

Torque-Speed characteristics

- At no load $n_{sync} \approx n_m$ (near) \rightarrow small slip \rightarrow small $I_R \rightarrow$ small $B_R \rightarrow$ small T_{ind} \nearrow E_{ind} is low
 - At heavy load \rightarrow slip increases \rightarrow Rotor speed $n_m \downarrow \rightarrow$ larger $I_R \rightarrow$ larger $B_R \rightarrow \delta \uparrow$ But $B_R \uparrow \rightarrow$ larger T_{ind}
- $\sin \delta$ keep decreasing until it's almost = 0, at this point, increasing load decreases T_{ind}
- This is called **pullout torque**

Modeling

$$T_{ind} = K B_R B_{net} \sin \delta$$

- K is a constant
- $B_R \propto I_R \rightarrow I_R \propto s \rightarrow s \propto \frac{1}{n_m}$
- $B_{net} \propto E_1 \rightarrow E_1$ assumed constant
- $\delta \propto s \rightarrow s \propto \frac{1}{n_m}$ ($\sin \delta \downarrow$ when $s \uparrow$)

Note: $\delta = \theta_R + 90^\circ$

$$\sin \delta = \frac{\sin(\theta_R + 90^\circ)}{\cos \theta_R}$$

$\cos \theta_R = \text{PF of Rotor}$

$$\theta_R = \tan^{-1}(sX_R / R_R)$$

Characteristics curve Regions

1- low slip Region $0.01 < s < 0.07$

- In this region, s increases linearly and n_m decreases linearly
- X_R negligible, $\text{PF} \approx 1$
- I_R increases linearly with s
- Normal operating range of an induction motor

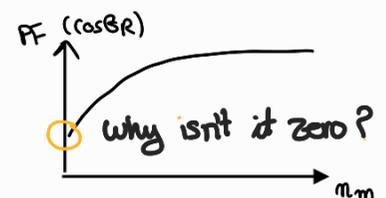
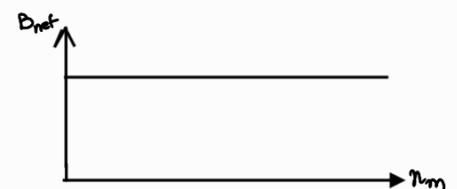
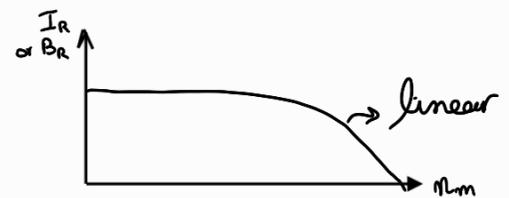
2- Moderate slip Region

- PF drops
- I_R does not increase rapidly with s
- Peak torque occurs (pullout torque) $\rightarrow T_{pullout} \approx 200-250\% T_{rated}$

3- High slip Region

- $T_{ind} \downarrow$ when load \uparrow
- Increase in I_R is totally overshadowed by decrease in PF_R

Starting torque $\approx 150\%$ of $T_{rated} \rightarrow$ So IM can be started at full load



Because

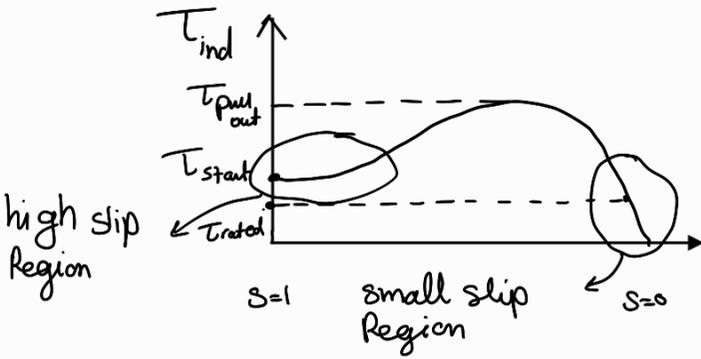
$$\text{PF} = \cos \left(\tan^{-1} \frac{sX_R}{R_R} \right)$$

