

Chapter 8

Speed Regulation

↪ Shaft speed ω_m ^{Higher}

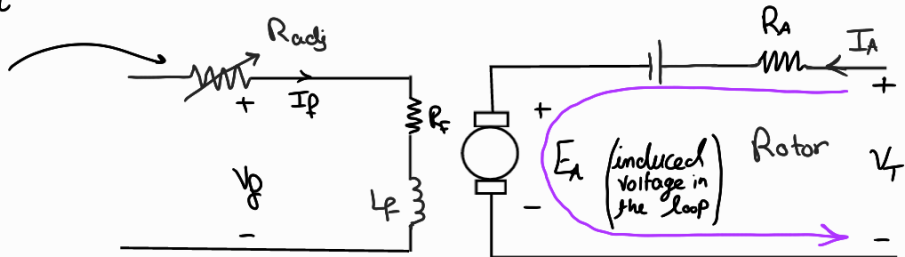
$$SR = \frac{\omega_{m,nl} - \omega_{m,fl}}{\omega_{m,fl}} \times 100\%$$

$$SR = \frac{n_{m,nl} - n_{m,fl}}{n_{m,fl}} \times 100\%$$

- SR should be + but can be negative in Runaway: motor لا يوقف
- In this case vibration causes stator to hit Rotor since air gap is small or (see lecture)

Types of DC motors

1. Permanent magnet
2. Separately excited
3. Shunt
4. Series
5. Compound



$$I_L = I_A$$

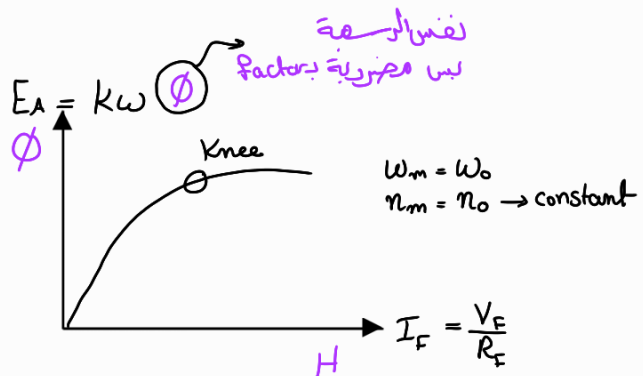
$$I_F = \frac{V_F}{R_F + R_{act}}$$

- I_f can be controlled

$$\left. \begin{aligned} e_{ind} &= K \phi \omega \\ \tau_{ind} &= K \phi I_A \\ V_I + I_A R_A + E_A &= 0 \end{aligned} \right\} \text{Equations needed for Analysis}$$

Magnetization Curve

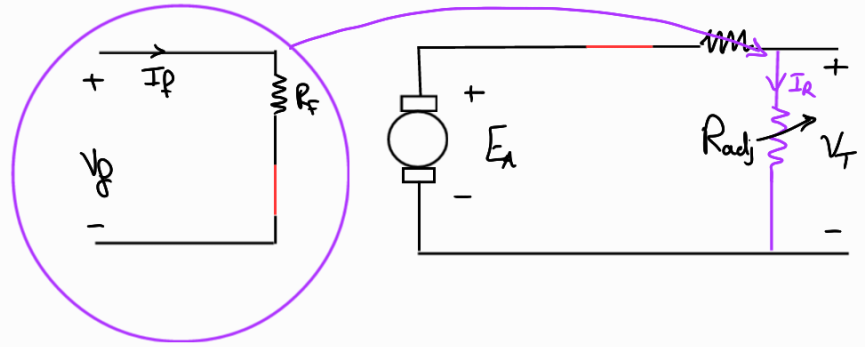
→ we find rated value from it



Shunt DC motor

At: $V_f = V_T$

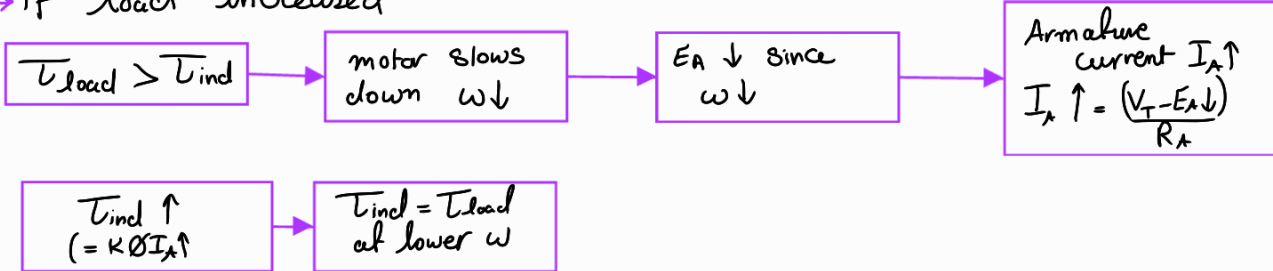
تتبع بتر حالة خاصة من
separately excited



$I_L = I_a + I_f$

* How does a shunt DC motor respond to a load?

