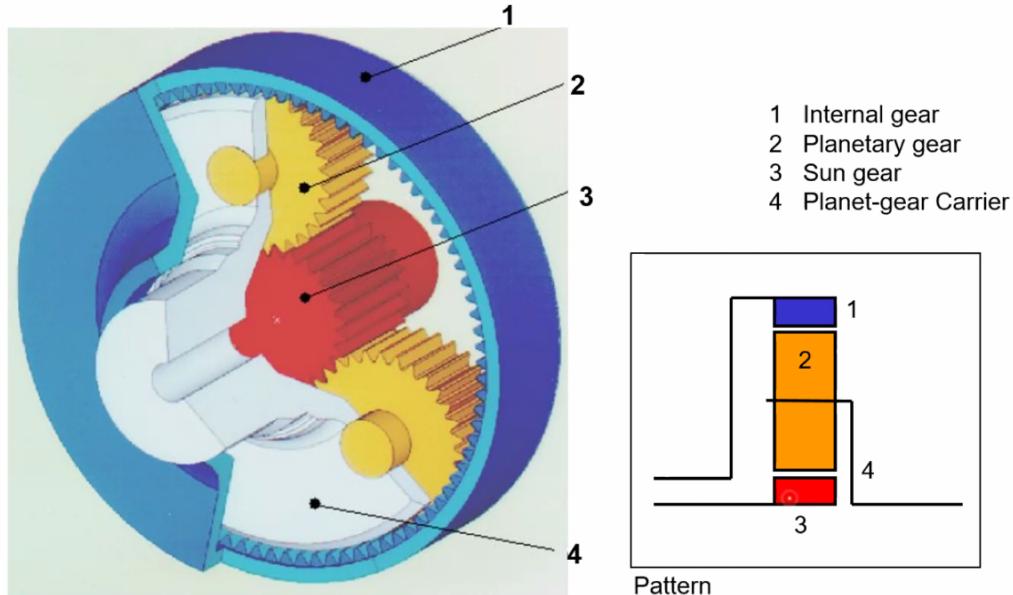


# planetary transmission : Simple planetary gear

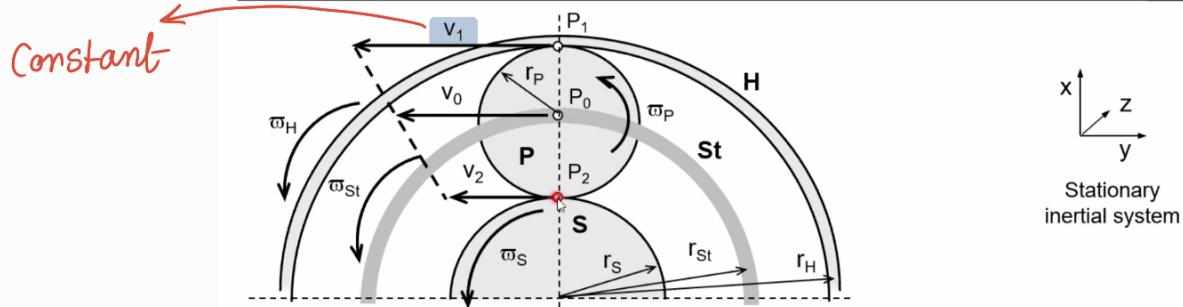


Components : Sun gear, ring gear , planetary gear and carrier

watch video : important

- ring gear Fixed  
or
- Sun gear Fixed  
or
- Carrier Fixed

## Kinematics of a Simple Planetary Gear Transmission



### Preliminary remarks:

- The simple planetary transmission possesses 2 degrees of freedom
- If the 3 angular velocities  $\omega_H$ ,  $\omega_S$  and  $\omega_{St}$  are introduced as general coordinates, there is a forced condition (kinematic bond) between them that leads to the basic equation of the planetary transmission

