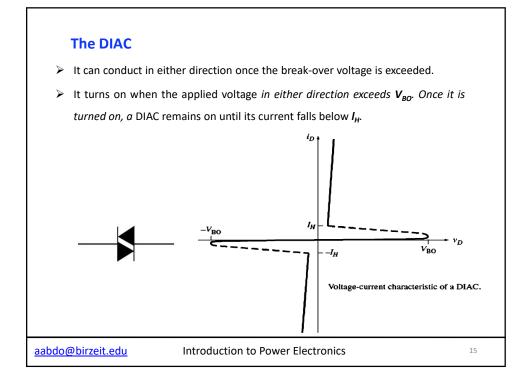


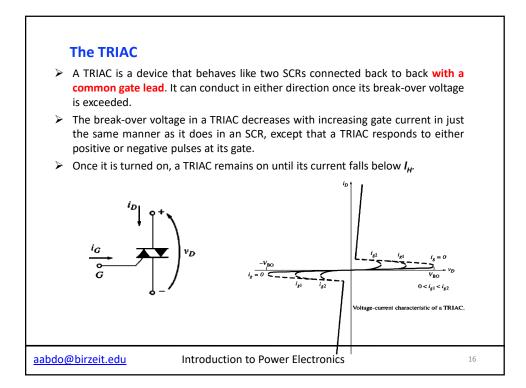


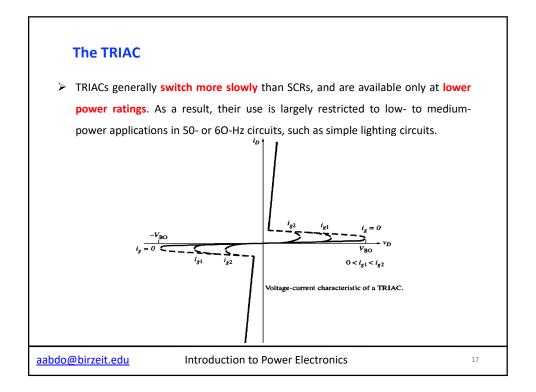


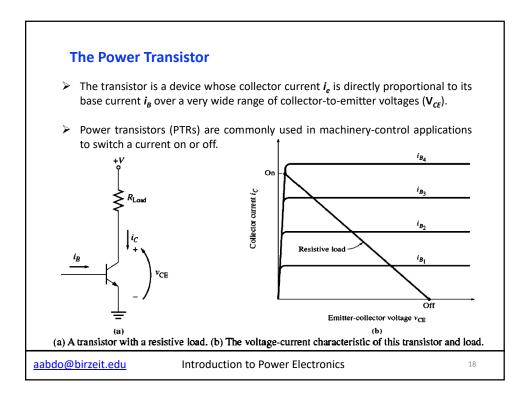


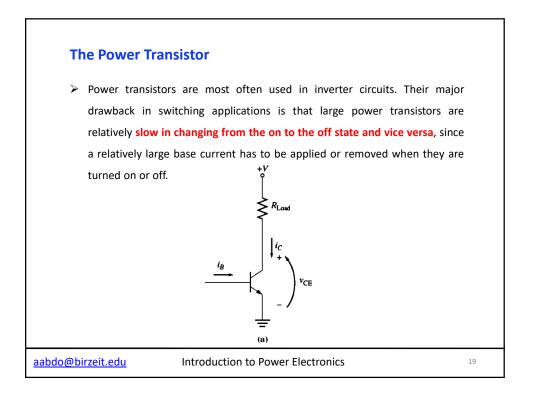


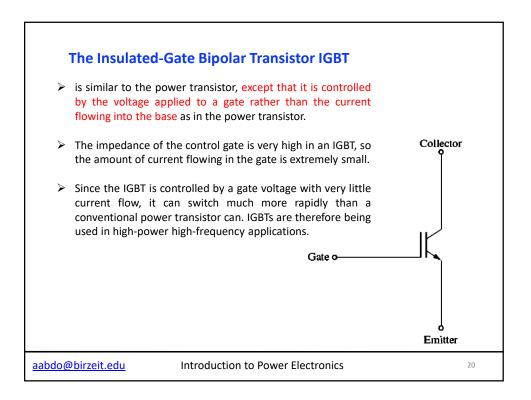


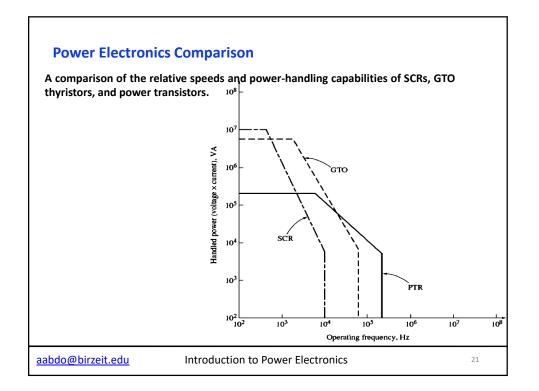


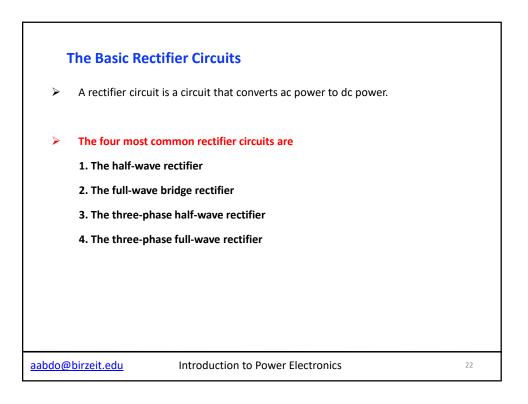










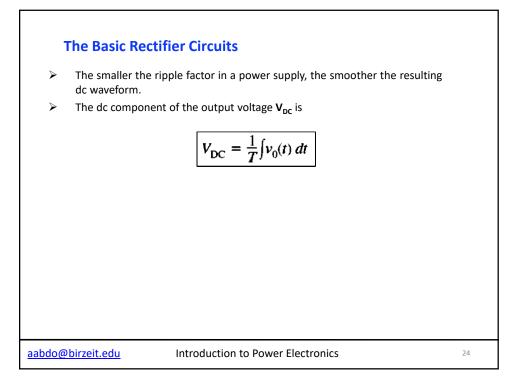