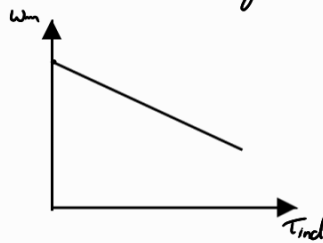
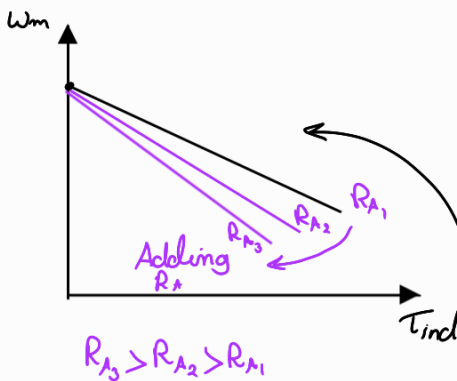
→ If load increased



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The terminal characteristics of a shunt DC motor & separately excited motor

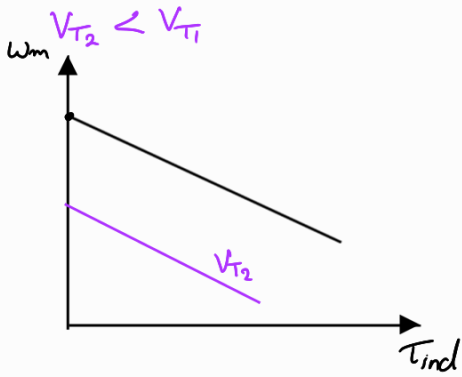
$$\omega = \frac{V_T}{K\phi} - \frac{R_A T_{ind}}{(K\phi)^2}$$



Parameter that controls the DC motor speed

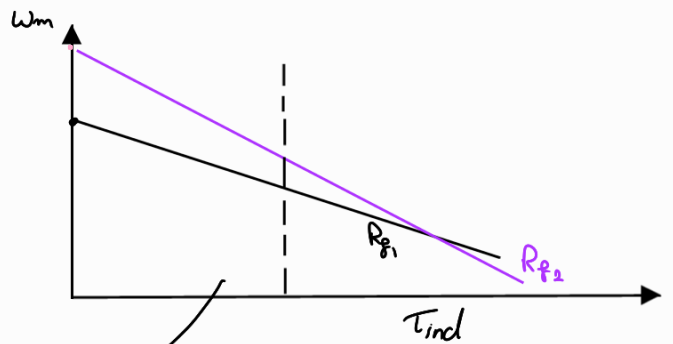
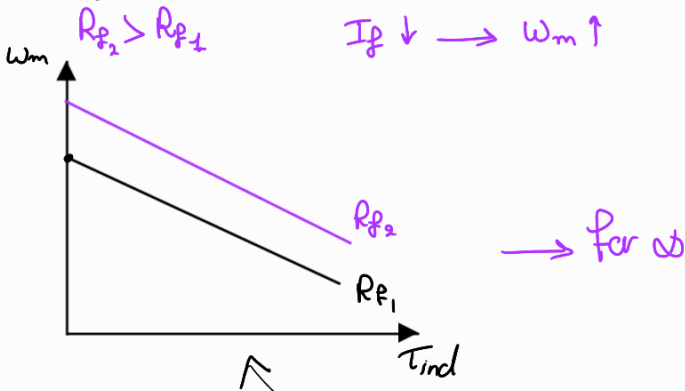
- Terminal voltage of Armature
- Flux by adjusting R_f
- R_A by adding External resistance (R_{ext} is connected on series) meaning that Electrical losses are increased and energy is less so less common method

