

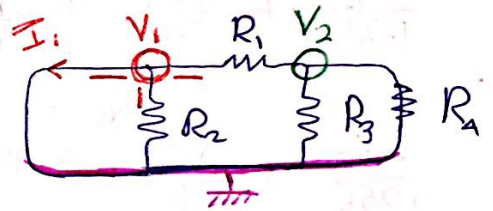
Chapter 4: Techniques of Circuit Analysis ⁽¹⁾

- Nodal Analysis
- Mesh Analysis
- Source Transformation
- Super Position
- Thevenin's Circuit
- Norton's Circuit
- Maximum Power Transfer

Nodal Analysis :-

To define Nodes :-

A node : a point that lines intersects



To use This technique :

→ You need to specify a Node where V is zero
Here it's colored in pink

→ other Nodes should gather 2 elements or more
And you should be able to find an equation
for each current :

Ex: At V_1 you can obtain :-

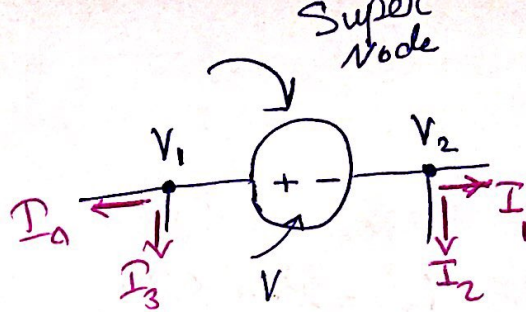
$$\frac{V_1 - V_2}{R_1} + \frac{V_1}{R_2} + \underbrace{I_1}_{\text{You can't find it's equation}} = 0$$

So this Node is useless

At V_2 you can obtain :-

Remark:

Super Node



Here: $V_1 - V_2 = V$

- And you cannot combine the two nodes in one equation

The Eq: $I_a + I_3 + I_1 + I_2 = 0$

Mesh Analysis

To define meshes

A mesh: A loop that contains no other loops

To use this technique:-

- You need to determine meshes and name them
- use Kirchoff's voltage law:-

Here:-

At I_1 ↑:-

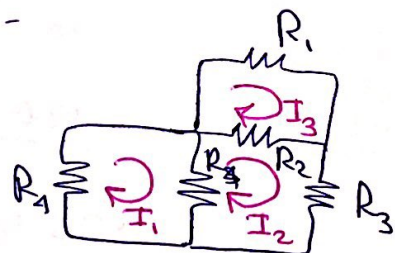
$$R_4(I_1) + (I_1 - I_2)R_4 = 0$$

At I_2 ↑

$$R_3(I_2) + R_2(I_2 - I_3) + R_4(I_2 - I_1)$$

At I_3 ↑

$$R_1 I_3 + R_2(I_3 - I_2)$$



The current of your first current mesh comes first

↑ when a resistance is between two meshes you take the difference of currents

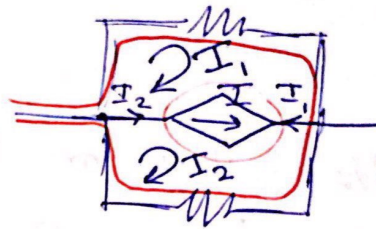
Remark

Super Mesh

- It occurs when there is a Current Source Between two Meshes

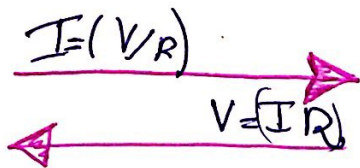
$$I_2 - I_1 = I$$

You Can Go in the Real path as shown



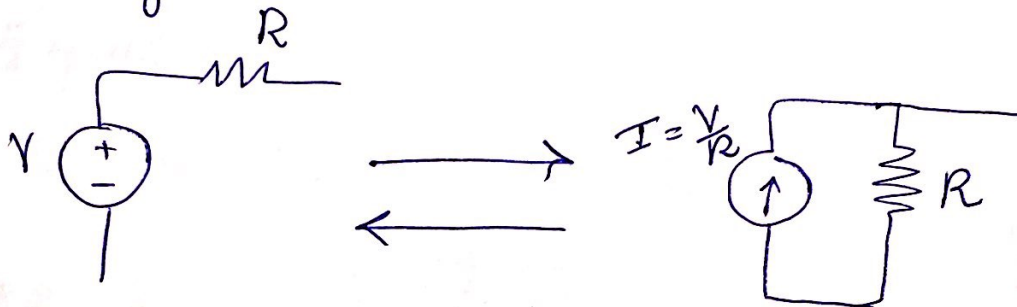
Source Transformation

Voltage Source
+ Resistance
(series)

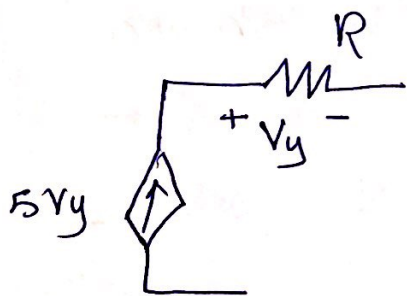


Current Source
+ Resistance
(parallel)

