

Equation sheet

Chapter 8

$$P(\text{vacuum}) = P_a - P$$

⇒ P: إذا زلنا سطحاً معيناً

عنه → إلى أي شيء

$$P = \rho g \Delta z$$

بما أن z هو المسافة من سطح G إلى سطح S من Top to G

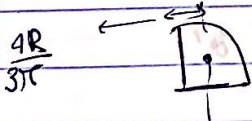
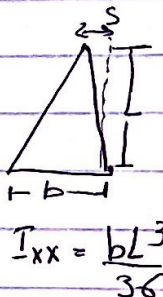
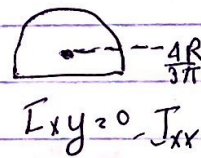
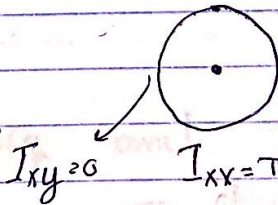
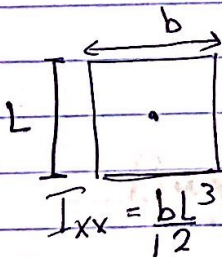
In Grates:

$$F = \rho g A h$$

Between surfaces and Body

$$y_{cp} = -\frac{\rho \sin \theta}{\rho g} \frac{I_{xx}}{A}$$

$$x_{cp} = -\frac{\rho \sin \theta}{\rho g} \frac{I_{xy}}{A}$$

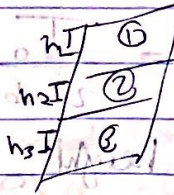


$$I_{xy} = \frac{b(b-2s)L}{72}$$

use moment for equilibrium

layered fluid below fluid? the unit
 kg/m^3
 $= \rho_g$

$$P_{CG_1} = (h_1)(\rho_1)g$$



$$P_{CG_2} = (2h_1)(\rho_1) + (h_2)(\rho_2)g$$

$$P_{CG_3} = (2h_1)(\rho_1) + (h_2)(\rho_2) + (h_3)(\rho_3)g$$

$$F_i = (P_{CG_i})A_i$$

ycp for each? Area \rightarrow using $y_{cp} = \frac{\rho \sin \theta I_{xx}}{F_i}$

$z_{cp} = z + y_{cp}$

moment $F_1 z_{cp1} + F_2 z_{cp2} = (F_1 + F_2) z_{cpR}$
 with sign

Buoyancy and Stability

$F_B = \rho_{fluid} V_{Body}$
 displaced volume
 average weight density for fluid

$$Q = W = \rho (h_1 + h_2 + \dots)$$

h = p / rho of ideal Gas
 h = p / rho of Temperature effect

Stability related to waterline Area :-

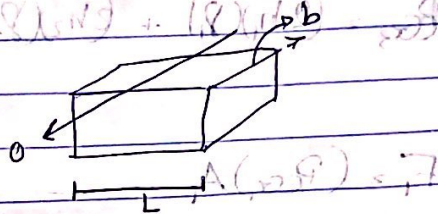
$$MG = \frac{IT_0}{V_{sub}} - GB$$

metacentric height

B → center of buoyancy

G → center of gravity

$$I_0 = \frac{bl^3}{12}$$



$MG > 0$ stable
 $MG < 0$ unstable

Uniform linear acceleration

$$\theta = \tan^{-1} \frac{ax}{g + a_z}$$

$G = \sqrt{ax^2 + (g + a_z)^2}$
 at point A $P_z = A G \sin \theta$
 $h \cos \theta$

Chapter 6. *capit. calculation?*

$$HGL = \frac{p}{\rho g} + \frac{V^2}{2g} + z$$

$Re < 2300$ Lam
 $Re > 4000$ Tur

$\Delta V \frac{1}{g} \dots$
 $B^* HGL 1 < HGL 2$

from 2 \rightarrow 1

for lam $\frac{L_e}{d} \approx 0.06 Re$

$L_e = 38d$ at critical Re

for Turb $\frac{L_e}{d} \approx 1.6 Re^{1/4}$

$h_f = f \frac{L}{d} \frac{V^2}{2g}$

$= \frac{4 \tau_w L}{\rho g d}$

for lam $h_f = \frac{32 \mu L V}{\rho g d^2} = \frac{128 \mu L Q}{\pi \rho g d^4}$

