

**Birzeit University**  
**Mechanical & Mechatronics Engineering Department**  
**Heat Transfer ME 431**

**Homework # 3 Steady State Conduction (7<sup>th</sup>.ed)**

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**3.12** A thermopane window consists of two pieces of glass 7 mm thick that enclose an air space 7 mm thick. The window separates room air at 20°C from outside ambient air at -10°C. The convection coefficient associated with the inner (room-side) surface is 10 W/m<sup>2</sup> · K.

(a) If the convection coefficient associated with the outer (ambient) air is  $h_o = 80$  W/m<sup>2</sup> · K, what is the heat loss through a window that is 0.8 m long by 0.5 m wide? Neglect radiation, and assume the air enclosed between the panes to be stagnant.

**3.62** A bakelite coating is to be used with a 10-mm-diameter conducting rod, whose surface is maintained at 200°C by passage of an electrical current. The rod is in a fluid at 25 C, and the convection coefficient is 140 W/m<sup>2</sup> · K.

What is the critical radius associated with the coating?

What is the heat transfer rate per unit length for the bare rod and for the rod with a coating of bakelite that corresponds to the critical radius? How much bakelite should be added to reduce the heat transfer associated with the bare rod by 25%?

**3.63** A storage tank consists of a cylindrical section that has a length and inner diameter of  $L = 2$  m and  $D_i = 1$  m, respectively, and two hemispherical end sections. The tank is constructed from 20-mm-thick glass (Pyrex) and is exposed to ambient air for which the temperature is 300 K and the convection coefficient is 10 W/m<sup>2</sup> · K. The tank is used to store heated oil, which maintains the inner surface at a temperature of 400 K. Determine the electrical power that must be supplied to a heater submerged in the oil if the prescribed conditions are to be maintained. Radiation effects may be neglected, and the Pyrex may be assumed to have a thermal conductivity of 1.4 W/m · K.

**3.81** A plane wall of thickness 0.1 m and thermal conductivity 25 W/m·K having uniform volumetric heat generation of 0.3 MW/m<sup>3</sup> is insulated on one side, while the other side is exposed to a fluid at 92 C. The convection heat transfer coefficient between the wall and the fluid is 500 W/m<sup>2</sup> ·K. Determine the maximum temperature in the wall.

**3.96** A cylindrical shell of inner and outer radii,  $r_i$  and  $r_o$ , respectively, is filled with a heat-generating material that provides a uniform volumetric generation rate (W/m<sup>3</sup>) of  $q$ . The inner surface is insulated, while the outer surface of the shell is exposed to a fluid at  $T_\infty$  and a convection coefficient  $h$ .

(a) Obtain an expression for the steady-state temperature distribution  $T(r)$  in the shell, expressing your result in terms of  $r_i$ ,  $r_o$ ,  $q$ ,  $h$ ,  $T_\infty$ , and the thermal conductivity  $k$  of the shell material.

(b) Determine an expression for the heat rate,  $q'(r_o)$ , at the outer radius of the shell in terms of  $q$  and shell dimensions.

**3.129** A long, circular aluminum rod is attached at one end to a heated wall and transfers heat by convection to a cold fluid.

(a) If the diameter of the rod is tripled, by how much would the rate of heat removal change?

(b) If a copper rod of the same diameter is used in place of the aluminum, by how much would the rate of heat removal change?

**3.136** Two long copper rods of diameter  $D = 10$  mm are soldered together end to end, with solder having a melting point of  $650^\circ\text{C}$ . The rods are in air at  $25^\circ\text{C}$  with a convection coefficient of  $10 \text{ W/m}^2 \cdot \text{K}$ . What is the minimum power input needed to effect the soldering?