

Refrigeration and air conditioning Homework 2

Answers table		
Question 2.1	a	Subcooled
	b	0.0375 Kg/s
Question 3.5	a	31.81 °C
	b	0.25 Kg/s
Question 3.6	a	-89.02 Kw
	b	-0.01 Kg/s
Question 3.9		16°C, 14°C
Question 4.4	a	681.5 W
	b	-384.22
Question 6.3		0.7 Pa/m
Question 6.5		9.38 m

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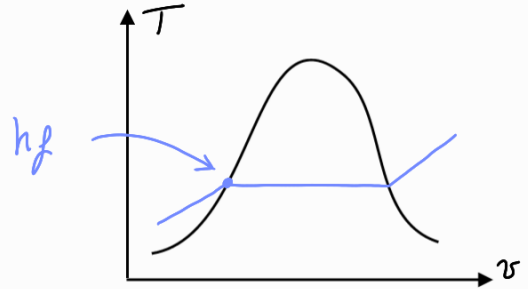
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Question 2.1

a) subcooled liquid since $T < T_{\text{sat}}$ at 250 kPa

b) From table B.1.1 and at $T = 120^\circ\text{C}$

$$h_{\text{water}} = h_f = 503.69 \text{ kJ/kg}$$



The expansion valve changes the pressure and temperature but enthalpy is constant so: $h_{\text{inlet}} = h_{\text{tank}} = 503.69 \text{ kJ/kg}$

The tank has a mixture of vapor and liquid with a quality of x at $P = 101.3 \text{ kPa}$ so:

$$h = h_f + x(h_{fg})$$

503.69

$$\left. \begin{array}{l} h_f = 419.02 \\ h_g = 2257.03 \end{array} \right\} \text{at } P = 101.3 \text{ kPa}$$

$$503.69 = 419.02 + x(2257.03)$$

$$x = 0.0375 = \frac{m_{\text{vap}}}{m_{\text{tot}}}$$

$$m_{\text{tot}} = 1 \text{ kg} \quad \text{so} \quad x = (m_{\text{vap}})(1) = m_{\text{vap}} = 0.0375$$

entering the tank from valve

Question 3.5

a)

$$(\sum \dot{m} h)_{\text{inlet}} = (\sum \dot{m} h)_{\text{outlet}}$$

$$(\dot{m}_a h_i)_{\text{air}} + (\dot{m}_w h_i)_{\text{water}} = (\dot{m}_a h_o)_{\text{air}} + (\dot{m}_w h_o)_{\text{water}}$$

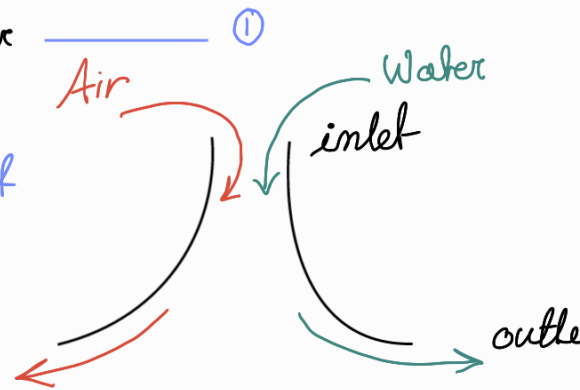
$$\dot{m}_i = P \dot{V}_i = \frac{1}{v} \dot{V}_i$$

$$h_i = 72 \text{ kJ/kg}$$

$$v = 0.892 \text{ m}^3/\text{kg}$$

} from psychrometric chart

$$\dot{m}_i = \frac{1}{0.892} \times 15 = 16.82 \text{ kg/s}$$



For the water:

From steam tables and by interpolation h_f of water is:

$$X = 38 \quad y = ?$$

$$X_1 = 35 \quad y_1 = 146.66$$

$$X_2 = 40 \quad y_2 = 167.51$$

$$\frac{X - X_1}{y - y_1} = \frac{X_2 - X_1}{y_2 - y_1} \longrightarrow y = 159.2 = h_f$$

