

Key Form A

Birzeit University  
Mathematics Department  
Math234-Section (1)  
Quiz#4

Instructor: Dr. Ala Talahmeh  
Time: 10 minutes  
Name:.....

First Semester 2022/2023  
Date: 11/1/2023  
Number:.....

Exercise#1 [3 marks]. Circle the correct answer.

- (1) One of the following is a subspace of  $\mathbb{R}^3$
- (a)  $S = \{(x, y, 2x - 3y) : x, y \in \mathbb{R}\}$
  - (b)  $S = \{(x, y, xy) : x, y \in \mathbb{R}\}$
  - (c)  $S = \{(1, y, z) : y, z \in \mathbb{R}\}$
  - (d)  $S = \{(x - y, y, 2) : x, y \in \mathbb{R}\}$
- (2) The set of vectors  $\{(1, \alpha)^T, (\beta, 1)^T\}$  is a spanning set for  $\mathbb{R}^2$  if
- (a)  $\alpha \neq 1$  and  $\beta \neq 1$
  - (b)  $\alpha\beta \neq 1$
  - (c)  $\alpha\beta = 1$
  - (d)  $\alpha \neq \beta$

Exercise#2 [3 marks]. Answer the following statements as True or False.

1. (.....) The set of vectors  $\{1, x, x^2, x^2 + x - 1\}$  is a spanning set of  $P_3$ .
2. (.....)  $\text{Span}\{1 + x, 1 - x\}$  is a subspace of  $P_2$

Exercise#3 [4 marks]. Let  $A$  be a matrix in  $\mathbb{R}^{2 \times 2}$ , and let

$$W = \{B \in \mathbb{R}^{2 \times 2} : AB = O\}.$$

Show that  $W$  is a subspace of  $\mathbb{R}^{2 \times 2}$ .

- (1.5) (i)  $AO = O \Rightarrow O_{2 \times 2} \in W$ , that is,  $W \neq \emptyset$ .
- (ii) Let  $B$  and  $C$  in  $W$ , that is,  $AB = O$  and  $AC = O$ .
- (1.5) then  $A(B+C) = AB + AC = O + O = O$ .
- $\therefore B+C \in W$ .
- (1.5) (iii) Let  $\alpha \in \mathbb{R}$  and  $B \in W$ . Then  $A(\alpha B) = \alpha(AB) = \alpha O = O$ .
- $\therefore \alpha B \in W$ .

Good Luck

Key Form B

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Time: 10 minutes  
Name:.....

First Semester 2022/2023  
Date: 11/1/2023  
Number:.....

Exercise#1 [3 marks]. Circle the correct answer.

- (1) One of the following is not a subspace of  $\mathbb{R}^3$
- (a)  $S = \{(x, y, 2x - 3y) : x, y \in \mathbb{R}\}$
  - (b)  $S = \{(x, y, xy) : x, y \in \mathbb{R}\}$
  - (c)  $S = \{(0, y, z) : y, z \in \mathbb{R}\}$
  - (d)  $S = \{(x - y, y, 0) : x, y \in \mathbb{R}\}$
- (2) The set of vectors  $\{(0, \alpha)^T, (\beta, 0)^T\}$  is a spanning set for  $\mathbb{R}^2$  if
- (a)  $\alpha \neq 1$  and  $\beta \neq 1$
  - (b)  $\alpha\beta \neq 1$
  - (c)  $\alpha\beta \neq 0$
  - (d)  $\alpha \neq \beta$

Exercise#2 [3 marks]. Answer the following statements as True or False.

1. (..........) The set of vectors  $\{1, x, x^2\}$  is a spanning set of  $P_4$ .
2. (..........)  $\text{Span}\{1 + x, 1 - x\}$  is a subspace of  $P_2$

Exercise#3 [4 marks]. Let  $A$  be a matrix in  $\mathbb{R}^{2 \times 2}$ , and let

$$W = \{B \in \mathbb{R}^{2 \times 2} : AB = O\}.$$

Show that  $W$  is a subspace of  $\mathbb{R}^{2 \times 2}$ .

see Form A.