Decreasing V_T



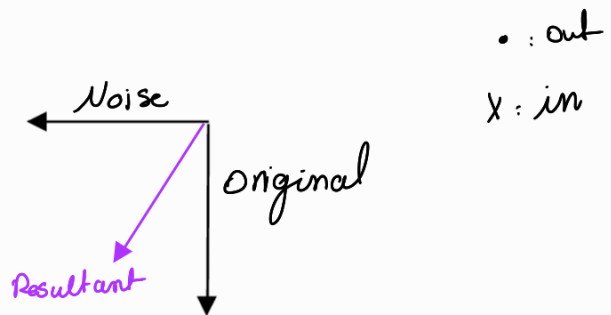
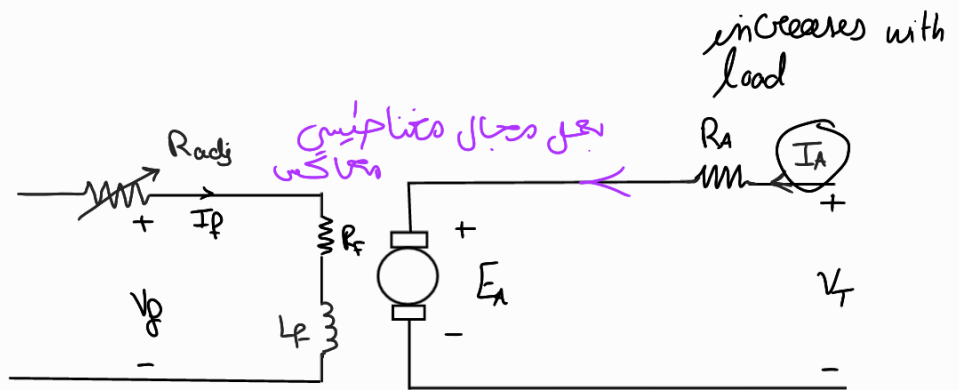
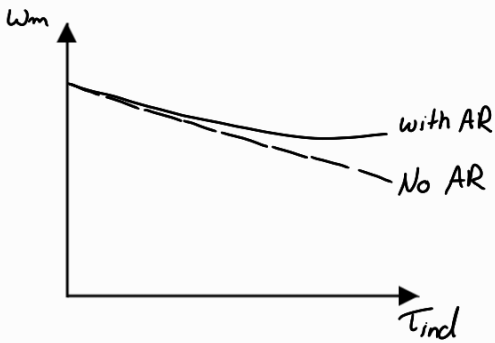
Note: Relation between flux and w_m is not linear

Changing $\phi \rightarrow R_f$



Armature Reaction

Noise Magnetic field



• : out
x : in

• A compensating windings are introduced to reverse the armature windings and so it is neglected

Changing R_F or Flux

1.	Increasing R_F causes I_F to decrease.	$I_F \downarrow = V_T / R_F \uparrow$
2.	Decreasing I_F , \Rightarrow decreases ϕ	-
3.	Decreasing ϕ lowers E_A instantaneously.	$E_A \downarrow = K\phi \downarrow \omega$
4.	Decreasing E_A causes I_A to increase.	$I_A \uparrow = (V_T - E_A \downarrow) / R_A$
5.	Increasing I_A , \Rightarrow increases τ_{ind} Note: $I_A \uparrow$ predominates over $\phi \downarrow$.	$\tau_{ind} \uparrow = K\phi \downarrow I_A \uparrow$
6.	Increasing τ_{ind} causes $\tau_{ind} > \tau_{load}$, hence motor speeds up ($\omega \uparrow$).	-
7.	Since $\omega \uparrow$, E_A increases again.	$E_A \uparrow = K\phi\omega \uparrow$
8.	Increasing E_A causes I_A to decrease.	$I_A \downarrow = (V_T - E_A \uparrow) / R_A$
9.	Decreasing I_A causes τ_{ind} to decrease until $\tau_{ind} = \tau_{load}$ at a higher speed ω	$\tau_{ind} \downarrow = K\phi I_A \downarrow$

بعد عويّة مكيّنة
بجهد الـ flux
يأثر الأخر

Example 8-1

input current = I_L

$$P_{conv} = E_A I_A = T_{ind} \omega_m$$

$$E_{A0} = K\phi\omega_0 \quad . \quad E_{A1} = K\phi\omega_1$$

under ω_0
No load

At no load $E_{A0} = V_T$

Changing terminal voltage

1.	Increasing V_A causes I_A to increase.	$I_A \uparrow = (V_A \uparrow - E_A) / R_A$
2.	Increasing I_A , \Rightarrow increases τ_{ind}	$\tau_{ind} = K\phi I_A \uparrow$
3.	Increasing τ_{ind} causes $\tau_{ind} > \tau_{load}$, hence motor speeds up ($\omega \uparrow$).	-
4.	Since $\omega \uparrow$, E_A increases.	$E_A \uparrow = K\phi\omega \uparrow$
5.	Increasing E_A causes I_A to decrease.	$I_A \downarrow = (V_T - E_A \uparrow) / R_A$
6.	Decreasing I_A causes τ_{ind} to decrease until $\tau_{ind} = \tau_{load}$ at a higher speed ω .	$\tau_{ind} \downarrow = K\phi I_A \downarrow$