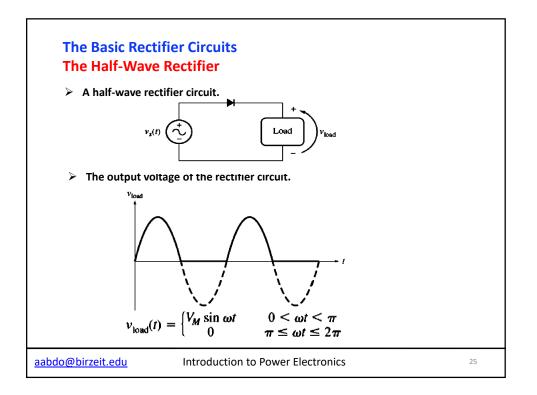
where V_{rms} is the rms value of the total output voltage from the rectifier and V_{DC} is the dc or average output voltage from the rectifier.

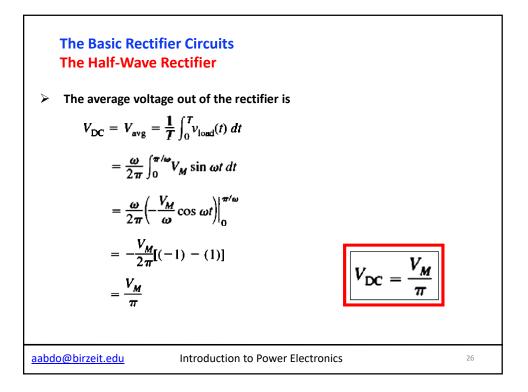
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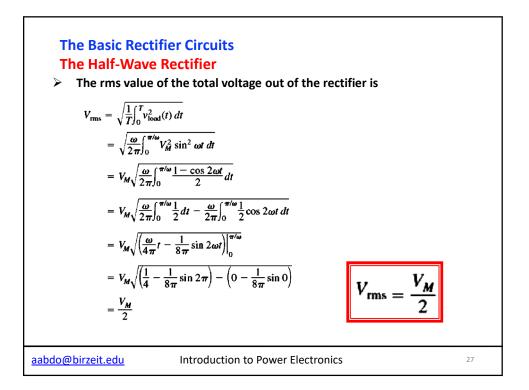
Introduction to Power Electronics