• To find h_o for air

We know that $T_{\text{sat}} = 31$

▶ from psychrometric chart, $(h_o)_{\text{air}} = 110 \text{ kJ/kg}$

Go Back to equation 1

$$(\dot{m}_a h_i)_{\text{air}} + (\dot{m}_w h_i)_{\text{water}} = (\dot{m}_a h_o)_{\text{air}} + (\dot{m}_w h_o)_{\text{water}}$$

$$(16.82)(72) + (20)(159.2) = (16.82)(110) + (20)(h_o)$$

$$(h_o)_{\text{water}} = 127.24 \text{ kJ/kg}$$

$$\text{But } h = C_p T \longrightarrow 127.24 = 4 \times T \longrightarrow T_{\text{water}} = 31.81^\circ\text{C}$$

$$b) \text{ humidity ratio} = \Delta W = \frac{(\dot{m}_{\text{vapor}})_{\text{process}}}{(\dot{m}_{\text{dry air}})_{\text{process}}}$$

$$\dot{m}_{\text{vapor}} = \dot{m}_{\text{dry air}} \Delta W$$
$$= 16.82 (W_{\text{outlet}} - W_{\text{inlet}})$$

← psychrometric chart

$$W_{\text{inlet}} = 0.013 \text{ Kg/Kg}$$

$$W_{\text{outlet}} = 0.028 \text{ Kg/Kg}$$

$$\dot{m}_{\text{vapor}} = 0.25 \text{ Kg/s}$$

Question 3.6

$$a) \dot{Q} = \dot{m} \Delta h$$

Inlet Conditions

$$T_{\text{dry bulb}} = 27^{\circ}\text{C}$$

$$\text{Relative humidity} = 50\%$$

From psychrometric chart

$$h = 56 \text{ kJ/kg}$$

$$\omega = 0.011 \text{ kg/kg}$$

$$v = 0.865$$

Outlet Conditions

$$T_{\text{dry bulb}} = 13^{\circ}\text{C}$$

$$\text{Relative humidity} = 90\%$$

From psychrometric chart

$$h = 31 \text{ kJ/kg}$$

$$\omega = 0.0085 \text{ kg/kg}$$

$$\dot{Q} = \dot{m} \Delta h = \frac{3.5}{0.865} (31 - 56) = -89.02 \text{ kW}$$

$$b) \dot{m}_{\text{vapor}} = \Delta \omega \dot{m}_{\text{dry air}}$$

$$= (0.0085 - 0.011) \times \frac{3.5}{0.865} = -0.01 \text{ kg/s}$$

↳ Condensation

Question 3.9

$$\begin{aligned}(\Delta W)_{\text{process}} &= \frac{\dot{m}_{\text{vapor}}}{\dot{m}_{\text{dry air}}} \\ &= \frac{0.0025}{0.36} = 6.94 \times 10^{-3} = W_{\text{outlet}} - W_{\text{inlet}}\end{aligned}$$

At inlet and from psychrometric chart

$$T_{\text{dry}} = 15^{\circ}\text{C}$$

Relative humidity = 20%

$$W_i = 0.002 \text{ kg/kg}, \quad h = 20 \text{ kJ/kg}$$

$$\text{So } W_{\text{outlet}} = 6.94 \times 10^{-3} + 2 \times 10^{-3} = 8.94 \times 10^{-3} \text{ kg/kg}$$

$$\sum(\dot{m}h)_{\text{inlet}} = \sum(\dot{m}h)_{\text{outlet}}$$

$$(\dot{m}_i h_i)_{\text{steam}} + (\dot{m}_i h_i)_{\text{air}} = (\dot{m}_o h_o)_{\text{air}}$$

$$(0.0025) \times (2676.05) + (0.36)(20) = (0.0025 + 0.36)(h_{\text{air}})$$

steam table \nearrow

$$h_{\text{air}_o} = 38.3 \text{ kJ/kg}$$

From psychrometric chart

$$T_{\text{dry}} = 16^{\circ}\text{C}$$

$$T_{\text{wet}} = 14^{\circ}\text{C}$$

Question 4.4

Room Area = $10 \times 7 \text{ m}^2$

Exterior wall: height = 3.5 high, length = 10 m
Steel backed with 10 mm of insulating board, 75 mm of glass fiber and 16 mm of gypsum board.