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Examples solving

Example 8-3

Rated power = 100 hp

Compensating windings → Armature reaction is ignored

line current = 126 A = I_L

If load is changed: I_A stays constant **Special Case**

$$1. I_A = I_L - I_F \\ = 126 - \frac{250}{41.67} = 120 \text{ A}$$

$$E_{A1} = (R_A)(I_A) + 250 \\ = 250 - (120)(0.03)$$

$$E_A = 246 \text{ V}$$

If $R_F = 50$

Since I_A is constant → $E_{A1} = E_{A2} = 246.4$

$$\frac{E_{A1}}{E_{A2}} = \frac{K \phi_1 n_1}{K \phi_2 n_2} \rightarrow 1 = \frac{\phi_1}{\phi_2} \frac{n_1}{n_2} \rightarrow n_2 = \frac{\phi_1}{\phi_2} n_1$$

we need this

In Magnetization curve

At $I_{F1} = 6 \text{ A} \rightarrow E_{A1} = 268 \text{ A}$

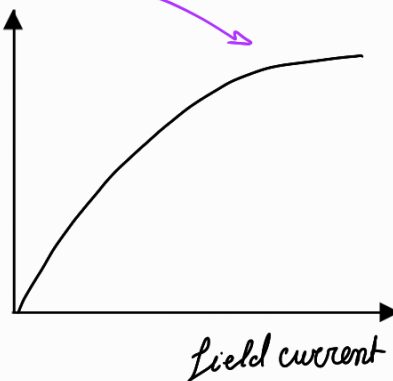
At $I_{F2} = 5 \text{ A} \rightarrow E_{A2} = 250 \text{ A}$

Curve values are at 1200

$$\frac{\phi_1}{\phi_2} = \frac{268}{250} = 1.076 \rightarrow \text{neglect } 1200 \text{ RPM}$$

open circuit voltage

$$n_2 = 1.076 (1103) = 1187 \text{ RPM}$$



Note:

$$n_2 = \frac{E_{A2}}{E_{A1}} n_1$$

If not use

For a Motor

$P_{out} = P_{given}$ if
 • At Full load conditions
 $P_{out} = P_{conv} - P_{core} - P_{losses}$
 if other conditions

Example 8-1

$$V_A = 250V$$

$$I_A = 120A$$

$$n = 1103$$

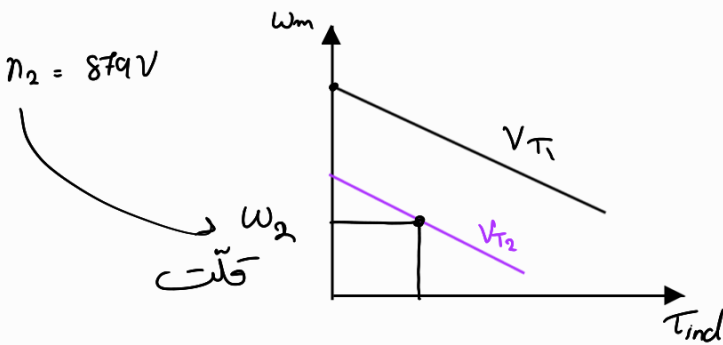
Speed if V_A is reduced to 200V?

$$E_{A1} = 246.4V \text{ at}$$

$$E_{A2} = 200 - (120)(0.03) = 196.4V$$

$$n_2 = \frac{E_{A2}}{E_{A1}} n_1$$

$$n_2 = 879V$$



The permanent Magnet DC motor

Disadvantage : I can't control the flux
Natural magnet losses
it's properties with time

Advantages: 1. No external field circuit is required → no field circuit

Copper losses

2. Smaller because no field circuit

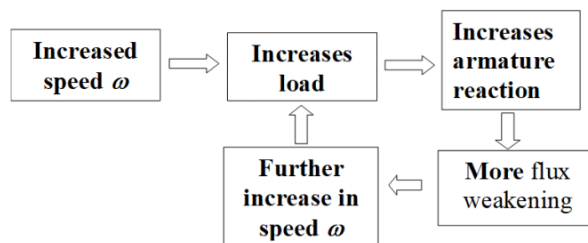
To control speed for this motor:

1. Armature voltage control

2. Armature resistance control

Open field circuit

- If field circuit is disconnected → motor speed increases and becomes uncontrollable → Runaway Condition



This continues until motor overspeeds. This condition is known as runaway.