These are physical parameters

and cannot become zero

لماذا هذا ال motor قادر على البدء بجهد عالي كيت

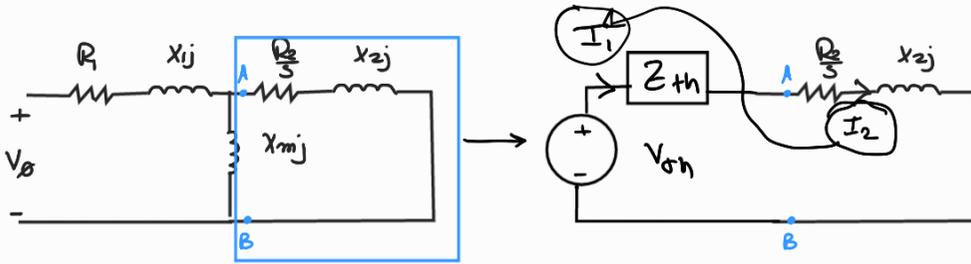
why is T_{start} is high Because PF is never zero



Deriving induction Torque equation

$$T_{ind} = \frac{P_{AG}}{\omega_{sync}}$$

Thevenin equivalent



$$V_{Th} = V_{oc}$$

$$V_{Th} = \frac{V_0 X_{mj}}{R_1 + (R_1 + X_{mj})j} \quad (\text{voltage divider})$$

$$|V_{Th}| = \frac{|V_0| \sqrt{X_m^2}}{\sqrt{R_1^2 + (R_1 + X_m)^2}} = \frac{V_0 X_m}{\sqrt{R_1^2 + (R_1 + X_m)^2}}$$

$$Z_{Th} = Z_{eq} = R_m + X_{Thj}$$

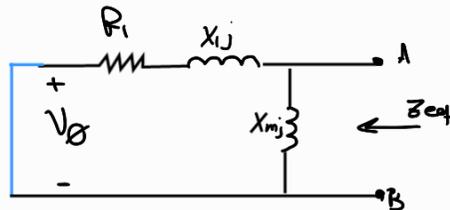
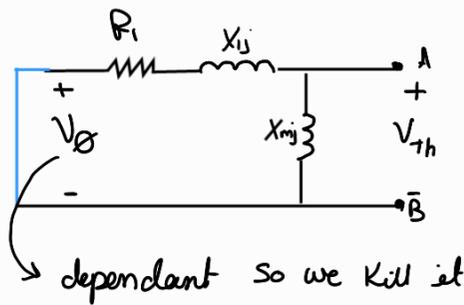
$$\text{Where } Z_{eq} = (R_1 + X_{1j}) \parallel (X_{mj}) = \frac{(R_1 + X_{1j}) X_{mj}}{(R_1 + X_{1j}) + X_{mj}}$$

$$\text{If } X_m \gg X_1, X_m \gg R_1$$

$$V_{Th} \approx \frac{V_0 X_m}{X_1 + X_m}$$

$$R_{Th} \approx R_1 \left(\frac{X_m}{X_1 + X_m} \right)^2, \quad X_{Th} \approx X_1$$