Single glazed window \rightarrow 30% of exterior wall

Computer and lights \rightarrow 24 h/d \rightarrow $\dot{Q} = 2 \text{ kW}$

$T_{\text{indoor}} = 20^\circ\text{C}$

a) Columbus, Ohio \rightarrow heating load at winter?

$$\begin{aligned}\dot{Q}_{\text{winter}} &= \dot{Q}_{\text{transmission}} + \dot{Q}_{\text{equipment}} \\ &= (U A \Delta T)_{\text{wall}} + (U A \Delta T)_{\text{window}} - 2 \text{ kW}\end{aligned}$$

$$\begin{aligned}U_{\text{wall}} &= \frac{1}{\sum R} = \frac{1}{L_1/k_1 + L_2/k_2 + L_3/k_3} \\ &= \frac{1}{0.32 + 0.1 + \frac{0.075}{0.044}} = 0.17\end{aligned}$$

insulation Board \uparrow Gypsum \uparrow fiber Glass \uparrow

$$A(\text{External wall}) = 3.5 \times 10 = 35 \text{ m}^2 - A_{\text{window}}$$

$$A(\text{window}) = \frac{30}{100} \times 35 = 10.5$$

$$\rightarrow A(\text{wall}) = 35 - 10.5 = 24.5$$

$$\Delta T = T_{out} - T_{in} = T_{out} - 20 = -35$$

From Table 4-3 \leftarrow

$$= -15$$

$$U_{window} = 6.2 \quad (\text{Table 4-4})$$

$$\Delta T = -35$$

$$\text{So } Q_{window} = 6.2 \times 10.5 \times 35 = 2278.5$$

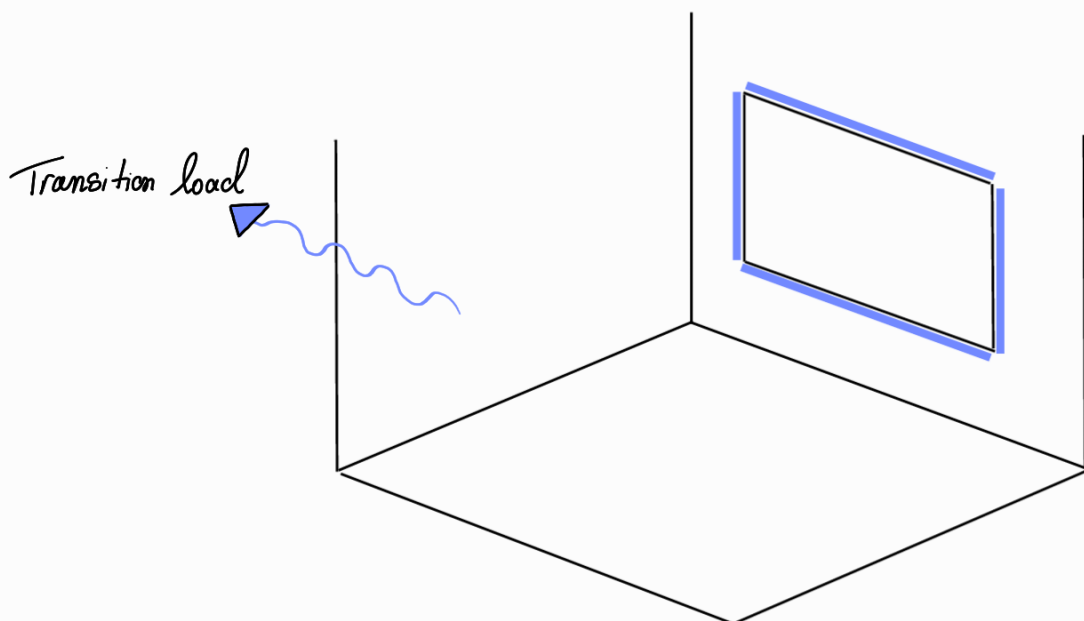
$$Q_{wall} = 0.47 \times 24.5 \times 35 = 403.03$$