To stop this:

V_T is shut downed or else the motor will be damaged from high current or vibration

Torque Speed characteristics of series DC motor

Note

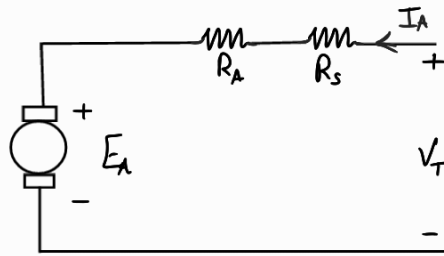
$$P_m = V_T I_L$$

$$V_T = E_A + I_A (R_A + R_S)$$

$$T \propto \omega$$

$$T_{ind} = K \Phi I_A$$

$$\Phi = C I_A$$



$$T_{ind} = K C I_A^2 \quad \text{Non-linear Relationship}$$

$$I_A = \frac{\sqrt{T_{ind}}}{\sqrt{K} \sqrt{C}}$$

ایہ تفسیر ہے کہ current بڑھتی ہے تو I_A بڑھتا ہے
 ادل ما اشدہ بڑھتی ہے High starting current

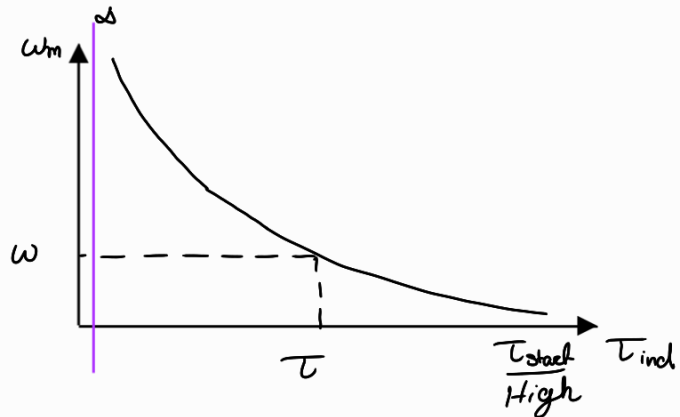
$$V_T = K \Phi \omega + \frac{\sqrt{T_{ind}}}{\sqrt{K} \sqrt{C}} (R_A + R_S)$$

$$\Phi = \frac{\sqrt{C}}{\sqrt{K}} \sqrt{T_{ind}}$$

$$V_T = \frac{\sqrt{K}}{\sqrt{K}} \sqrt{C} \sqrt{T_{ind}} \omega + \frac{\sqrt{T_{ind}}}{\sqrt{K} \sqrt{C}} (R_A + R_S)$$

$$\frac{\sqrt{T_{ind}} \sqrt{K} \sqrt{C}}{\sqrt{T_{ind}} \sqrt{K} \sqrt{C}} \omega = \frac{V_T - \frac{\sqrt{T_{ind}}}{\sqrt{K} \sqrt{C}} (R_A + R_S)}{\frac{\sqrt{T_{ind}} \sqrt{K} \sqrt{C}}{\sqrt{T_{ind}} \sqrt{K} \sqrt{C}}}$$

$$\omega = \frac{V_T}{\sqrt{T_{ind}} \sqrt{K} \sqrt{C}} - \frac{R_A + R_S}{K C}$$



Disadvantage of this motor

At light load (no load) speed goes to ∞

So we cannot start the motor with no load + can't take load off suddenly

See slide 44 (from lecture)

We control it by changing terminal voltage

Example 8-5

$$E_A = V_T - I_A (R_A + R_S)$$

$$= 250 - 50(0.08) = 246 \text{ V}$$

$$n_2 = \frac{E_{A2}}{E_{A1}} n_1$$

$$\text{Magnetomotive force} = 25 \times 50 = 1250$$

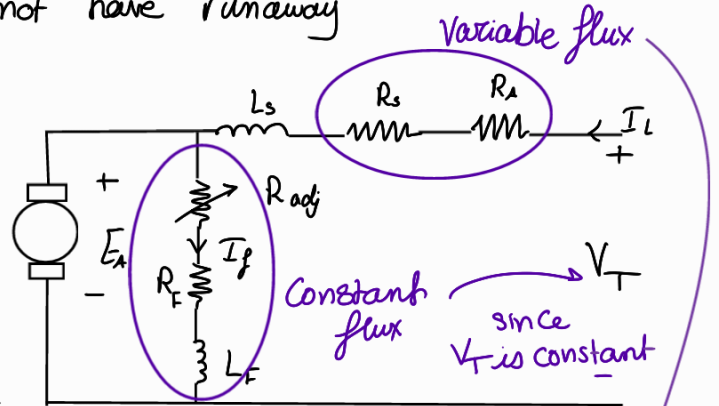
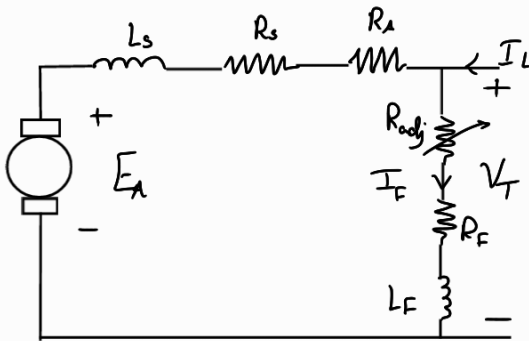
$$\text{So } E_{A2} \approx 80$$