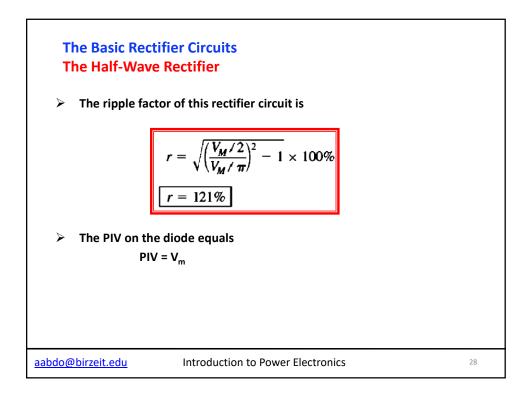
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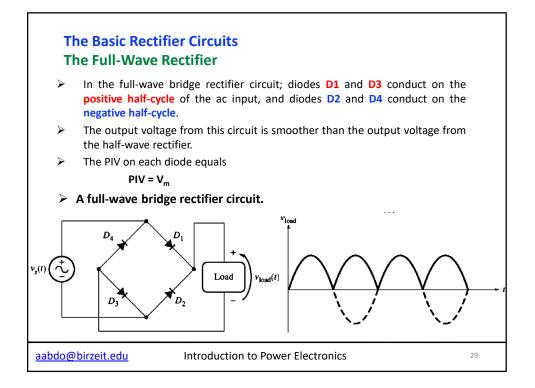