### Derivation of the basic equation:

- Considering the absolute velocities of the points  $P_0$ ,  $P_1$  and  $P_2$  within the inertial system, this results in:  $v_1 = r_H \cdot \omega_H$ ,  $v_2 = r_S \cdot \omega_S$  and  $v_0 = r_{St} \cdot \omega_{St}$
- The parallel velocity vectors  $v_1$  and  $v_2$  form a trapeze where the distance between  $v_1$  and  $v_0$  and between  $v_2$  and  $v_0$  equals the planetary radius  $r_P$

## Kinematics of a Simple Planetary Gear Transmission

Thus, it is valid that

$$v_0 = \frac{v_1 + v_2}{2} \Rightarrow 2 \cdot v_0 = v_1 + v_2$$

$$2 \cdot r_{St} \cdot \omega_{St} = r_H \cdot \omega_H + r_S \cdot \omega_S$$

Furthermore:  $r_{St} = r_H - r_P$

$$\begin{aligned} r_{St} &= r_S + r_P \\ 2 \cdot r_{St} &= r_H + r_S \end{aligned}$$

$$(r_H + r_S) \cdot \omega_{St} = r_H \cdot \omega_H + r_S \cdot \omega_S$$

- If the equation above is divided by  $r_S$  and if the angle-of-rotation velocities  $\omega_H$ ,  $\omega_S$  and  $\omega_{St}$  are substituted by the speeds  $n_H$ ,  $n_S$  and  $n_{St}$ , the basic equation results in

$$\left( \frac{r_H}{r_S} + 1 \right) \cdot n_{St} = \frac{r_H}{r_S} \cdot n_H + n_S$$

- The ratio of the rolling-circuit radii  $r_H / r_S$  equals the (negative) transmission ratio of the planetary stationary transmission where the bar is retained ( $n_{St}=0$ ).

$$n_{St} = 0 \Rightarrow \frac{r_H}{r_S} \cdot n_H + n_S = 0 \Rightarrow \frac{n_S}{n_H} = -\frac{r_H}{r_S}$$

With stationary transmission ratio:  $i_0 = \frac{r_H}{r_S}$

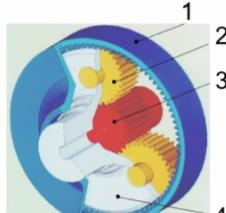
$$(i_0 + 1) \cdot n_{St} = i_0 \cdot n_H + n_S$$

Stationary Gear ratio

Carrier

sum gear  
ring gear  
(internal gear)

⇒ possible transmission ratios



- 1 Internal gear
- 2 Planetary gear
- 3 Sun gear
- 4 Bar  
(Planet-gear carrier)

$$(i_0 + 1) \cdot n_{St} = i_0 \cdot n_H + n_S$$

By clutches (Braked  $\Rightarrow n_{St} = 0$ )

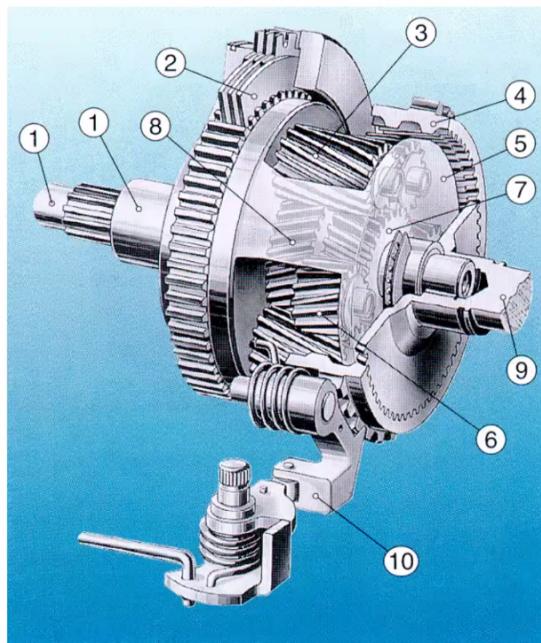
Input	Output	Braked	Transmission i	Conventional transmissions i for $i_0 = 2 \Leftrightarrow 4$
Sun gear	Internal gear	Planet-g. carrier	$i = -i_0$	$i = -4 \Leftrightarrow -2$
Internal gear	Sun gear	Planet-g. carrier	$i = 1 / (-i_0)$	$i = -0.5 \Leftrightarrow -0.25$
Sun gear	Planet-g. carrier	Internal gear	$i = 1 + i_0$	$i = 3 \Leftrightarrow 5$
Planet-g. carrier	Sun gear	Internal gear	$i = 1 / (1 + i_0)$	$i = 0.2 \Leftrightarrow 0.3$
Internal gear	Planet-g. carrier	Sun gear	$i = 1 + (1/i_0)$	$i = 1.25 \Leftrightarrow 1.5$
Planet-g. carrier	Internal gear	Sun gear	$i = i_0 / (1+i_0)$	$i = 0.67 \Leftrightarrow 0.8$