$$n_2 = \left(\frac{246}{80}\right)(1200) = 3690 \text{ RPM}$$

$$T_{\text{ind}} = \frac{P}{\omega} = \frac{E_A I_A}{\omega} = \frac{(246)(50)}{\frac{3690 \times 2\pi}{60}} = 31.85 \text{ N.m}$$

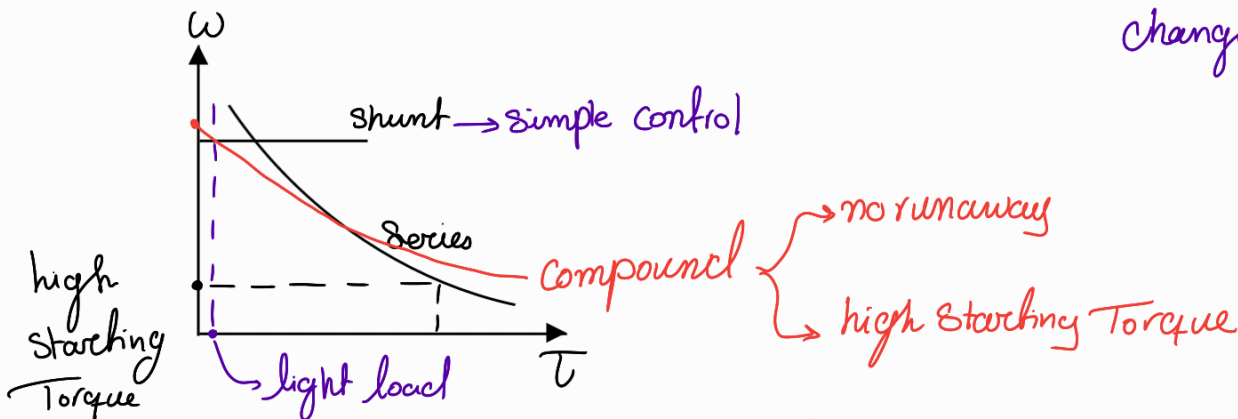
The compounded DC motor

- It has a shunt and a series field and it compounds best features of both shunt & series motors and does not have runaway



Better connection than this
 Since V_T is related to field resistance
 and so relation between V_T, I_F is simple
 In the second, I_F depends on I_L

since R_A is variable
 That depends on load
 R_A changes $\rightarrow I_A$
 changes $\rightarrow \Phi$ changes

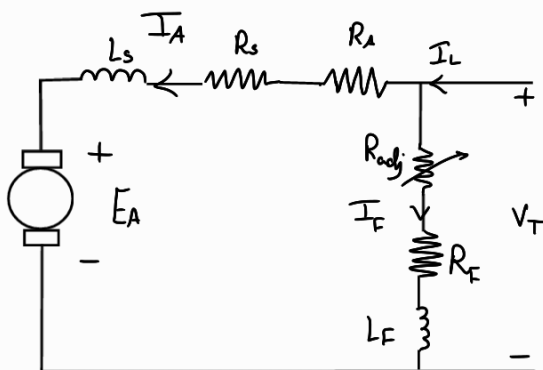
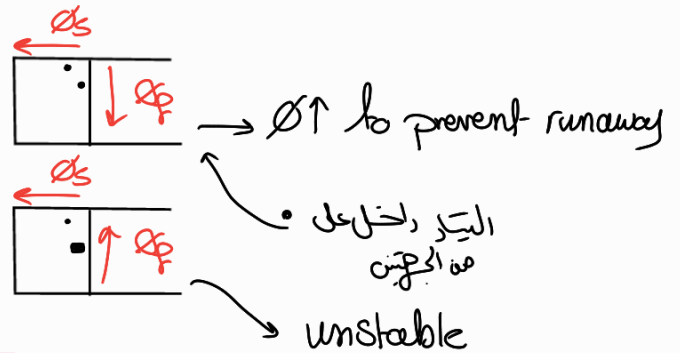


runaway occurs for series (Back)

series \rightarrow shunt

$\Phi_{net} = \Phi_s + \Phi_f$ Cumulatively compounded

$\Phi_{net} = \Phi_s - \Phi_f$ Differentially compounded



$I_f = \frac{V_T}{R_f}$ constant

I_A is variable that depends on the load

At light load \rightarrow shunt اقرب
 At higher load \rightarrow series اقرب

Speed control is done by controlling:-

field resistance

Voltage V_A

Armature Resistance R_A

DC Generator

- Same Structure as motor
 - \rightarrow S.E
 - \rightarrow Shunt
 - \rightarrow Compound

