

H.W # 1

Internal combustion engines

Q1

$$1) r_v = \frac{V_1}{V_2} = \frac{1}{0.17} = 5.85$$

$$2) \text{Displacement volume} = \text{cylinder volume} - \text{clearance}$$

$$= 0.83 + \text{cylinder volume}$$

$$= 0.83 + \frac{mRT_1}{P_1}$$

$$= \frac{0.83 + 0.1 + 0.287}{100 + \frac{1}{305}} = 0.0726 \text{ m}^3$$

$$= 72.6 \text{ liter}$$

$$3) Q_{in} = 400 \text{ kJ/kg} = C_v(T_3 - T_2)$$

$$T_2 = T_1 (r_v)^{0.4} = 620 \text{ K}$$

$$T_3 = \frac{400}{0.707} + 620 = 1185.8 \text{ K}$$

$$T_4 = T_3 \left(\frac{1}{r_v}\right)^{0.4} = 584 \text{ K}$$

$$Q_{out} = C_v(T_4 - T_1) = 197 \text{ kJ/kg}$$

$$W = q_{in} - q_{out} = 400 - 197 = 203 \text{ kJ}$$

$$W = mW = 0.1(203) = 20.3 \text{ kJ}$$

$$4) \eta_{thermal} = \frac{W}{q_{in}} \times 100\% = 50.7\%$$

$$5) v_1 = \frac{V_1}{m} = 0.875 \text{ m}^3/\text{kg}$$

$$v_2 = \frac{v_1}{r_v} = 0.149 \text{ m}^3/\text{kg}$$

$$= \frac{1}{15} (50.8) \times 10^2 \neq \frac{\pi (0.343)^2}{4} =$$

$$v_c = \frac{v_1}{v_2} = \frac{50.8 - 8}{\frac{50.8}{15}} = 12.6$$

$$\eta_{\text{otto}} = 1 - \frac{1}{v_c^{k-1}} = 0.637 \neq 100\% = 63.7\%$$

$$v_2 = \frac{v_1}{\left(\frac{p_2}{p_1}\right)^{1/k}} = 0.0612 \text{ m}^3$$

$$v_c = 16.35$$

$$T_2 = T_1 (v_c)^{0.4} = 917 \text{ K}$$

$$T_3 = \frac{v_3}{v_2} T_2 = 1498 \text{ K}$$

$$T_4 = T_3 \left(\frac{v_3}{v_4}\right)^{0.4} = 546 \text{ K}$$

$$q_{\text{in}} = c_p (T_3 - T_2) = 813.4 \text{ kJ/kg}$$

$$q_{\text{out}} = c_w (T_4 - T_1) = 176.4 \text{ kJ/kg}$$

$$\eta = \frac{q_{\text{in}} - q_{\text{out}}}{q_{\text{in}}} \neq 100\% = 78.3\%$$

Q5

$$T_2 = T_1 r_r^{0.4} = 909 \text{ K}$$

$$T_3 = T_2 \frac{v_3}{v_2} = 1818 \text{ K}$$

$$q_{in} = c_p(T_3 - T_2) = 1273 \text{ KJ/Kg}$$

$$T_4 = T_3 (r_r)^{-0.4} = 600 \text{ K}$$

$$q_{out} = c_v(T_4 - T_1) = 45 \text{ KJ/Kg}$$

$$w = 1058 \text{ KJ/Kg}$$

$$v_1 = \frac{R T_1}{P_1} = 5.861 \text{ m}^3/\text{Kg}$$

$$m_{ep} = \frac{w}{v_1 - v_2} = \frac{1058}{\frac{15}{16} (5.861)} = 1301 \text{ bar}$$

Q6

$$\text{Swept Volume} = v_s = \frac{(0.15)^2 \pi \times 0.2 \times 1}{4} = 0.0035 \text{ m}^3$$

$$v_1 = 1.1 v_s = 0.00385 \text{ m}^3$$

$$v_2 = 0.1 v_s = 0.00035 \text{ m}^3$$

$$v_r = \frac{v_1}{v_2} = 11$$

$$v_3 = v_2 + 0.06 v_s = 5.6 \times 10^{-4} \text{ m}^3$$

$$x = \frac{v_3}{v_2} = 1.6$$

$$\eta_{\text{Diesel}} = 1 - \frac{1}{v_r^{k-1}} \left[\frac{x^k - 1}{k(x-1)} \right] = 57.5\%$$