$$I_1 = \frac{V_{Th}}{Z_{Th} + \frac{R_2}{s} + X_{2j}}$$

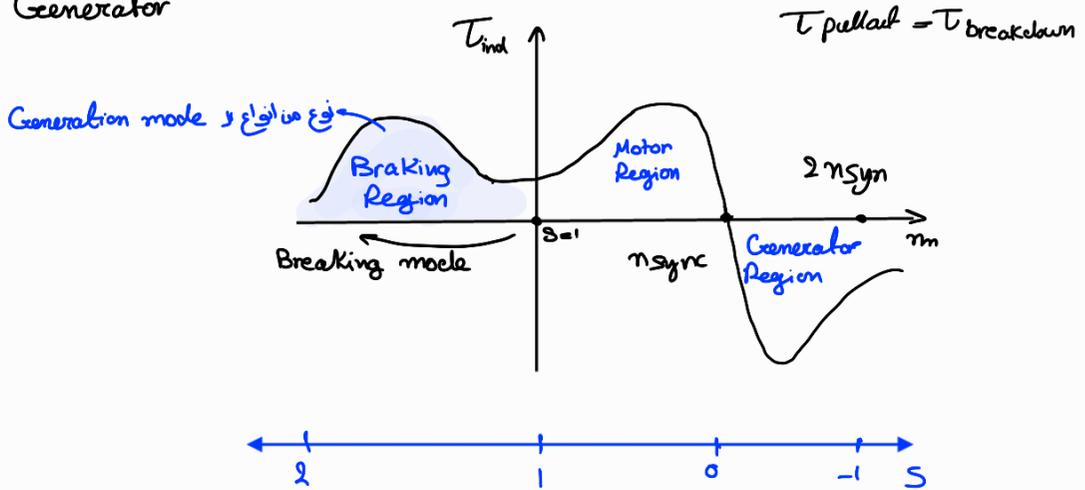


We know that $P_{AG} = 3I_2^2 \frac{R_2}{s}$

$$T_{ind} = \frac{3I_2^2 \frac{R_2}{s}}{\omega_{sync}} = 3 \times \left(\frac{V_{Th}}{Z_{Th} + \frac{R_2}{s} + X_{2j}} \right)^2 \times \frac{R_2}{s} / \omega_{sync}$$

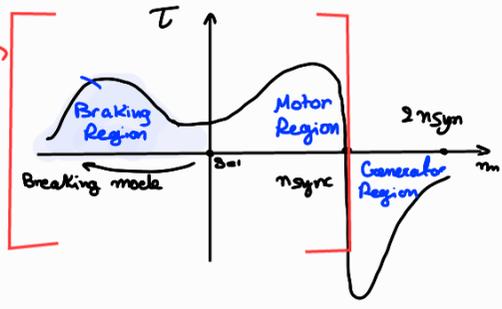
$$T_{ind} = \frac{3 \times \left[\frac{V_{Th}^2}{(R_m + \frac{R_2}{s})^2 + (X_{Th} + X_L)^2} \right] \times \frac{R_2}{s}}{\omega_{sync}}$$