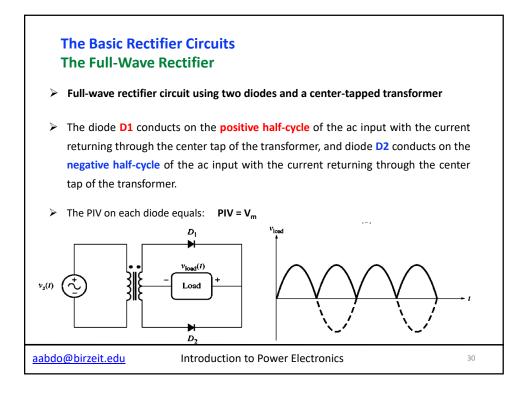


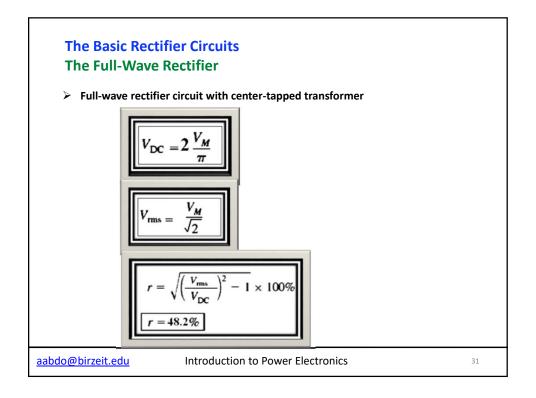


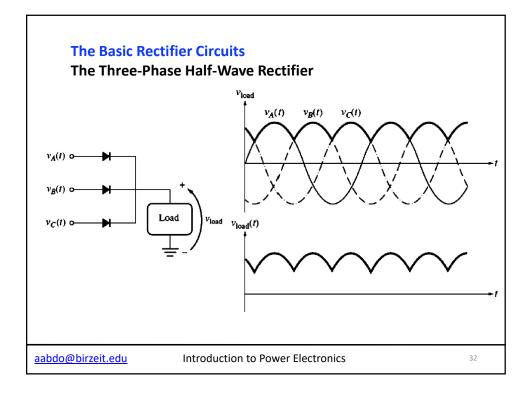


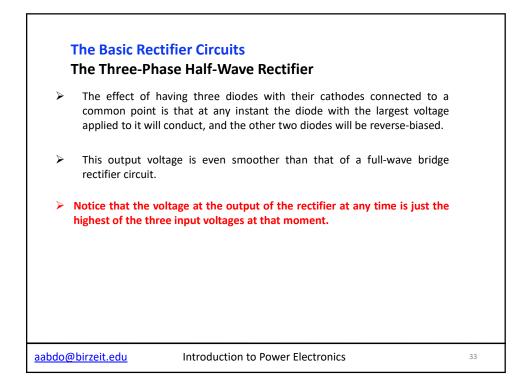


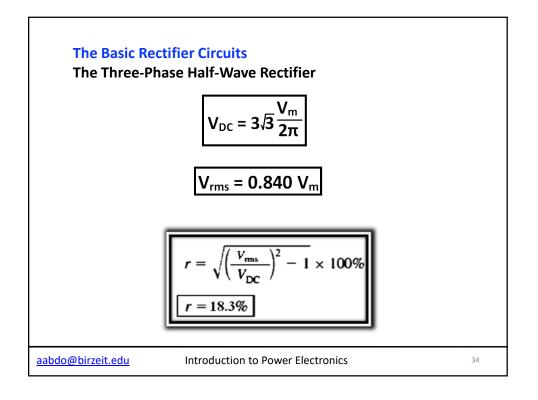


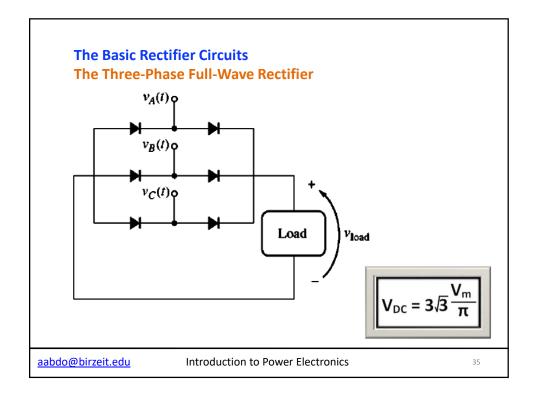


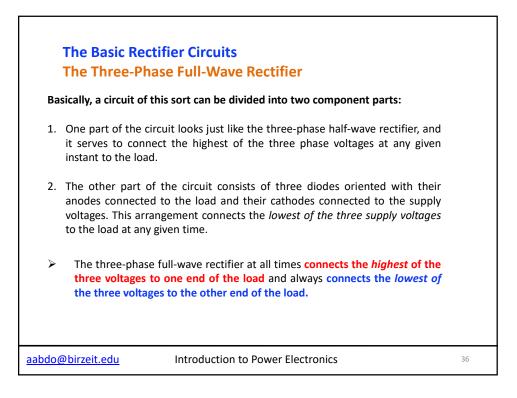