$$i_0 = \text{Radius}_{\text{Int. gear}} / \text{Radius}_{\text{Sun gear}} = \text{stationary transmission ratio}$$

Degrees of freedom of the System: 2  
 ↙  
 simple planetary gear

## Ravigneaux Planetary Gear Set

Two gear sets nested into each other joint by a planet gear carrier.



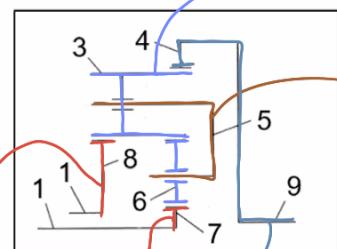
- 1 Drive shafts
- 2 Multidisc clutch
- 3 Broad planetary gear
- 4 Internal gear
- 5 Planet-gear carrier
- 6 Narrow planetary gear
- 7 Small sun gear
- 8 Big sun gear
- 9 Output
- 10 Parking lock

2 Planetary gears

1 planetary gear Carrier

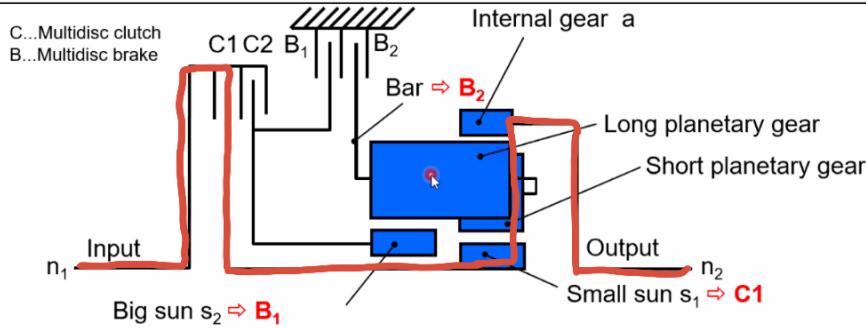
2 sun gears

1 internal gear



Pattern

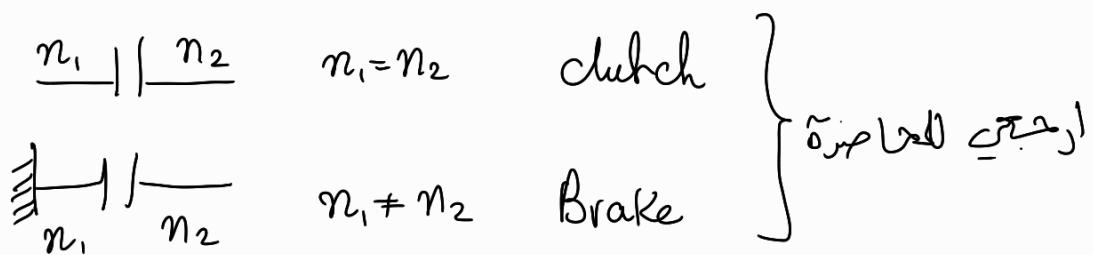
## Ravigneaux Planetary Gear Set



Gear 1  $\rightarrow$   $n_1 = n_2$   
 $B_2, C_1 \rightarrow$  engagement

Combining the different clutches results in the following transmission possibilities:

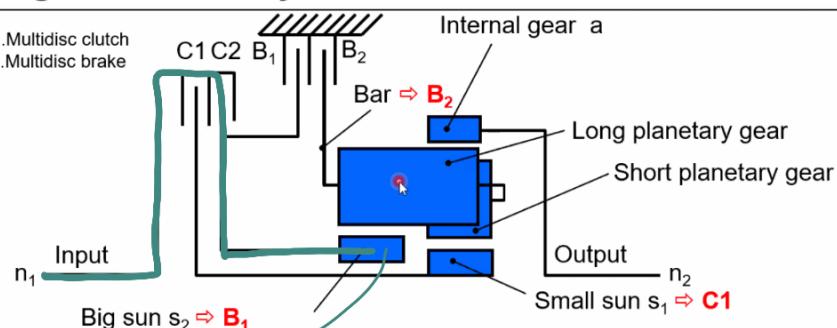
Gear	1	2	3	R
C1	●		●	
C2			●	●
B1		●		
B2	●			●
$i = \frac{n_1}{n_2}$	$\frac{Z_a}{Z_{S1}}$	$\frac{1 + \left( \frac{Z_{S2}}{Z_{S1}} \right)}{1 + \left( \frac{Z_{S2}}{Z_a} \right)}$	1	$-\frac{Z_a}{Z_{S2}}$



Reverse gear  $\rightsquigarrow$  ( بدو )

See Recording 50min

## Ravigneaux Planetary Gear Set



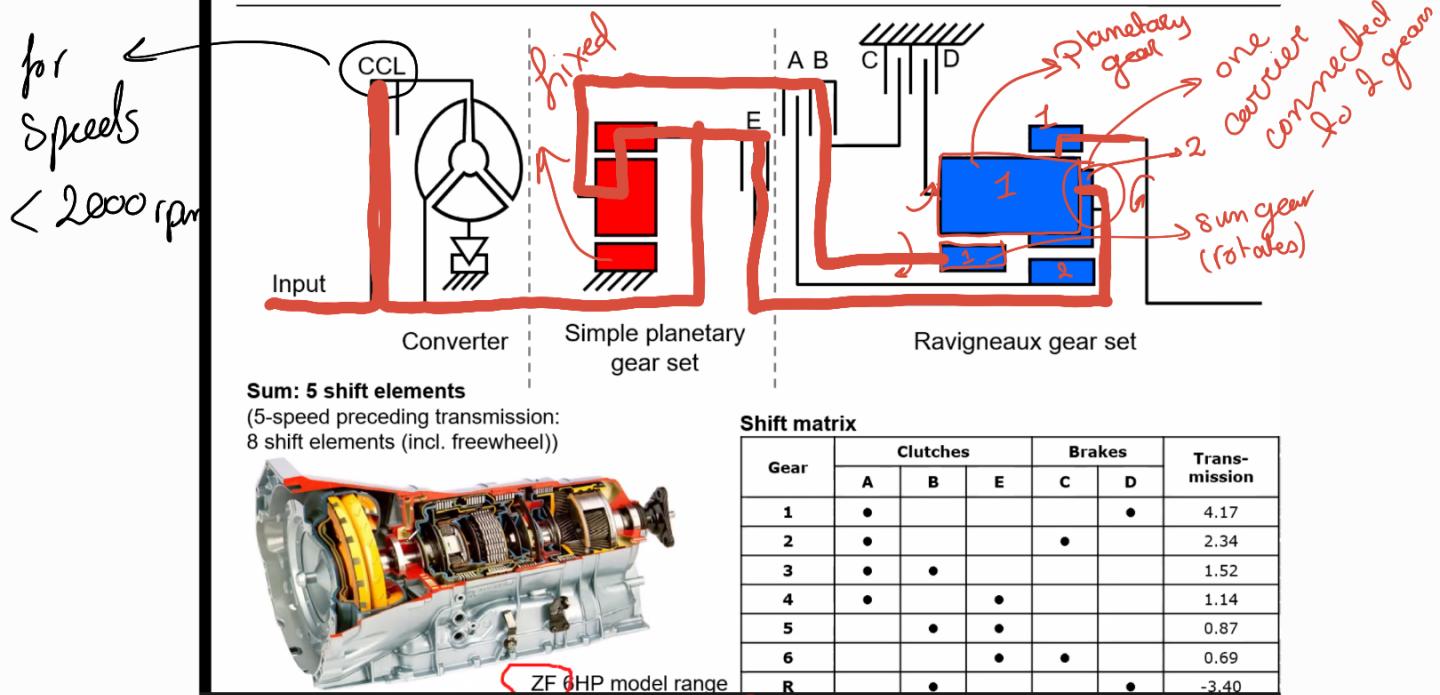
Combining the different clutches results in the following transmission possibilities:

Gear	1	2	3	R
C1	●	●	●	
C2			●	●
B1		●		
B2	●			●
$i = \frac{n_1}{n_2}$	$\frac{Z_a}{Z_{S1}}$	$\frac{1 + \left( \frac{Z_{S2}}{Z_{S1}} \right)}{1 + \left( \frac{Z_{S2}}{Z_a} \right)}$	1	$-\frac{Z_a}{Z_{S2}}$

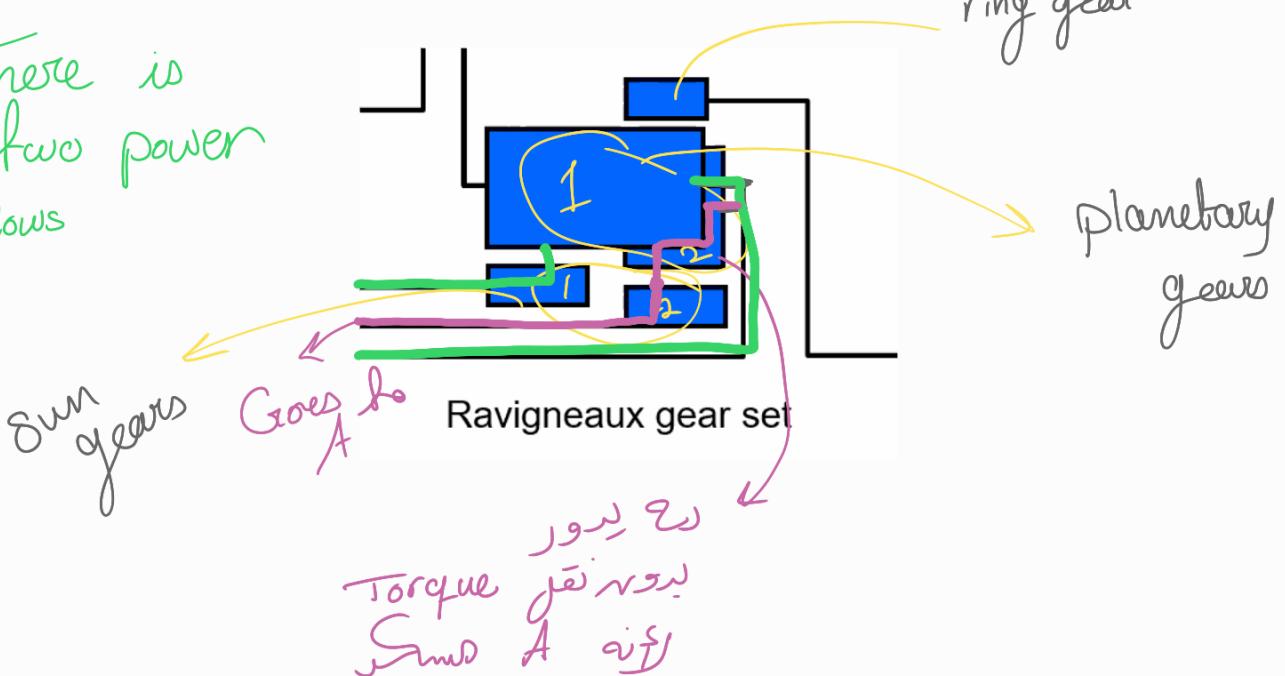
# Gear 5

## 6-Speed AT according to Leppeletier

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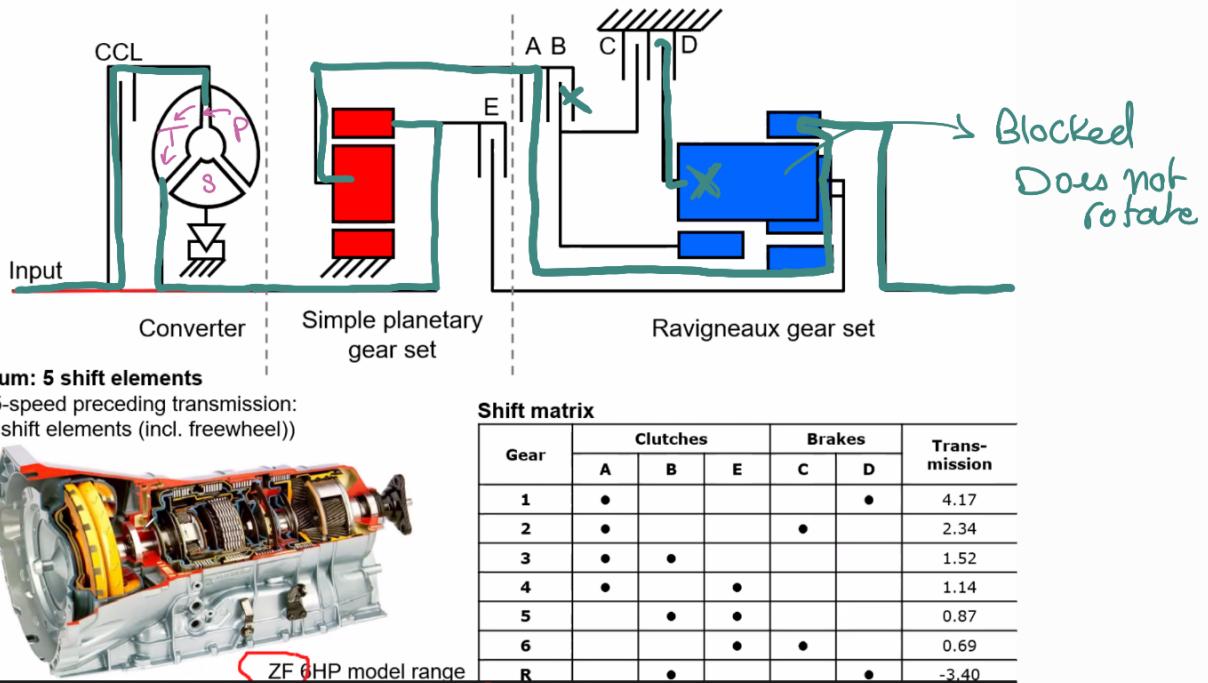