$f = \frac{64}{Re}$

for Turb: $\frac{1}{\sqrt{f}} = -1.8 \log \left(\frac{(6/d)}{3.7} + \frac{6.9}{Re} \right)$

Problems Types

① find hf

$$Re \rightarrow Q \rightarrow f \rightarrow hf = f \frac{L}{d} \frac{V^2}{2g}$$

② V, Q

$$f = hf \frac{d}{L} \frac{2g}{V^2}$$

Start with \rightarrow fully rough $\rightarrow \frac{1}{\sqrt{f}} = -2 \log_{10} \left(\frac{\epsilon/d}{3.7} \right)$

$f \sim V \sim Re \sim \frac{Vd}{\nu}$ \rightarrow constant

new $f \sim V \sim \dots$

③ d

$$f = \frac{\pi^2}{18} \frac{gh^3}{L Q^2} d^5$$

Moody

$$Re = \frac{4Q}{\pi d \nu}$$

Kinematic
Viscous

Cross f

$$\frac{G}{d}$$

Then iterate

④ L

$$h_p = \frac{P}{\rho g Q} = hf = f \frac{LV^2}{d^5}$$

if hori & minor losses neg

Re \rightarrow f_{cd} \rightarrow f (using eq.)

Hydraulic diameter

$$D_H = \frac{4 \times \text{Area}}{b + d}$$

$D_H = 4h$ \rightarrow distance apart / 2

lam
 $\tau_w = \frac{3\mu V}{h}$

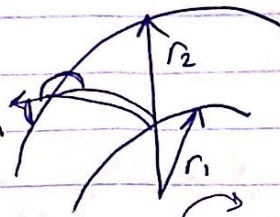
Turb
 $\Delta p_L = \frac{64}{96} D_H$

Equation sheet

$1 \text{ mm Hg} = 0.133322 \text{ kPa}$
 $1 \text{ L} = 0.001 \text{ m}^3$

Chapter 11:

$$Q = 2\pi r_1 b_1 V_{1n} = 2\pi r_2 b_2 V_{2n}$$



حساب
 التدرجات
 اذا عرفت
 السرعة
 في كل من
 الطرفين

$$V_{b2} = u_2 - \frac{V_{2n}}{\tan \beta_2}$$

$$u_1 = r_1 \omega \quad u_2 = r_2 \omega$$

$$T = \rho Q (r_2 V_{b2} - r_1 V_{b1})$$

$$P_w = \rho Q \omega (r_2 V_{b2} - r_1 V_{b1})$$

First assumption

$$V_{n1} = V_1$$

$$\alpha_1 = 90^\circ$$

$$Bhp = \frac{P_w}{\eta_p}$$

$$H = \frac{u_2 V_{b2} - u_1 V_{b1}}{g}$$

To avoid cavitation:

