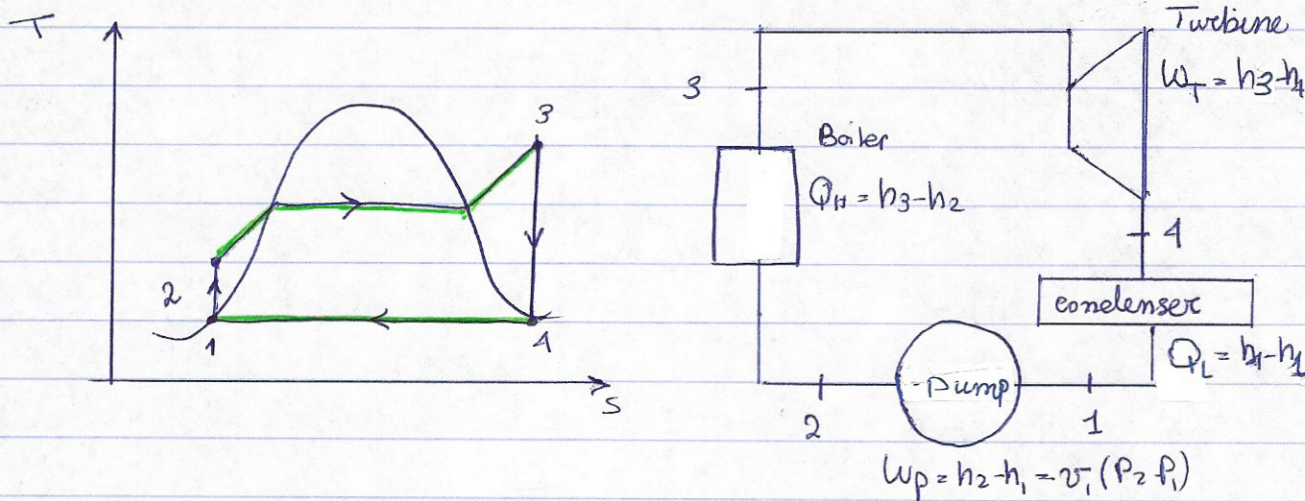


Chapter 9: Power & Refrigeration systems with phase change

Ideal Rankine cycle



- From 2 → 3 : pressure is constant
- From 4 → 1 : pressure is constant
- From 4 → 2 : entropy is constant
- From 3 → 1 : entropy is constant

$$W_P = h_2 - h_1 = v_f(P_2 - P_1)$$

where $h_1 = h_f @ P_1$
 $v = v_f @ P_1$

- In the pump we can use relation $w = v_f dp = v_f(P_2 - P_1)$

To find efficiency: $\eta_{Rankine} = \frac{W_T - W_P}{Q_H} = \frac{Q_H - Q_L}{Q_H}$

$$= \frac{(h_3 - h_2) - (h_4 - h_1)}{(h_3 - h_2)}$$

effect of pressure & temperature on the Rankine cycle

$$\eta \propto 1 - \frac{T_L}{T_H}$$

$T_L \downarrow \eta \uparrow$
 $T_H \uparrow \eta \uparrow$

1- Decreasing the pressure of the condenser ($\downarrow T_L$)

$P_{\text{cond}} = P_{\text{sat}}$ at T_L and T_L here is usually not controlled

it is obtained by lake, river or ocean water

2- Superheating the steam to high temperatures ($\uparrow T_H$)

The temperature T_H is also limited to assure that the metals can handle it

3- Increasing the boiler temperature ($\uparrow T_H$)