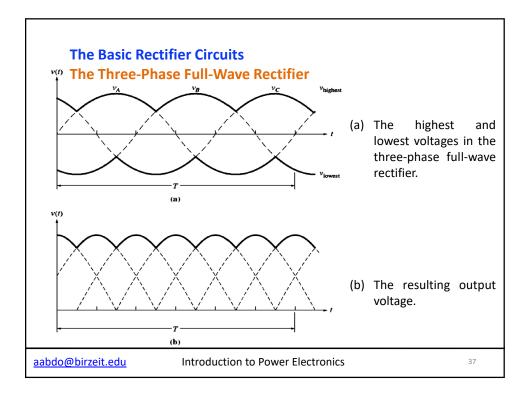


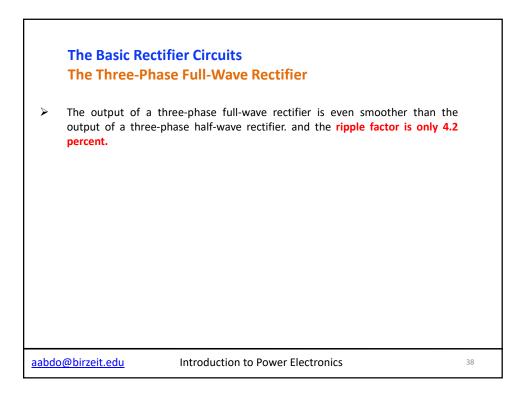


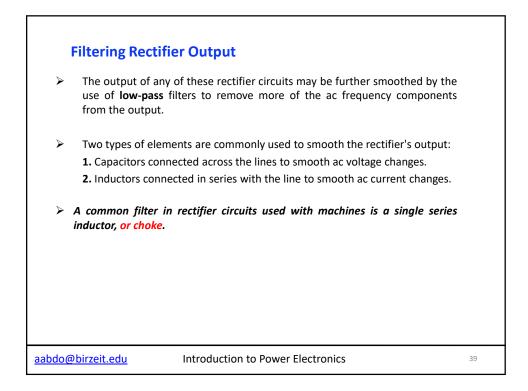


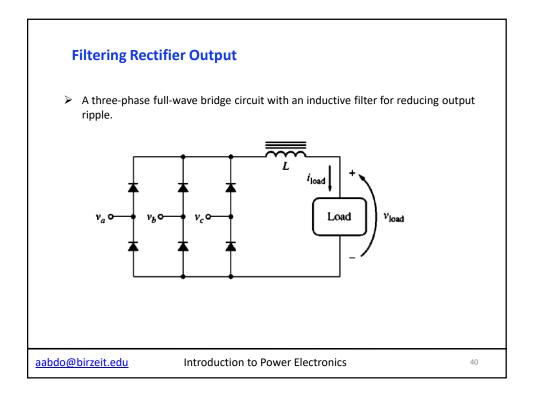


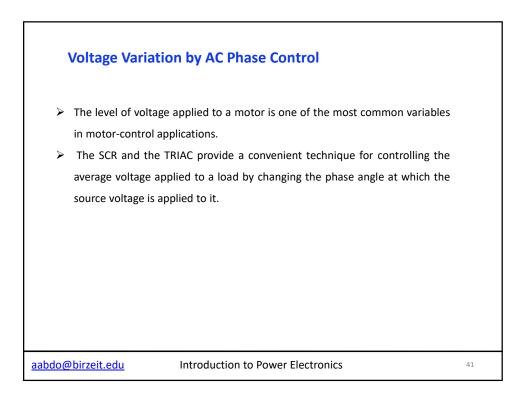


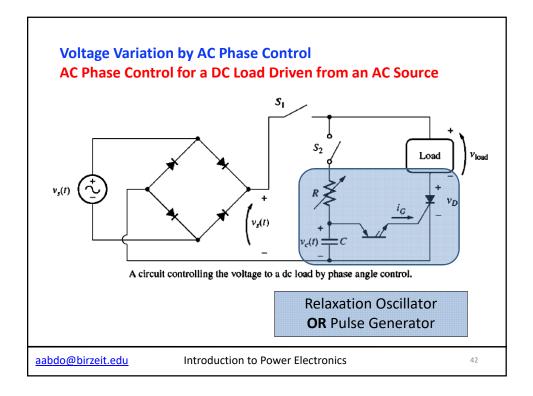