There is two power flows

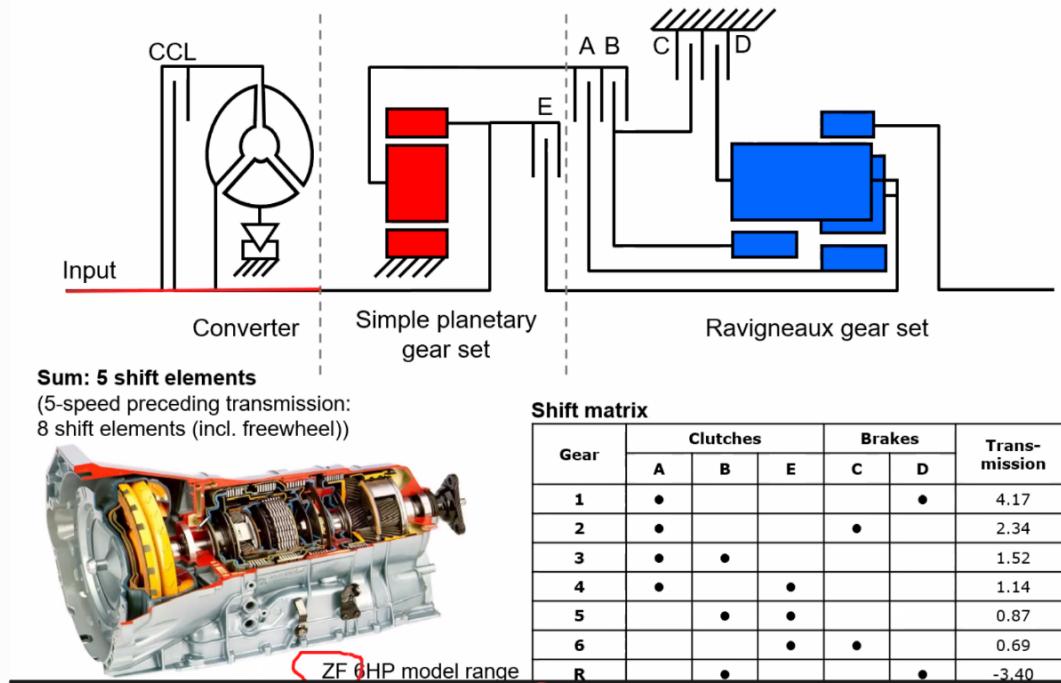


# Gear 1

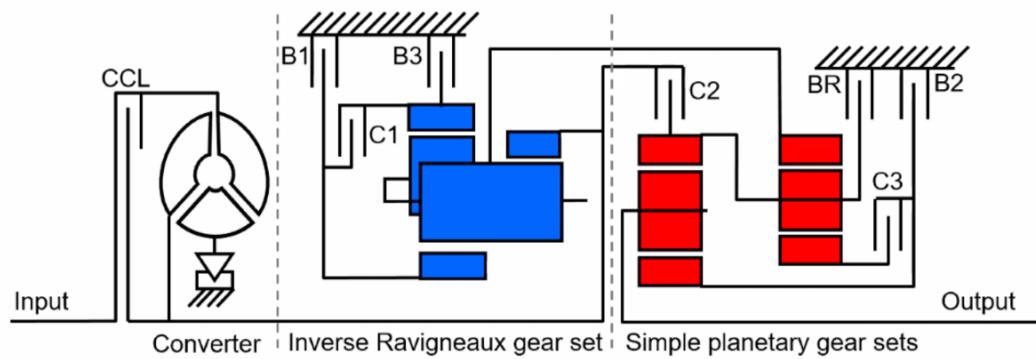
## 6-Speed AT according to Lepeletier



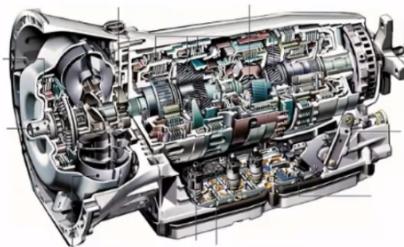
## 6-Speed AT according to Lepeletier



## 7-Speed AT according by DaimlerChrysler principle



Sum: 7 shift elements



Shift matrix

Gear	Clutches			Brakes			
	C1	C2	C3	B1	B2	B3	BR
1						•	
2				•	•	•	
3	•			•		•	
4	•		•			•	
5	•	•	•				
6		•	•	•			
7	•	•	•				•
R1				•		•	•
R2		•	•			•	•

2 speeds for reverse  
Gears 5, 6, 7 as help to downshift

## 7-Speed AT according by DaimlerChrysler principle