- R stays the same



- Remark: If the Voltage or Current Source are dependant Then if the Source That it depends on is in the area of Transforming You Cannot Transform



You Can't transform this

Super Position :

- Currents and Voltages Come from different Sources in the Circuit so you can kill one source, find ~~the other's~~ I and V then kill the other source and find the others I and V
- If it's a Voltage source you can kill it by making a short circuit
- If it's a Current source you can kill it by making an open circuit

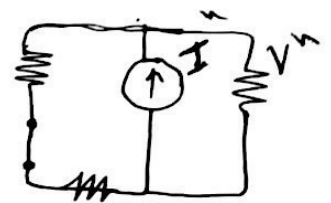
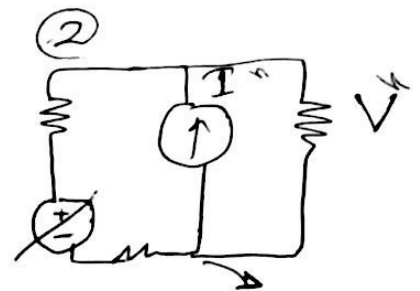
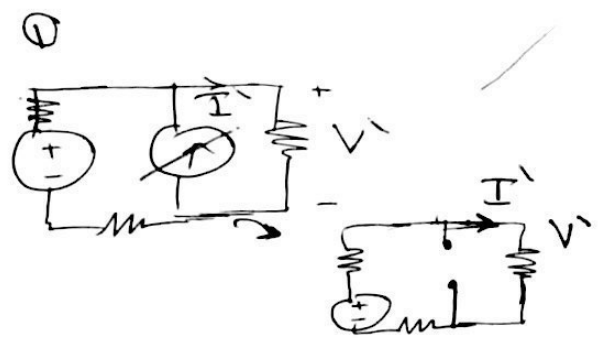
$$I = I' + I''$$

$$V = V' + V''$$

I' and V' are in ①

I'' and V'' are in ②

Ex:



- Thevenin Circuit -

↳ There are 3 Cases :-

1] Circuit Contains Only independent Sources
 $R_{th} = R_{eq}$ after killing all sources
 $V_{th} = V_{oc}$

2] Circuit Contains dependent and independent Sources

$$R_{th} = \frac{V_{th}}{I_{sc}}$$

3] Circuit Contains only dependent Sources

$$R_{th} = \frac{V_T}{I_T} \quad \text{Dead Circuit}$$

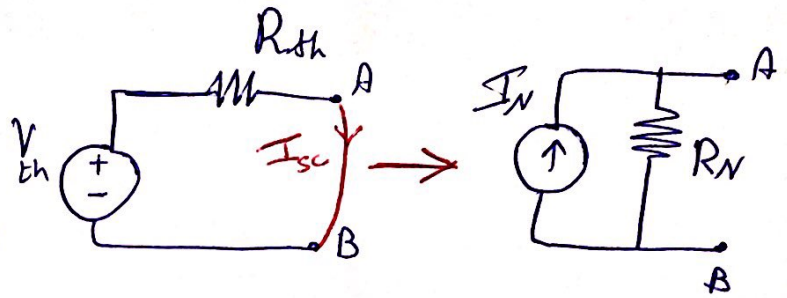
$$V_{th} \text{ here} = 0$$

• You put a V_T and you find I_T
or you put I_T and you find V_T

Norton Circuit

$$I_{sc} = I_N$$

• and R_N can be found depending on the case



Assessment Problem: P139

$$I_N = I_3$$

$$I_1 = 15A$$

$$I_2$$

$$8(I_2 - I_1) + 2I_2 + 12(I_2 - I_3) + 10I_2 = 0$$

$$12(I_3 - I_2) = 0$$

$$8(I_2 - 15) + 2I_2 + 12(I_2 - I_3) + 10I_2 = 0$$

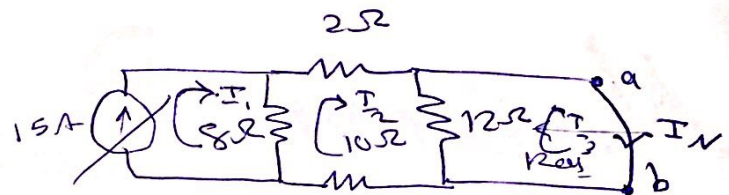
$$32I_2 - 12I_3 = 120$$

$$I_3 = I_2$$

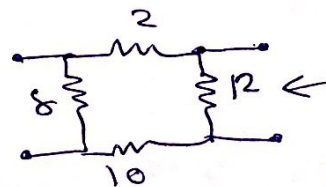
$$32I_2 - 12I_2 = 120$$

$$I_2 = 6$$

$$I_3 = 6 = I_N$$



$R_N =$



Maximum Power transfer

$$P_{L_{max}} = \frac{V_{th}^2}{4R_L}$$

$$R_L = R_{th}$$