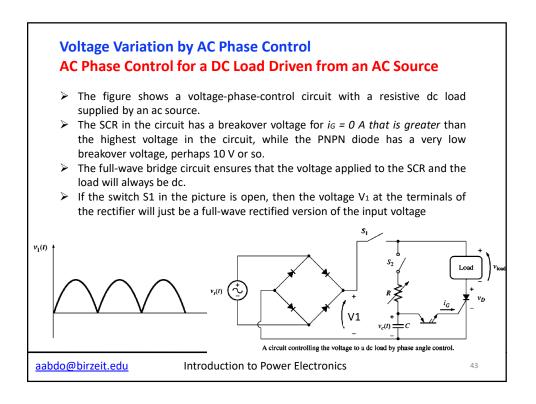


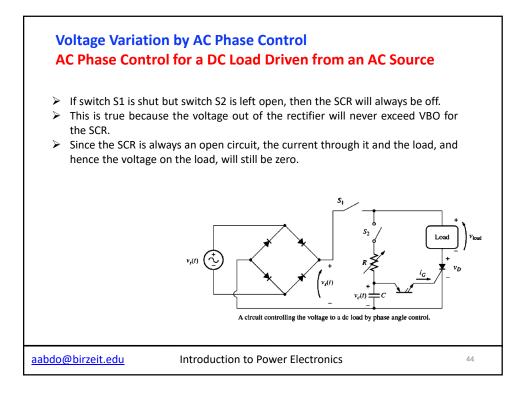


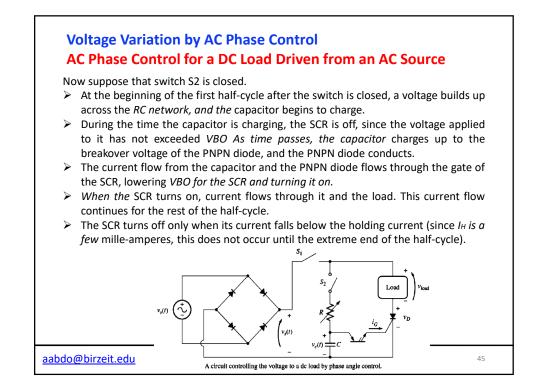


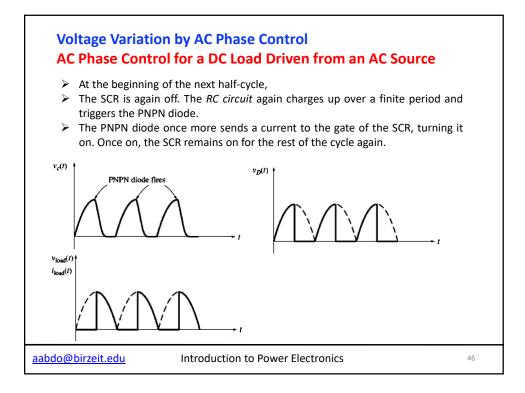


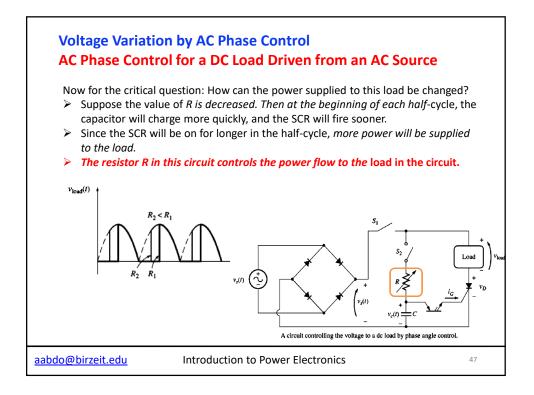


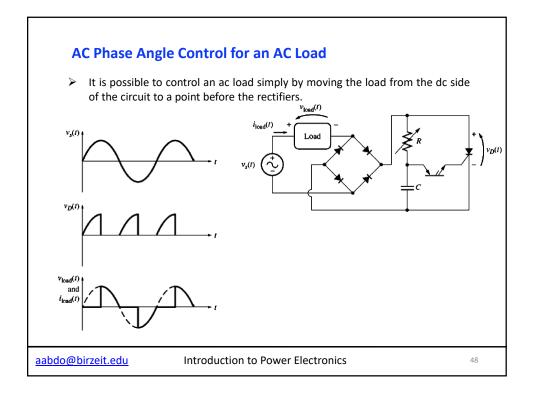


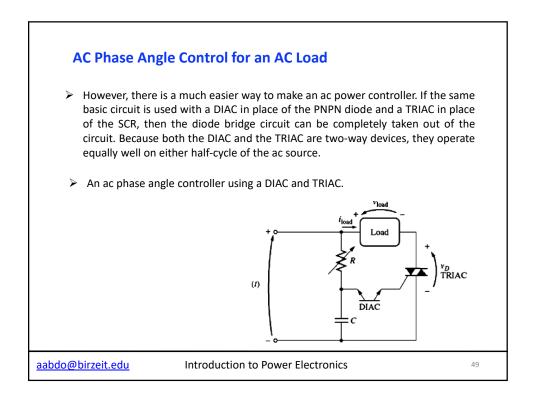