$n > n_{sync} \rightarrow$ Generator

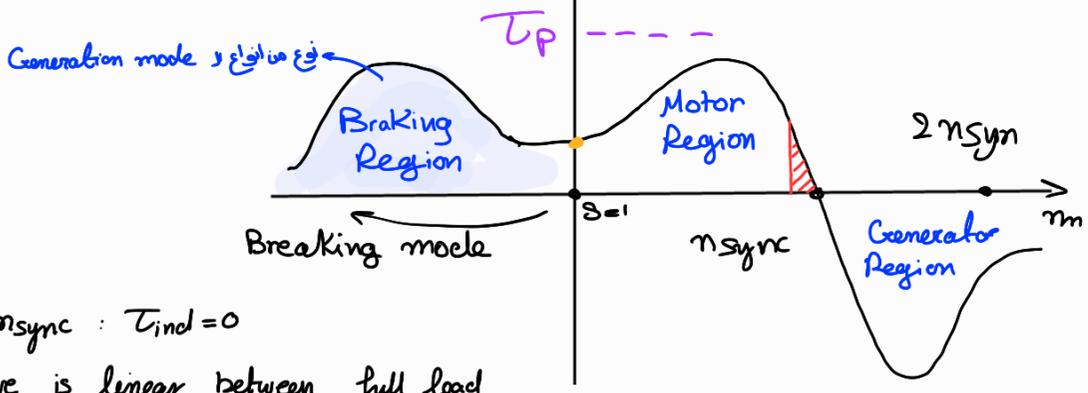


For new cars

working region \leftarrow



$n > n_{sync} \rightarrow$ Generator



At $n_{sync} : T_{ind} = 0$

* curve is linear between full load and no load

* $T_{max} = T_{pullout} = 2-3 T_{rated}$

* starting $T = 1.5 T_{rated}$

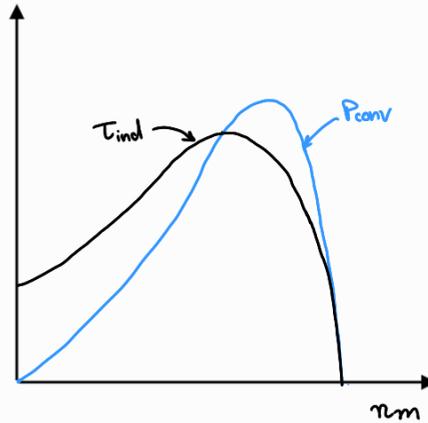
T_{ind} depends on: \checkmark (Voltage app)²
 $\checkmark n_{sync}$

How does Braking occur?

When the magnetic field rotation is reversed by switching two stator phases the motor will be turning backward relative to it, T_{ind} will stop the machine rapidly (braking) (plug reversal) \rightarrow This is called plugging

Converted power

- $P_{conv} = T_{ind} \omega_m$
- P_{max} occurs at different speed to T_{max}



Maximum Pullout Torque

Pullout torque when power consumed by $\frac{R_2}{s}$ is highest

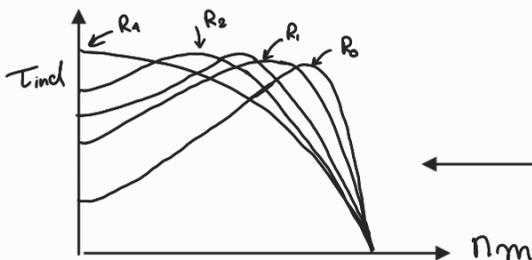
$$\frac{R_2}{s} = \sqrt{R_{Th}^2 + (X_{Th} + X_2)^2}$$

$$s_{max} = \frac{R_2}{\sqrt{R_{Th}^2 + (X_{Th} + X_2)^2}}$$

$$T_{max} = \frac{3 V_{Th}^2}{2 \omega_{sync} \left[R_{Th} + \sqrt{R_{Th}^2 + (X_{Th} + X_2)^2} \right]}$$

Adding resistance to machine impedances:

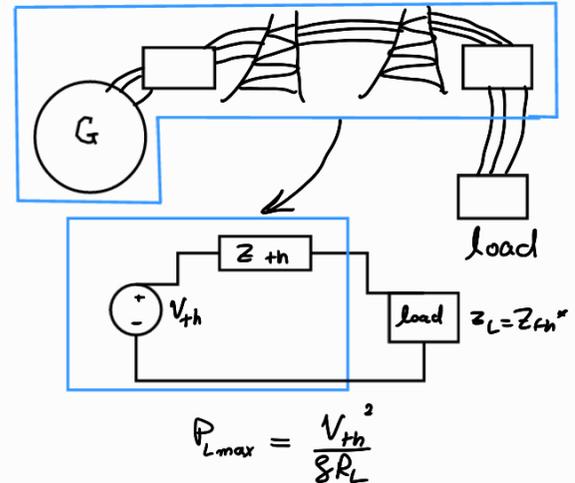
- starting torque
- Max pullout speed



T_{max} :

- Torque is related to the square of the applied voltage
- Torque is also inversely proportional to the machine impedances
- Slip is dependent upon rotor resistance
- Torque is independent to rotor resistance

- T_{max} is independent of R_2
- As R_2 increases s_{max} increases
- Max torque remains constant but pullout speed decreases
- Starting torque increases



$$P_{Lmax} = \frac{V_{Th}^2}{8R_L}$$

Speed Control of induction motors

- 1- pole changing
- 2- Stator voltage control
- 3- Supply Frequency control
- 4- Rotor resistance control

Note:

- Changing Frequency will change reactances and V_{rated}
reducing $f \rightarrow$ increases by factor $f_{new}/f_{old} \rightarrow X_{new} = \frac{f_{new}}{f_{old}} X_{old}$
increasing $f \rightarrow$ decreases by factor $f_{new}/f_{old} \leftarrow$ same f_{old}
- $$V_{rated} = \frac{f_{new}}{f_{old}} V_{old}$$