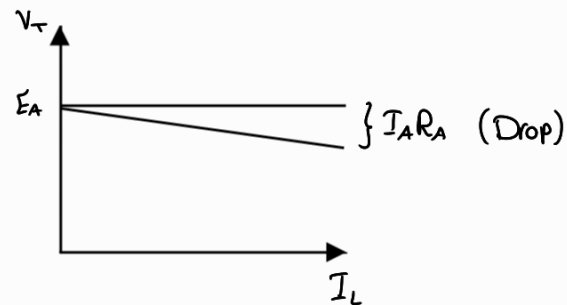
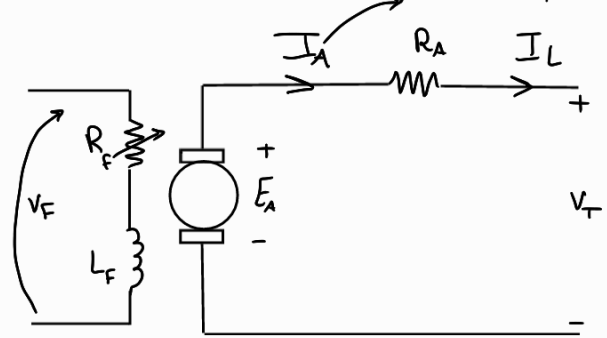
Separately excited DC Generator

$$V_T = E_A - I_A R_A$$

E_A needs to be increased to decrease drop

$E_A = K\Phi\omega$ \rightarrow field current
 So: Φ or ω are increased to increase E_A

عكس اتجاه التيار في ال motor

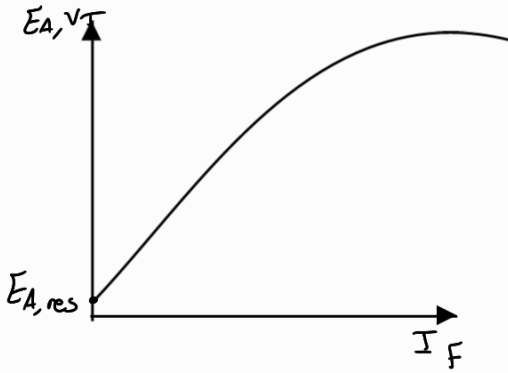


Best type of generator:

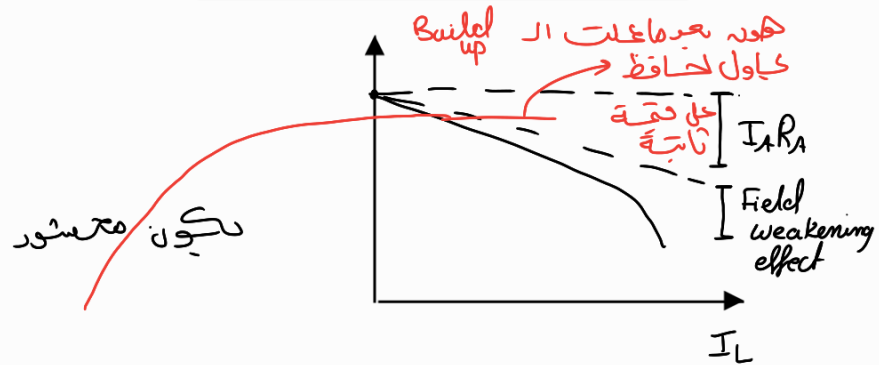
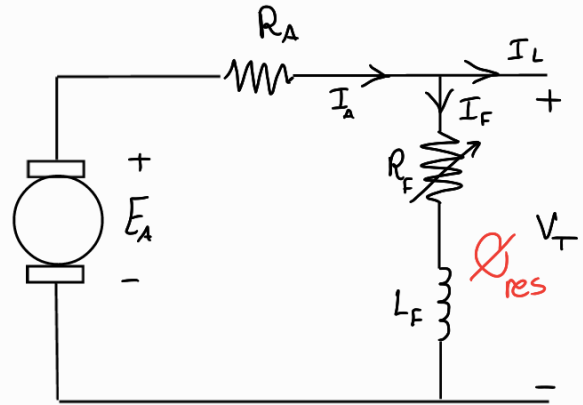
Terminal voltage is constant while changing load