Good Luck

Key Form A

Birzeit University  
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Math234-Section (5)  
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First Semester 2022/2023  
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Exercise#1 [3 marks]. Circle the correct answer.

- (1) One of the following is not a subspace of  $P_4$
- (a)  $\{f(x) \in P_4 : f'(x) = 0\}$
  - (b)  $\{f(x) \in P_4 : f(1) = 1\}$
  - (c)  $\{f(x) \in P_4 : f(1) = 0\}$
  - (d)  $\{f(x) \in P_4 : f(x) = ax^3 + bx^2, a, b \in \mathbb{R}\}$
- (2) The set of vectors  $\{(\alpha, \beta)^T, (1, -1)^T\}$  is a spanning set for  $\mathbb{R}^2$  if
- (a)  $\alpha \neq 1$  and  $\beta \neq 1$
  - (b)  $\alpha\beta \neq 1$
  - (c)  $\alpha \neq -\beta$
  - (d)  $\alpha \neq \beta$

Exercise#2 [3 marks]. Answer the following statements as True or False.

1. (.....T.....) The set of vectors  $\{1, x, x^2, x^2 + x - 1\}$  is not a spanning set of  $P_4$ .
2. (.....F.....) Let  $A$  be an  $m \times n$  matrix. If  $N(A) \neq \{0\}$  and  $Ax = b$  is consistent, then the linear system  $Ax = b$  has a unique solution.

Exercise#3 [4 marks]. Let

$$W = \{p(x) \in P_3 : p''(x) + 2p'(x) = 0\}.$$

Show that  $W$  is a subspace of  $P_3$ .

- (i) Let  $p(x) = 0$ . Then  
 $p''(x) + 2p'(x) = 0 + 2(0) = 0 \Rightarrow p(x) = 0 \in W \Rightarrow W \neq \emptyset$ .
- (ii) Let  $p(x), q(x) \in W$ , that is,  $p''(x) + 2p'(x) = 0$  and  $q''(x) + 2q'(x) = 0$ .  
Then  $(p+q)''(x) + 2(p+q)'(x) = (p''(x) + 2p'(x)) + (q''(x) + 2q'(x)) = 0 + 0 = 0$   
 $\therefore p+q \in W$ .
- (iii) Let  $\alpha \in \mathbb{R}$  and  $p(x) \in W$ . Then  $(\alpha p)''(x) + 2(\alpha p)'(x)$   
Good Luck  $= \alpha(p''(x) + 2p'(x)) = \alpha \cdot 0 = 0$ .  
 $\therefore \alpha p \in W$ .

Key Form B

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<sup>2x1.5</sup>  
Exercise#1 [3 marks]. Circle the correct answer.

- (1) One of the following is a subspace of  $P_4$
- (a)  $\{f(x) \in P_4 : f(0) = 1\}$
  - (b)  $\{f(x) \in P_4 : f(1) = 1\}$
  - (c)  $\{f(x) \in P_4 : f(1) = 0\}$
  - (d)  $\{f(x) \in P_4 : f(x) = x^3 + bx^2, b \in \mathbb{R}\}$
- (2) The set of vectors  $\{(\alpha, \beta)^T, (1, 1)^T\}$  is a spanning set for  $\mathbb{R}^2$  if
- (a)  $\alpha \neq 1$  and  $\beta \neq 1$
  - (b)  $\alpha\beta \neq 1$
  - (c)  $\alpha\beta = 1$
  - (d)  $\alpha \neq \beta$

<sup>2x1.5</sup>  
Exercise#2 [3 marks]. Answer the following statements as True or False.

1. (~~.....F.....~~) The set of vectors  $\{1, x, x^2, x^2 + x - 1\}$  is a spanning set of  $P_4$ .
2. (~~.....T.....~~) Let  $A$  be an  $m \times n$  matrix. If  $N(A) = \{0\}$  and  $Ax = b$  is consistent, then the linear system  $Ax = b$  has a unique solution.

Exercise#3 [4 marks]. Let

$$W = \{p(x) \in P_3 : p''(x) + 2p'(x) = 0\}.$$

Show that  $W$  is a subspace of  $P_3$ .

see Form A.

Good Luck