$$Q_{heating} = 2278.5 + 403.03 - 2000 = 681.5 \text{ W}$$

$$b) \quad Q_{window} = 3.3 \times 10.5 \times 35 = 1212.75$$

$$Q_{heating} = 1212.75 + 403.03 - 2000 = -384.22 \text{ kW}$$

► So no need for heating since equipments load > heating load



Question 6.3

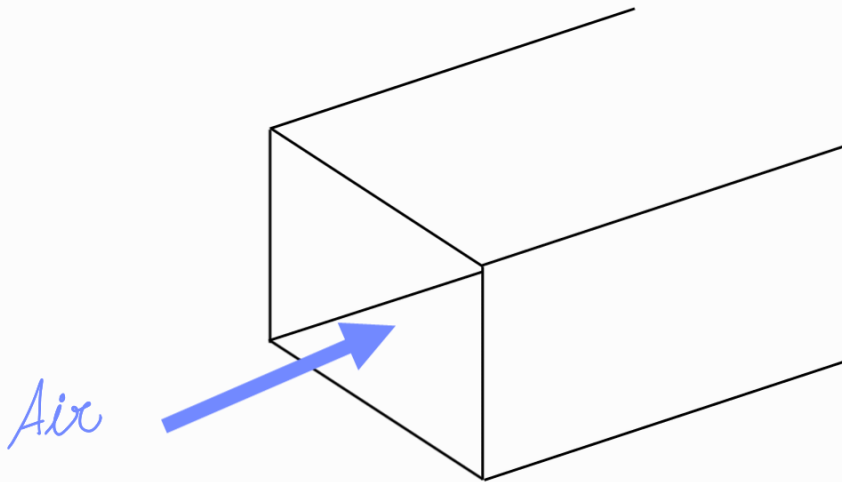
Rectangular Duct $0.25 \times 1\text{m}$

$$\dot{V} = 1.2 \text{ m}^3/\text{s}$$

$$D_{eq} = \frac{4 \times \text{Area}}{\text{perimeter}} = \frac{2ab}{a+b} = \frac{2 \times 0.25 \times 1}{1+0.25} = 0.4$$

$$\text{velocity} = \frac{1.2}{\text{Area}} = \frac{1.2}{0.25 \times 1} = 4.8 \text{ m/s}$$

$$\text{pressure drop/meter} = 0.7 \text{ Pa/m}$$



Question 6.5

A duct: $0.4 \times 0.8 \rightarrow D_h = \frac{2ab}{a+b} = \frac{2 \times 0.4 \times 0.8}{0.8+0.4} = 0.533$

inner radius = 0.2 m

outer radius = 1 m

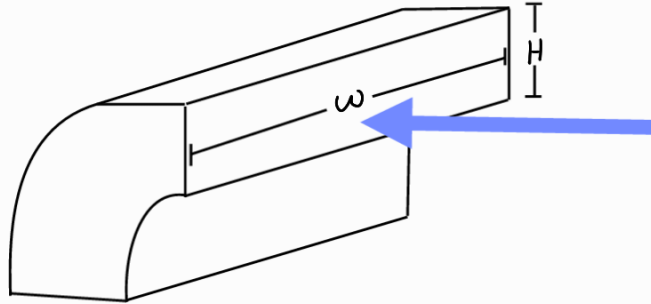
Velocity = 10 m/s

$L_{eq} = ?$

From Fig 6-8

$$\frac{\text{inner}}{\text{outer}} = \frac{0.2}{1} = 0.2$$

$$\frac{\omega}{H} = \frac{0.8}{0.4} = 2$$



$$\frac{P_{loss}}{\gamma^2 \frac{\rho}{2}} = 0.3$$

$$P_{loss} = 0.3 \times (10^3)^2 \times \frac{1.25}{2} = 18.75$$

Pressure drop / meter = 2 Pa/m

$$L_{eq} = \frac{P_{loss}}{\text{Pa/m}} = \frac{18.75}{2} = 9.375 \text{ m}$$