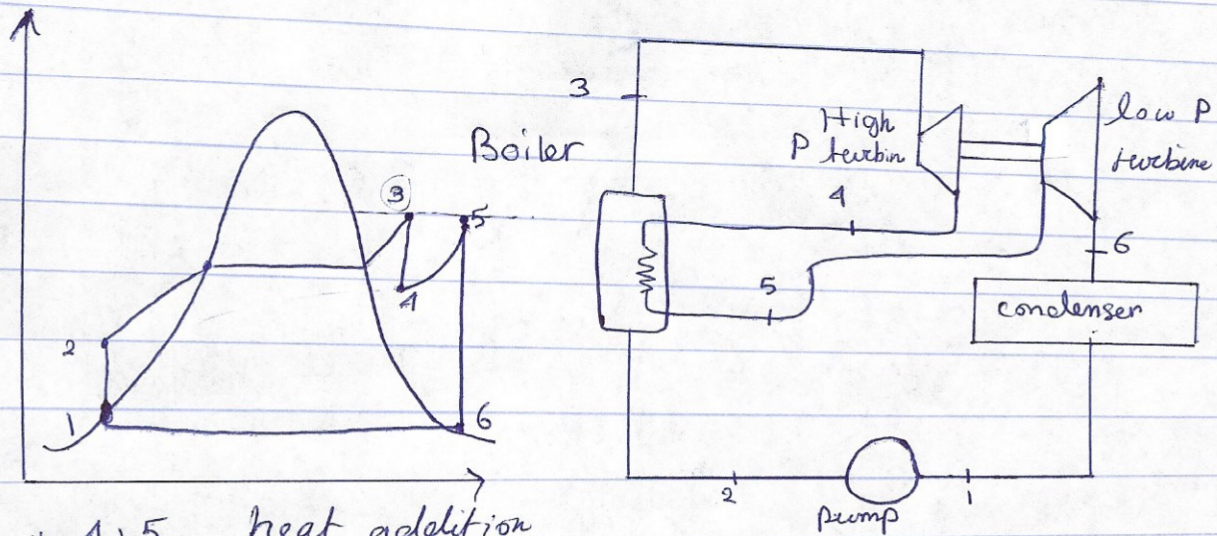
the moisture content of the steam at the turbine exit increases this results in the cavitation of the turbine blades

The ideal re-heat Rankine cycle

The expansion process takes place in two stages

1- high pressure stage

2- low pressure stage



* 4 → 5 heat addition
at a lower pressure

$$Q_H = Q_{\text{primary}} + Q_{\text{reheat}} \\ = (h_3 - h_2) + (h_5 - h_4)$$

$$W_T = W_{\text{Low T}} + W_{\text{High T}} = (h_3 - h_4) + (h_5 - h_6)$$

$\eta \uparrow$ by 1 to 5 percent

Notice that $P_4 = P_5 = P_{\text{reheat}}$

- This cycle will increase the efficiency and yet avoid moisture in the steam in the turbine

The ideal regenerative rankine cycle

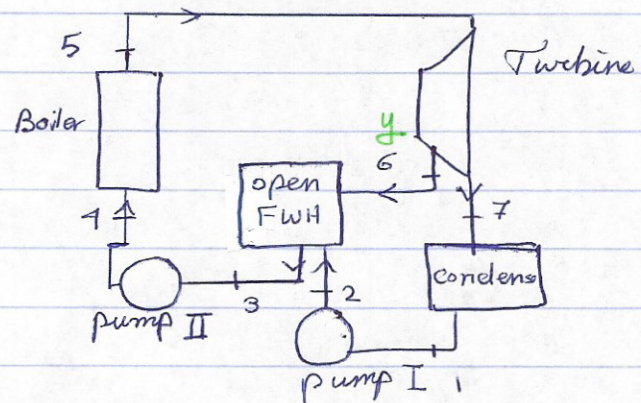
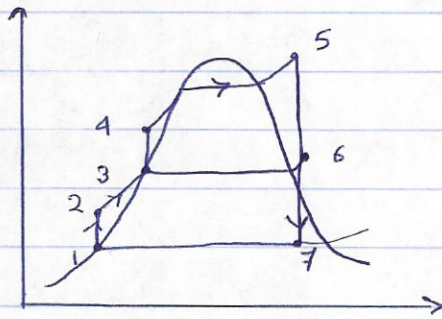
FWH: regenerator or Feed water heater

Types of FWH:

- 1- closed FWH
- 2- Open FWH = Mixing chamber

1- open FWH (Direct contact)