$$\text{NPSH} \leq \frac{P_a - P_v}{\rho g} - \delta_i - h_p$$

From graph

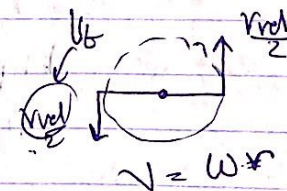
right-hand side

left-hand side

$$\frac{P_i}{\rho g} + \frac{V_i^2}{2g} - \frac{P_v}{\rho g}$$

$$P_i = u_2 \rho Q$$

if δ is neg \rightarrow below

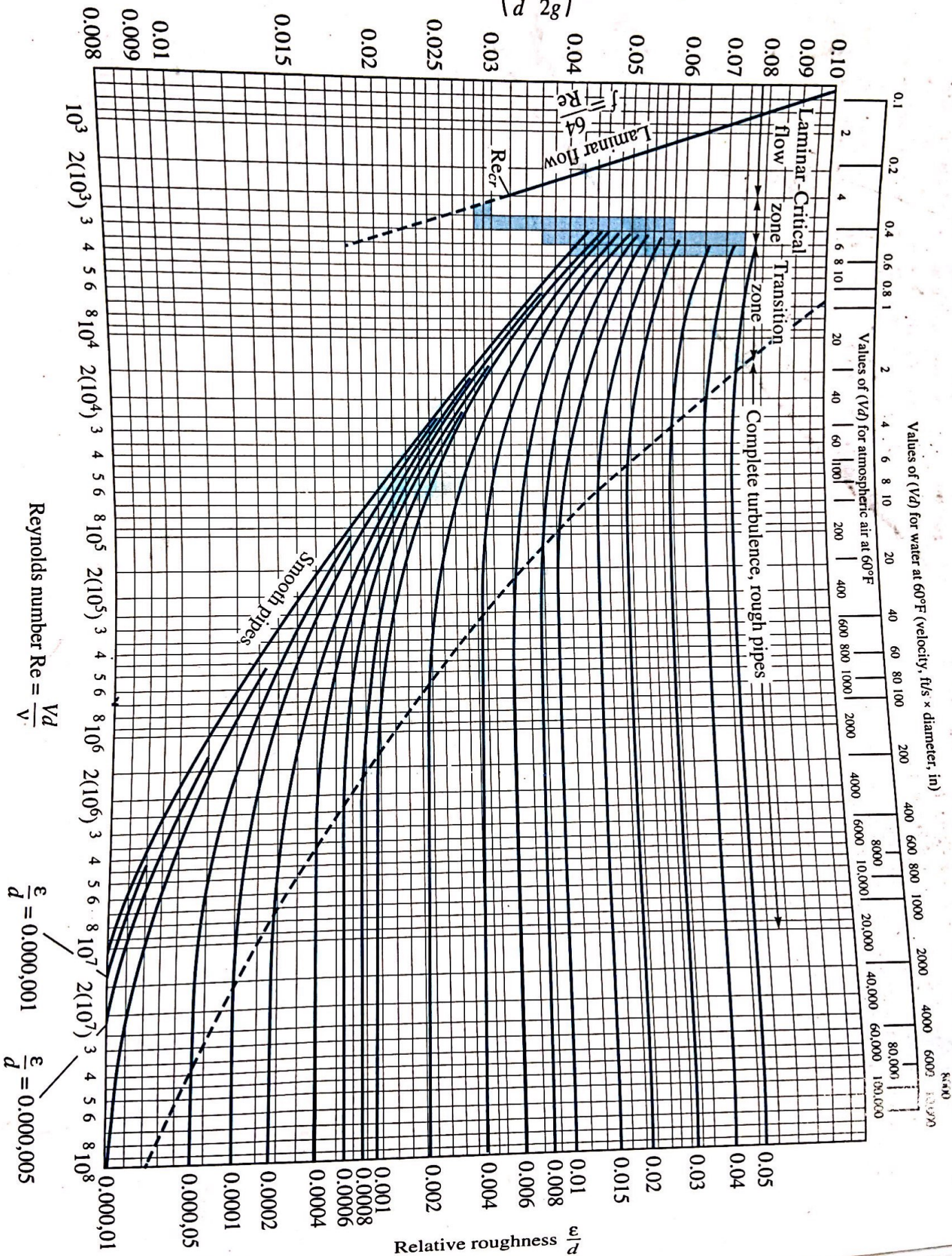


Centrifugal pump:

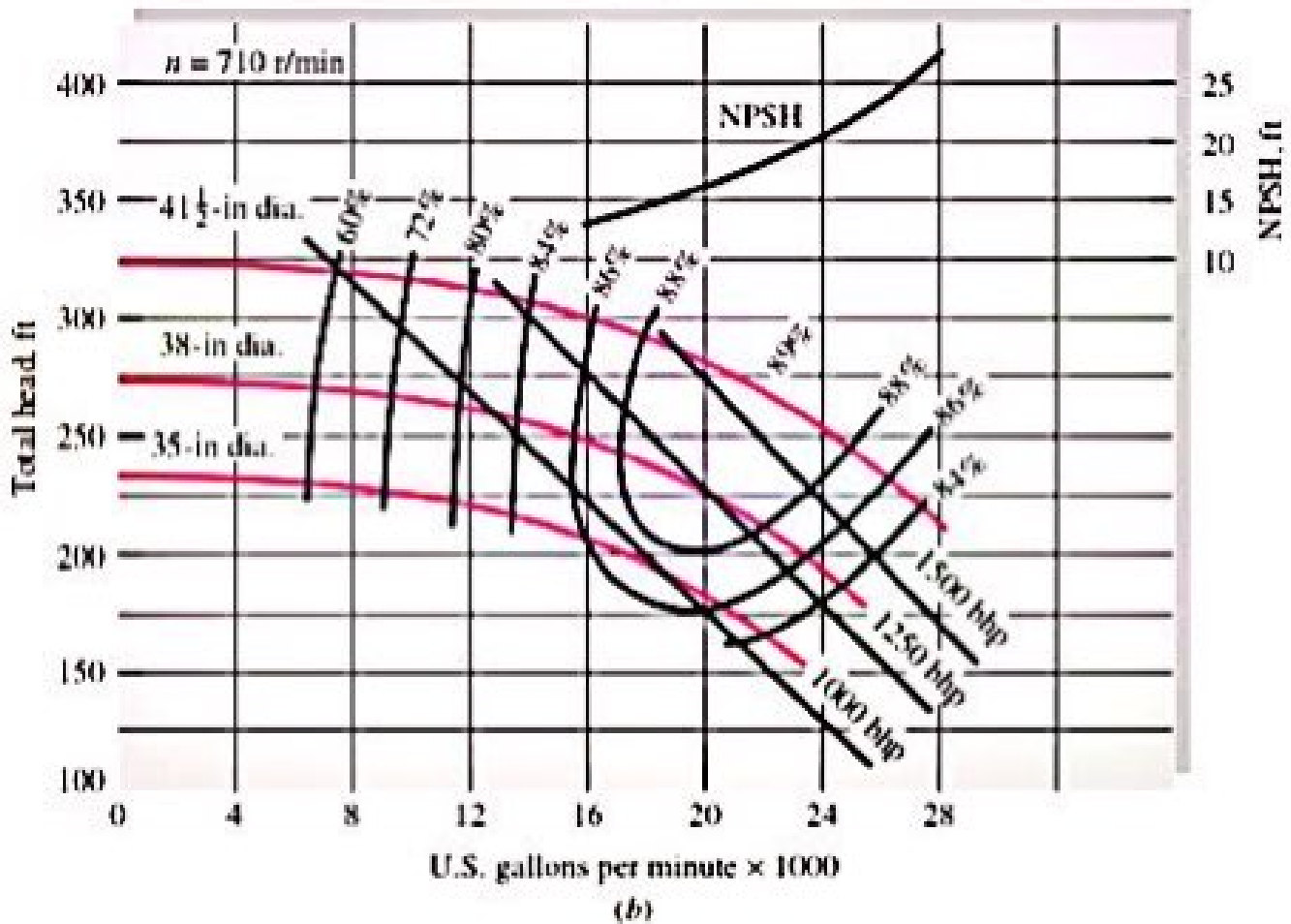
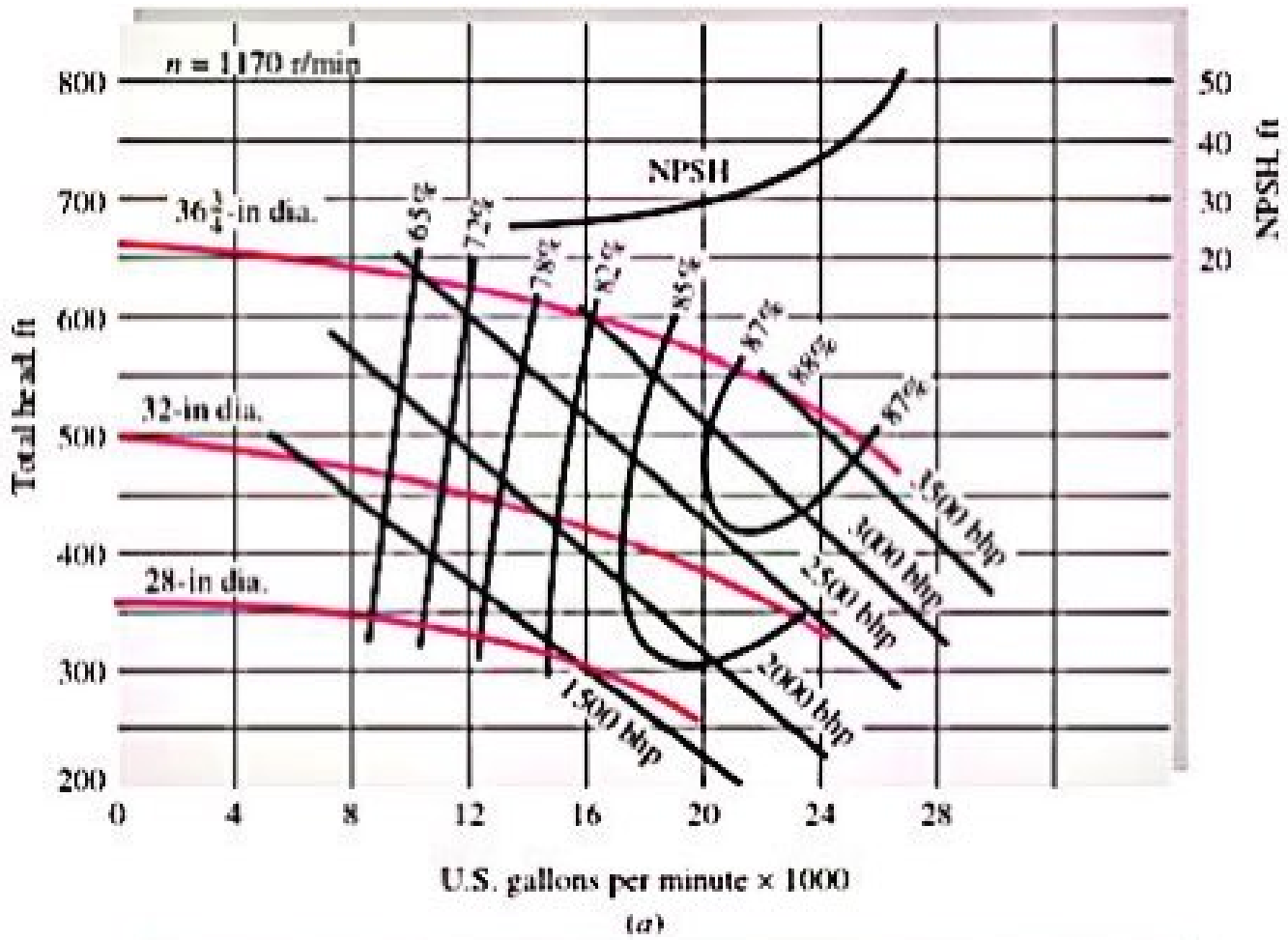
$$H = h_p - h_f = \frac{P_2 - P_1}{\rho g} + \frac{V_2^2 - V_1^2}{2g} + \delta_2 - \delta_1$$