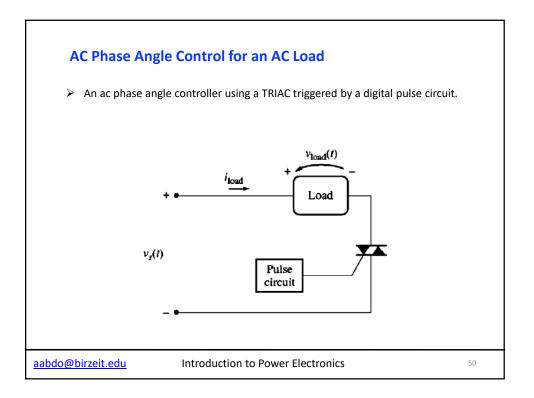


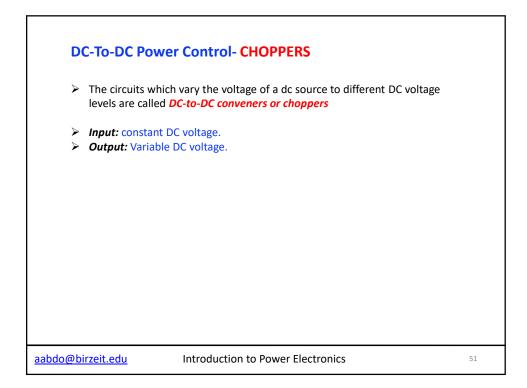


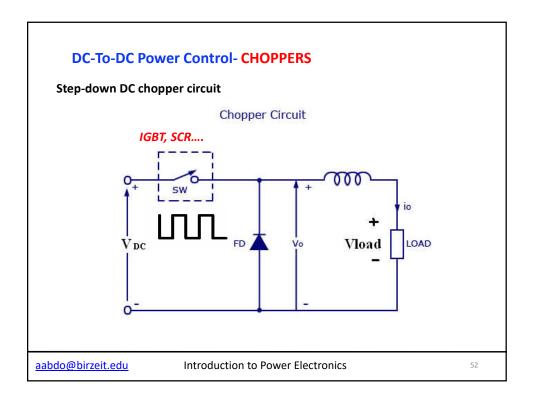


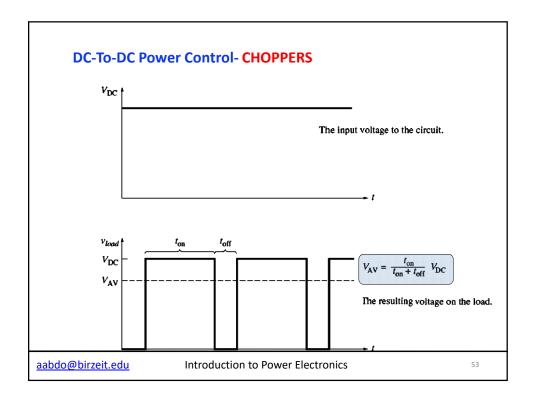


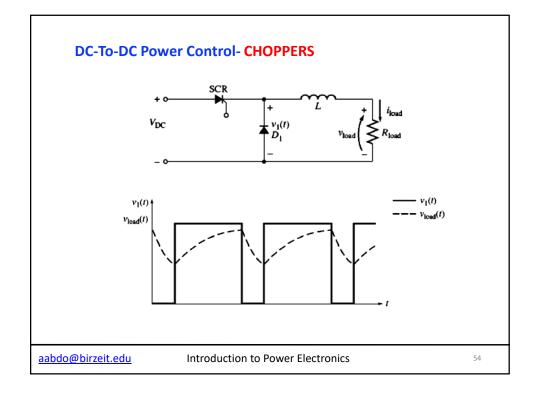












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