In an open FWH we mix the steam with water coming out of the pump



$$q_H = h_5 - h_4$$

$$q_L = (1-y)(h_7 - h_1)$$

$$W_T = (h_5 - h_6) + (1-y)(h_5 - h_7)$$

$$W_p = (1-y) W_{\text{pump I}} + W_{\text{pump II}}$$

$$\downarrow \qquad \qquad \downarrow$$

$$(\rho_1(P_2 - P_1)) \quad (\rho_3(P_4 - P_3))$$

6, 2 have same pressure

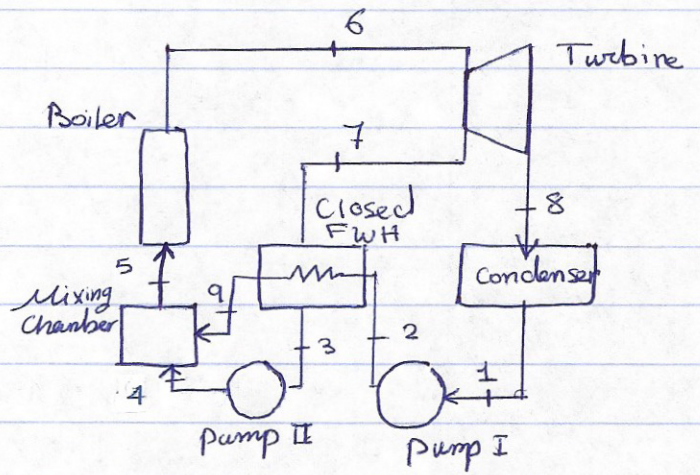
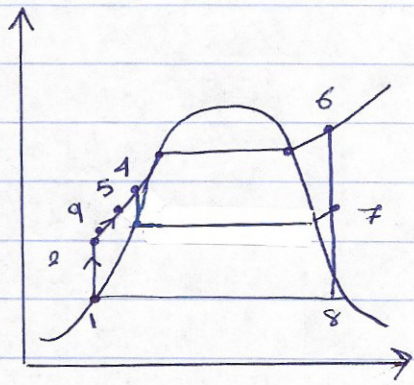
$$y = \frac{\dot{m}_6}{\dot{m}_5} \quad 0 < y < 0.2$$

• water coming out of 2 mixes with steam making a sat liq

2- Closed FWH

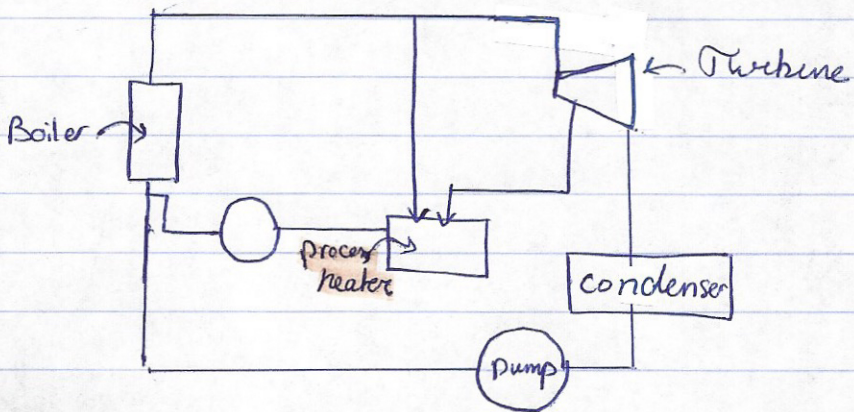
No mixing occurs, so two streams can have diff pressures

$$P_{73} \neq P_{29} \quad \text{But} \quad P_4 = P_9$$



Cogeneration:

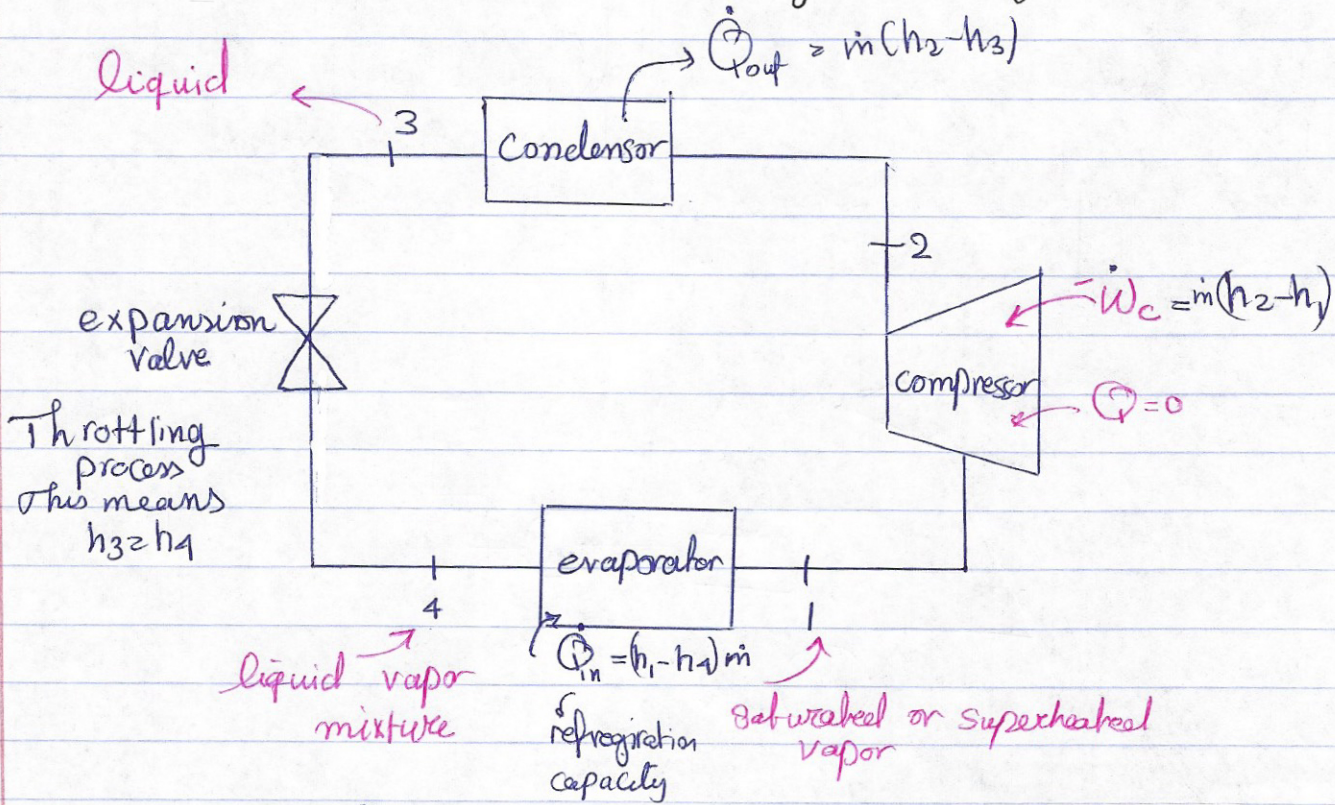
- we use the already existing work potential as a process heat
↳ energy input in the form of heat



combined Gas-Vapor power cycle

- operates at higher temp than steam cycle
- can achieve high thermal efficiencies up to 60%

9.9 Vapor-Compression Refrigeration cycle



$$\text{COP: } \beta = \frac{Q_{in}}{W_c} = \frac{h_1 - h_4}{h_2 - h_1}$$

ton of refrigeration
= 211 kJ/min
(power unit)

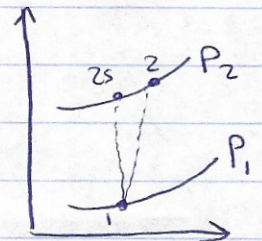
$$\beta_{max} = \frac{T_c}{T_H - T_c} \Rightarrow \text{Carnot coefficient of performance}$$

Actual vapor-compression cycle

$$W_{act} > W_s \text{ in compressor}$$

• Isentropic efficiency of the compressor

$$\eta_c = \frac{h_{2s} - h_1}{h_2 - h_1}$$



The vapor-compression heat pump cycle

coefficient of performance

$$\gamma = \frac{h_2 - h_3}{h_2 - h_1} = \frac{\dot{Q}_{out}}{\dot{W}_c}$$

Carnot γ γ γ

$$\gamma_{max} = \frac{T_H}{T_H - T_C} \approx T_L$$