$$\text{Power} = \frac{\rho g Q H}{\eta}$$

$$\text{Friction factor } f = \frac{h}{\left(\frac{L}{d}\right) \left(\frac{V^2}{2g}\right)}$$



$$\text{Reynolds number } Re = \frac{Vd}{\nu}$$



Nominal diameter, in

	Screwed				Flanged				
	$\frac{1}{2}$	1	2	4	1	2	4	8	20
Valves (fully open):									
Globe	14	8.2	6.9	5.7	13	8.5	6.0	5.8	5.5
Gate	0.30	0.24	0.16	0.11	0.80	0.35	0.16	0.07	0.03
Swing check	5.1	2.9	2.1	2.0	2.0	2.0	2.0	2.0	2.0
Angle	9.0	4.7	2.0	1.0	4.5	2.4	2.0	2.0	2.0
Elbows:									
45° regular	0.39	0.32	0.30	0.29					
45° long radius					0.21	0.20	0.19	0.16	0.14
90° regular	2.0	1.5	0.95	0.64	0.50	0.39	0.30	0.26	0.21
90° long radius	1.0	0.72	0.41	0.23	0.40	0.30	0.19	0.15	0.10
180° regular	2.0	1.5	0.95	0.64	0.41	0.35	0.30	0.25	0.20
180° long radius					0.40	0.30	0.21	0.15	0.10
Tees:									
Line flow	0.90	0.90	0.90	0.90	0.24	0.19	0.14	0.10	0.07
Branch flow	2.4	1.8	1.4	1.1	1.0	0.80	0.64	0.58	0.41