$$T_3 = 2073 \text{ K}$$

$$V_2 = V_1 + \frac{1}{8} V_1 = \frac{9}{8} V_1$$

$$V_2 = \frac{1}{8} V_1$$

$$r_v = \frac{V_1}{V_2} = 9$$

$$T_2 = T_1 r_v^{0.4} = 742 \text{ K}$$

$$P_2 = P_1 r_v^k = 21.7 \text{ bar}$$

$$x = \frac{T_3}{T_2} = 2.8$$

$$P_3 = P_2, \quad \frac{V_4}{V_3} = \frac{V_1}{V_3}, \quad r_v = \frac{V_1}{V_2}$$

$$\frac{r_v V_2}{V_3} = \frac{V_4}{V_3}, \quad x = \frac{V_3}{V_2}$$

$$\frac{V_4}{V_3} = \frac{r_v}{x}$$

$$T_4 = T_3 \left(\frac{r_v}{x} \right)^{1.4} = 1300 \text{ K}$$

$$P_4 = P_3 \left(\frac{x}{r_v} \right)^{1.4} = 4.23 \text{ bar}$$

$$\eta_D = 1 - \frac{1}{r_v^{k-1}} \left[\frac{x^k - 1}{k(x-1)} \right] = 46.8 \%$$

$$q_{in} = c_p (T_3 - T_2) = 1332 \text{ kJ/kg}$$

$$q_{out} = c_v (T_4 - T_1) = 711 \text{ kJ/kg}$$

$$w = q_{in} - q_{out} = 621 \text{ kJ/kg}$$

$$\dot{m} = \frac{\dot{V}_s}{v_1}$$

$$v_1 = \frac{R T_1}{P_1} = 0.875 \text{ m}^3/\text{kg}$$

$$V_s = 9.42 \times 10^{-4} \text{ m}^3$$

$$\dot{V} = V_s \times \frac{1800}{2} \times \frac{1}{60} = 14.13 \times 10^{-3} \text{ m}^3/\text{s}$$

$$\dot{m} = \frac{\dot{V}}{v_1} = 1.61 \times 10^{-3} \text{ kg/s}$$

$$\text{Power per cylinder} = \dot{m} w = 1000 \text{ W}$$

$$\text{for entire engine:} \\ \text{power} = 6000 \text{ W}$$

$T_2 = 273 + 60 = 333 \text{ K}$ $A/F = 18/1$ $r_v = 16/1$
 $T_2 = T_1 (r_v)^{0.4} = 100 \text{ kPa}$
 $V_1 = 16 V_2 = 1009 \text{ K}$

$m_{air} = \frac{V_1}{V_1}$, $V_1 = \frac{0.287 \times 333}{100} = 0.956 \text{ m}^3/\text{kg}$

$m_{air} = 1.05 \times 10^3 \text{ kg/cycle}$
 $\Rightarrow \dot{m}_{fuel} = \frac{m_{air}}{18} = 0.058 \times 10^3 \text{ kg/cycle}$

$\dot{q}_{in}^{total} = \dot{m}_{fuel} \times 42500 = 2471 \text{ kg}$
 $\dot{q}_{in} \text{ or constant volume} = \dot{q}_{in}^{total} / 2 = 1237 \text{ kJ} = \dot{q}_{in}$

$T_3 = \dot{q}_{in}/c_v + T_2 = 2732 \text{ K}$
 $P_2 = P_1 r_v^{1.4} = 48.5 \text{ bar}$

$P_3 = P_2 T_3/T_2 = 131 \text{ bar}$

$\dot{q}_{in}'' = \dot{q}_{in}$
 $T_4 = \frac{\dot{q}_{in}''}{c_p} + T_3 = 3964 \text{ K}$

$P_4 = P_3$; $V_3 = V_2 = \frac{V_1}{r_v}$, $V_5 = V_1$

$\frac{T_4}{V_4} = \frac{T_3}{V_3}$
 $\frac{T_4}{V_4} = \frac{T_3}{V_1} r_v$

$\frac{V_1}{V_4} = \frac{T_3}{T_4} r_v = T_4 \left(\frac{T_4}{T_3 r_v} \right)^{0.4} = 1518 \text{ K}$

$T_5 = T_4 \left(\frac{V_4}{V_1} \right)^{-1.4} = 1.6 \text{ bar}$

$P_5 = P_4 \left(\frac{V_4}{V_1} \right)^{1.4} = 0.95 \text{ kJ}$

$Q_{out} = m r c_v (T_5 - T_1) = 2470 \text{ kJ}$

$\omega = \dot{q}_{in} - \dot{q}_{out} = 2470 \text{ kJ}$

$\eta = \frac{\omega}{\dot{q}_{in}} \approx 100\%$