Shunt DC Generator

Residual gives mechanical energy $\rightarrow E_A = K \Phi_{res} \omega_m$

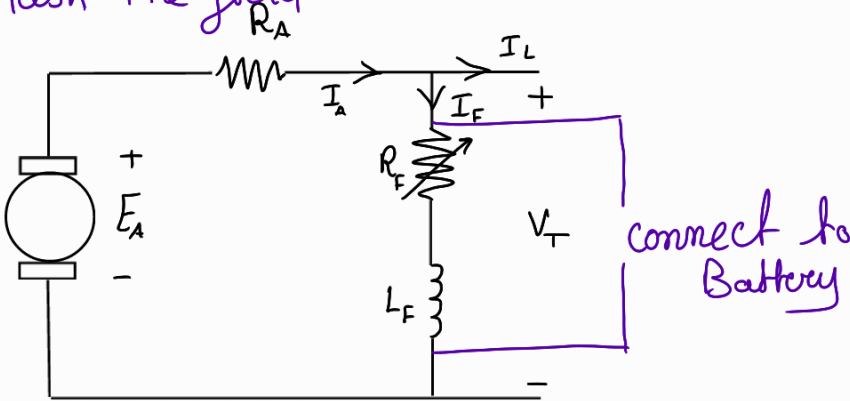


Φ_{res} exists in material



If there was no Φ_{res}

1. Flash the field

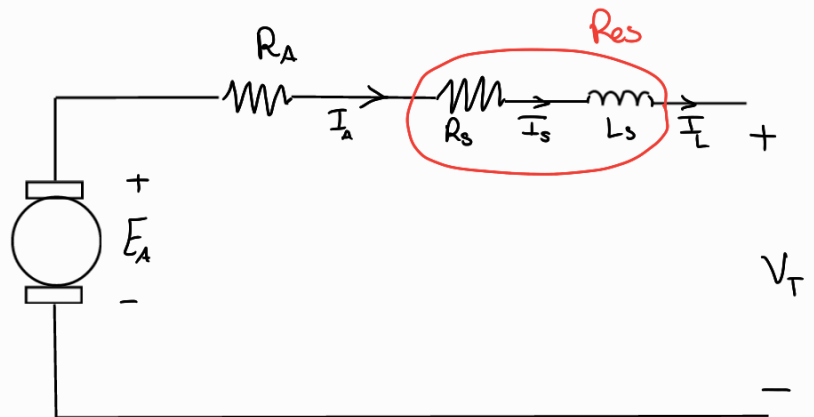
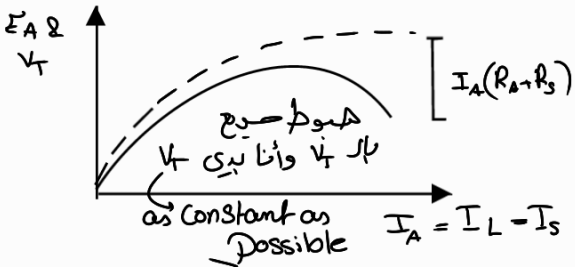


2. to turn the direction of rotation of generator

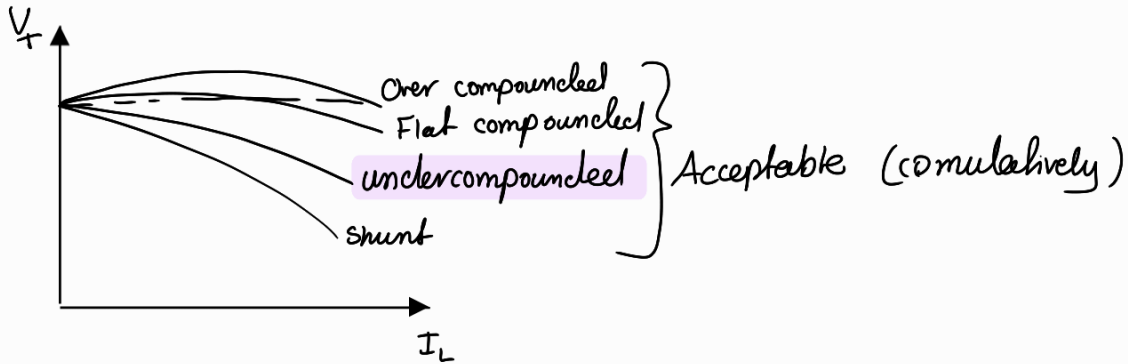
Series DC Generator

$$V_T = E_A - (R_A + R_S) I_A$$

Characteristics are Bad



Compound DC Generators → to control it $\begin{cases} \omega_m \\ I_F \end{cases}$
Comulatively



Differentially : Bad → Unacceptable

